


# Extended Quintessence with exponential coupling



DESY Theory Workshop 2004  
28th Sept – 1st October  
DESY Hamburg

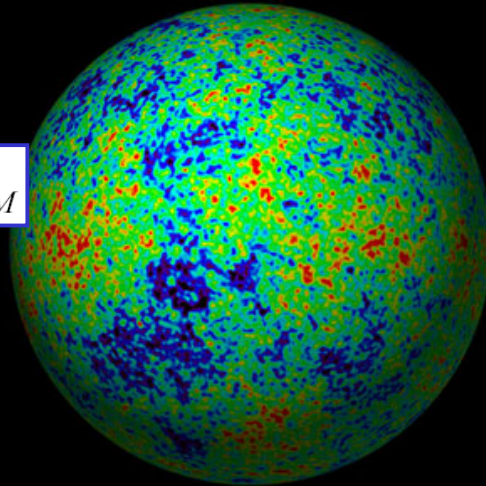
**Valeria Pettorino (Univ. of Naples)**

**C. Baccigalupi (SISSA, Trieste), G. Mangano (Univ. of Naples)**

# Modern cosmology

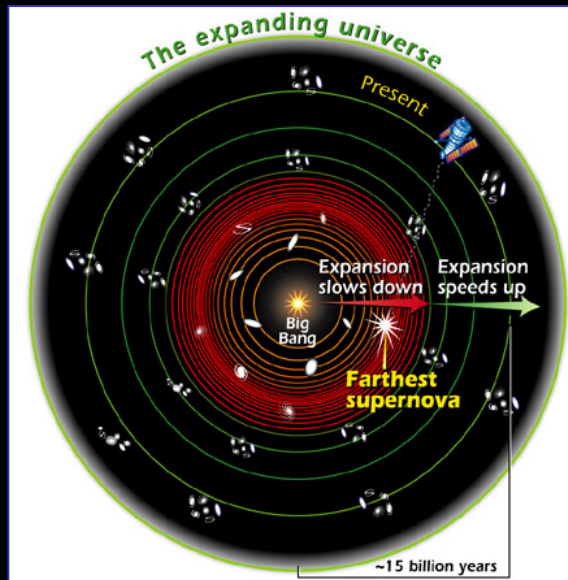
CMB

$$\Omega_{\Lambda} \approx 1 - \Omega_M$$



S  
u  
p  
e  
r  
n  
o  
v  
a  
e  
I  
a

$$\Omega_{\Lambda} \approx 1.4\Omega_M + 0.2$$



Large Scale Structures



HST

# Content of the Universe

$$\Omega_{tot} = 1$$

$$\Omega_b = 0.045$$

$$\Omega_{DM} = 0.225$$

$$\Omega_{DE} = 0.73$$



Part of the energy in the universe which does not cluster.

# Dark Energy scalar field

Cosmological constant

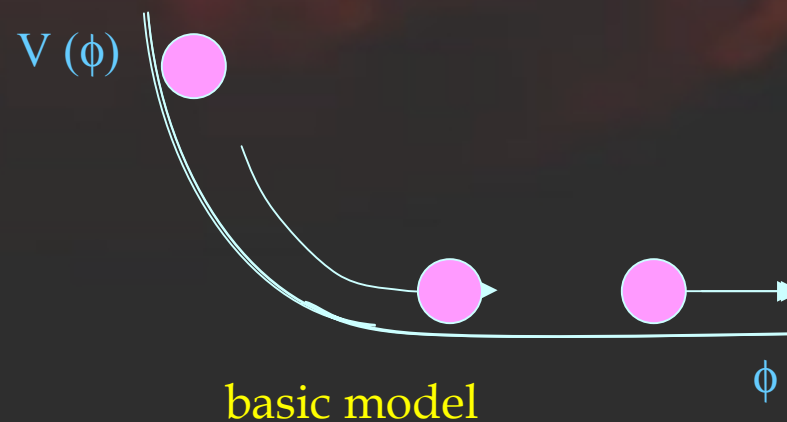
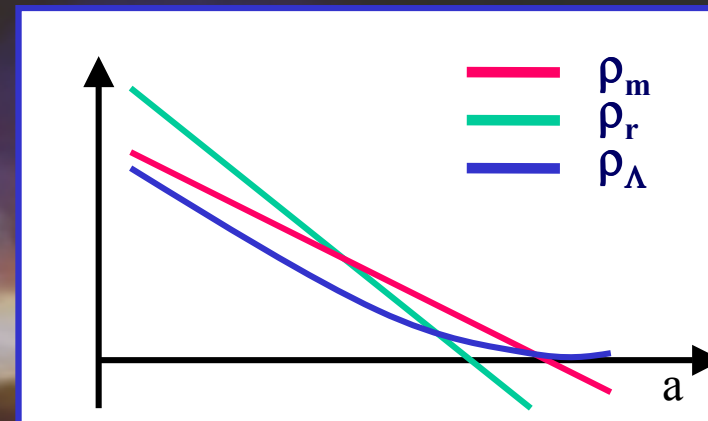
Constant energy contribution

Why so small?  
Why same order right now?



Dark energy

Dynamical energy contribution



basic model



# DE and tracker fields

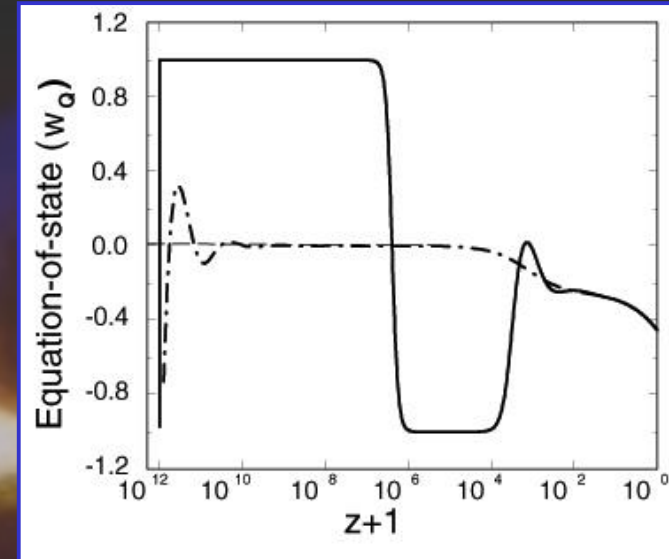
Cosmological constant



Dark Energy



Tracker fields



A subclass of Quintessence models admits a useful property: any solution within a wide range of initial conditions converges to an attractor solution, providing the amount of energy density required today.

Liddle & Scherrer, Steinhardt et al

# $w_Q$ and tracker fields

In most tracker models  $w_Q$  today is predicted to be too different from  $-1$  to be allowed by observations. The potential  $V$  needs to be flattened, thus shrinking the range of initial conditions.

LSS CMB H Sup Ia



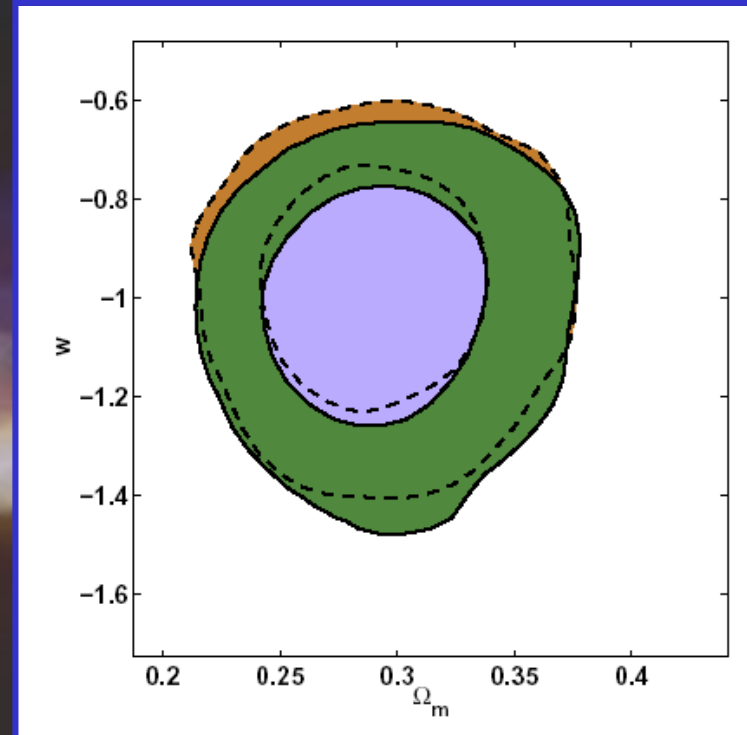
$$w_Q < -0.78 \text{ at } 95\%$$

Spergel et al 2003

Weller & Lewis 2003

$$w_Q = -0.91^{+0.13}_{-0.15}$$

Tegmark 2004

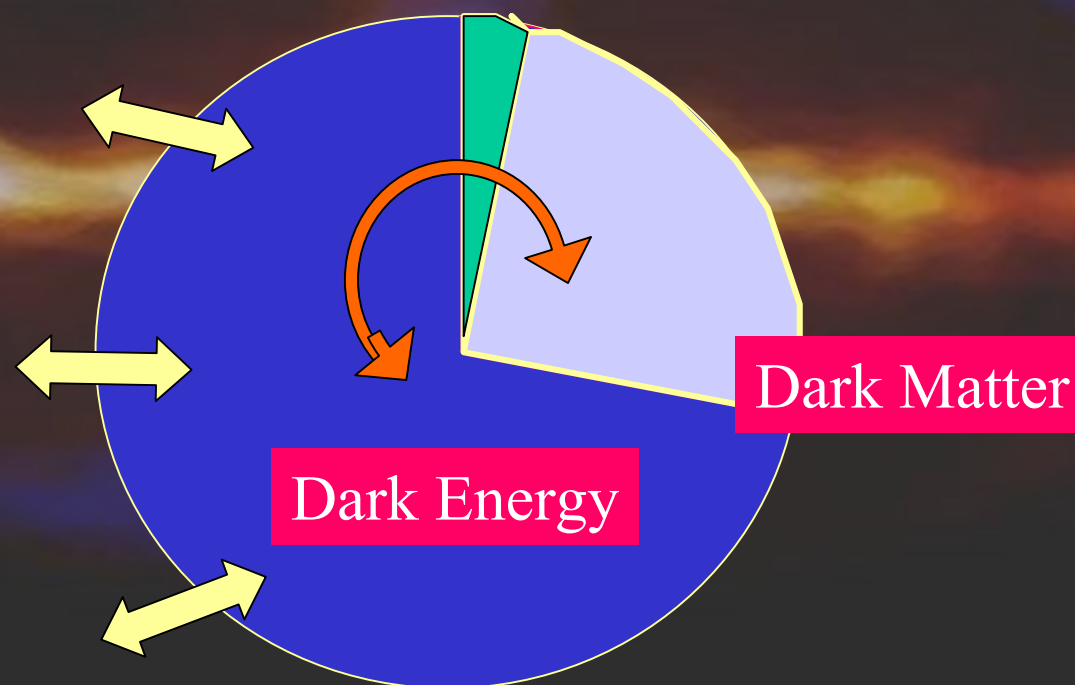


As the allowed range shrinks, tracker fields become less appealing.

# Coupling Dark energy

Essential to understand how Dark Energy interacts with other entities

Gravity



# Dark energy

Cosmological constant



Dark energy



Non coupled DE



Coupled DE



Tracker fields



Dark energy  
& Gravity



Dark Energy  
& Dark Matter

Perrotta Baccigalupi  
Matarrese 2000

Extended  
Quintessence

Amendola 2000

V.P. Mangano, Miele  
2002



# Scalar tensor theories

Scalar field

Ricci scalar

$$S = \int d^4x \sqrt{-g} \left[ \frac{1}{2\kappa} f(\phi, R) - \frac{1}{2} \omega(\phi) \phi^{;\mu} \phi_{;\mu} - V(\phi) + \mathcal{L}_{\text{fluid}} \right]$$

= 1

$$\frac{f(\phi, R)}{2\kappa} = F(\phi)R$$

# The coupling

## Scalar tensor theories of gravity

Induced Gravity  
(IG)

$$F(\phi)R = \xi\phi^2 R$$

Non minimal  
Coupling (NMC)

$$F(\phi)R = \frac{R}{16\pi G} + \xi\phi^2 R$$

Exponential  
Coupling

$$F(\phi)R = \frac{R}{16\pi G} \exp(\xi\phi)$$

Dilatonic-inspired  
coupling

# Cosmological expansion

In a FRW space, the relevant equations change

...both for the background...

$$\mathcal{H}^2 = \left(\frac{\dot{a}}{a}\right)^2 = \frac{1}{3F} \left( a^2 \rho_{fluid} + \frac{1}{2} \dot{\phi}^2 + a^2 V - 3\mathcal{H}\dot{F} \right)$$

$$\ddot{\phi} + 2\mathcal{H}\dot{\phi} - \frac{\xi}{16\pi a} \rho_{m_0} + a^2 V_{\phi} = 0$$

...and for the field

Where we have used

$$R \simeq \frac{1}{F} \frac{\rho_{m_0}}{a^3}$$

$$\tilde{\rho}_{\phi} = \frac{1}{2a^2} \dot{\phi}^2 + V(\phi) - \frac{3\mathcal{H}\dot{F}}{a^2}$$

# Observational constraints

Time variation of the gravitational constant

$$\left| \frac{G_t}{G} \right| = \left| \frac{F_t}{F} \right|$$

$$< 10^{-11} / yr$$

Local laboratories and solar system experiments

Effects on the J.B.D. parameter  
(Bertotti et al. Nature 2004)

$$\xi = \sqrt{\frac{16\pi}{\omega_{JBD}}}$$

$$\omega_{JBD} \equiv \frac{F}{F_\phi^2} \geq 4 \times 10^4$$

Effects induced on photon trajectories from G variation

Nucleosynthesis

$$-1.4 \leq \Delta N \leq 0.6 \rightarrow -0.1 \leq \xi\phi \leq 0.3$$

This bound guarantees a value for  ${}^4\text{He}$  and Deuterium in concordance with recent estimates.

$$0.228 \leq Y_p \leq 0.256$$

$$2.4 \times 10^{-5} \leq D/H \leq 3.2 \times 10^{-5}$$

# R-boost

The coupling generates a new purely gravitational effect called R-boost

$$\ddot{\phi} + 2H \dot{\phi} - \frac{a^2 F_\phi R}{2} + a^2 V_\phi = 0$$

When

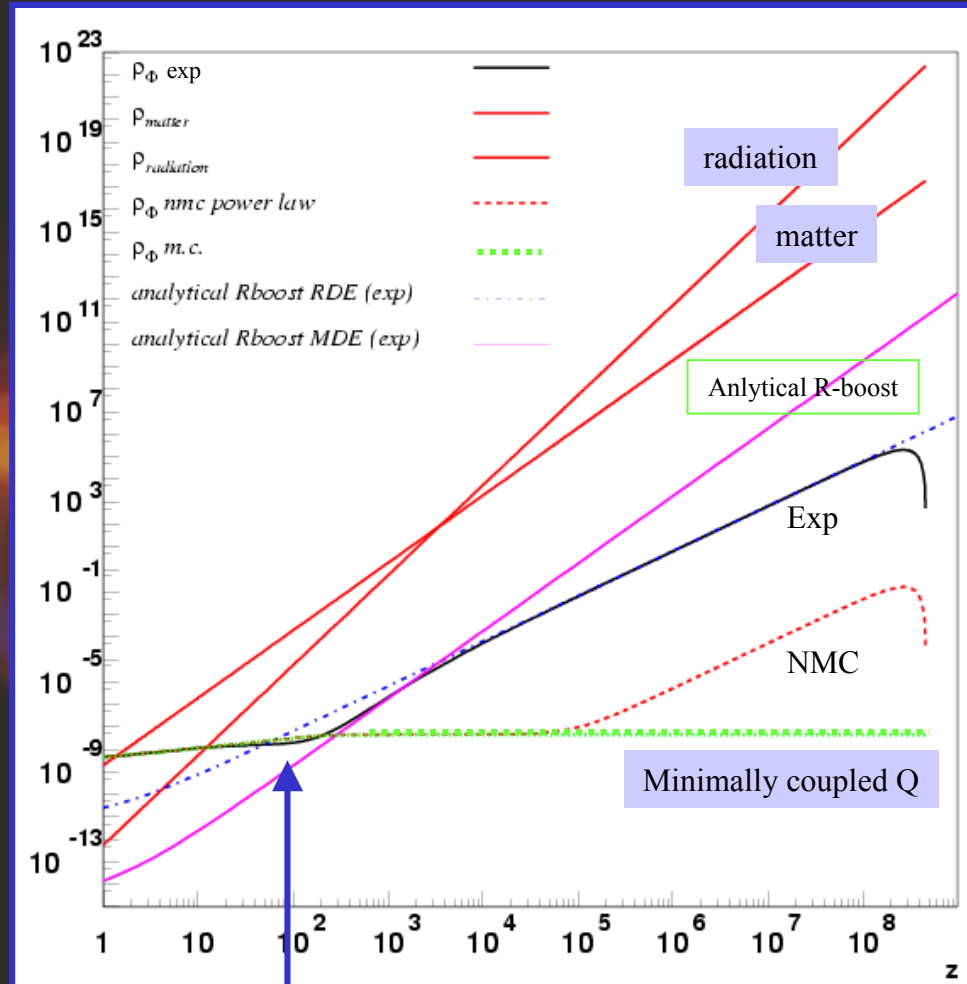
$$R \cong \frac{1}{F} \frac{\rho_{m_0}}{a^3} \neq 0$$

there is an effective gravitational potential acting on the field

Baccigalupi Matarrese  
Perrotta 2000



# Energy density behaviour



$$\dot{\phi}_{beg} = 0$$

$$\omega_{JBD} = 10^5$$

$$\xi = 1.6 \times 10^{-2}$$

The RDE is dominated by the R-boost

$$2H\dot{\phi} \approx \frac{a^2 F_{\phi} R}{2}$$

slow roll

The minimally coupled solution is equivalent to a cosmological constant in RDE. It moves only recently, when it reaches the tracker solution

V becomes important: end of slow-roll;  $\rho_{\phi}$  reaches the required value today

# RDE & MDE

## Analytical solutions of the K.G. equation

RDE

$$a \propto \tau$$

$$\phi(\tau) = \frac{\xi}{4} \rho_{m_0} \sqrt{\frac{3}{8\pi\rho_{r_0}}} \tau + \phi_{beg}$$

$$\frac{1}{2} \dot{\phi}_t^2 = \frac{1}{2} \frac{\dot{\phi}^2}{a^2} = \frac{3}{32} \frac{\rho_{m_0}^2 \xi^2}{\rho_{r_0} 8\pi} (1+z)^2$$

MDE

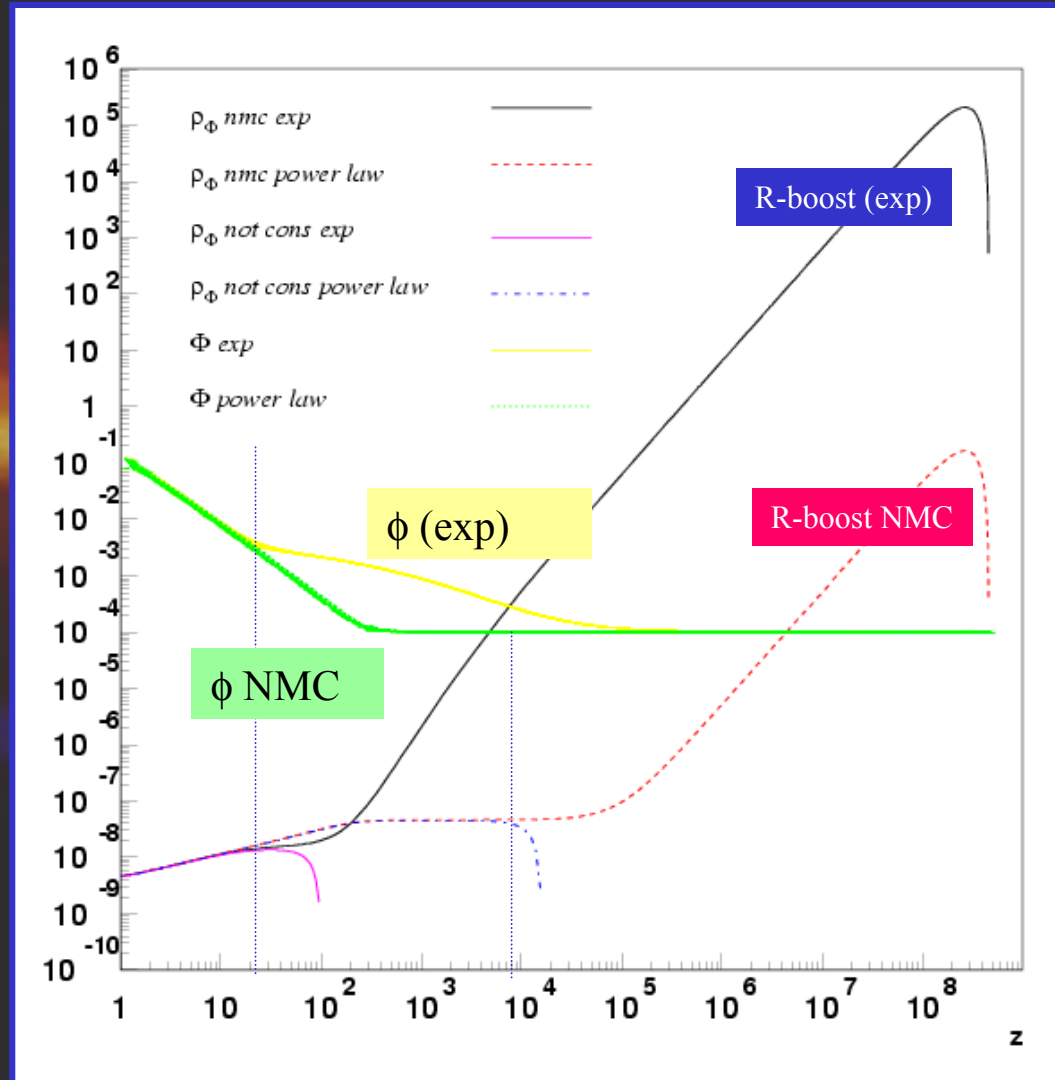
$$a \propto \tau^2$$

$$\phi(\tau) = \frac{3}{16\pi} \xi \log \tau + const$$

$$\frac{1}{2} \dot{\phi}_t^2 = \frac{1}{2} \frac{\dot{\phi}^2}{a^2} = \frac{3}{256\pi} \xi^2 \rho_{m_0} (1+z)^3$$

Independent of  $\phi_{beg}$

# R-boost effects



# Stability

If we look for scaling solutions of the K.G. equation:

$$\rho_\phi \propto a^{-n}$$

when the background is:

$$\rho \propto a^{-m}$$

we find that the R-boost solution is given by:

$$\phi_e = \phi_0 \left( \frac{t}{t_0} \right)^{-\frac{n}{m} + 1}$$

and F  
must be:

$$\frac{F_\phi}{F} = A\phi^B$$

B(m,n) = 0 for  
exp coupling

**$\phi_e$  is an  
attractor**

# Conclusions

- The coupling generates a purely gravitational effect called R-boost.

- The R-boost dynamics is the most relevant effect during the initial motion of the field, dominated by kinetic energy.


- The R-boost is an attractor, independently of  $V$ , that restores a large basin of attraction even if the true potential is flat.

- The exponential coupling gives a stronger effect than the power law NMC model both on  $\rho_\phi$  and on  $\phi$ .

- The exponential coupling, of dilatonic-inspiration, is the simplest expression for the coupling to give scaling solutions to K.G. equation.



# Extended Quintessence with exponential coupling



DESY Theory Workshop 2004  
28th Sept – 1st October  
DESY Hamburg