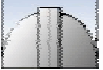


# Small Scale Structure and Cold Dark Matter



**Matthias Steinmetz (AIP)**



**AIP**



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# Outline

- Small scale structures as a test of cosmological models
- Density profiles of dark matter halos
- Shapes of dark matter halos
- Substructure of dark matter halos
  - ◆ abundance
  - ◆ accretion rates
- Summary and conclusion

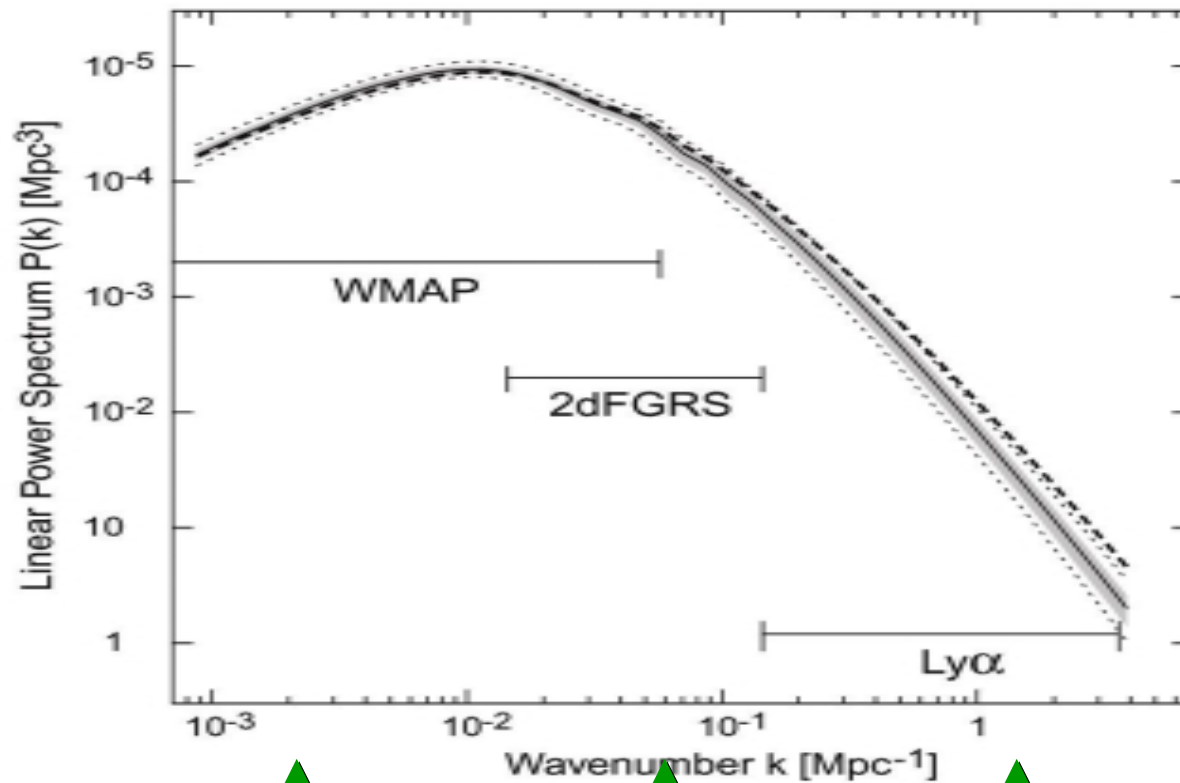
# Cosmology after WMAP



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Cosmic  
Microwave  
background

Large-Scale  
Structure

Quasar  
Absorption  
Lines

Substructure  
in the Galaxy

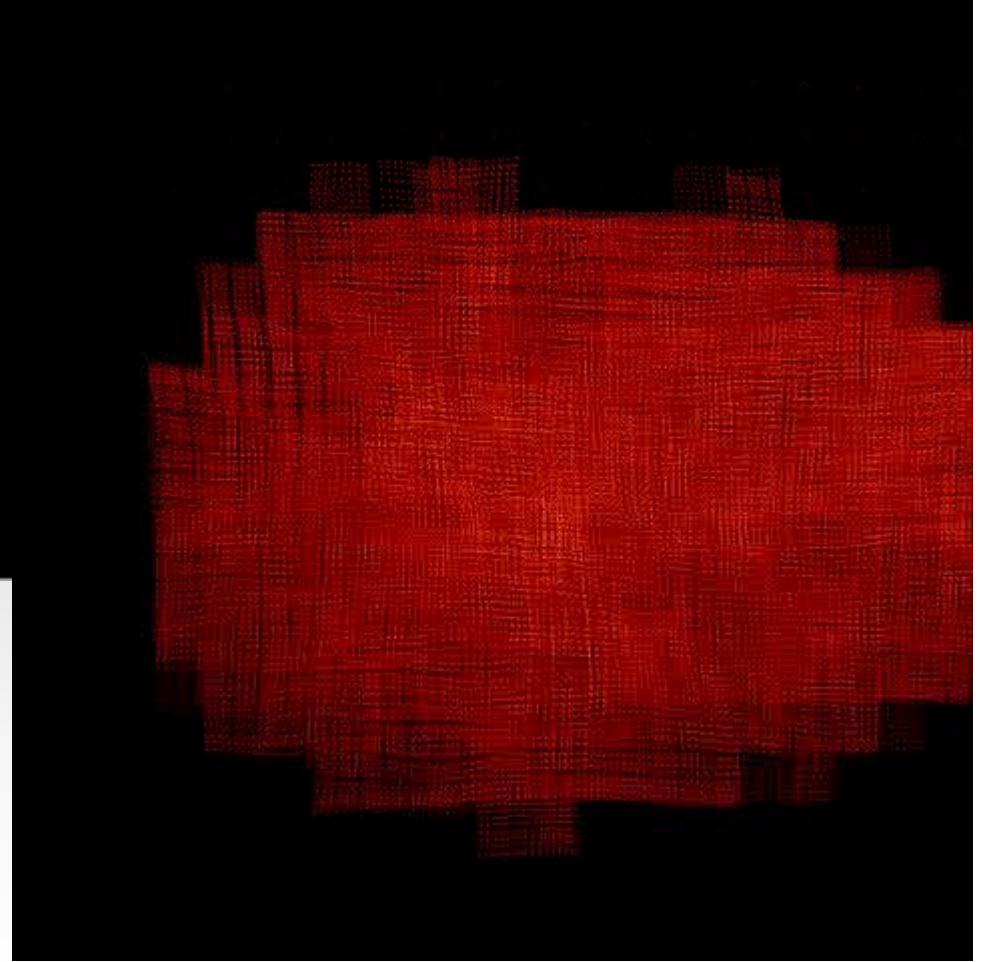


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# Structure formation by gravitational instability





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# Formation of the Milky Way: what do the textbooks say ...

## ■ The Milky Way formed 10 billion years ago

- ◆ the disk is thin ⇨ substantial accretion
- ◆ the oldest thin disk stars >10 billion years old
- ◆ rotational support, ordered motion ⇨ mixed up by mergers

## ■ however

- ◆ many disks are warped and/or lopsided (>50%?)
- ◆ difficult to create long-living features



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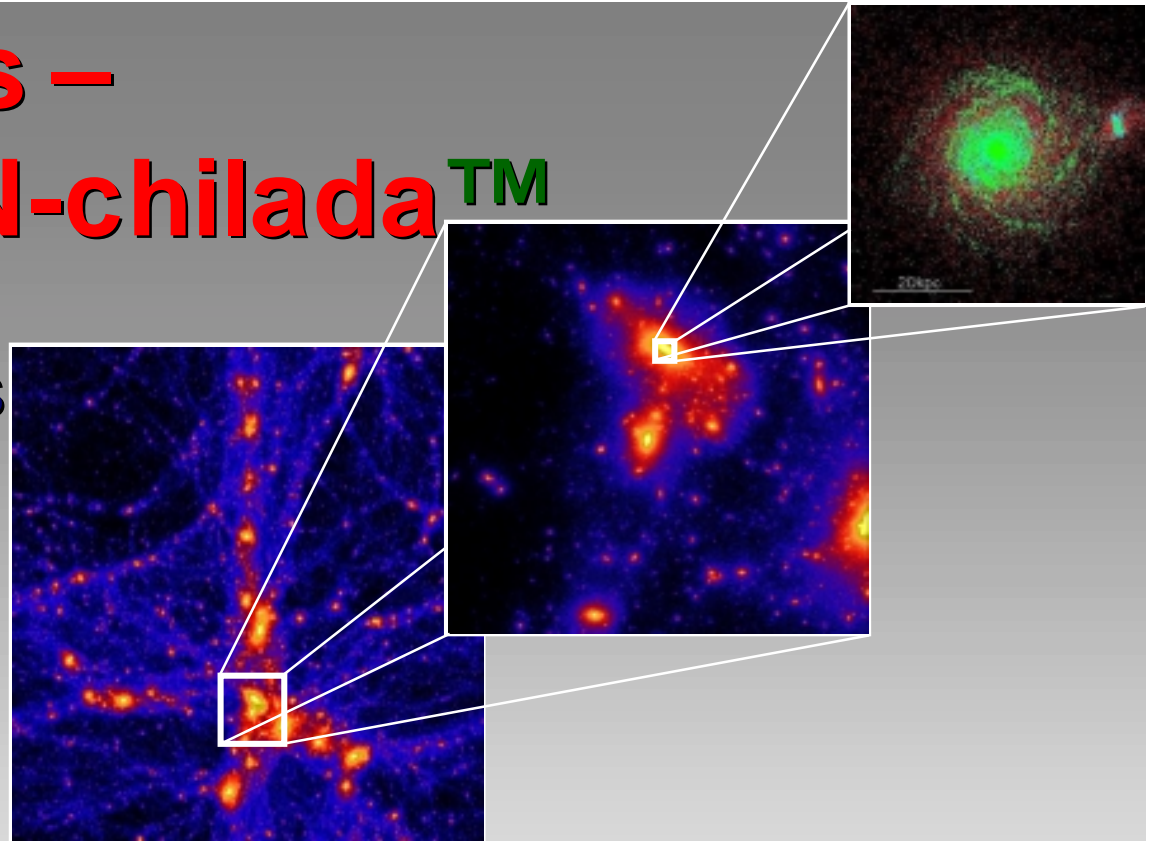
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# Simulations – the whole N-chilada™

- re-simulate individual halos at much higher resolution

- ◆ dark matter, stars: **N-body**
- ◆ gas: **SPH**
- ◆ including gas physics
  - radiative cooling processes
  - heating due to photoionizing UV background
  - star formation: **phenomenological recipes**
  - feedback due to supernovae, stellar winds etc.
  - metal enrichment
- ◆ tidal forces of the environment



™: George Lake

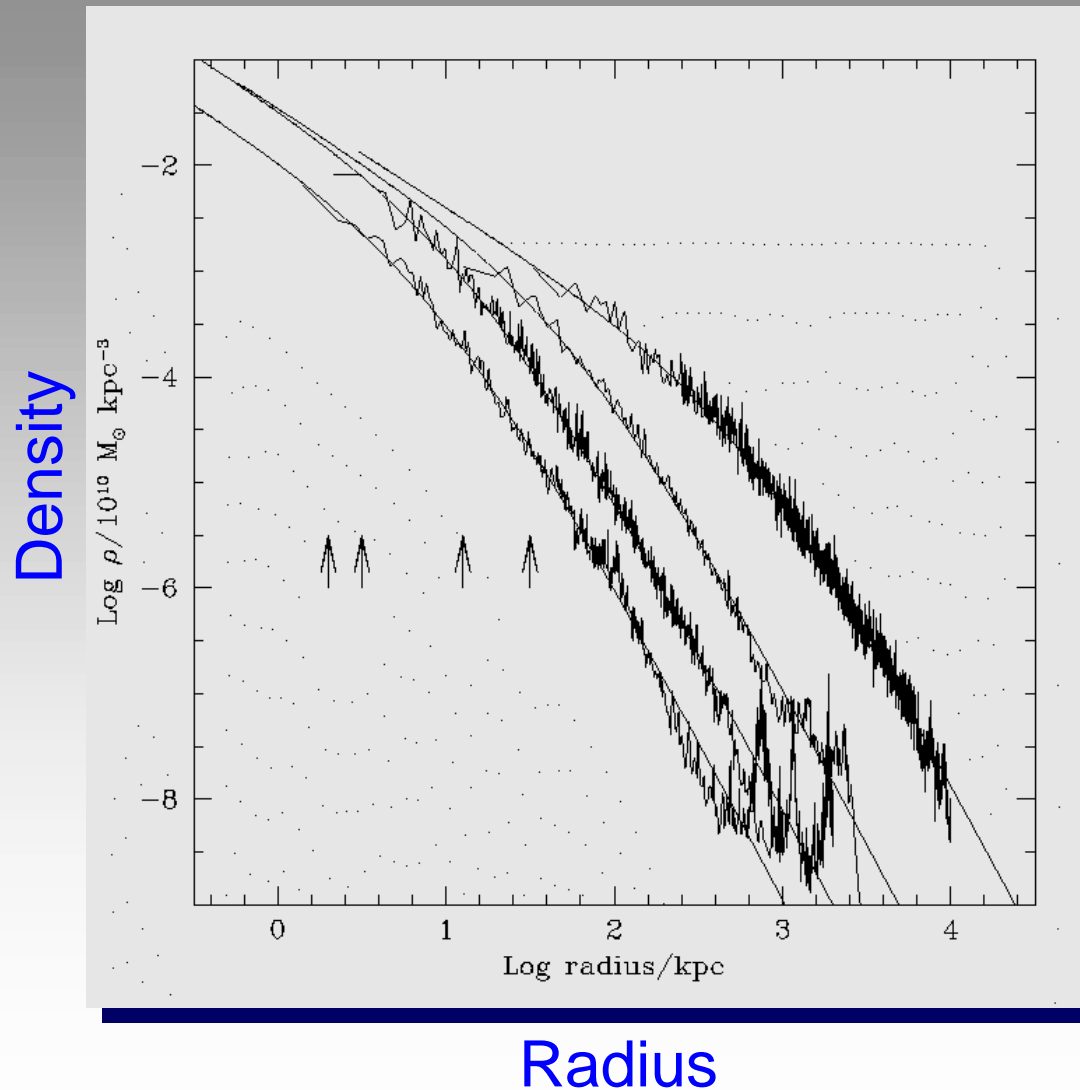


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# The Density Profile of Cold Dark Matter Halos



- Mass profiles of dark halos are independent of halo mass and cosmological parameters

$$\frac{\rho(r)}{\rho_{crit}} = \frac{\delta_c}{(r/r_s)(1+r/r_s)^2}$$

Navarro, Frenk &  
White 1997

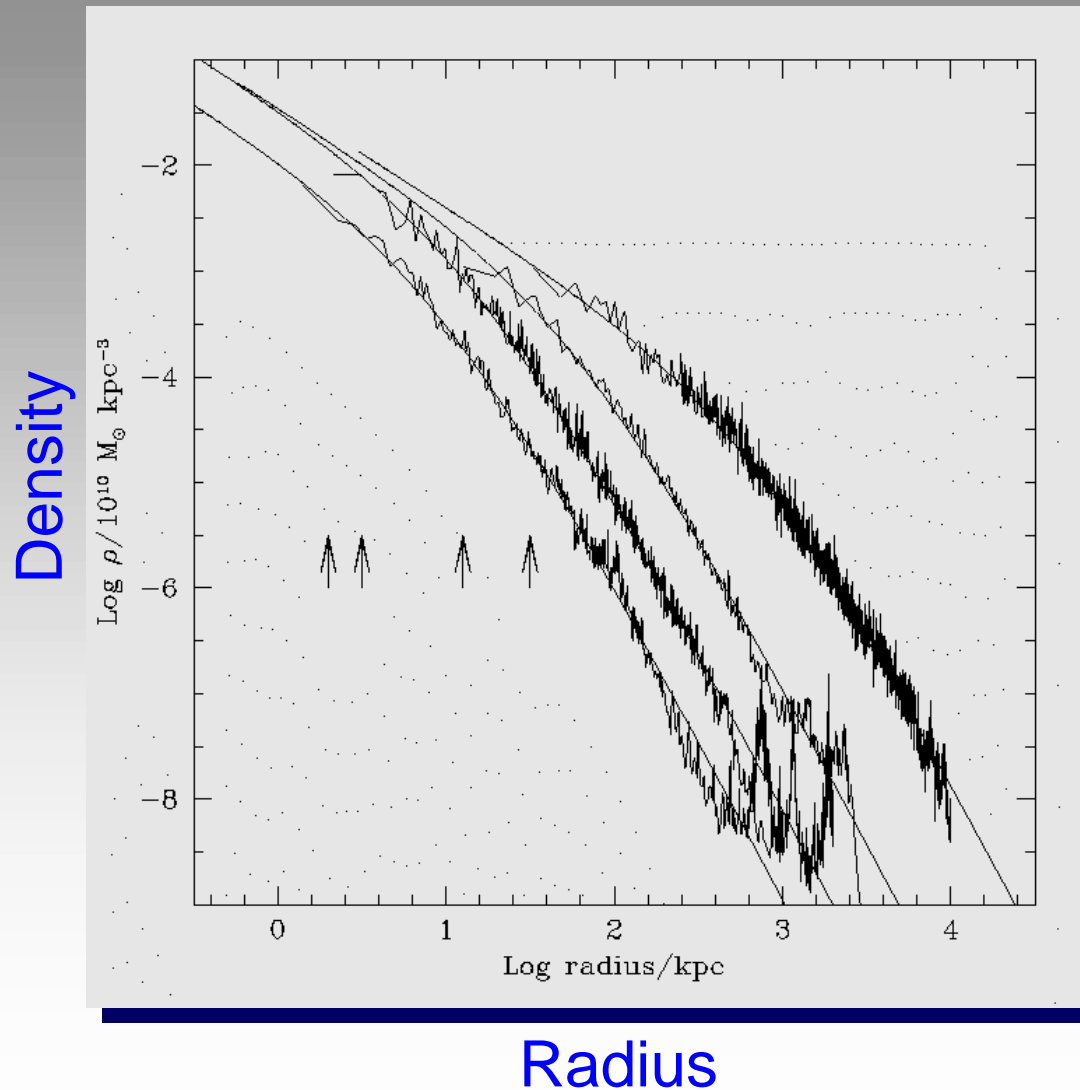


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# The Density Profile of Cold Dark Matter Halos



- There is no obvious density 'plateau' or 'core' near the center
- The profile is shallower than isothermal near the center
- How much shallower?
  - NFW: -1
  - Moore: -1.5

Navarro, Frenk &  
White 1997





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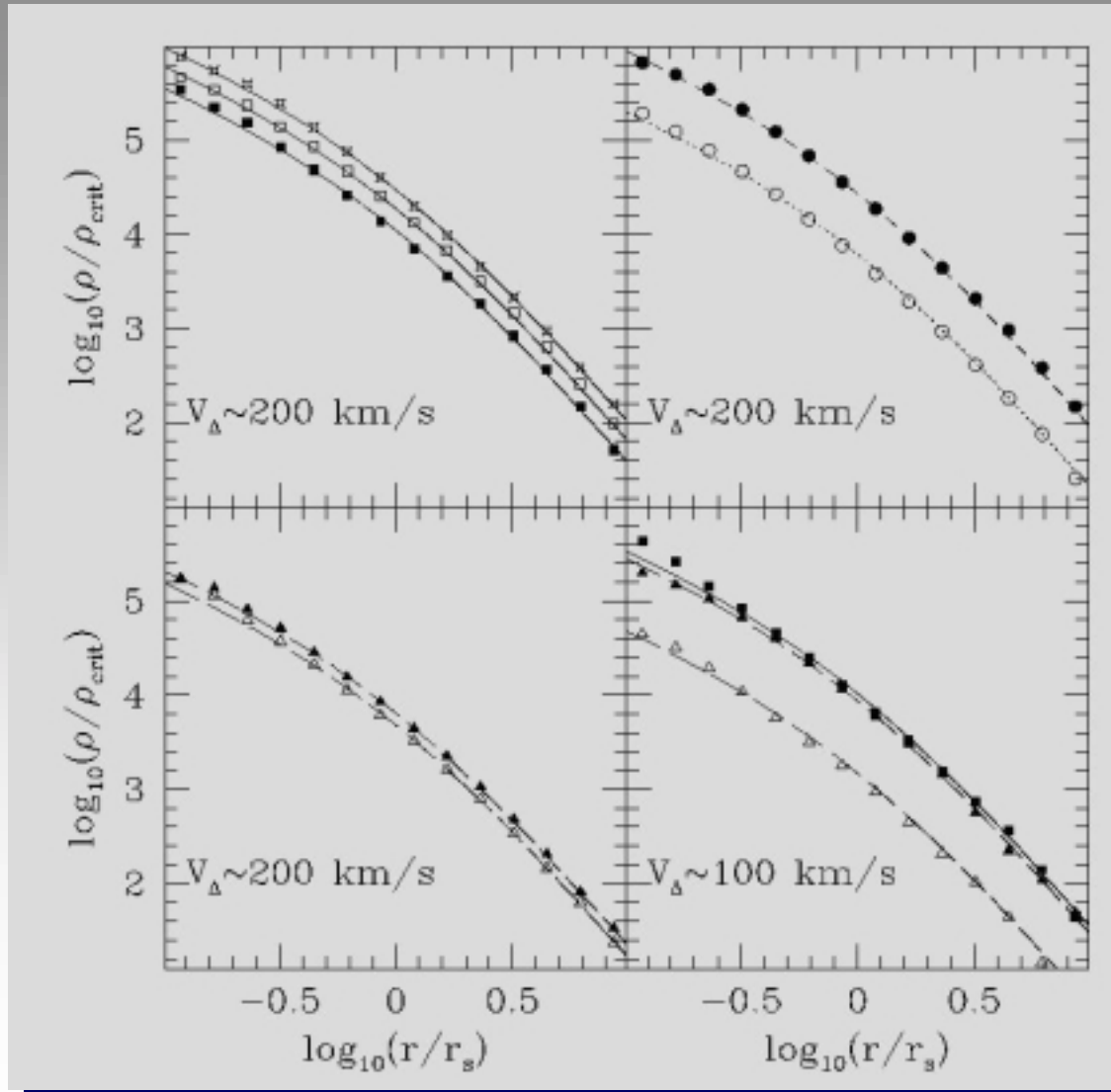
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# Halo profiles for different CDM and WDM cosmologies

$\sigma_8$

WDM



$\Gamma$

$V_c$

Eke, Navarro &  
Steinmetz 2001

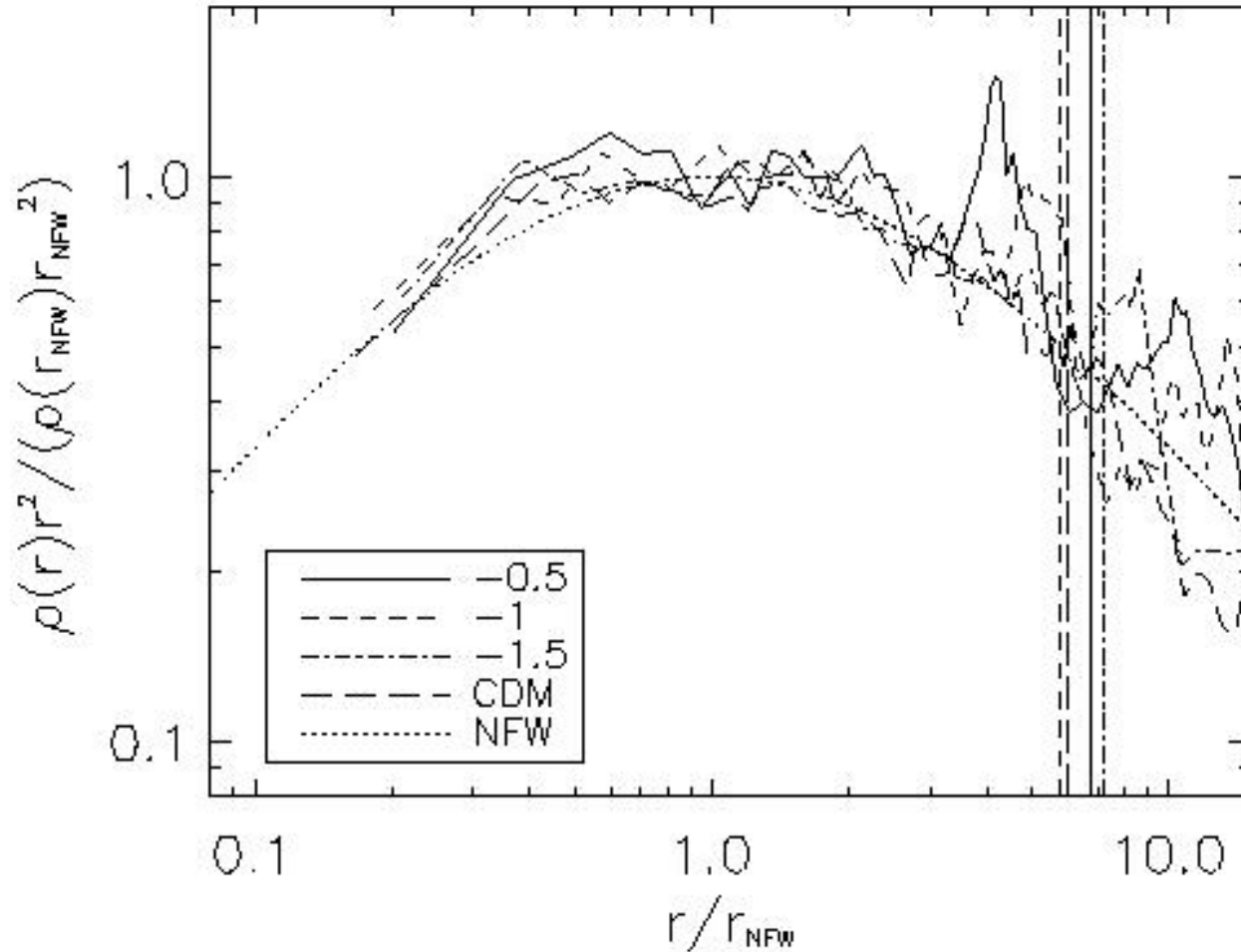


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# Halo profiles for non-hierarchical models



Huss, Jain & Steinmetz 1999 10

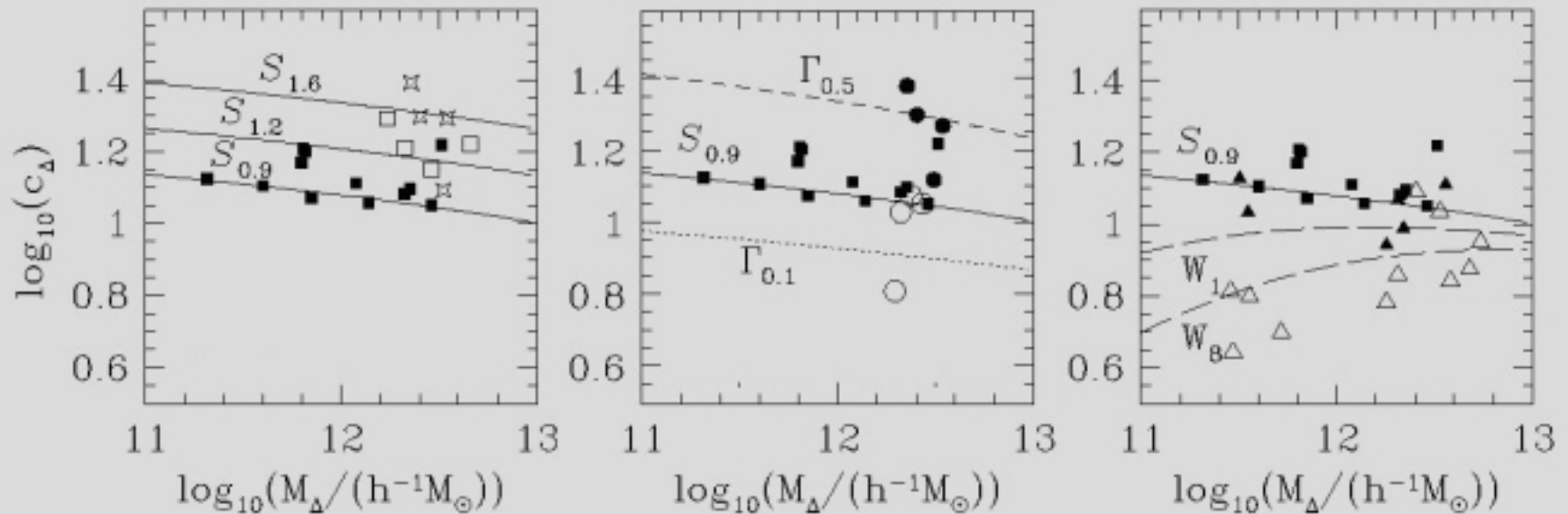


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# Halo concentration vs cosmological parameters



$\Rightarrow$  for CDM-type models:  $c=R_{\text{vir}}/R_s \approx 10$   
for galaxy halos

Eke, Navarro &  
Steinmetz 1999 11

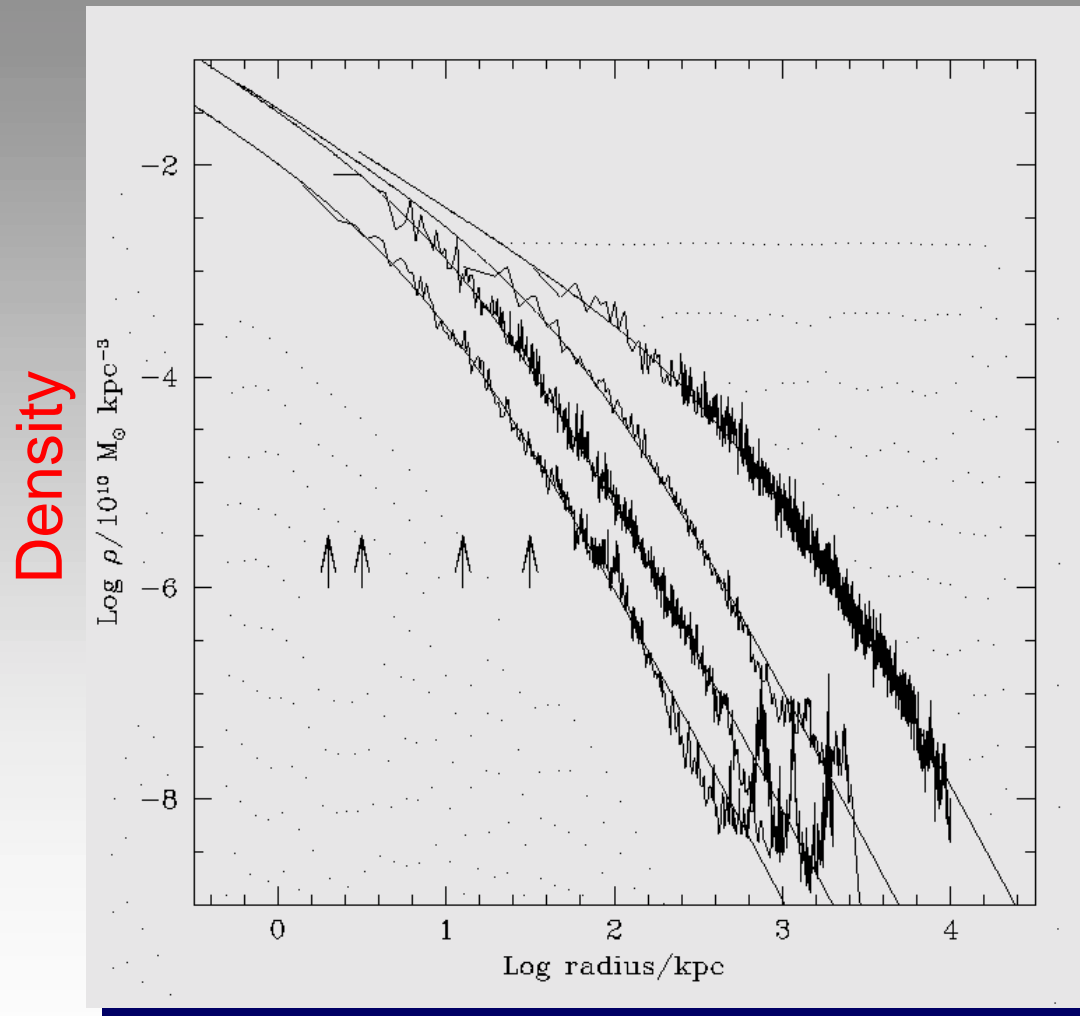


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# The Density Profile of Cold Dark Matter Halos



Radius

Halo fitting  $\rightarrow$  two parameters:

- Circular velocity  $v_c$
- Concentration  $c = R_{\text{vir}}/R_s$
- Cosmology ( $\Omega$ ,  $\Lambda$ ,  $\sigma_8$ , power spectrum) determines  $c$

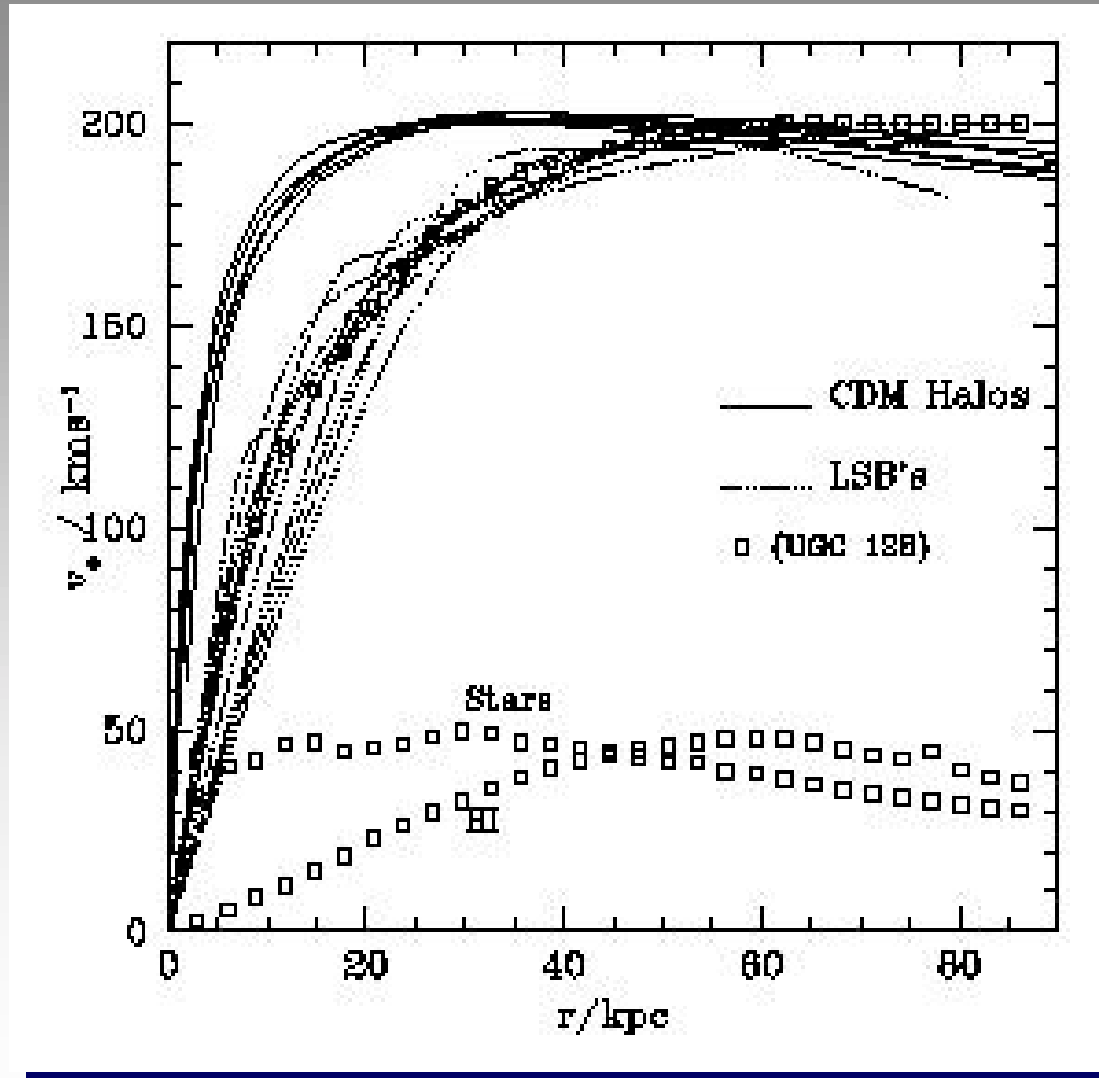


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# Constraint: Rotation Curves of low surface brightness galaxies (LSBs)



Moore et al. 1999

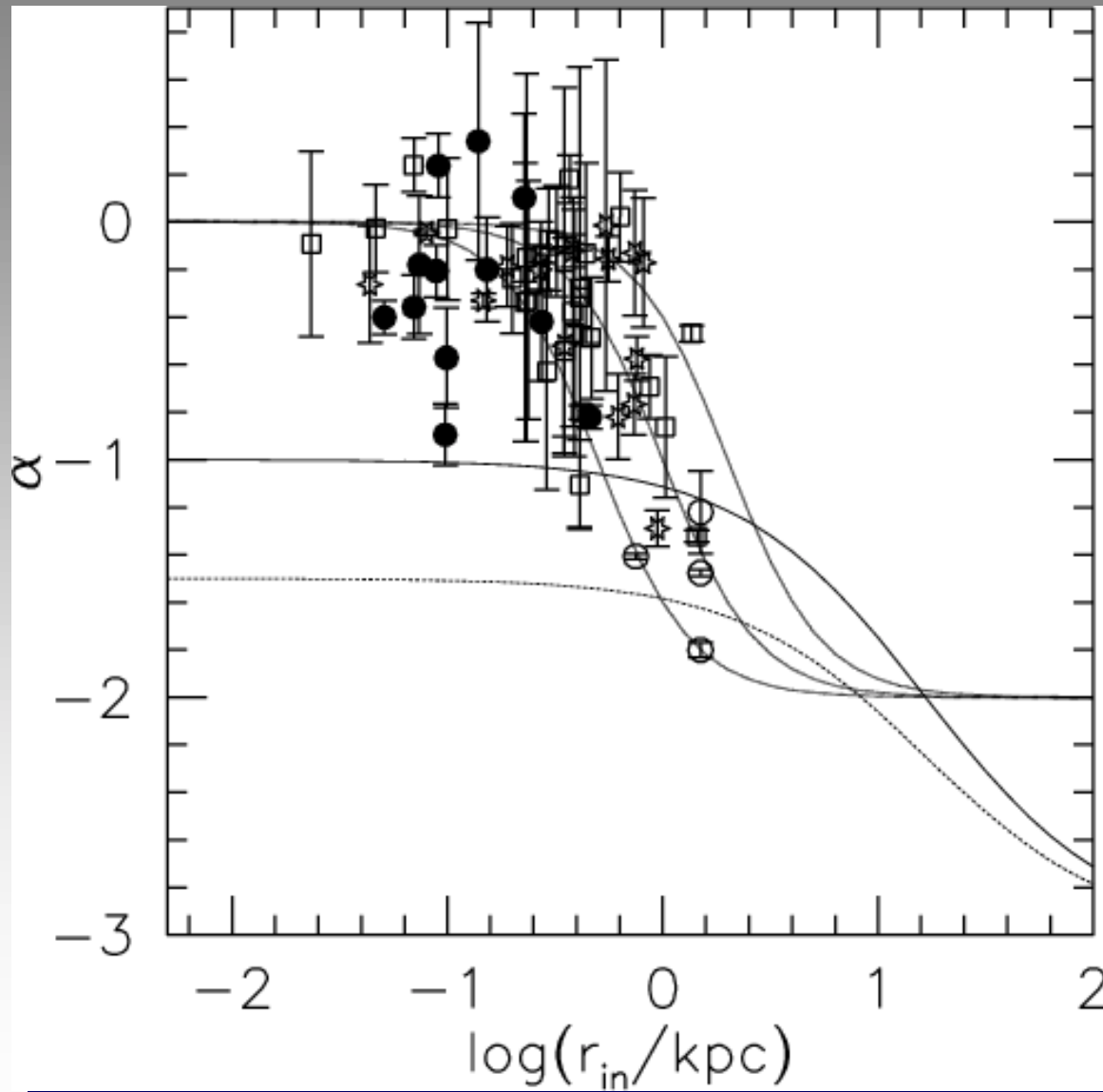


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# Dark matter profiles of LSBs



**LSBs seem  
to have  
cores**



**CDM halos**

McGaugh et al. 2002



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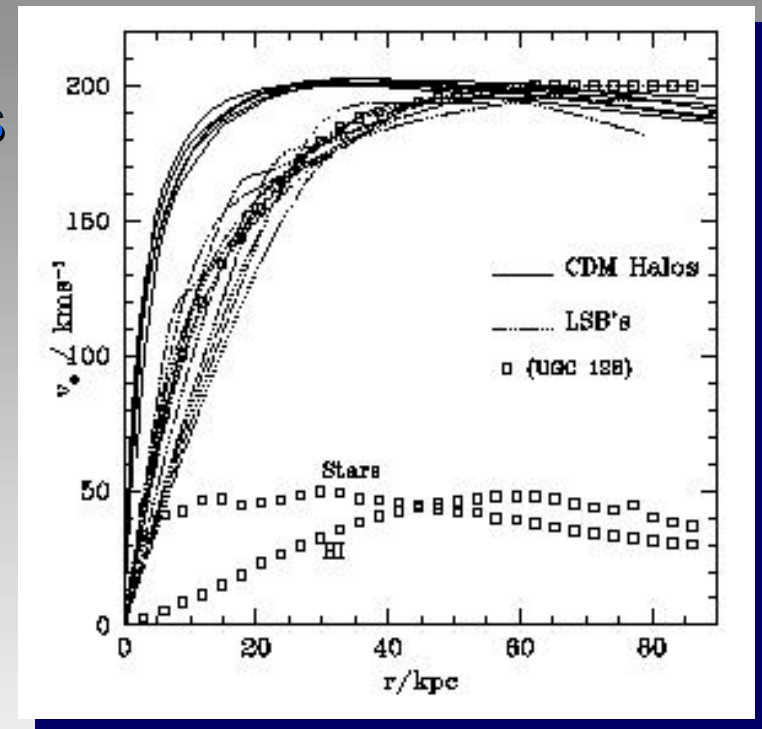
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# LSB rotation curves vs cusps

## ■ Some caveats:

- ◆ Strictly, the disagreement is between **gas rotation speeds** and **halo circular velocities**.
- ◆ The two may differ if:
  - halo is not spherical
  - velocity dispersion of the gas or disk thickness is important
  - there are departures from equilibrium.
- ◆ The disagreement reported so far is with **fitting formulae**, not with the **actual structure** of simulated CDM halos: simulating dwarf halos at high resolution is hard.





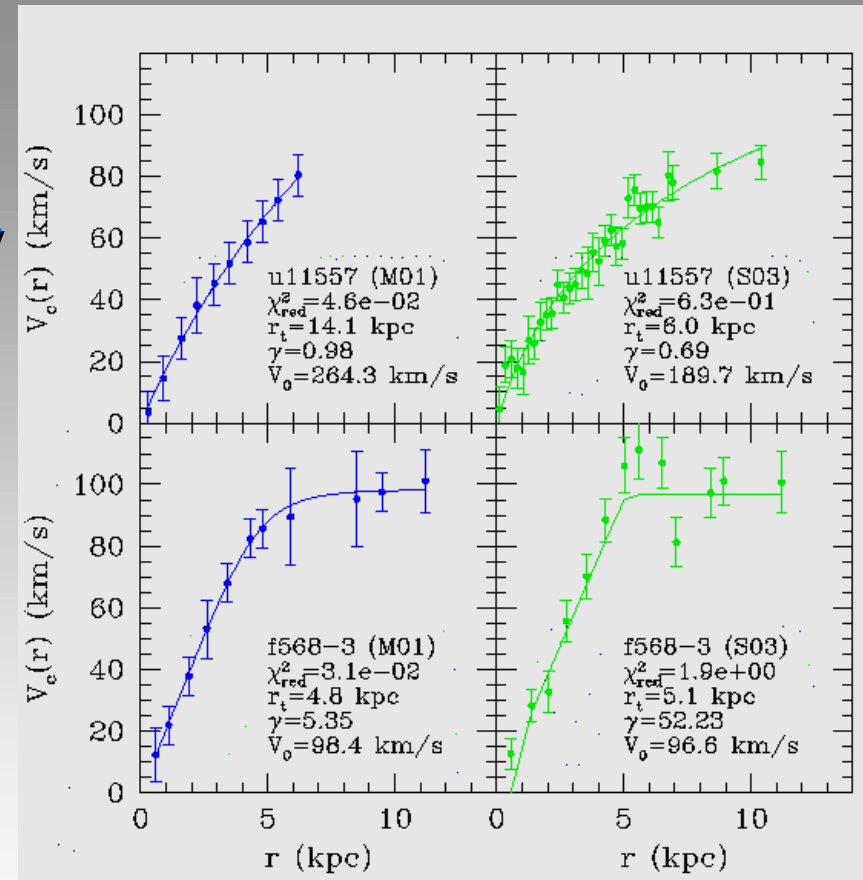
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# LSB rotation curves vs cusps

- More caveats:
  - ◆ Early HI rotation curve datasets were spuriously affected by **beam smearing**. The situation has improved with the H-alpha observations
  - ◆ Some disagreements between observers remain, as does some **ambiguity** in the interpretation of published data.



McGaugh et al

Swaters et al



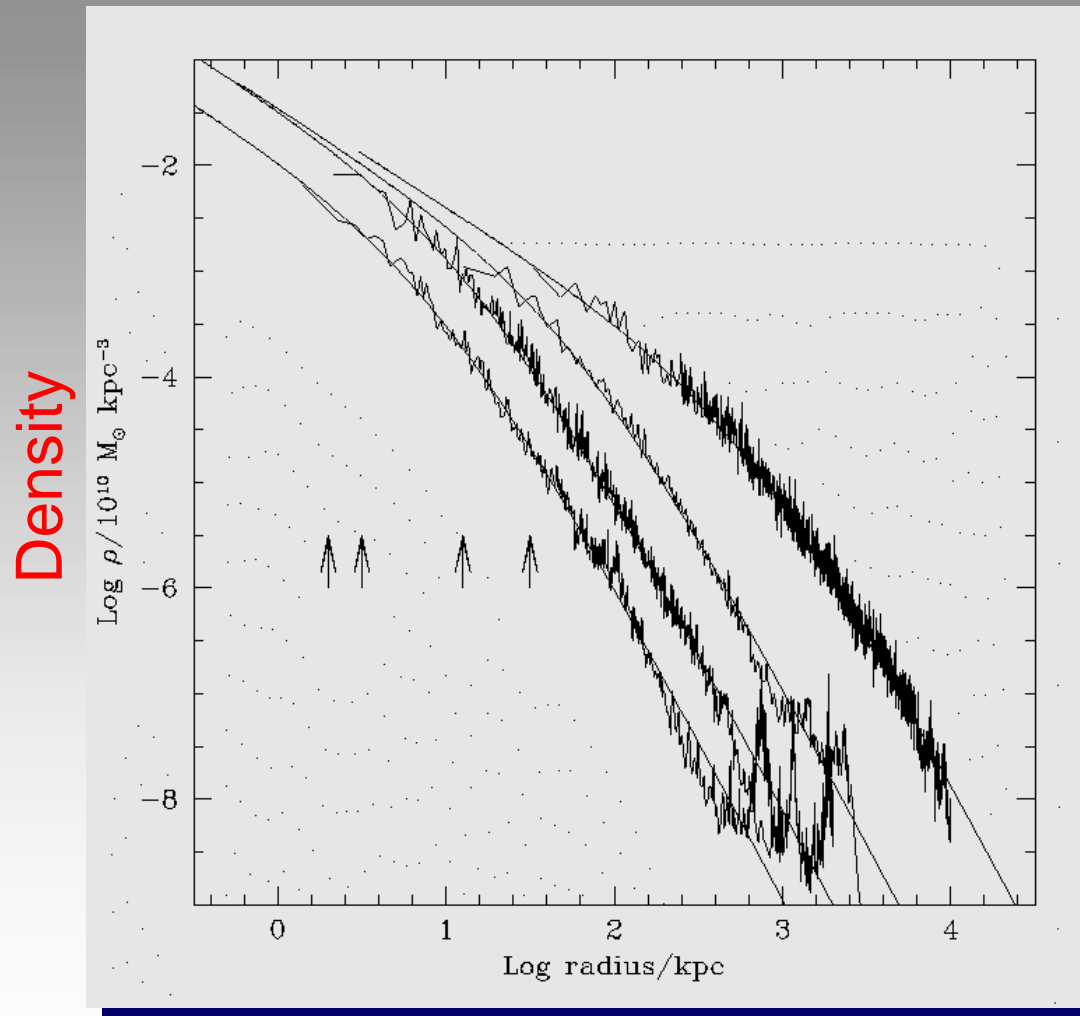


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# The Density Profile of Cold Dark Matter Halos



Radius

- Halo fitting → two parameters:
- Circular velocity  $v_c$
  - Concentration  $c = R_{\text{vir}}/R_s$
  - Cosmology ( $\Omega$ ,  $\Lambda$ ,  $\sigma_8$ , power spectrum) determines  $c$



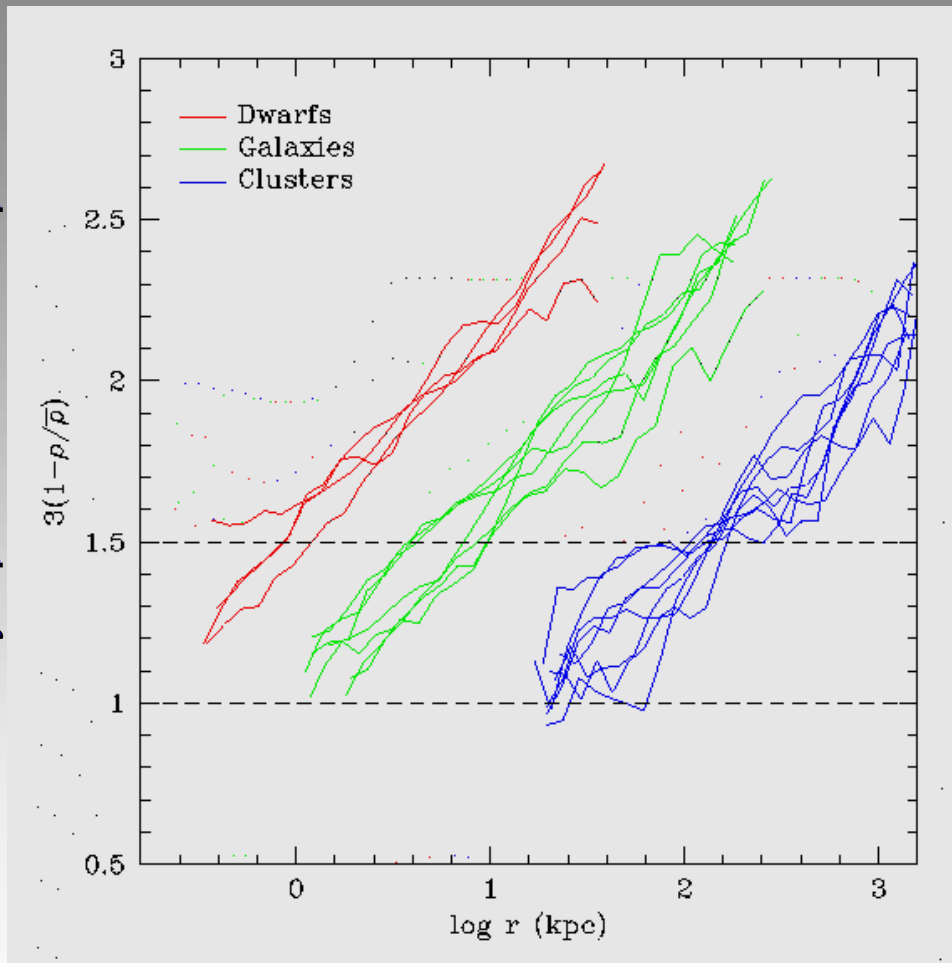
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# Recent results for $\Lambda$ CDM halos

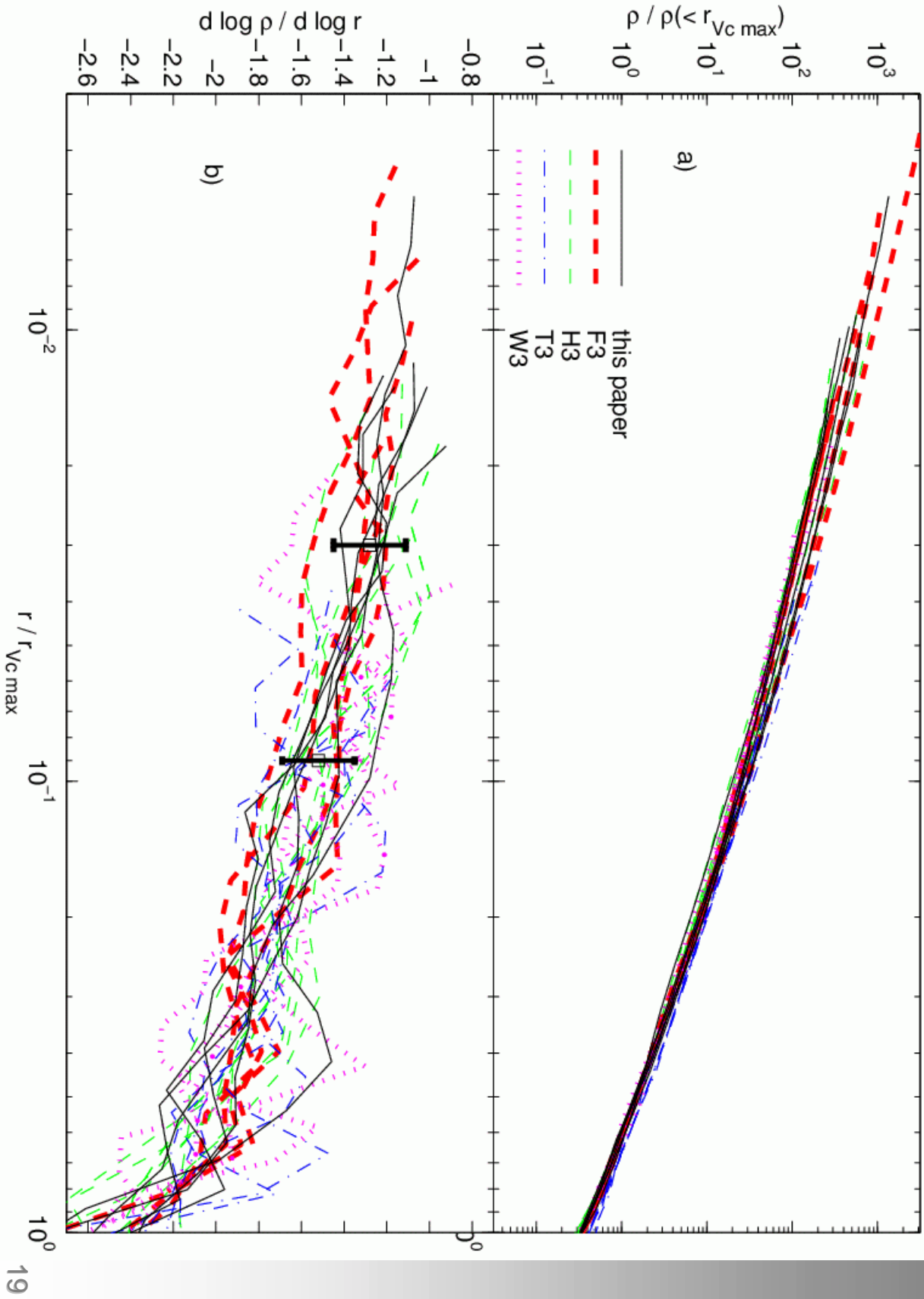
Maximum Asymptotic Inner Slope

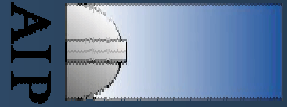


Radius

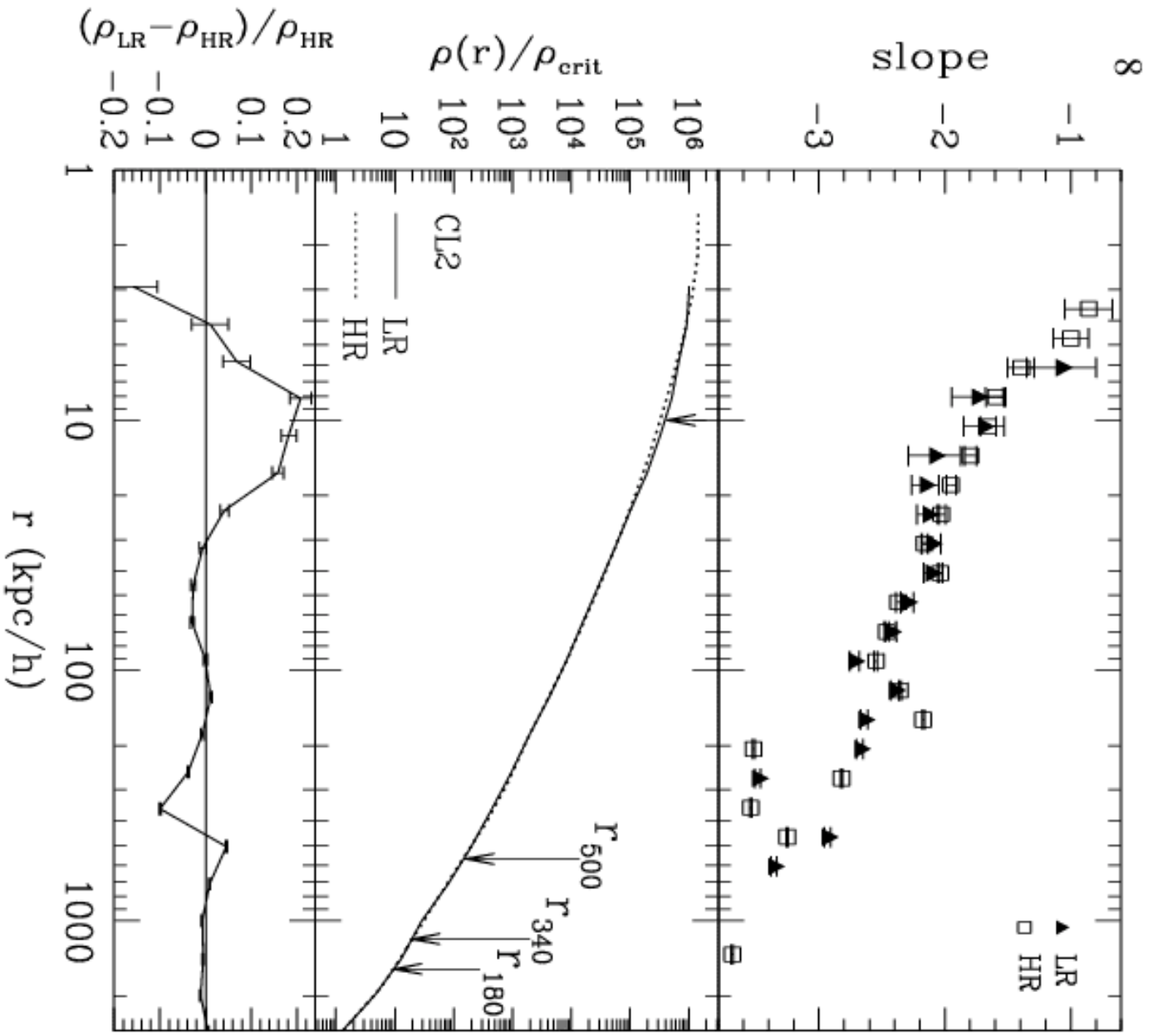
- The total mass enclosed within a given radius is robustly measured in the simulations.
- Combined with the local density, it may be used to derive an upper limit to the inner asymptotic logarithmic slope
- No obvious convergence to a power law

Hayashi, et al 2003





# Gottloeber et al



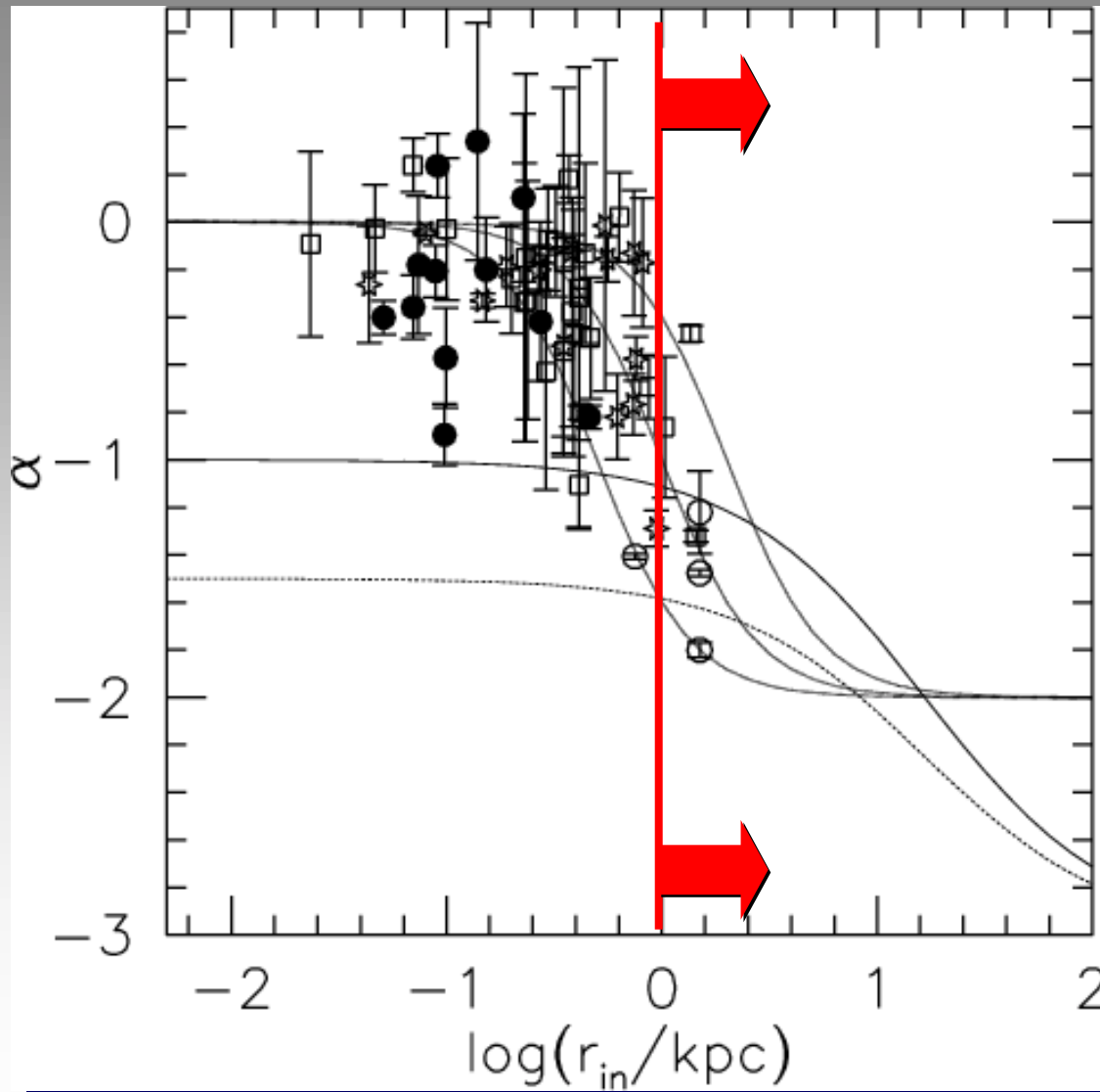


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# Dark matter profiles of LSBs



**LSBs seem  
to have  
cores**



**CDM halos**

**???**

McGaugh et al. 2002

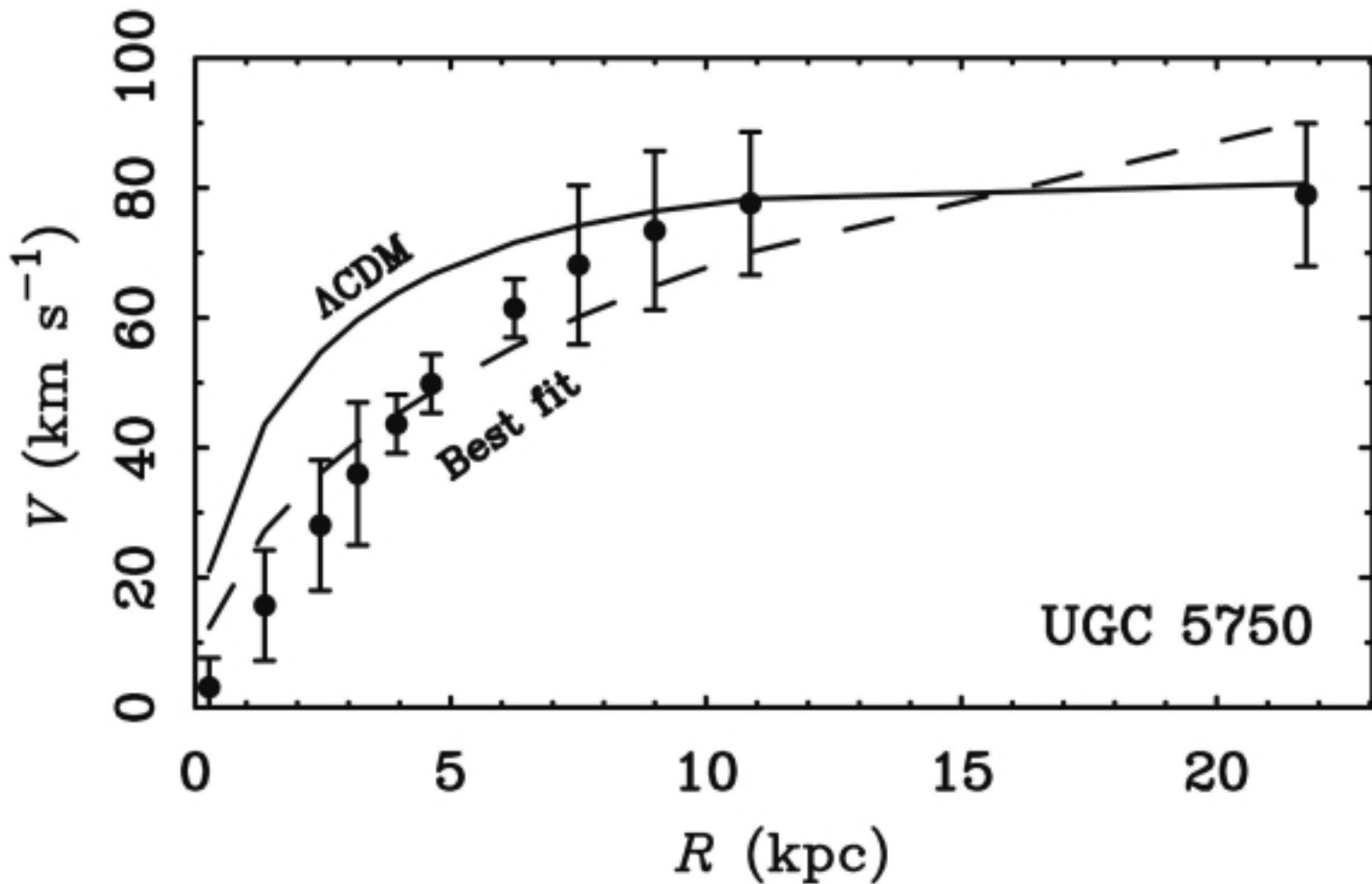
# Concentration as inferred from LSBs



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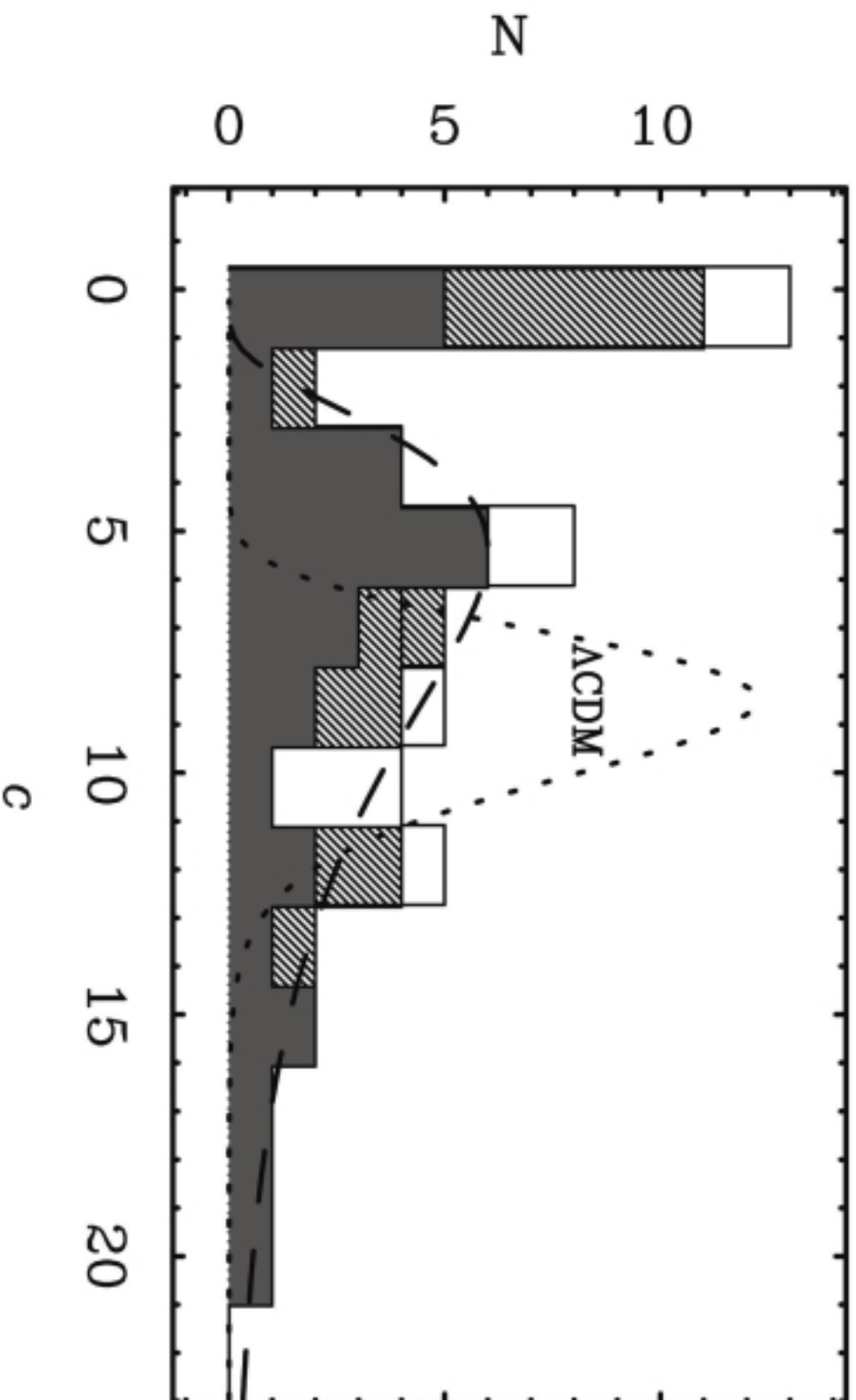
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⇒ best fit:  $c \approx 2$  ⇔  $c \approx 10$  (CDM) McGaugh et al. 2002

# LSBs Concentration as inferred from





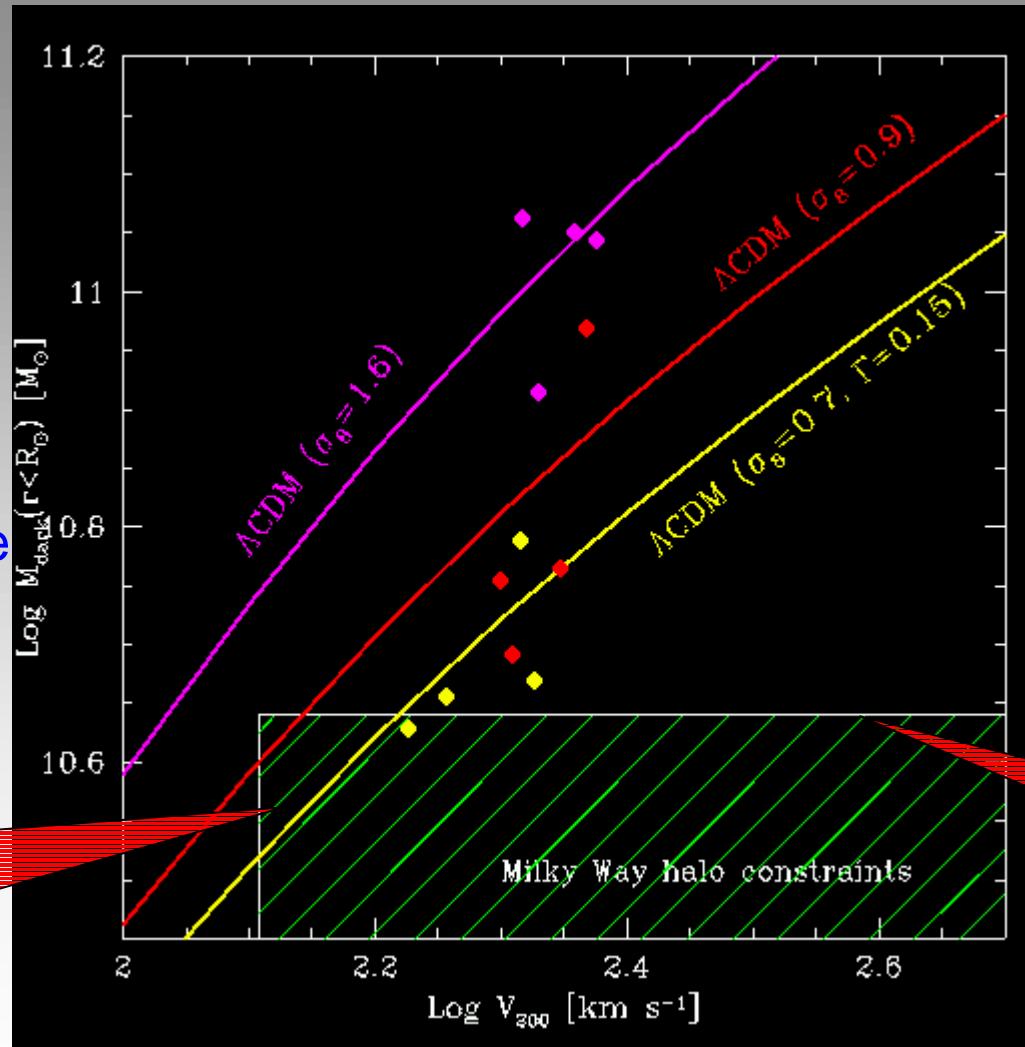
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# Dark Matter in the Milky Way

Dark Mass  
within the  
Solar Circle



MW  
dynamics  
 $\Rightarrow c \leq 10$

Constraint from  
universal  
baryon  
fraction

Dark mass  
constraint  
from Oort limit

Halo Mass (Circular Velocity)

Eke, Navarro  
& Steinmetz 2000



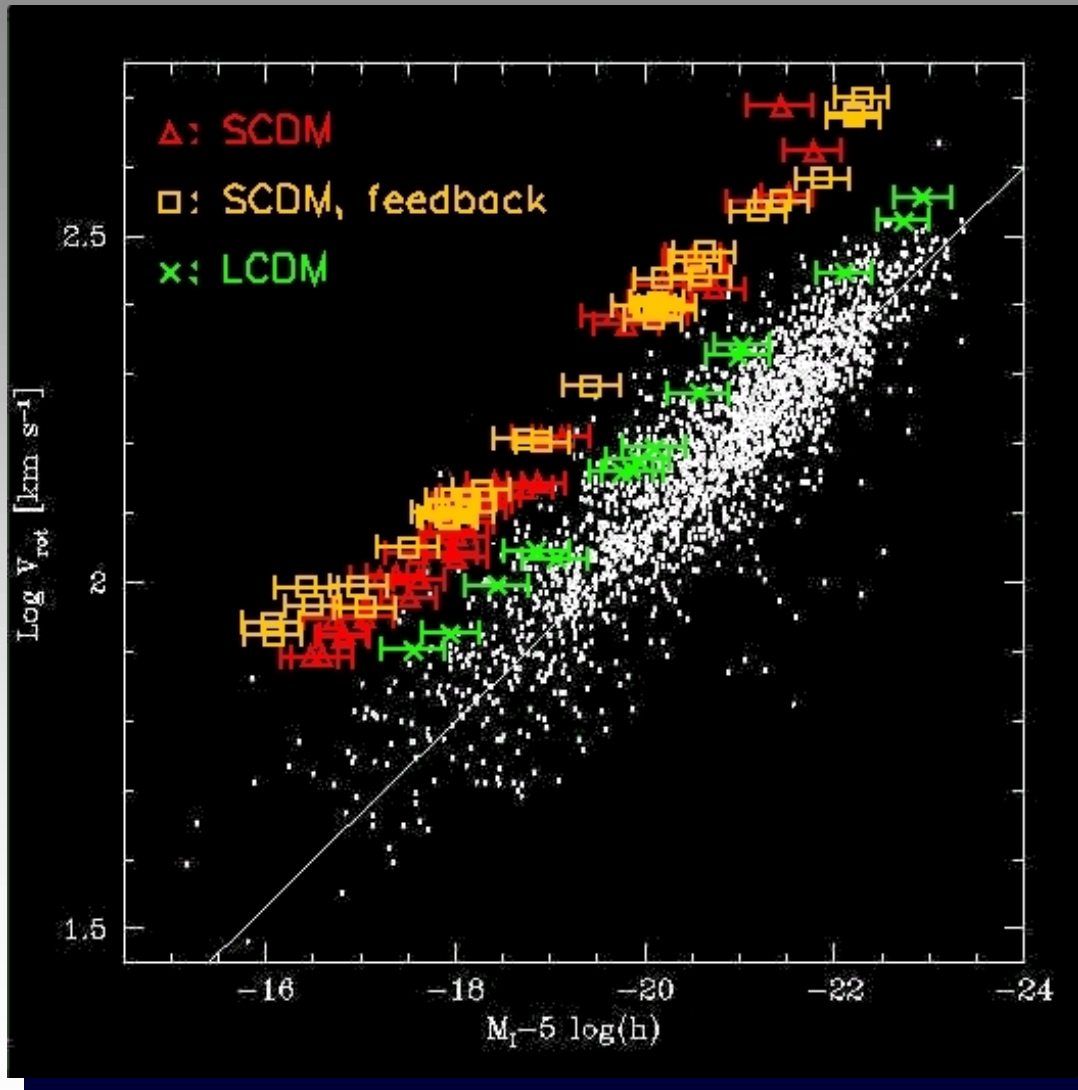


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# The Tully-Fisher Relation



Zero-point of  
Tully-Fisher  
relation  
 $\Rightarrow c \leq 10$

Eke, Navarro &  
Steinmetz 2001

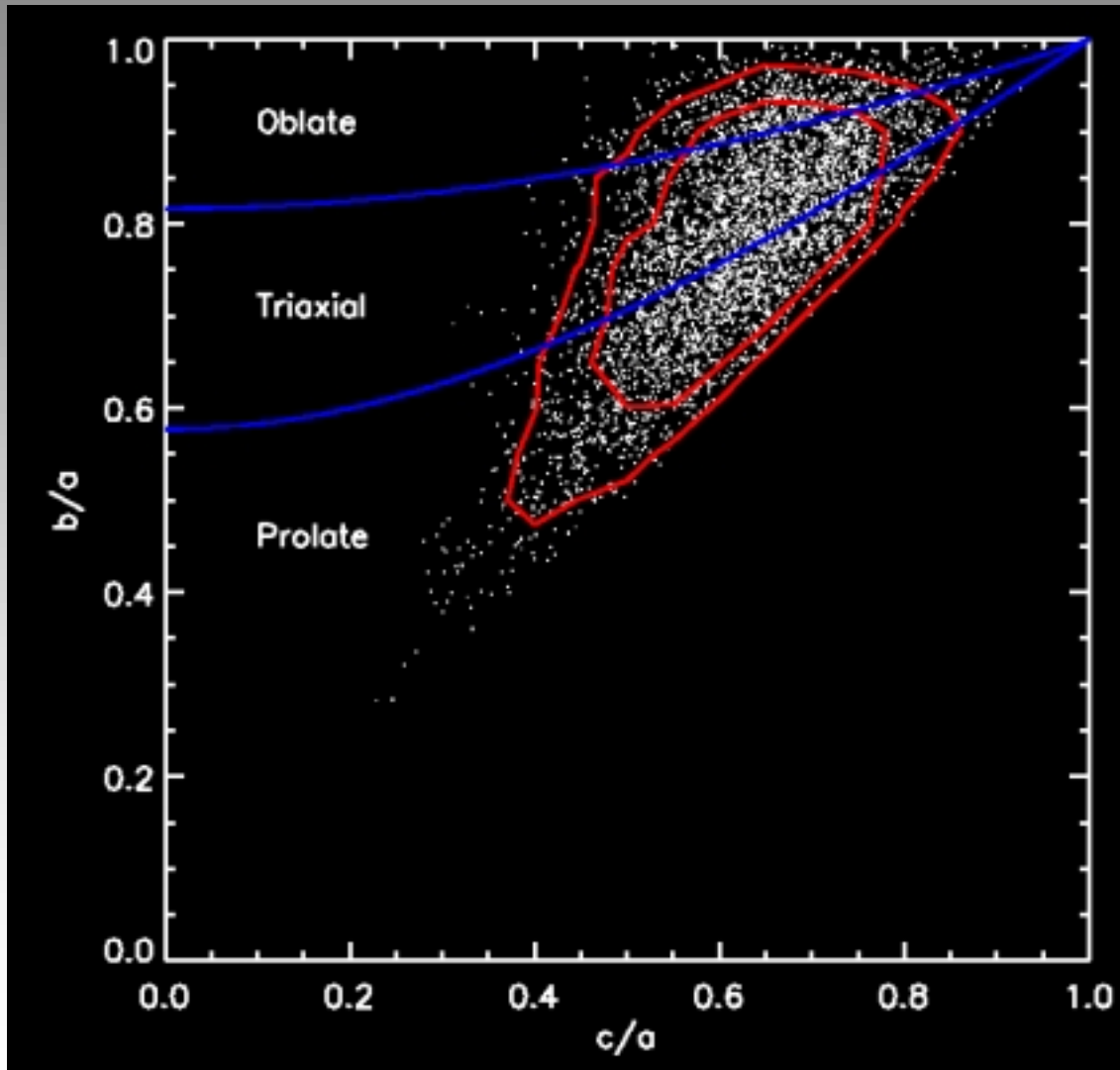


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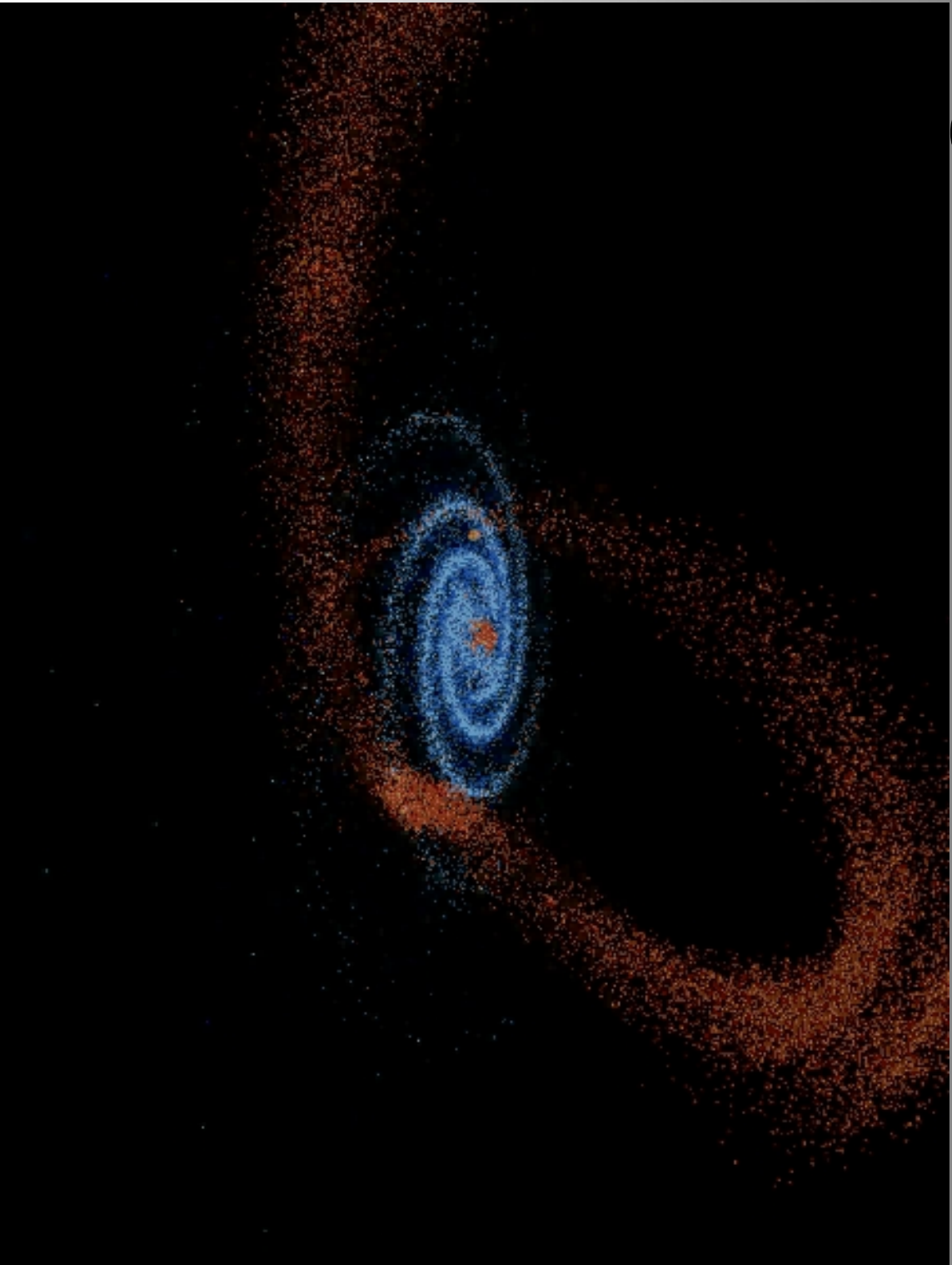
# Shapes of Dark Matter Halos



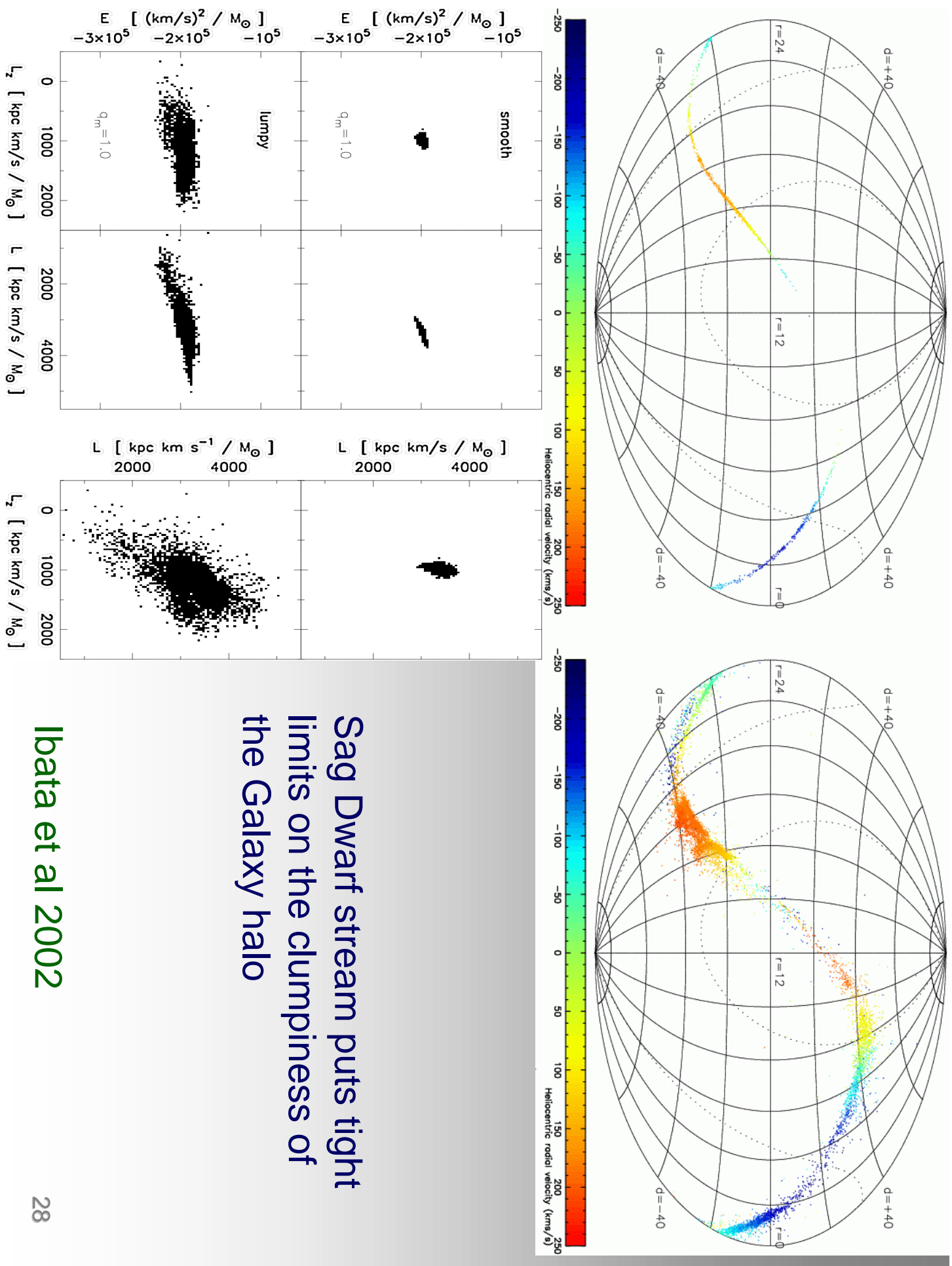
- Mostly prolate or triaxial

Bailin & Steinmetz 2004

# Sagittarius Dwarf

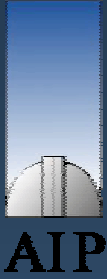


Majewski et al. 2003

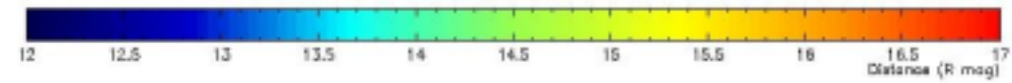
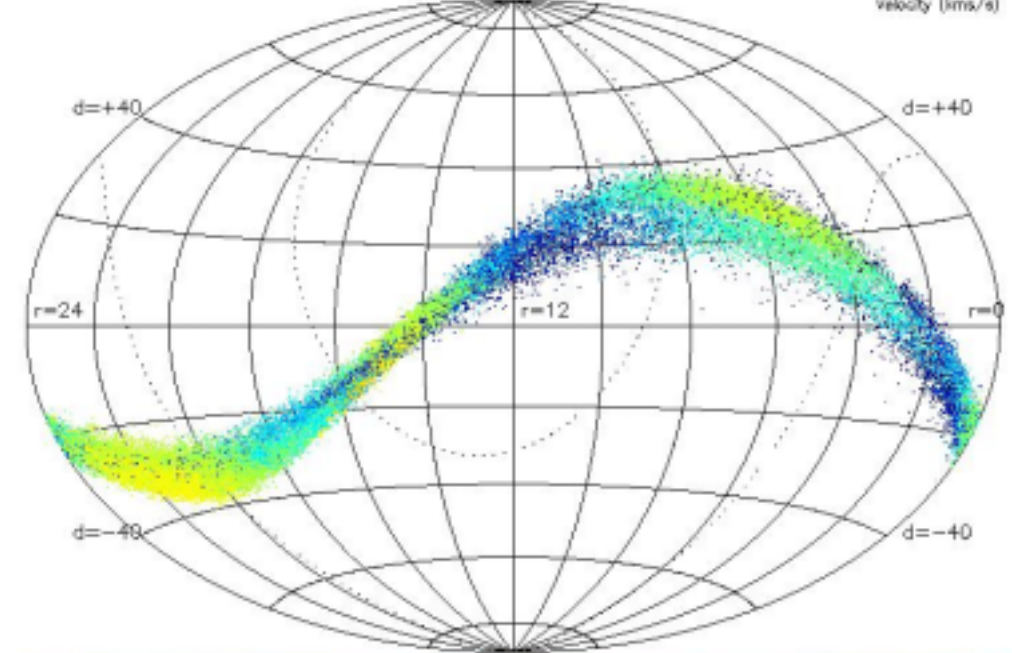
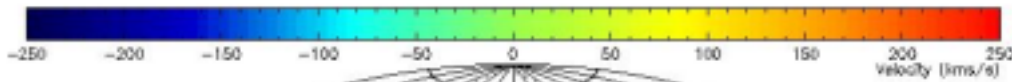
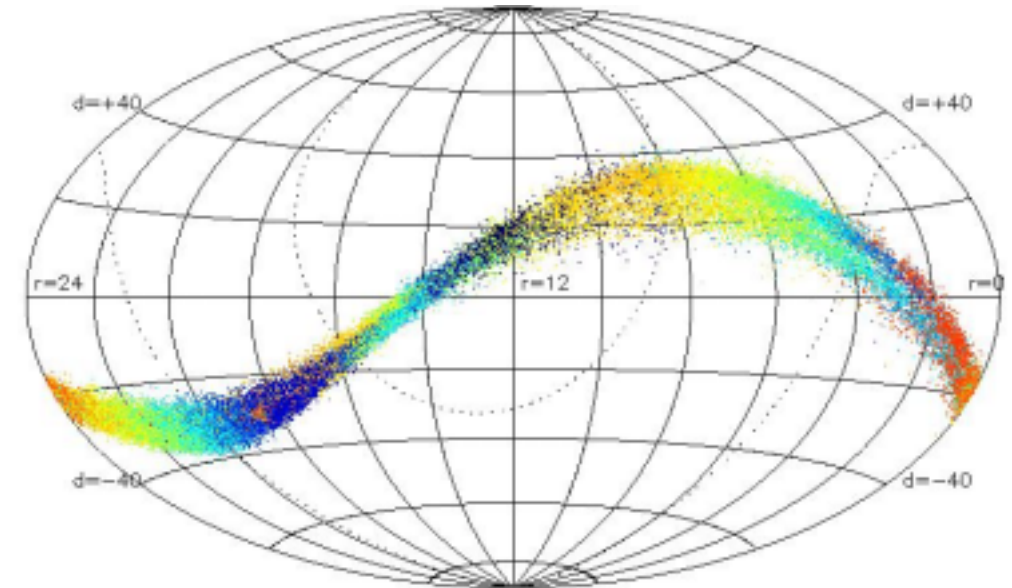


Sag Dwarf stream puts tight limits on the clumpiness of the Galaxy halo

Ibata et al 2002



VELOCITIES



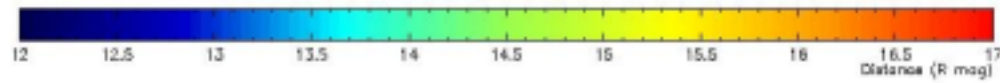
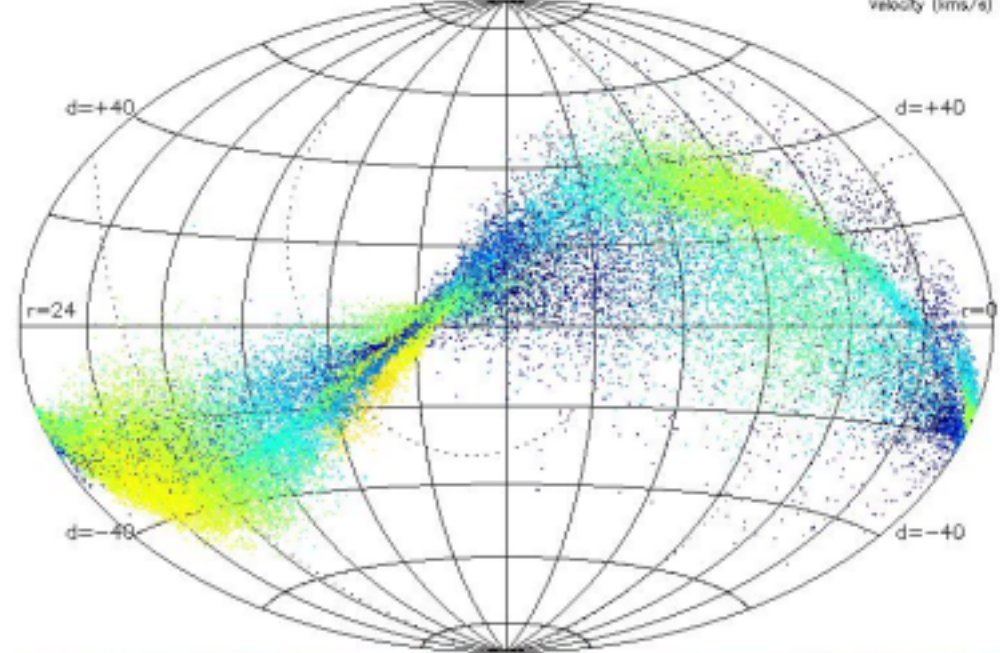
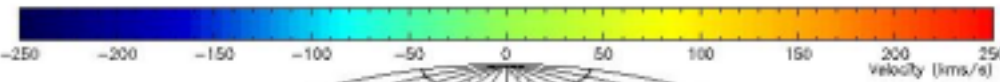
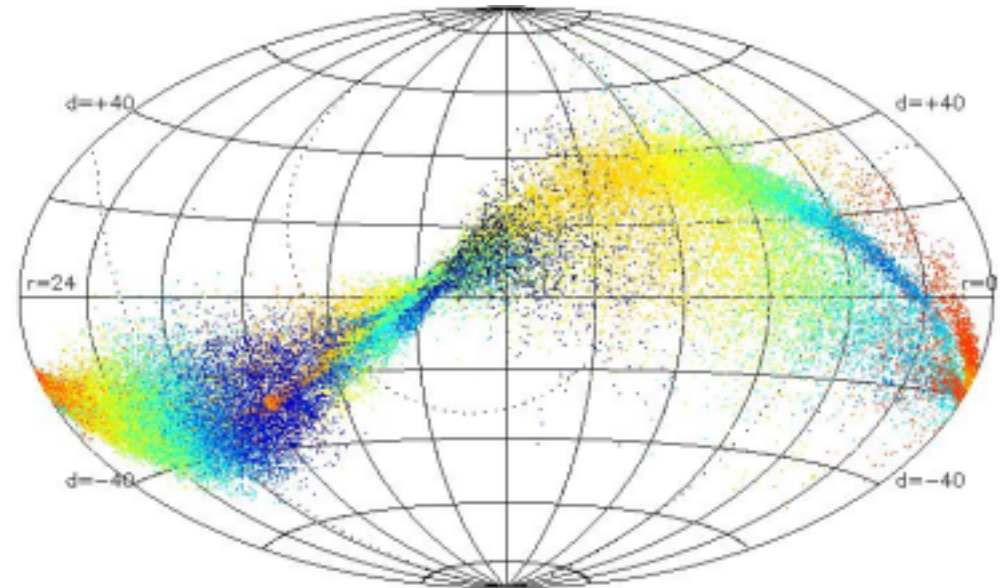
$$q_m = 1.0$$

$$v_c = 220 \text{ km/s}$$

Sag Dwarf stream  
puts tight limits on  
the flattening of the  
Galaxy halo



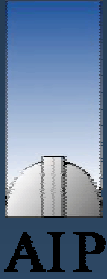
VELOCITIES



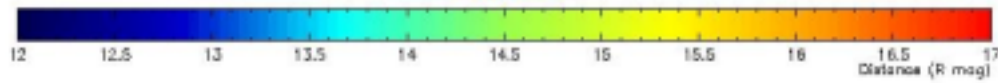
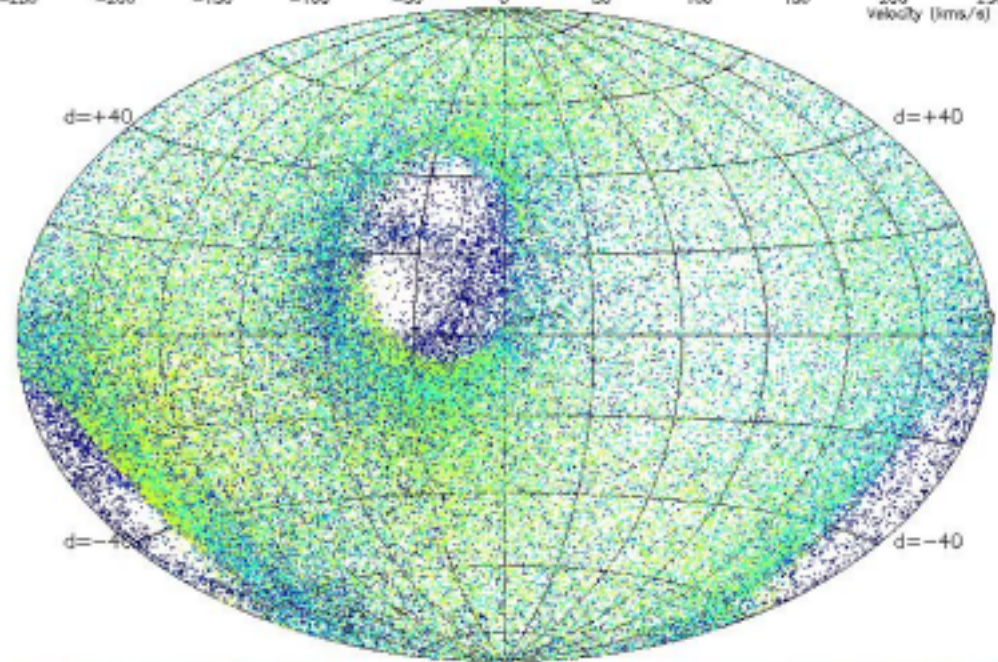
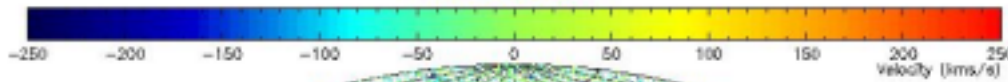
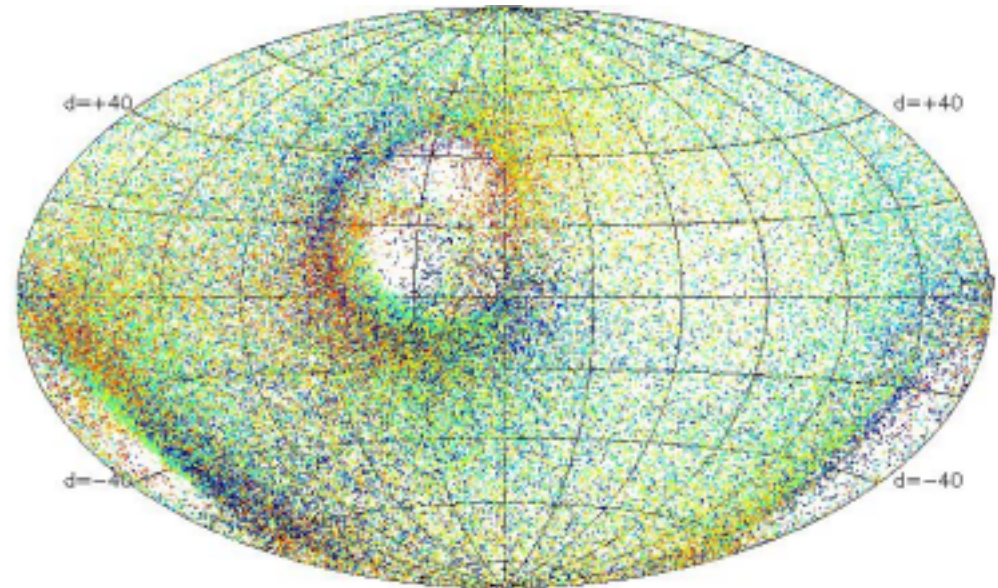
$$q_m = 0.9$$

$$v_c = 220 \text{ km/s}$$

Sag Dwarf stream  
puts tight limits on  
the flattening of the  
Galaxy halo



VELOCITIES

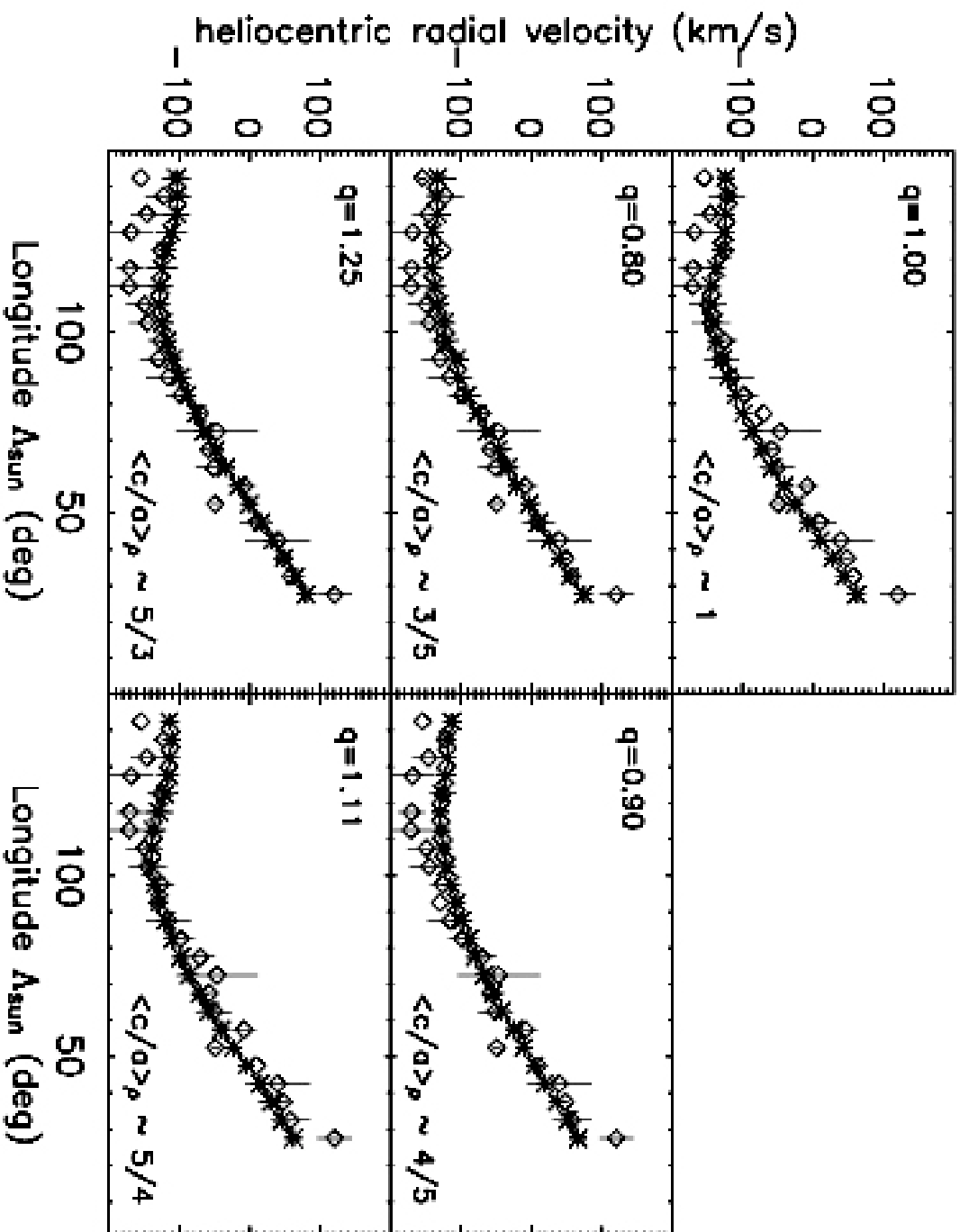


$$q_m = 0.7$$

$$v_c = 220 \text{ km/s}$$

**Sag Dwarf stream  
puts tight limits on  
the flattening of the  
Galaxy halo**

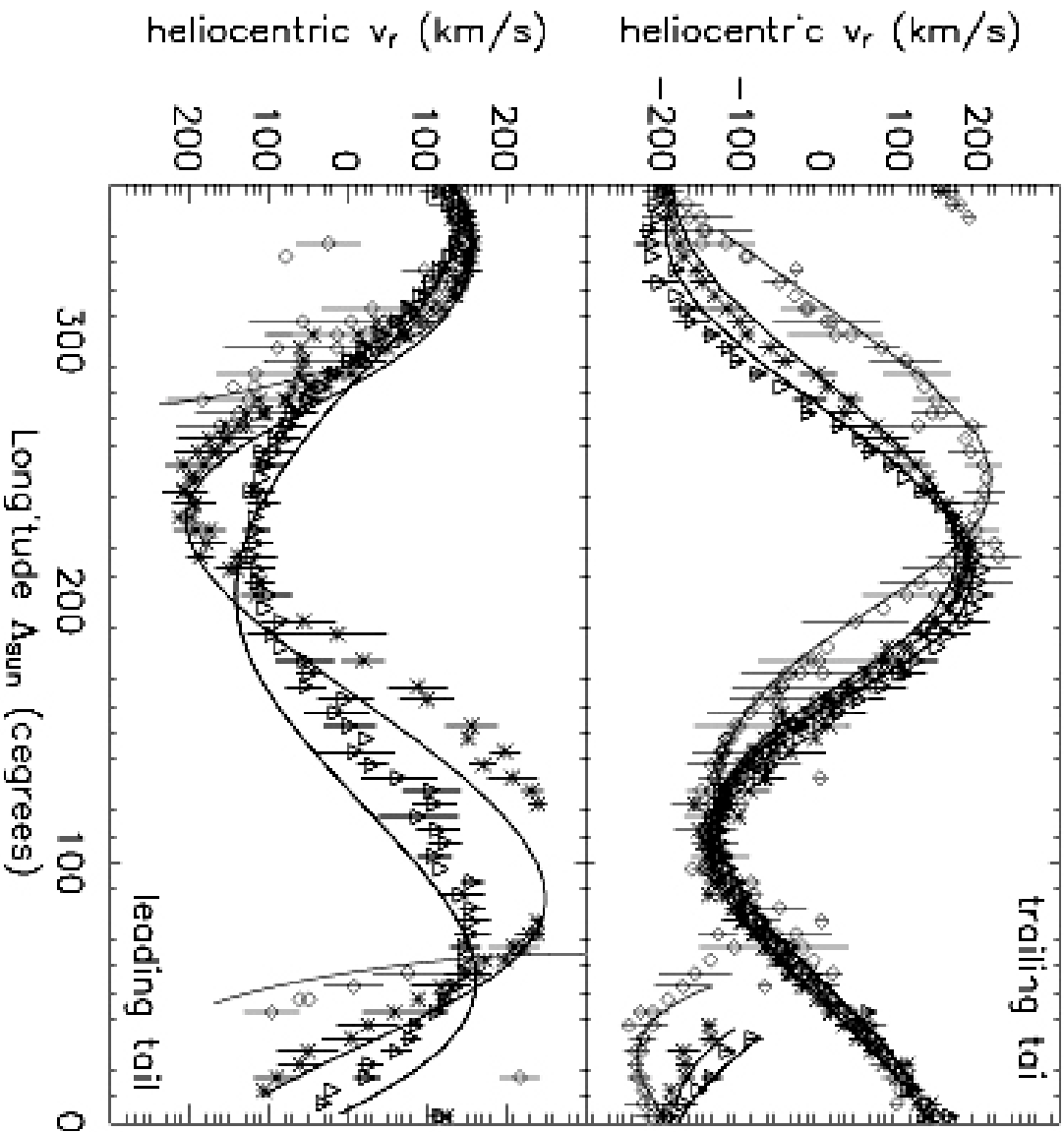
# Stars stripped within last 2 Gyr

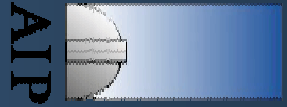




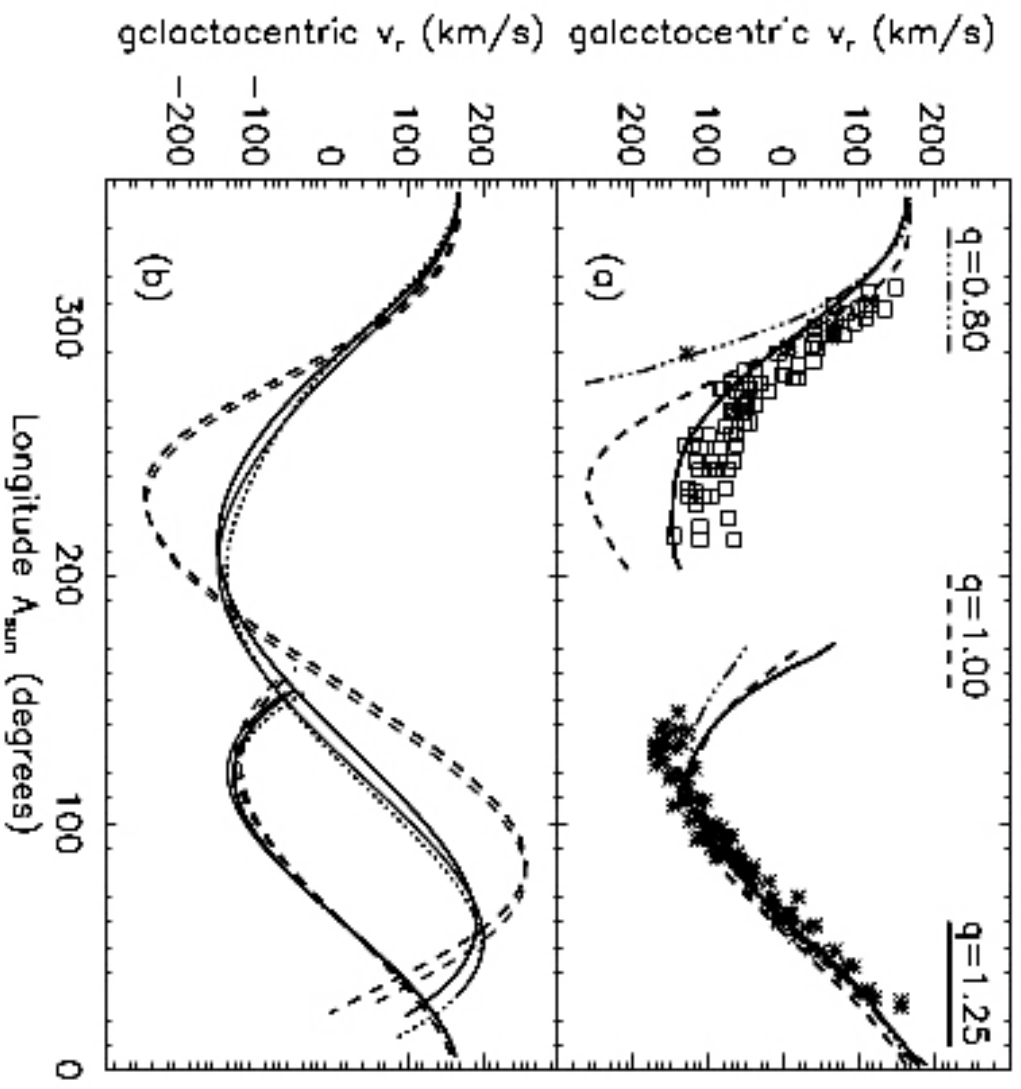


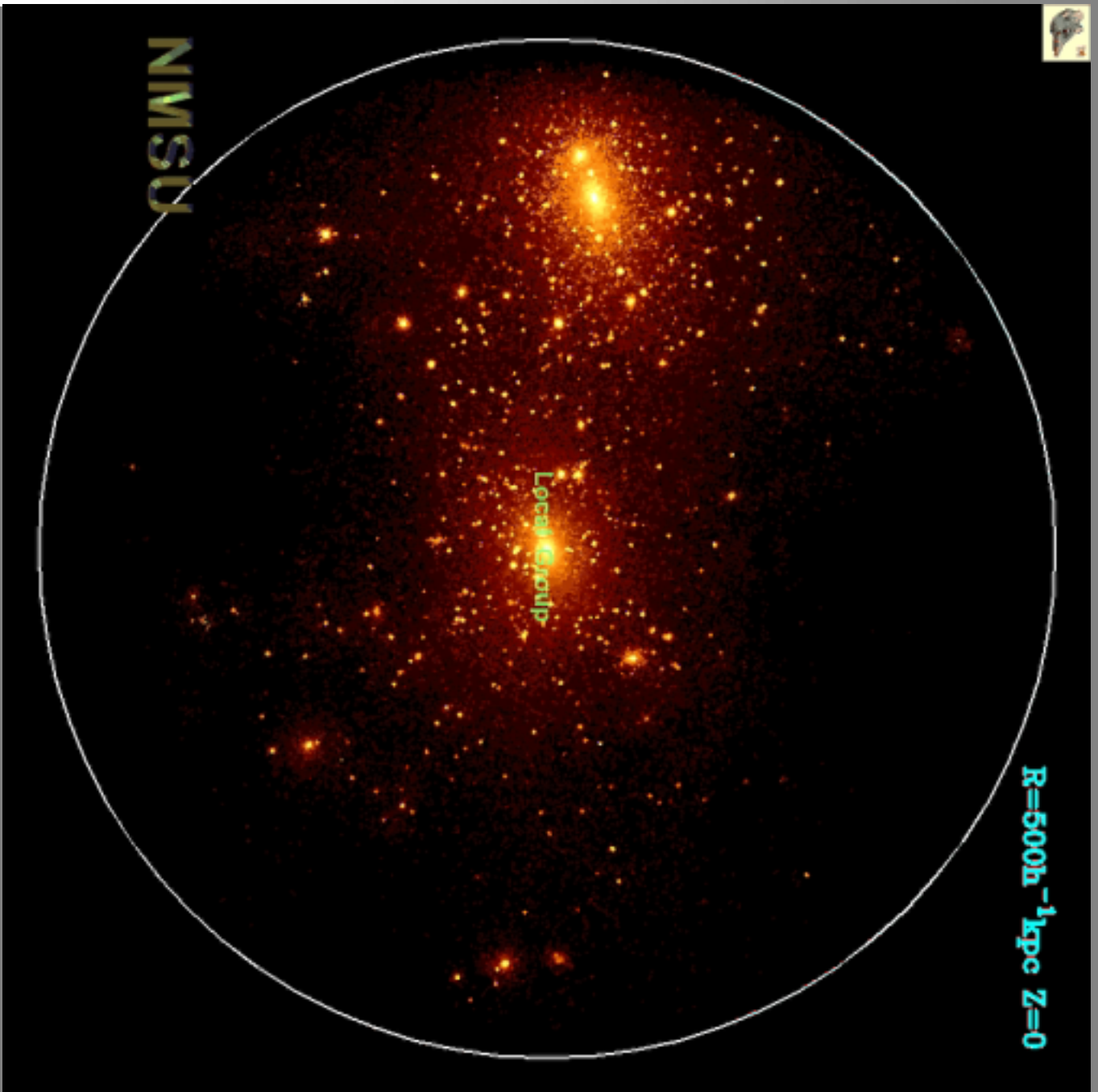
# Stars stripped within last ~4 Gyr





# Stars stripped within last ~4 Gyr





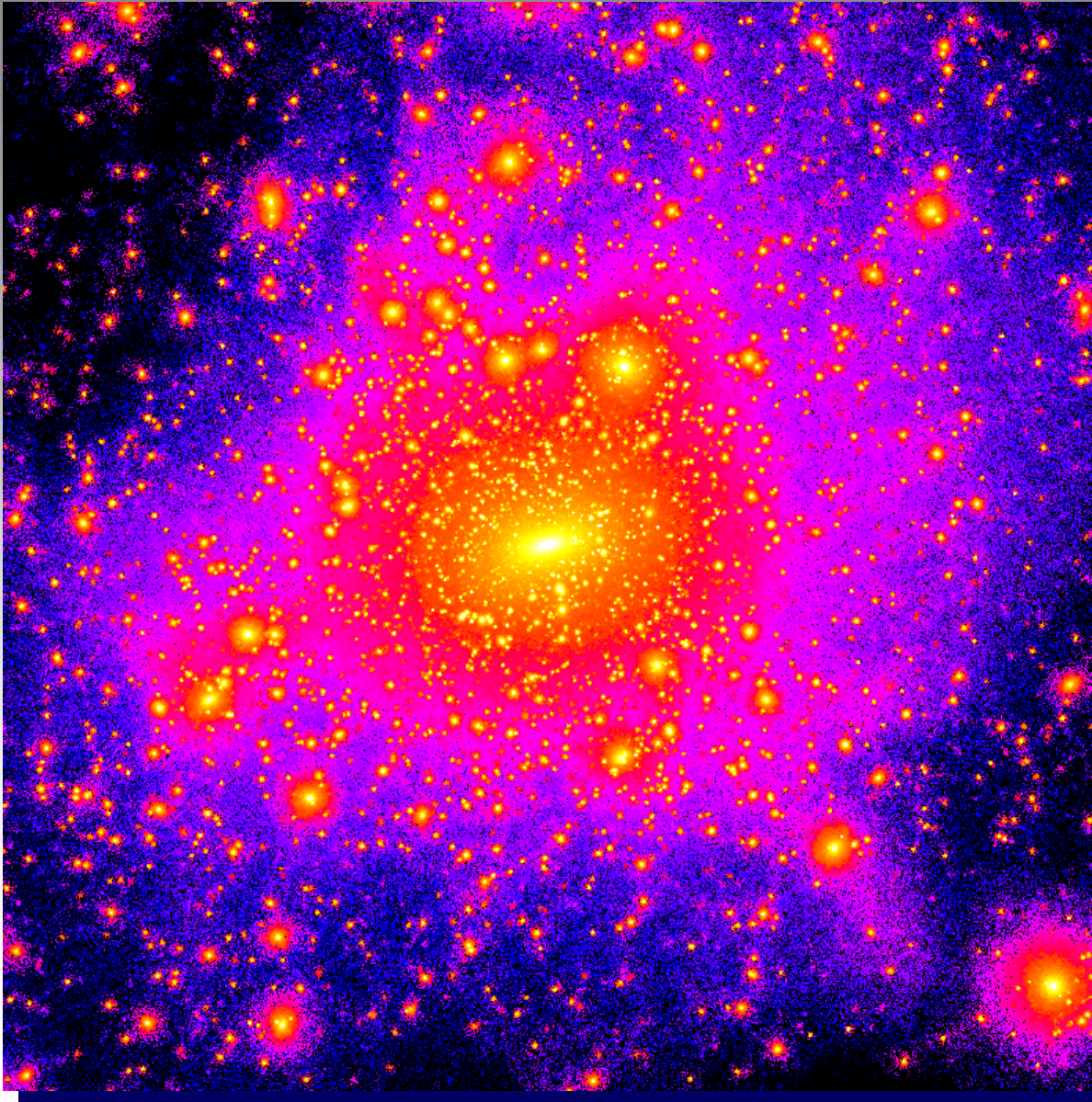


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# The halo of a $\Lambda$ CDM galaxy halo



Navarro et al 2001



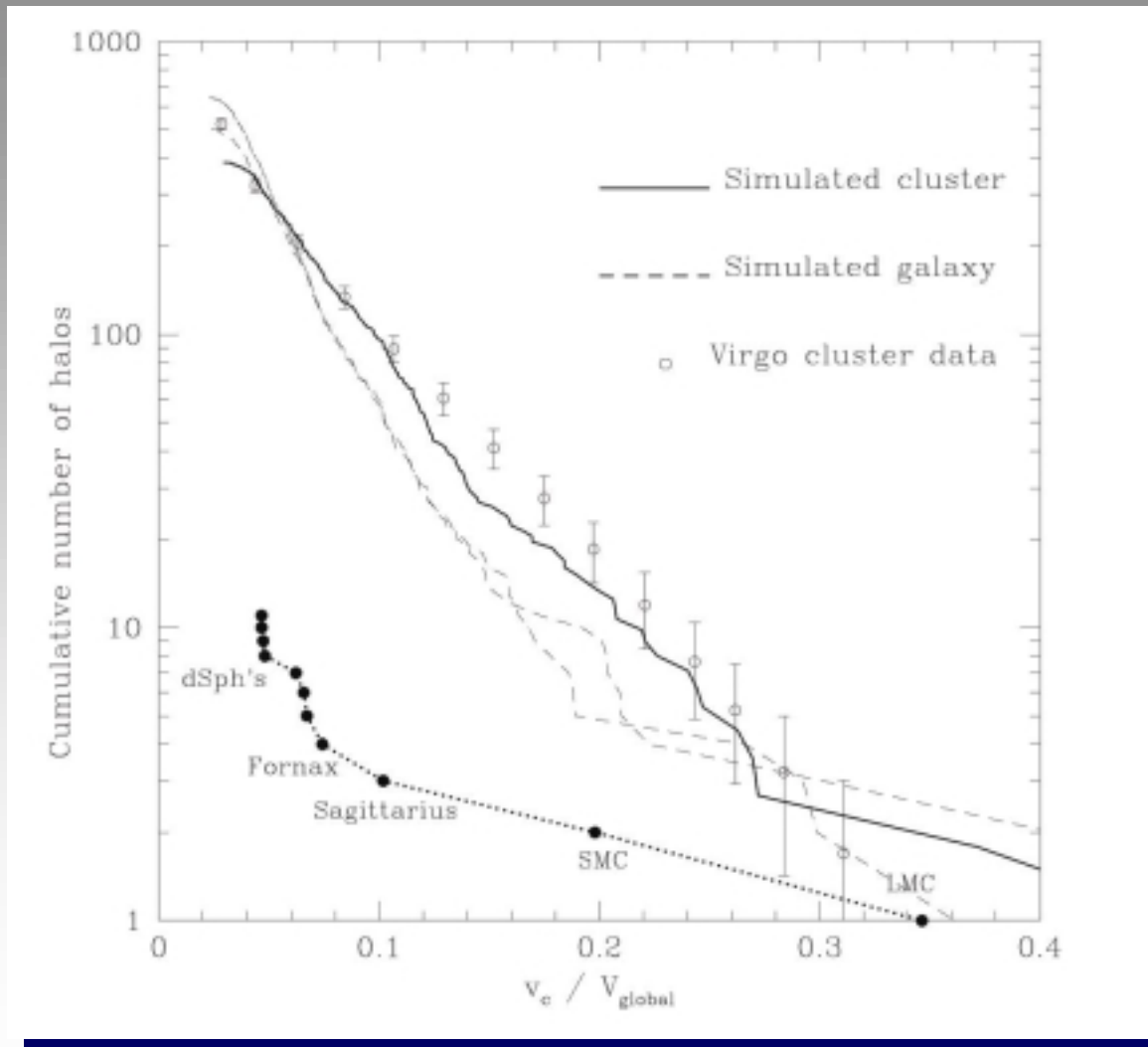
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# Substructure and the abundance of Milky Way satellites

cumulative number



circular velocity

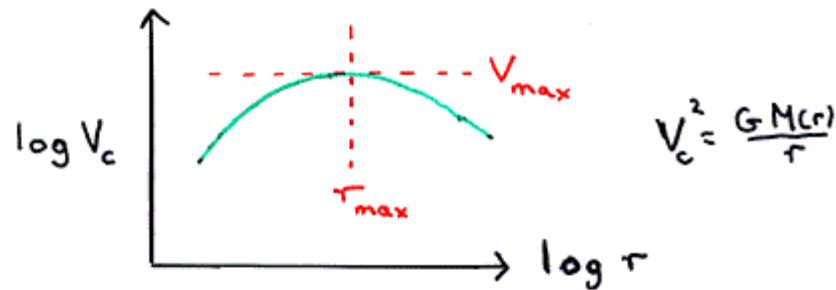
Moore et al 1999  
Klypin et al 1999



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## DWARF SPHEROIDAL HALOS

	$\sigma$ (km/s)	$r_h$ (pc)
Sculptor	6.6	150
Carina	6.8	290
Sextans	6.6	470
Leo II	6.7	225

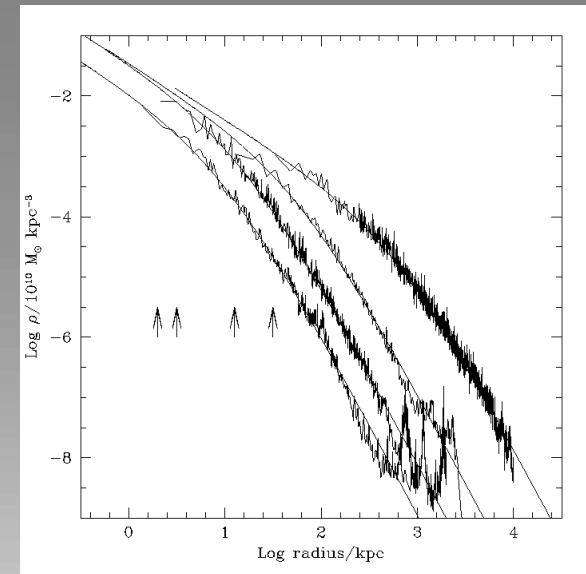


$$\sigma^2 = \frac{1}{3} \frac{1}{M_x} \int V_c^2(r) \frac{dM_x}{dr} dr \approx \frac{1}{3} V_c^2(r_h)$$

$$\rightarrow \sigma = \frac{1}{\sqrt{3}} f\left(\frac{r_h}{r_{max}}\right) V_{max}$$

For  $\Lambda$ CDM simulations  $r_{max} \approx 5 \text{ kpc} \frac{V_{max}}{20 \text{ km/s}}$

For NFW shape:  $\sigma = 6.5 + r_h = 300 \rightarrow V_{max} = 22 \text{ km/s}$



Dark Halos are shallower than isothermal (logarithmic slope  $> -2$ ) near the center.

S.D.M. White 2000



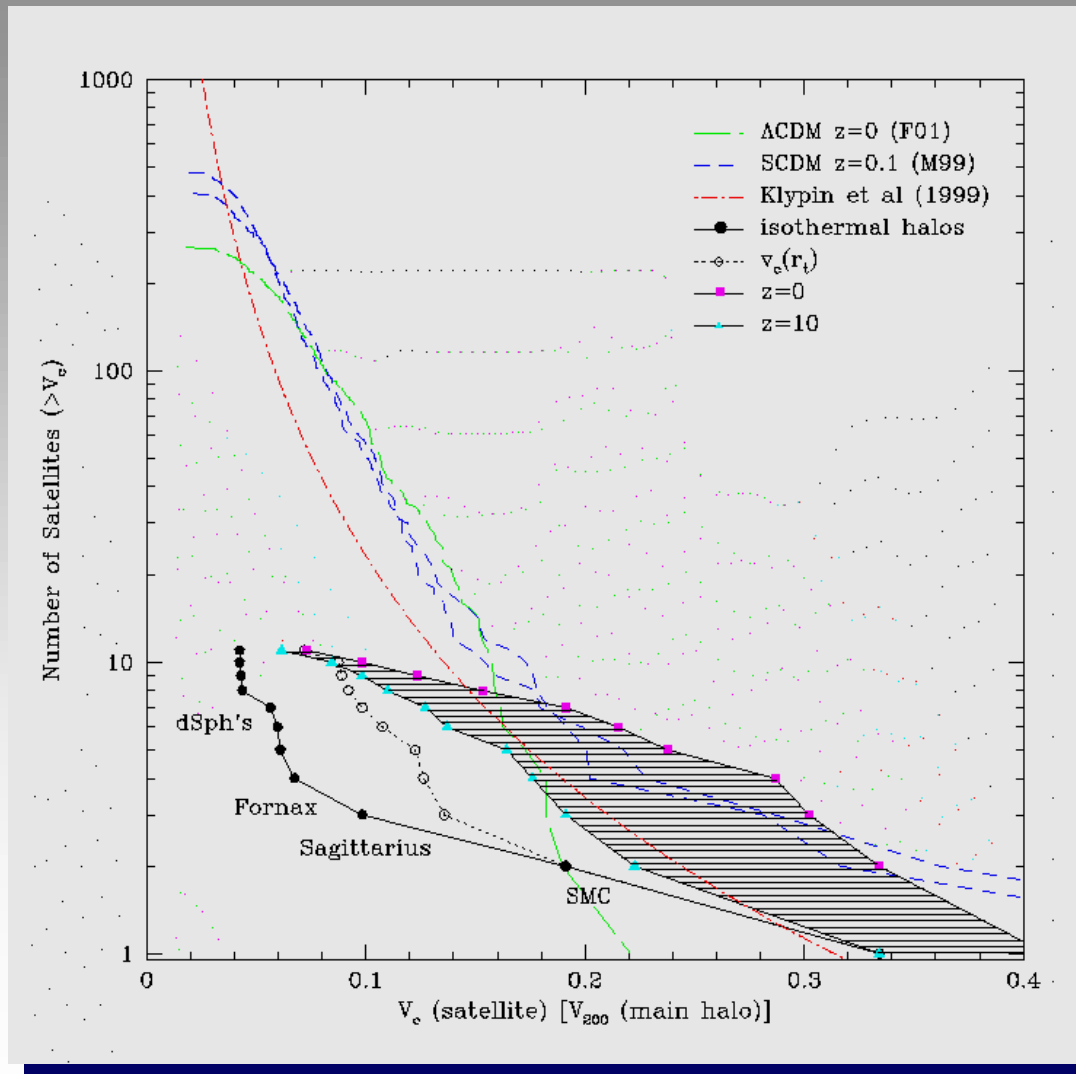
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# Substructure and the abundance of Milky Way satellites

cumulative number



circular velocity

Once the structure of the halos is taken into account, there is good agreement between the number of massive substructure halos and the number of Milky Way satellites.

Hayashi et al 2002

z: 49.5

redshift

X-Y

color: age

X-Z

$H_0$  color: age  
20kpc





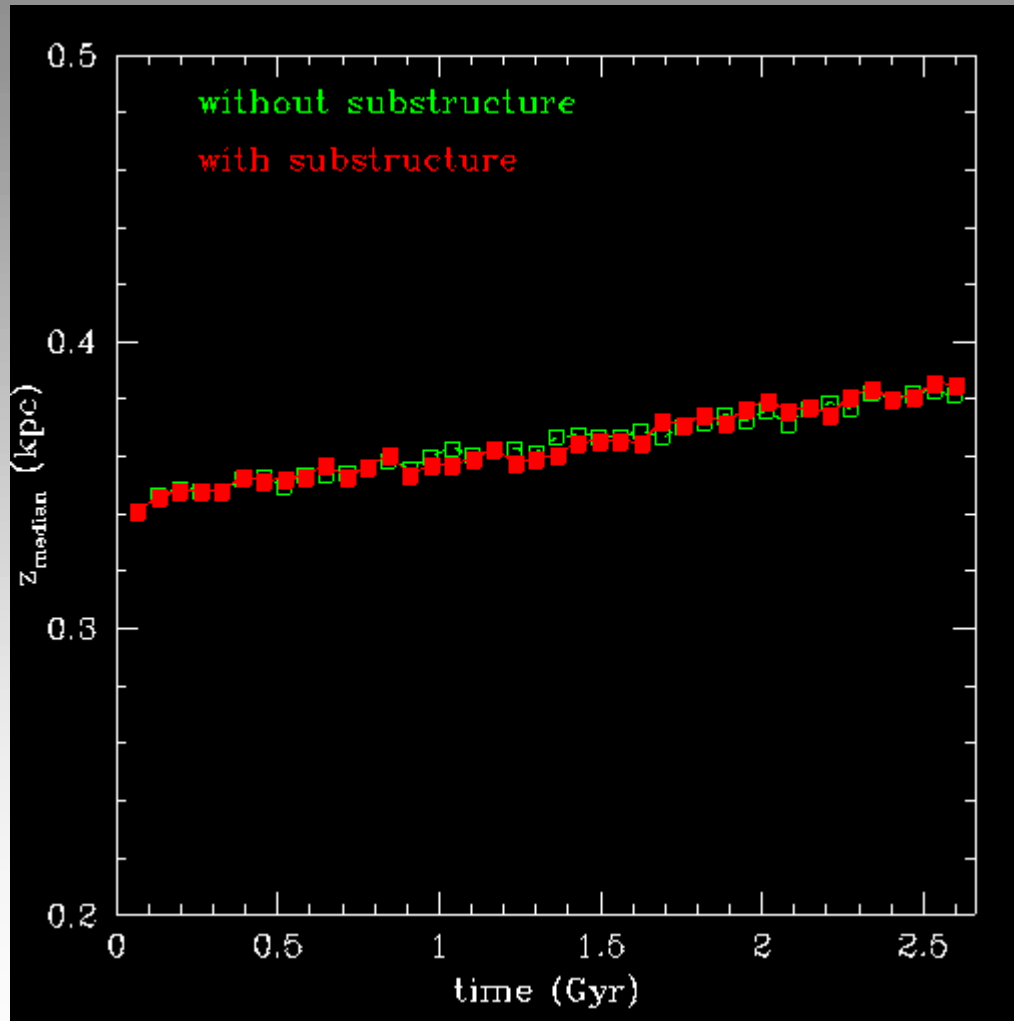
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# Heating of a Milky Way-like stellar disk by substructure

Stellar disk thickness



Time in Gyrs

Green curve:  
without  
substructure  
Red curve:  
with  
substructure

Substructure halos seem to contribute little to the thickening of the disk!



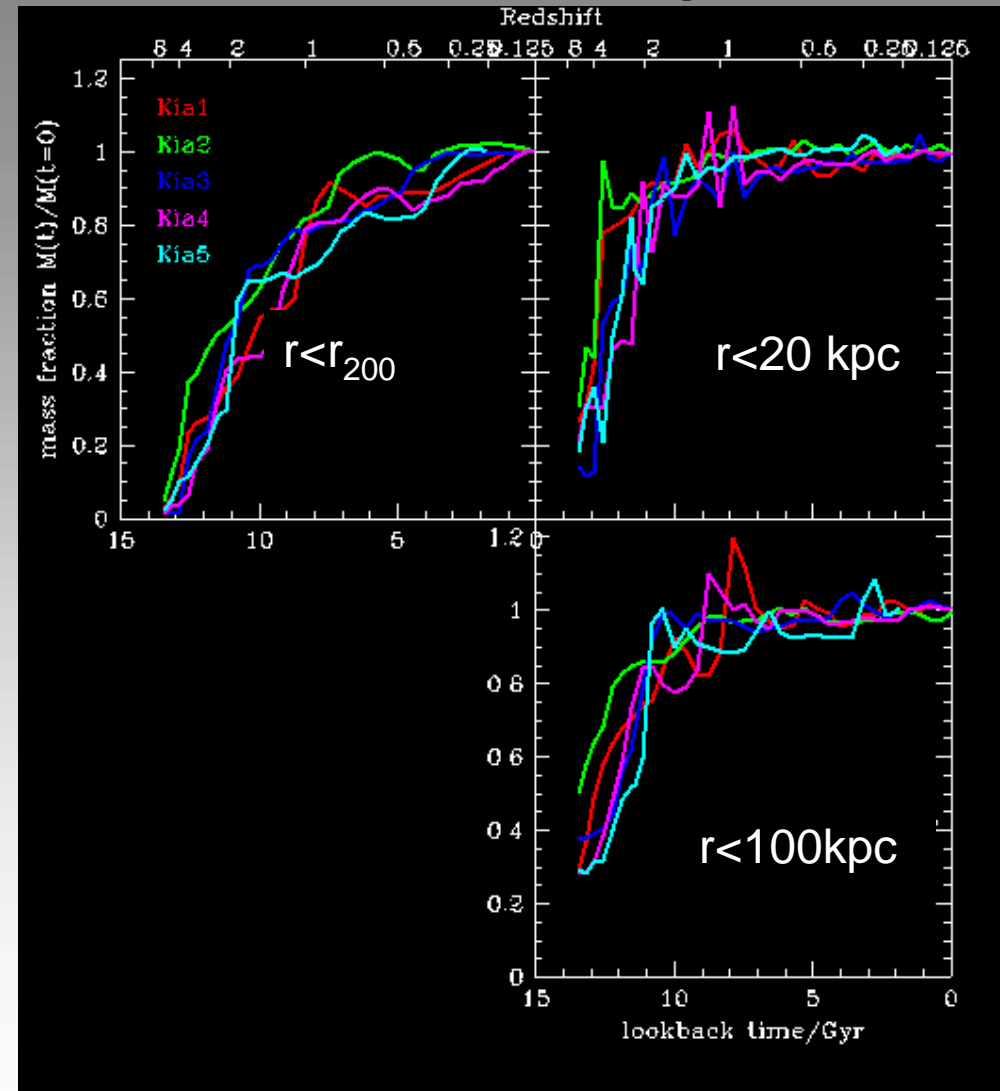
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# Dark mass accretion history

- Similar temporal evolution of the dark matter component
- ~50% of the mass inside  $r_{200}$  assembled by  $z \sim 2$
- Mass inside 20 and 100 kpc ~ constant in the last 10 Gyrs





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# Conclusions

- Small scale structures can be used to further test cosmological models
- Test on scales that have not been used to design and calibrate the cosmological model
  - ◆ density profiles of dark matter halos
  - ◆ shapes of dark matter halos
  - ◆ substructure
  - ◆ ...
- SSS provides serious challenges for the concordance model that merit further investigations
- Solution: Astronomy or Astrophysics or Particle Physics ?