

# Gravireggeons in Extra Dimensions and Interactions of Cosmic Neutrinos with Nucleons

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## SUMMARY

- Large compact extra dimensions
- Gravitons and multigravity scattering amplitude
- Ultra-high energy neutrino-nucleon interactions
- Conclusions

## Large Compact Extra Dimensions

*(Arkani-Hamed, Dimopoulos and Dvali, 1998)*

*String inspired hypothesis* ( $D = 4 + d$ ):

$$E_D = M_4 \times K_d$$

$M_4$  – Minkovsky space-time

$K_d$  – d-dimensional compact space  
of size  $R_c$

$$ds^2 = g_{\mu\nu} dx^\mu dx^\nu + \gamma_{ab} dy^a dy^b$$

Gravity propagates in the bulk,  
gauge and matter fields are  
confined to 3-dimensional brane

*Relation between Planck mass and gravity scale in  $D$ -dimensions:*

$$M_{\text{Pl}} = V_d M_D^{2+d}$$

$V_d = (2\pi R_c)^d$  – volume of compactified ED

If  $d = 6$  and  $R_c^{-1} = 10 \text{ MeV} \Rightarrow M_D = 1 \text{ TeV}$

*Linearized quantum gravity:*

$$g_{AB} = \eta_{AB} + \frac{2}{M_D^{1+d/2}} h_{AB}(x, y)$$

*Kaluza-Klein (KK) expansion:*

$$h_{AB}(x, y) = \frac{1}{V_d} \sum_n \exp[-n y/R_c] h_{AB}^{(n)}(x)$$

*Masses of KK modes:*

$$m_n = \frac{n}{R_c}$$

$\Rightarrow$  mass splitting of spectrum:  $\Delta m \sim R_c^{-1}$

Universal coupling of massive  
KK gravitons to SM fields

$$\mathcal{L} = -\frac{1}{M_{\text{Pl}}} T^{\mu\nu} \sum_n G_{\mu\nu}^{(n)}$$

Smallness of coupling constant is compensated by high multiplicity of final states

*Production of KK gravitons:*

$$\sigma_{\text{KK}} \sim \frac{s^{d/2}}{M_D^{2+d}}$$

⇒ collider phenomenology at TeV energies  
(gravity effects in the planckian region)

What is multigraviton exchange contribution to high energy scattering? (at  $\sqrt{s} \gtrsim M_D$ )

## Gravitational Regge-Eikonal Approach

*(Kisselev and Petrov, 2003/04)*

Scattering of two particles in transplanckian kinematical region

$$\sqrt{s} \gg M_D, \quad -t$$

Massless graviton and its KK massive excitations lie on Regge trajectories

$$\frac{s^2}{-t + \frac{n^2}{R_c^2}} \rightarrow -\frac{1 + \exp(-i\pi\alpha_n(t))}{\sin\pi\alpha_n(t)} \alpha'_g \left(\frac{s}{s_0}\right)^{\alpha_n(t)}$$

*Leading vacuum trajectories:*

$$\alpha_n(t) = 2 + \alpha'_g t - \frac{\alpha'_g}{R_c^2} n^2, \quad n = 0, 1, \dots$$

$n =$  KK number

*Slop is related to the string scale:*

$$\alpha'_g = M_s^{-2}, \quad M_s = M_D \left( \frac{g_s^2}{4\pi} \right)^{2/(2+d)}$$

- **5-dimensional amplitude ( $d = 1$ )**

$$A(s, t, k) = -2iR_c s \int d^2b e^{iq_\perp b + k\phi} \int_{-\pi}^{\pi} d\phi \left[ e^{i\chi(s, b, \phi)} - 1 \right]$$

$R_c \phi$  – 5-th component of impact parameter



*Imaginary part of the eikonal:*

$$\text{Im } \chi(s, b, \phi) \simeq \frac{G_5 s}{8\pi^{1/2}} \frac{\alpha'_g}{R_g^3(s)} \exp \left[ - (b^2 + R_c^2 \phi^2) / 4R_g^2(s) \right]$$

“Transverse gravitational radius”

$$R_g(s) = \sqrt{\alpha'_g \ln(s/s_0)}$$

*Generalization for  $d > 1$  is straightforward*

$\alpha'_g = 0$  (zero slope strings)  
 $\Rightarrow$  pure real eikonal  
 (Giudice, Rattazzi and Wells, 2002)

*Eikonal is small outside the region:*

$$b^2 \lesssim R_0^2(s) = 4\alpha'_g \ln(s/s_0) \ln(s/M_D^2)$$

$\Rightarrow$  *inelastic (D-dimensional) cross section:*

$$\sigma_D^{\text{in}}(s) \simeq \begin{cases} \text{const } R_0^{2+d}(s) & R_c \gg R_0(s) \\ \text{const } R_0^2(s) R_c^d & R_c \ll R_0(s) \end{cases}$$

- **Collision of SM particles on the brane**

Impact parameter is two-dimensional

$$\text{Im } \chi(s, b) \simeq \frac{s}{M_D^2} \left( \frac{M_s}{M_D} \right)^d \exp[-b^2/4R_g(s)]$$

*Inelastic cross section:*

$$\sigma_{\text{in}}(s) \simeq \frac{4\pi}{M_s^2} \ln(s/s_0) \ln(s/M_D^2)$$

$$M_D \sim 1 \text{ TeV}, \quad M_s \simeq 0.46(0.56) M_D, \quad \text{for } d = 4(6)$$

*Real part of the eikonal (with zero graviton mode subtracted):*

$$\text{Re } \tilde{\chi}(s, b) |_{b \gg R_g(s)} \simeq \frac{s}{M_D^2} \left( \frac{M_s}{M_D} \right)^d \left[ R_g(s)/b \right]^2 J_2 \left[ b/R_g(s) \right]$$

Zero impact parameter

$$\frac{\text{Re } \tilde{\chi}(s, 0)}{\text{Im } \chi(s, 0)} \sim \ln s$$

## Distinct behavior in D infinite flat dimensions

*(Amati, Ciafaloni and Veneziano, 1987)*

$\text{Im } \chi_D(s, b)$  is the same, but

$$\text{Re } \chi_D(s, b) = \left[ \frac{b_c(s)}{b} \right]^d$$

- 4-dimensional scattering amplitude
- Both real and imaginary part exhibits exponential fall-off:

$$\text{Re } \tilde{A}(s, t), \text{ Im } A(s, t) \Big|_{|t|R_g(s) \gg 1} \sim \exp[t\alpha'_g \ln(s/s_0)]$$

- *Real part (with pole term subtracted) dominates at  $t = 0$ :*

$$\frac{\text{Re } \tilde{A}(s,0)}{\text{Im } A(s,0)} \sim \ln s$$

To compare, D-dimensional amplitude

$$\text{Re } A_D(s, t) \Big|_{|t| \gg b_c^{-2}(s)} \sim |t|^{-(d+2)^2/4(d+1)}$$

$\text{Im } A_D(s, t)$  coincides with  $\text{Im } A(s, t)$

Inelastic processes do not feel that colliding particles are confined to the brane

In what processes can we look for multigravity effects?

Weakly interacting particles with transplanckian energies ( $\sqrt{s} \gtrsim M_D$ )

$\Rightarrow$  cosmic neutrinos?

## Ultra-High Energy Neutrino Interactions

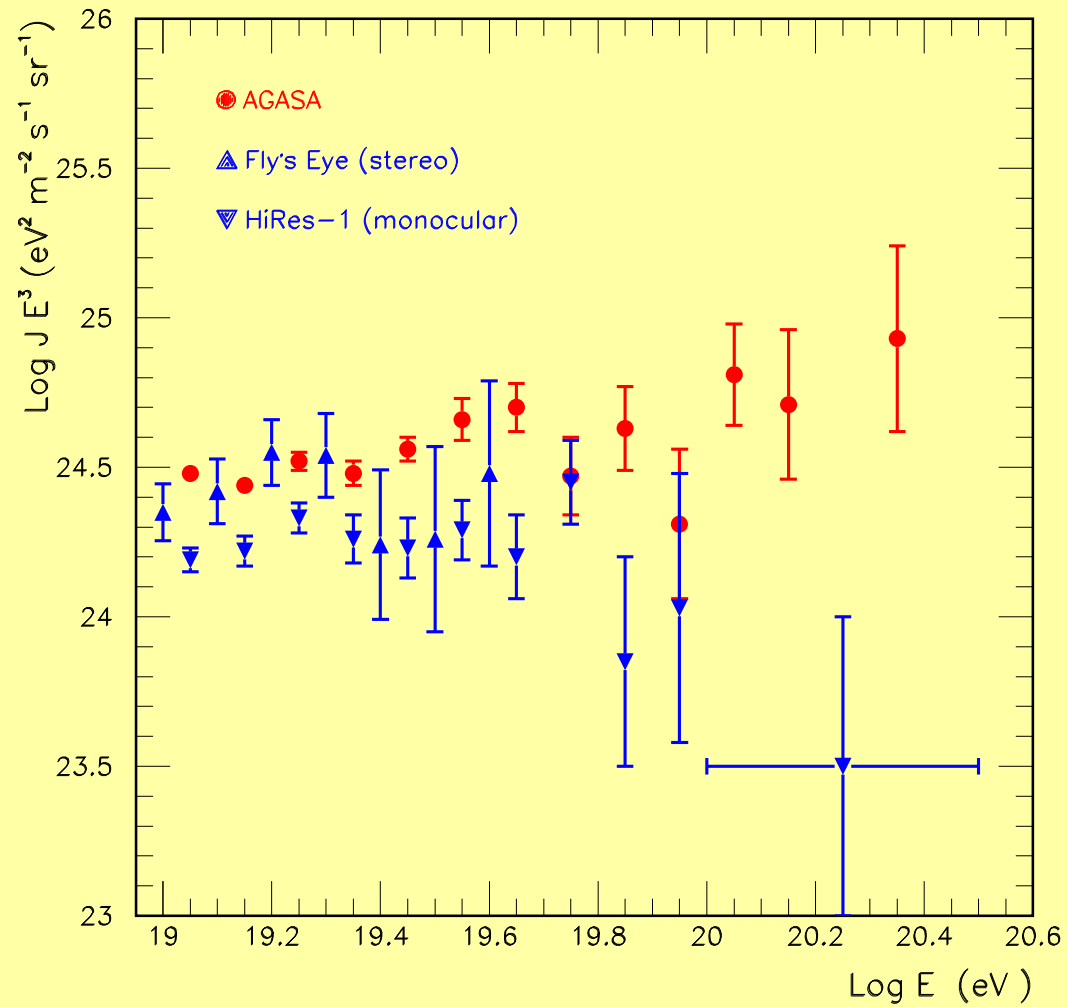
SM neutrino-nucleon scattering is very weak even at ultra-high energies (UHE)

$$\sigma_{\text{SM}}^{\nu\text{N}} \simeq 2.36 \cdot 10^{-5} \left( \frac{E_\nu}{10^{19} \text{ eV}} \right)^{0.363} \text{ mb}$$

$$(10^{16} \text{ eV} \lesssim E_\nu \lesssim 10^{21} \text{ eV})$$

New interactions may dominate

UHE cosmic neutrinos – one of possibilities to explain Greisen-Zatsepin-Kuzmin (GZK) puzzle



Upper end of the cosmic ray energy spectrum as observed by AGASA and HiRes/FlyEye (Anchordoqui *et. al*, 2004)



*Proton scattering off cosmic microwave background during UHE cosmic ray (CR) propagation:*

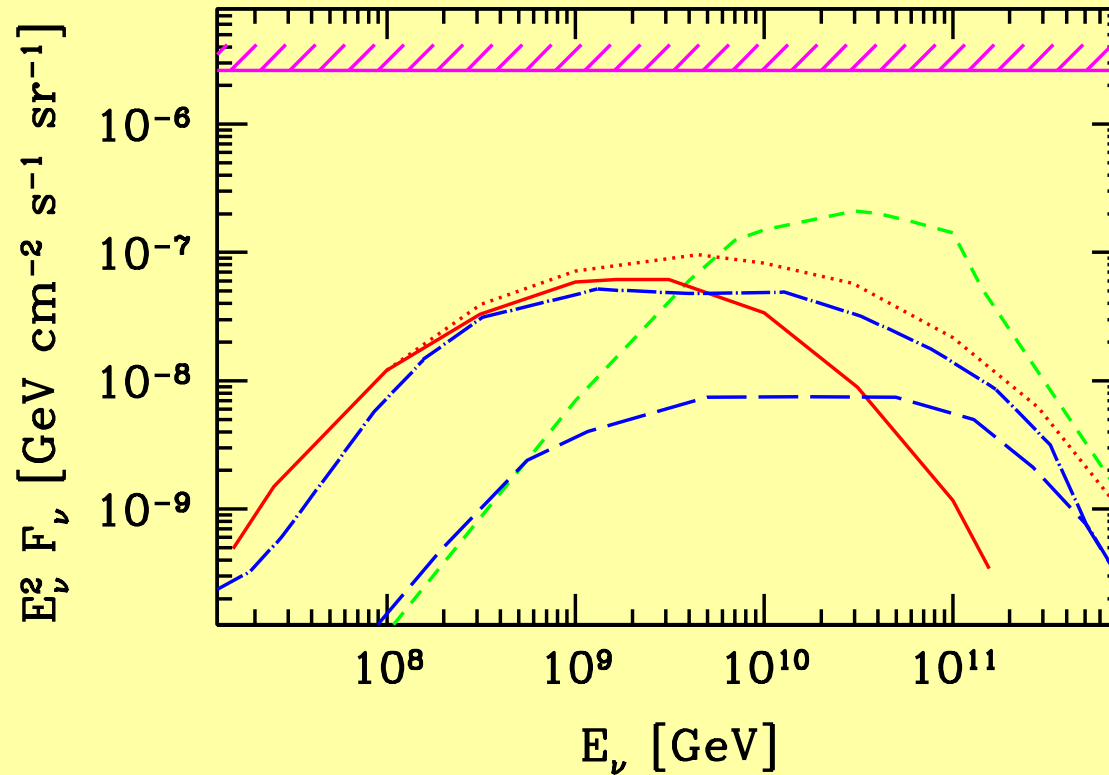


$\Rightarrow$  GZK cut-off of CR spectrum  
at  $E \simeq 5 \cdot 10^{19}$  eV

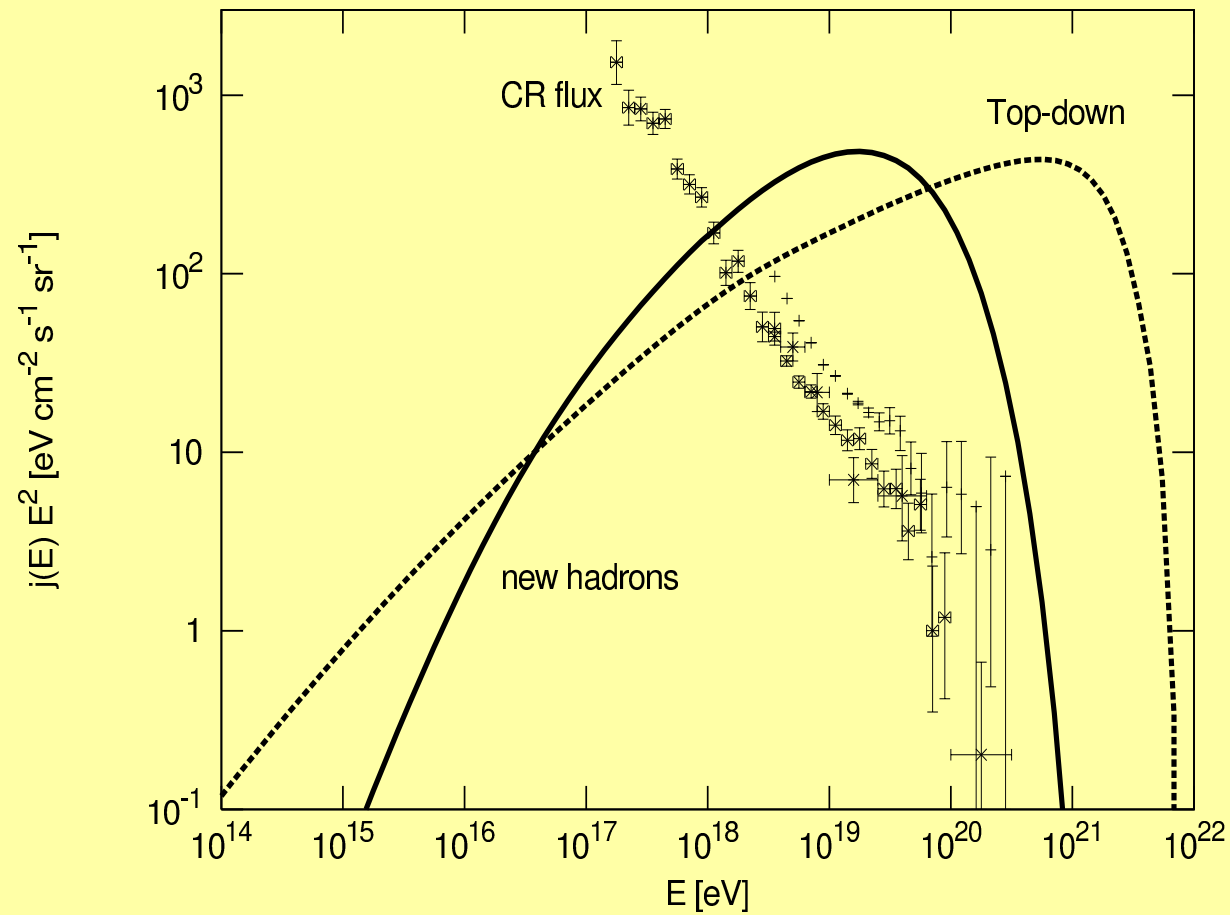
Consequence decays of charged pions  
( $\pi^{\pm} \rightarrow \mu^{\pm} \nu_{\mu}$ ,  $\mu^{\pm} \rightarrow e^{\pm} \nu_e \nu_{\mu}$ )

$\Rightarrow$  flux of cosmogenic UHE neutrinos

UHE primaries of CR are neutrinos  
+ neutrino interactions beyond SM  
 $\Rightarrow$  excess of UHECR flux?



Predictions of the cosmogenic neutrino flux,  $F_\nu = \sum_i [F_{\nu_i} + F_{\bar{\nu}_i}]$ . Dotted line: flux from paper by Protheroe *et al.* (1996) assuming a maximum energy of  $E_{\text{max}} = 3 \cdot 10^{21}$  eV for the ultrahigh energy cosmic rays. Shaded: theoretical upper limit of the neutrino flux from “hidden” astrophysical sources that are non-transparent to ultrahigh energy nucleons (Mannheim *et al.* (2001)).



Neutrino fluxes in exotic ultra-high energy cosmic ray models. Solid line is the neutrino flux in model of new hadrons whereas dashed line is the neutrino flux in topological defect model (Aramo *et al.* (2004)).

*Neutrino interaction length:*

$$L_\nu = \frac{m_N}{\rho_W \sigma_{\nu N}} \simeq 1.7 \cdot 10^7 \left( \frac{\text{pb}}{\sigma_{\nu N}} \right) \text{ km we}$$

(we  $\equiv$  water equivalent)

To separate neutrino-initiated showers from hadronic ones – looking for quasi-horizontal air showers

Non-observation of horizontal showers by Fly's Eye and AGASA  $\Rightarrow$  upper bound on the neutrino flux  $\Phi_\nu$

$$(\Phi_\nu \sigma_{\nu N})(E_\nu) \leq 3.74 \cdot 10^{-42} \left( \frac{E_\nu}{1\text{GeV}} \right)^{-1.48} \text{ GeV}^{-1} \text{ s}^{-1} \text{ sr}^{-1}$$

( $10^8 \text{ GeV} \leq E_\nu \leq 10^{11} \text{ GeV}$ )

- **Multigravity neutrino-nucleon scattering**

$$\sigma_{\text{grav}}^{\nu\text{N}}(\mathbf{s}) = \sum_{\mathbf{i}} \int_{x_{\text{min}}}^1 dx f_{\mathbf{i}}(\mathbf{x}, \mu^2) \hat{\sigma}_{\mathbf{i}}(\hat{\mathbf{s}})$$

$f_{\mathbf{i}}(\mathbf{x}, \mu^2)$  – parton distribution function (PDF)  
 $\hat{\mathbf{s}} = \mathbf{x}\mathbf{s}$  – partonic subprocess energy

PDF set based on analysis of DIS data

(Alekhin, 2002)

$\Rightarrow$  *multigravity (inelastic) cross section:*

$$\sigma_{\text{grav}}^{\nu\text{N}}(E_{\nu} = 10^{12} \text{ GeV}) \simeq \begin{cases} 0.87 \cdot 10^{-1} \text{ mb} & d = 2 \\ 0.46 \cdot 10^{-3} \text{ mb} & d = 4 \end{cases}$$

## *Detection of UHE cosmic neutrinos:*

- Neutrino telescopes (MACRO, Baikal, AMANDA II)

Future detectors: NT200+ (Baikal), IceCube, ANTARES, NESTOR

- Observation of neutrino-induced air showers (AGASA, Fly's Eye/HiRes, Yakutsk, RICE, GLUE, FORTE)

Future projects: NUTEL, EUSO, OWL, Telescope array,  
**Pierre Auger observatory**

- **Neutrino detection by ground arrays**

*Number of air showers with energy larger than  $E_{th}$  for time interval  $T$ :*

$$N_{sh}(E > E_{th}) = T N_A \int_{E_{th}}^{\infty} dE_{\nu} \Phi_{\nu}(E_{\nu}) \sigma_{\nu N}(E_{\nu}) \mathcal{A}(E_{\nu})$$

$$(N_A = 6.022 \cdot 10^{23} \text{ g}^{-1})$$

$\mathcal{A}(E_{\nu})$  is the detector acceptance

*Pierre Auger observatory:*

$$\mathcal{A}(E > 10^{10} \text{ GeV}) \approx 30 \text{ km}^3 \text{ we sr}$$

(Capelle et al., 1998)

d	2	3	4	5	6
$E_{\text{th}} = 10^8 \text{ GeV}$	34.9	2.00	0.32	0.21	0.20
$E_{\text{th}} = 10^9 \text{ GeV}$	30.2	1.66	0.21	0.12	0.12
$E_{\text{th}} = 10^{10} \text{ GeV}$	13.2	0.74	0.06	0.03	0.02

Yearly event rates for nearly horizontal neutrino induced showers with  $E_{\text{sh}} \geq E_{\text{th}}$  for *cosmogenic neutrino flux* (Protheroe, 1996) at three values of threshold energy  $E_{\text{th}}$  and  $E_{\text{max}} = 3 \cdot 10^{21} \text{ eV}$ . Number of events corresponds to one side of the Auger ground array.

d	2	3	4	5	6
$E_{\text{th}} = 10^8 \text{ GeV}$	270	18.7	1.72	0.77	0.71
$E_{\text{th}} = 10^9 \text{ GeV}$	264	18.2	1.55	0.63	0.57
$E_{\text{th}} = 10^{10} \text{ GeV}$	227	16.3	1.21	0.38	0.34

The same as in the previous Table, but for the neutrino flux in topological defects model (Aramo *et al.*, 2004) and  $E_{\text{max}} = 7 \cdot 10^{21} \text{ eV}$ .



## CONCLUSIONS

- Summing up gravireggeons results in  $D$ -dimensional Planck mass in the eikonal
- Real part of 4-dimensional amplitude has exponential falloff in  $t$ , contrary to  $D$ -dimensional amplitude
- Inelastic processes are the same, whether colliding particles are confined to the brane or propagate in the bulk
- Ultra-high energy neutrino scattering off nucleons is one of promising processes to search for multigravity effects
- Up to tens of quasi-horizontal air showers induced by cosmic neutrinos can be detected at the Auger observatory per year