

Precise Predictions for the Higgs-Boson Masses in the NMSSM

P. DRECHSEL^{1*}, L. GALETA^{2†}, S. HEINEMEYER^{2,3‡}, AND G. WEIGLEIN^{1§}

¹*DESY, Notkestraße 85, D-22607 Hamburg, Germany*

²*Instituto de Física de Cantabria (CSIC-UC), Santander, Spain*

³*Instituto de Física Teórica, (UAM/CSIC), Universidad Autónoma de Madrid, Cantoblanco, E-28049 Madrid, Spain*

Abstract

The particle discovered in the Higgs boson searches at the LHC with a mass of about 125 GeV can be identified with one of the neutral Higgs bosons of the Next-to-Minimal Supersymmetric Standard Model (NMSSM). We calculate predictions for the Higgs-boson masses in the NMSSM using the Feynman-diagrammatic approach. The predictions are based on the full NMSSM one-loop corrections supplemented with the dominant and sub-dominant two-loop corrections within the Minimal Supersymmetric Standard Model (MSSM). These include contributions at $\mathcal{O}(\alpha_t\alpha_s, \alpha_b\alpha_s, \alpha_t^2, \alpha_t\alpha_b)$, as well as a resummation of leading and subleading logarithms from the top/scalar top sector. Taking these corrections into account in the prediction for the mass of the Higgs boson in the NMSSM that is identified with the observed signal is crucial in order to reach a precision at a similar level as in the MSSM. The quality of the approximation made at the two-loop level is analysed on the basis of the full one-loop result, with a particular focus on the prediction for the Standard Model-like Higgs boson that is associated with the observed signal. The obtained results will be used as a basis for the extension of the code `FeynHiggs` to the NMSSM.

*email: peter.drechsel@desy.de

†email: leo@ifca.unican.es

‡email: Sven.Heinemeyer@cern.ch

§email: Georg.Weiglein@desy.de

1 Introduction

The spectacular discovery of a boson with a mass around 125 GeV by the ATLAS and CMS experiments [1, 2] at CERN constitutes a milestone in the quest for understanding the physics of electroweak symmetry breaking. Any model describing electroweak physics needs to provide a state that can be identified with the observed signal. While within the present experimental uncertainties the properties of the observed state are compatible with the predictions of the Standard Model (SM) [3, 4], many other interpretations are possible as well, in particular as a Higgs boson of an extended Higgs sector.

One of the prime candidates for physics beyond the SM is supersymmetry (SUSY), which doubles the particle degrees of freedom by predicting two scalar partners for all SM fermions, as well as fermionic partners to all bosons. The most widely studied SUSY framework is the Minimal Supersymmetric Standard Model (MSSM) [5, 6], which keeps the number of new fields and couplings to a minimum. In contrast to the single Higgs doublet of the (minimal) SM, the Higgs sector of the MSSM contains two Higgs doublets, which in the \mathcal{CP} conserving case leads to a physical spectrum consisting of two \mathcal{CP} -even, one \mathcal{CP} -odd and two charged Higgs bosons. The light \mathcal{CP} -even MSSM Higgs boson can be interpreted as the signal discovered at about 125 GeV, see e.g. [7, 8].

Going beyond the MSSM, this model has a well-motivated extension in the Next-to-Minimal Supersymmetric Standard Model (NMSSM), see e.g. [9, 10] for reviews. The NMSSM provides in particular a solution for naturally associating an adequate scale to the μ parameter appearing in the MSSM superpotential [11, 12]. In the NMSSM, the introduction of a new singlet superfield, which only couples to the Higgs- and sfermion-sectors, gives rise to an effective μ -term, generated in a similar way as the Yukawa mass terms of fermions through its vacuum expectation value. In the case where \mathcal{CP} is conserved, which we assume throughout the paper, the states in the NMSSM Higgs sector can be classified as three \mathcal{CP} -even Higgs bosons, h_i ($i = 1, 2, 3$), two \mathcal{CP} -odd Higgs bosons, A_j ($j = 1, 2$), and the charged Higgs boson pair H^\pm . In addition, the SUSY partner of the singlet Higgs (called the singlino) extends the neutralino sector to a total of five neutralinos. In the NMSSM the lightest but also the second lightest \mathcal{CP} -even neutral Higgs boson can be interpreted as the signal observed at about 125 GeV, see, e.g., [13, 14].

The measured mass value of the observed signal has already reached the level of a precision observable, with an experimental accuracy of better than 300 MeV [15], and by itself provides an important test for the predictions of models of electroweak symmetry breaking. In the MSSM the masses of the \mathcal{CP} -even Higgs bosons can be predicted at lowest order in terms of two SUSY parameters characterising the MSSM Higgs sector, e.g. $\tan\beta$, the ratio of the vacuum expectation values of the two doublets, and the mass of the \mathcal{CP} -odd Higgs boson, M_A , or the charged Higgs boson, M_{H^\pm} . These relations, which in particular give rise to an upper bound on the mass of the light \mathcal{CP} -even Higgs boson given by the Z -boson mass, receive large corrections from higher-order contributions. In the NMSSM the corresponding predictions are modified both at the tree-level and the loop-level. In order to fully exploit the precision of the experimental mass value for constraining the available parameter space of the considered models, the theoretical predictions should have an accuracy that ideally is at the same level of accuracy or even better than the one of the experimental value. The theoretical uncertainty, on the other hand, is composed of two sources, the parametric and the

intrinsic uncertainty. The theoretical uncertainties induced by the parametric errors of the input parameters are dominated by the experimental error of the top-quark mass (where the latter needs to include the systematic uncertainty from relating the measured mass parameter to a theoretically well-defined quantity, see e.g. [16–18]). However, the largest theoretical uncertainty at present arises from unknown higher-order corrections, as will be discussed below.

In the MSSM¹ beyond the one-loop level, the dominant two-loop corrections of $\mathcal{O}(\alpha_t\alpha_s)$ [19–24] and $\mathcal{O}(\alpha_t^2)$ [25, 26] as well as the corresponding corrections of $\mathcal{O}(\alpha_b\alpha_s)$ [27, 28] and $\mathcal{O}(\alpha_t\alpha_b)$ [27] are known since more than a decade. (Here we use $\alpha_f = Y_f^2/(4\pi)$, with Y_f denoting the fermion Yukawa coupling.) These corrections, together with a resummation of leading and subleading logarithms from the top/scalar top sector [29] (see also [30, 31] for more details on this type of approach), a resummation of leading contributions from the bottom/scalar bottom sector [27, 28, 32–35] (see also [36, 37]) and momentum-dependent two-loop contributions [38, 39] (see also [40]) are included in the public code `FeynHiggs` [21, 29, 41–45]. A (nearly) full two-loop EP calculation, including even the leading three-loop corrections, has also been published [46, 47], which is, however, not publicly available as a computer code. Furthermore, another leading three-loop calculation of $\mathcal{O}(\alpha_t\alpha_s^2)$, depending on the various SUSY mass hierarchies, has been performed [48, 49], resulting in the code `H3m` (which adds the three-loop corrections to the `FeynHiggs` result up to the two-loop level). The theoretical uncertainty on the lightest \mathcal{CP} -even Higgs-boson mass within the MSSM from unknown higher-order contributions is still at the level of about 3 GeV for scalar top masses at the TeV-scale, where the actual uncertainty depends on the considered parameter region [29, 43, 50, 51].

Within the NMSSM beyond the well known full one-loop results [52–55] several codes exist that calculate the Higgs masses in the pure $\overline{\text{DR}}$ scheme with different contributions at the two-loop level. Amongst these codes `SPheno` [56, 57] incorporates the most complete results at the two-loop level, including SUSY-QCD contributions from the fermion/sfermions of $\mathcal{O}(\alpha_t\alpha_s, \alpha_b\alpha_s)$, as well as pure fermion/sfermion contributions of $\mathcal{O}(\alpha_t^2, \alpha_b^2, \alpha_t\alpha_b, \alpha_\tau^2, \alpha_\tau\alpha_b)$, and contributions from the Higgs/higgsino sector in the gauge-less limit of $\mathcal{O}(\alpha_\lambda^2, \alpha_\kappa^2, \alpha_\lambda\alpha_\kappa)$ [58] as well as mixed contributions from the latter two sectors of $\mathcal{O}(\alpha_\lambda\alpha_t, \alpha_\lambda\alpha_b)$. The included Higgs/higgsino contributions are genuine to the NMSSM, they are proportional to the NMSSM parameters $\lambda^2 = 4\pi \cdot \alpha_\lambda$ and $\kappa^2 = 4\pi \cdot \alpha_\kappa$. The tools `FlexibleSUSY` [59], `NMSSMTools` [60, 61] and `SOFTSUSY` [62–64] include NMSSM corrections of $\mathcal{O}(\alpha_t\alpha_s)$ and $\mathcal{O}(\alpha_b\alpha_s)$ supplemented by certain MSSM corrections. `NMSSMCalc` [54, 55, 65, 66] provides the option to perform the NMSSM Higgs mass calculation up to $\mathcal{O}(\alpha_t\alpha_s)$ with the $\overline{\text{DR}}$ renormalisation scheme applied to the top-/stop-sector, while in the electroweak sector at one-loop order on-shell conditions are used. It has been noticed in a comparison of spectrum generators in the NMSSM that are currently publicly available that the numerical differences between the various codes can be very significant, often exceeding 3 GeV in the prediction of the SM-like Higgs even for the set-up where all predictions were obtained within the $\overline{\text{DR}}$ renormalisation scheme [67]. While the sources of discrepancies between the different codes could be identified [67], a reliable estimate of the remaining theoretical uncertainties should of course also address issues related to the use of different renormalisation schemes. Beyond the pure $\overline{\text{DR}}$ scheme, so far only the code `NMSSMCalc` [54, 55, 65, 66] provides a prediction in a

¹As mentioned above, we focus in this paper on the case of real parameters, i.e. the \mathcal{CP} -conserving case.

mixed OS/ $\overline{\text{DR}}$ scheme, where genuine two-loop contributions in the NMSSM up to $\mathcal{O}(\alpha_t\alpha_s)$ have been incorporated. The resummation of logarithmic contributions beyond the two-loop level is not included so far in any of the public codes for Higgs-mass predictions in the NMSSM. Accordingly, at present the theoretical uncertainties from unknown higher-order corrections in the NMSSM are expected to be still larger than for the MSSM.

Concerning the phenomenology of the NMSSM it is of particular interest whether this model can be distinguished from the MSSM by confronting Higgs sector measurements with the corresponding predictions of the two models. In order to facilitate the identification of genuine NMSSM contributions in this context it is important to treat the predictions for the MSSM and the NMSSM within a coherent framework where in the MSSM limit of the NMSSM the state-of-the-art prediction for the MSSM is recovered.

With this goal in mind, we seek to extend the public tool `FeynHiggs` to the case of the NMSSM. As a first step in this direction we present in this paper a full one-loop calculation of the Higgs-boson masses in the NMSSM, where the renormalisation scheme and all parameters and conventions are chosen such that the well-known MSSM result of `FeynHiggs` is obtained for the MSSM limit of the NMSSM. We supplement the full one-loop result in the NMSSM with all higher-order corrections of MSSM type that are implemented in `FeynHiggs`, as described above. In our numerical evaluation we use our full one-loop result in the NMSSM to assess the quality of the approximation that we make at the two-loop level. We find that for a SM-like Higgs boson that is compatible with the detected signal at about 125 GeV this approximation works indeed very well. We analyse in this context which genuine NMSSM contributions are most relevant when going beyond the approximation based on MSSM-type higher-order corrections. We then apply our most accurate prediction including all higher-order contributions to a phenomenologically interesting scenario. We compare our prediction both with the result in the MSSM limit and with the code `NMSSMCalc` [65]. We discuss in this context the impact of higher-order contributions beyond the ones of $\mathcal{O}(\alpha_t\alpha_s)$, that are not implemented in `NMSSMCalc`.

The paper is organized as follows. In sect. 2 we describe our full one-loop calculation in the NMSSM, specify the renormalisation scheme that we have used and discuss the contributions that are expected to be numerically dominant at the one-loop level. The incorporation of higher-order contributions of MSSM-type is addressed in sect. 3. Our numerical analysis for the prediction at the one-loop level, including a discussion of the quality of the approximation in terms of MSSM-type contributions, and for our most accurate prediction including higher-order corrections is presented in sect. 4. The conclusions can be found in sect. 5.

2 One-loop result in the NMSSM

For the sectors that are identical for the calculation within the MSSM the conventions as implemented in `FeynHiggs` are used, as described in [44]. Therefore the present section is restricted to the quantities genuine to the NMSSM. For a more detailed discussion of the NMSSM, see e.g. [9].

2.1 The relevant NMSSM sectors

The superpotential of the NMSSM for the third generation of fermions/sfermions reads

$$W = Y_t (\hat{H}_2 \cdot \hat{Q}_3) \hat{u}_3 - Y_d (\hat{H}_1 \cdot \hat{Q}_3) \hat{d}_3 - Y_\tau (\hat{H}_1 \cdot \hat{L}_3) \hat{e}_3 + \lambda \hat{S} (\hat{H}_2 \cdot \hat{H}_1) + \frac{1}{3} \kappa \hat{S}^3, \quad (1)$$

with the quark and lepton superfields $\hat{Q}_3, \hat{u}_3, \hat{d}_3, \hat{L}_3, \hat{e}_3$ and the Higgs superfields $\hat{H}_1, \hat{H}_s, \hat{S}$. The $SU(2)_L$ -invariant product is denoted by a dot. The Higgs singlet and doublets are decomposed into \mathcal{CP} -even and \mathcal{CP} -odd neutral scalars ϕ_i and χ_i , and charged states ϕ_i^\pm ,

$$H_1 = \begin{pmatrix} v_1 + \frac{1}{\sqrt{2}}(\phi_1 - i\chi_1) \\ -\phi_1^- \end{pmatrix}, \quad H_2 = \begin{pmatrix} \phi_2^+ \\ v_2 + \frac{1}{\sqrt{2}}(\phi_2 + i\chi_2) \end{pmatrix}, \quad S = v_s + \frac{1}{\sqrt{2}}(\phi_s + i\chi_s), \quad (2)$$

with the real vacuum expectation values for the doublet- and the singlet-fields, $v_{\{1,2\}}$ and v_s . Since \hat{S} transforms as a singlet, the D -terms remain identical to the ones from the MSSM. Compared to the \mathcal{CP} -conserving MSSM the superpotential of the \mathcal{CP} -conserving NMSSM contains additional dimensionless parameters λ and κ , while the μ -term is absent. This term is effectively generated via the vacuum expectation-value of the singlet field,

$$\mu_{\text{eff}} = \lambda v_s. \quad (3)$$

As in the MSSM it is convenient to define the ratio

$$\tan \beta = \frac{v_2}{v_1}. \quad (4)$$

Soft SUSY-breaking in the NMSSM gives rise to the real trilinear soft-breaking parameters A_λ and A_κ , as well as to the soft-breaking mass term m_S^2 of the scalar singlet-field,

$$\mathcal{L}_{\text{soft}} = -m_1^2 H_{1i}^\dagger H_{1i} - m_2^2 H_{2i}^\dagger H_{2i} - m_S^2 |S|^2 - \left[\lambda A_\lambda S (H_2 \cdot H_1) + \frac{1}{3} \kappa A_\kappa S^3 + \text{h.c.} \right] \quad (5)$$

The Higgs potential V_H can be written in powers of the fields,

$$V_H = \dots - T_{\phi_1} \phi_1 - T_{\phi_2} \phi_2 - T_{\phi_s} \phi_s \quad (6)$$

$$+ \frac{1}{2} (\phi_1, \phi_2, \phi_s) \mathbf{M}_{\phi\phi} \begin{pmatrix} \phi_1 \\ \phi_2 \\ \phi_s \end{pmatrix} + \frac{1}{2} (\chi_1, \chi_2, \chi_s) \mathbf{M}_{\chi\chi} \begin{pmatrix} \chi_1 \\ \chi_2 \\ \chi_s \end{pmatrix} + (\phi_1^-, \phi_2^-) \mathbf{M}_{\phi^\pm\phi^\pm} \begin{pmatrix} \phi_1^+ \\ \phi_2^+ \end{pmatrix} + \dots,$$

where the coefficients bilinear in the fields are the mass matrices $\mathbf{M}_{\phi\phi}$, $\mathbf{M}_{\chi\chi}$ and $\mathbf{M}_{\phi^\pm\phi^\pm}$. For the \mathcal{CP} -even fields the (symmetric) mass matrix reads

$$\mathbf{M}_{\phi\phi} = \begin{pmatrix} \hat{m}_A^2 s_\beta^2 - M_Z^2 c_\beta^2 & (\hat{m}_A^2 + M_Z^2) s_\beta c_\beta & \mu_{\text{eff}} (2\lambda v c_\beta - \kappa v s_\beta) + \frac{\lambda v}{\mu_{\text{eff}}} c_\beta \\ \cdot & \hat{m}_A^2 c_\beta^2 - M_Z^2 s_\beta^2 & \mu_{\text{eff}} (2\lambda v s_\beta - \kappa v c_\beta) + \frac{\lambda v}{\mu_{\text{eff}}} s_\beta \\ \cdot & \cdot & \lambda \kappa v^2 c_\beta s_\beta + \frac{\lambda^2 v^2}{\mu_{\text{eff}}^2} \hat{m}_A^2 + \frac{\kappa}{\lambda} \mu_{\text{eff}} \left(4 \frac{\kappa}{\lambda} \mu_{\text{eff}} + A_\kappa \right) \end{pmatrix}, \quad (7)$$

where s_β and c_β denote the sine and cosine of the angle β , and

$$\hat{m}_A^2 = M_{H^\pm}^2 - M_W^2 + \lambda^2 v^2. \quad (8)$$

The lower triangle in eq. (7) is filled with the transposed matrix element. For the \mathcal{CP} -conserving case the mixing into the eigenstates of mass and \mathcal{CP} can be described at lowest order by the following unitary transformations

$$\begin{pmatrix} h_1 \\ h_2 \\ h_3 \end{pmatrix} = \mathbf{U}_{e(0)} \begin{pmatrix} \phi_1 \\ \phi_2 \\ \phi_s \end{pmatrix}, \quad \begin{pmatrix} A_1 \\ A_2 \\ G_0 \end{pmatrix} = \mathbf{U}_{o(0)} \begin{pmatrix} \chi_1 \\ \chi_2 \\ \chi_s \end{pmatrix}, \quad \begin{pmatrix} H^\pm \\ G^\pm \end{pmatrix} = \mathbf{U}_{c(0)} \begin{pmatrix} \phi_1^\pm \\ \phi_2^\pm \end{pmatrix}. \quad (9)$$

The matrices $\mathbf{U}_{\{e,o,c\}(0)}$ transform the Higgs fields such that the mass matrices are diagonalised at tree level. The new fields correspond to the five neutral Higgs bosons h_i and A_j , the charged pair H^\pm , and the Goldstone bosons G^0 and G^\pm .

In eq. (7) the third row and column depend explicitly on μ_{eff} . The numerical value of μ_{eff} has an important impact on the singlet admixture after performing the rotation into the mass eigenstate basis. For instance, for values of μ_{eff} large enough that

$$(\mathbf{M}_{\phi\phi})_{33} \gg (\mathbf{M}_{\phi\phi})_{i3}, \quad i \in \{1, 2\}, \quad (10)$$

the mass of the singlet becomes decoupled from the doublet masses.

The superpartner of the scalar singlet appears as a fifth neutralino. The corresponding 5×5 mass-matrix reads

$$\mathbf{Y} = \begin{pmatrix} M_1 & 0 & -M_Z s_w \cos \beta & M_Z s_w \sin \beta & 0 \\ 0 & M_2 & M_Z c_w \cos \beta & -M_Z c_w \sin \beta & 0 \\ -M_Z s_w \cos \beta & M_Z c_w \cos \beta & 0 & -\mu_{\text{eff}} & \lambda v \sin \beta \\ M_Z s_w \sin \beta & -M_Z c_w \sin \beta & -\mu_{\text{eff}} & 0 & \lambda v \cos \beta \\ 0 & 0 & \lambda v \sin \beta & \lambda v \cos \beta & -2 \frac{\kappa}{\lambda} \mu_{\text{eff}} \end{pmatrix}. \quad (11)$$

It is diagonalised by a unitary matrix

$$\mathbf{D}_\mathbf{Y} = \mathbf{N}^* \mathbf{Y} \mathbf{N}^\dagger = \text{diag} \{ m_{\tilde{\chi}_1^0}, m_{\tilde{\chi}_2^0}, m_{\tilde{\chi}_3^0}, m_{\tilde{\chi}_4^0}, m_{\tilde{\chi}_5^0} \}. \quad (12)$$

Also in eq. (11) μ_{eff} can have a significant influence on the mixing between the singlino and the doublet higgsino fields. For instance, for sufficiently large values of μ_{eff} such that

$$(\mathbf{Y})_{55} \gg (\mathbf{Y})_{i5}, \quad i \in \{3, 4\}, \quad (13)$$

the singlino mass decouples from the masses of higgsinos and gauginos.

2.2 Renormalisation Scheme

In order to derive the counterterms entering the 1-loop corrections to the Higgs-boson masses the independent parameters appearing in the linear and bilinear terms of the Higgs potential in eq. (6) have to be renormalised. The set of independent parameters from the Higgs-sector used for the presented calculation is formed by

$$\begin{array}{ll} \text{MSSM-like:} & T_{h_{1,2}}, \mu_{\text{eff}}, M_{H^\pm}^2, \tan \beta, M_W^2, M_Z^2 \\ \text{genuine NMSSM:} & T_{h_3}, \kappa, \lambda, A_\kappa, v = \sqrt{v_1^2 + v_2^2}. \end{array} \quad (14)$$

Here T_{h_i} denotes the tadpole coefficient for the field h_i (as indicated by the subscript) in the mass eigenstate basis. Parameters that do not enter the MSSM calculation are considered as genuine of the calculation in the NMSSM. Although the vacuum expectation value v is not a parameter genuine to the NMSSM, its appearance as an independent parameter is a specific feature of the NMSSM Higgs-mass calculation, see below.

For all parameters appearing only in the NMSSM-calculation, besides the additional tadpole coefficient, a $\overline{\text{DR}}$ -scheme is applied. This is a difference to the calculations performed in [54,55,65,66], where the electric charge e is renormalised instead of the parameter v . These two parameters are related to each other by

$$v = \frac{\sqrt{2}s_w M_W}{e} \rightarrow v \left(1 + \frac{\delta v}{v}\right) = v \left[1 + \frac{1}{2} \left(\frac{\delta M_W^2}{M_W^2} + \frac{\delta s_w^2}{s_w^2} - 2\delta Z_e\right)\right], \quad (15)$$

with the renormalisation constants for the W -boson mass, δM_W^2 , the sine of the weak mixing angle, δs_w^2 , where $s_w^2 \equiv 1 - M_Z^2/M_W^2$, $s_w^2 + c_w^2 = 1$, and the electric charge renormalised as

$$e \rightarrow e(1 + \delta Z_e). \quad (16)$$

Considering δM_W^2 and δs_w^2 already fixed by on-shell conditions for the gauge-boson masses [44], either δZ_e or δv in eq. (15) can be fixed by an independent renormalisation condition (and the other counterterm is then a dependent quantity). The renormalisation prescription [54] where δZ_e is fixed by renormalising e in the static limit results in a non- $\overline{\text{DR}}$ renormalisation for δv . For the self-energies in the Higgs sector δv enters the counterterms for the renormalised Higgs potential,

$$V_{\text{H}} \rightarrow V_{\text{H}} + \delta V_{\text{H}}, \quad (17)$$

with coefficients involving λ and κ , like

$$\frac{\delta^{(2)}}{\delta\phi_s\delta\phi_i}\delta V_{\text{H}} \Big|_{\phi_l,\chi_m,\phi_n^\pm=0} \supset -\kappa\mu_{\text{eff}} \{\sin\beta, \cos\beta\} (\delta v + \dots), \quad (18)$$

for the self-energies with each an external doublet and singlet field. The ellipsis in eq. (18) denote other renormalisation constants that are fixed in the $\overline{\text{DR}}$ -scheme and thus do not contribute with a finite part. However, a finite contribution from δv would lead to a κ -dependence of all loop contributions entering via δv , in particular also of the corrections from the fermions and sfermions (while the fermion and sfermion contributions to the unrenormalised self-energy are κ -independent). A finite contribution from δv would furthermore imply the rather artificial feature that a self-energy involving an external gauge singlet field would receive a counterterm contribution involving the renormalisation constant δZ_e for the electric charge. We therefore prefer to use the $\overline{\text{DR}}$ -scheme for the renormalisation of v , which means that we use a scheme where δZ_e is a dependent counterterm. This leads to the relation

$$\delta Z_e^{\text{dep}} = \frac{1}{2} \left[\frac{\delta s_w^2}{s_w^2} + \frac{\delta M_W^2}{M_W^2} - \frac{\delta v^2}{v^2} \right], \quad (19)$$

which implies

$$\delta Z_e^{\text{dep}}|^{\text{fin}} = \frac{1}{2} \left[\frac{\delta s_w^2}{s_w^2} + \frac{\delta M_W^2}{M_W^2} \right]^{\text{fin}} \quad (20)$$

for the finite part of δZ_e^{dep} . In this scheme the numerical value for the electric charge e (and accordingly for the electromagnetic coupling constant α) is determined indirectly via eq. (20). In order to avoid a non-standard numerical value for α in our numerical results, we apply a two-step procedure: in the first step we apply a $\overline{\text{DR}}$ renormalisation for v as outlined above. As a second step we then reparametrise this result in terms of a suitably chosen expression for α . By default we use the same convention as for the MSSM result that is implemented in `FeynHiggs`, namely the expression for the electric charge in terms of the Fermi constant G_F , in order to facilitate the comparison between the `FeynHiggs` result in the MSSM and our new result in the NMSSM. Taking the MSSM limit of our new NMSSM result, the MSSM result as implemented in `FeynHiggs` is recovered, since the described calculational differences are genuine NMSSM effects that vanish in this limit. For the numerical comparison with `NMSSMCalc` we will use instead $\alpha(M_Z)$. The procedure of the reparametrisation is outlined in the following section.

2.3 Reparametrisation of the electromagnetic coupling

The couplings g^I and g^{II} in two different renormalisation schemes are in general related to each other by

$$g^I (1 + \delta Z_g^I) = g^{II} (1 + \delta Z_g^{II}) \quad , \quad (21)$$

because of the equality of the bare couplings. The corresponding shift in the numerical values of the coupling definitions is obtained from the finite difference of the two counterterms, $\Delta \equiv g^{II} \delta Z_g^{II} - g^I \delta Z_g^I$. Accordingly, a reparametrisation from the numerical value of the coupling used in scheme I to the one of scheme II can be performed via

$$g^I = g^{II} + \Delta \quad . \quad (22)$$

Since Δ is of one-loop order, its insertion into a tree-level expression generates a term of one-loop order, etc.

In our calculation the reparametrisation of the electromagnetic coupling is only necessary up to the one-loop level, since all corrections of two-loop and higher order that we are going to incorporate have been obtained in the gauge-less limit (some care is necessary regarding the incorporation of the MSSM-type contributions of $\mathcal{O}(\alpha_t^2)$, see [26, 68]). At this order the shift Δ can simply be expressed as $\Delta = g^{II} (\delta Z_g^{II} - \delta Z_g^I)$. Specifically, for the reparametrisation of the electromagnetic coupling constant G_F the parameter shift Δ_{G_F} reads

$$\Delta_{G_F} = e \left(\delta Z_e - \delta Z_e^{\text{dep}} - \frac{1}{2} \Delta r^{\text{NMSSM}} \right) \quad . \quad (23)$$

Here δZ_e is the counterterm of the charge renormalisation within the NMSSM according to the static (Thomson) limit,

$$\delta Z_e = \frac{1}{2} \Pi^{\gamma\gamma}(0) + \frac{s_w}{c_w} \frac{\Sigma_T^{\gamma Z}(0)}{M_Z^2} \quad , \quad (24)$$





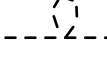
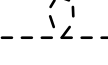
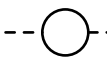
(i,j)	(1 2, 1 2)	(1, s)	(2, s)	(s, s)
order	$\mathcal{O}(Y_t^2)$	$\mathcal{O}(\lambda Y_t)$	$\mathcal{O}(\lambda Y_t)$	$\mathcal{O}(\lambda^2)$
fields	top/stop	stop	stop	stop
topologies				
				
				

Table 1: Topologies and their order in terms of the couplings in the top/stop sector that contribute to the self-energies of the \mathcal{CP} -even fields ϕ_i at one-loop order in the gauge-less limit. The numbers 1 and 2 denote the doublet-states as external fields, while s denotes an external singlet. The internal lines depict either a top (solid) or a scalar top (dashed).

and $\Pi^{\gamma\gamma}(0)$, $\Sigma_T^Z(0)$ are the derivative of the transverse part of the photon self-energy and the transverse part of the photon– Z self-energy at zero momentum transfer, respectively. The counterterm δZ_e^{dep} has been defined in eq. (19), and for the quantity Δr^{NMSSM} we use the result of [69] (see also [70]).² The numerical value for the electromagnetic coupling e in this parametrisation is obtained from the Fermi constant in the usual way as $e = 2M_W s_w \sqrt{G_F \sqrt{2}}$.

Similarly, for the reparametrisation of the electromagnetic coupling defined in the previous section in terms of $\alpha(M_Z)$ the parameter shift $\Delta_{\alpha(M_Z)}$ reads

$$\Delta_{\alpha(M_Z)} = e \left(\delta Z_e - \delta Z_e^{\text{dep}} - \frac{1}{2} \Delta \alpha \right). \quad (25)$$

The numerical value of e in this parametrisation is obtained from $\alpha(M_Z) = \alpha(0)/(1 - \Delta\alpha)$, and $\alpha(0)$ is the value of the fine-structure constant in the Thomson limit.

2.4 Dominant Contributions at One-Loop Order

As explained above, we will supplement our full one-loop result with all available higher-order contributions of MSSM type. This means in particular that the two-loop contributions are approximated by the two-loop corrections in the MSSM (i.e. omitting genuine NMSSM corrections) as included in `FeynHiggs`, and further corrections beyond the two-loop level are included. In order to validate this approximation we analyse at the one-loop level the size of genuine NMSSM corrections w.r.t. the MSSM-like contributions.

Since the corrections from the top/stop sector are usually the by far dominant ones, we start with a qualitative discussion of those contributions before we perform a numerical analysis in the following section. In the MSSM the leading corrections from the top/stop sector are commonly denoted as $\mathcal{O}(\alpha_t)$, indicating the occurrence of two Yukawa couplings Y_t . In the limit where all other masses of the SM particles and the external momentum

²For the sample scenario defined in tab. 2 below the numerical value of Δr^{NMSSM} from [69] turns out to be close to 3.8%, with only a weak dependence on λ for the range of λ values discussed in this paper.

are neglected compared to the top-quark mass, for dimensional reasons the correction to the squared Higgs-boson mass furthermore receives a contribution proportional to m_t^2 . This gives rise to the well-known coefficient $G_F m_t^4$ of the leading one-loop contributions. In the NMSSM the formally leading contributions either are of $\mathcal{O}(Y_t^2)$ (involving two Yukawa couplings), of $\mathcal{O}(\lambda Y_t)$ (involving one Yukawa coupling), or of $\mathcal{O}(\lambda^2)$ (involving no Yukawa coupling). The various contributions from the top/stop sector are summarized in tab. 1. The contributions in the second column are the ones of MSSM-type, while the entries in the third through fifth column represent the genuine NMSSM corrections, involving only scalar tops.³

For the doublet fields, the couplings between the Higgs- and stop-fields in the gauge-less limit are proportional to the top-quark Yukawa-coupling,

$$i\Gamma_{\phi_2 \tilde{t}_i \tilde{t}_j} = i\sqrt{2}Y_t \left[A_t \cdot c_{ij}^{\phi_2}(\theta_{\tilde{t}}) + m_t \cdot (-1)^{1-i} \delta_{ij} \right], \quad i\Gamma_{\phi_1 \tilde{t}_i \tilde{t}_j} = i\sqrt{2}Y_t \mu_{\text{eff}} \cdot c_{ij}^{\phi_1}(\theta_{\tilde{t}}), \quad (26a)$$

while the corresponding coupling for the singlet field reads

$$i\Gamma_{\phi_s \tilde{t}_i \tilde{t}_j} = i\sqrt{2}\lambda \cot \beta m_t \cdot c_{ij}^{\phi_s}(\theta_{\tilde{t}}). \quad (26b)$$

The non-vanishing quartic Higgs–stop couplings read

$$i\Gamma_{\phi_2 \phi_2 \tilde{t}_i \tilde{t}_j} = -iY_t^2 \cdot \delta_{ij}, \quad i\Gamma_{\phi_1 \phi_s \tilde{t}_i \tilde{t}_j} = -i\lambda Y_t \cdot c_{ij}^{\phi_1 \phi_s}(\theta_{\tilde{t}}). \quad (27)$$

Here functions of the mixing angle of the stop-sector, $\theta_{\tilde{t}}$, are denoted by c with the appropriate indices and superscripts for the involved fields. These functions c can never be larger than 1. In the singlet–stop coupling we have explicitly spelled out a factor $\lambda v_1 Y_t = \lambda m_t \cot \beta$ to highlight the appearance of the factor m_t in eq. (26b) instead of the usual factor $m_t/M_W \sim Y_t$ in eq. (26a).

The genuine NMSSM couplings of a singlet to stops are seen to follow the pattern mentioned above, i.e. they give rise to contributions of $\mathcal{O}(\lambda Y_t)$ (third and fourth column in tab. 1) or $\mathcal{O}(\lambda^2)$ (fifth column), whereas the MSSM-like contributions are of $\mathcal{O}(Y_t^2)$ (second column). Those different patterns do not only indicate a distinction between the MSSM-like and the genuine NMSSM contributions, but also give rise to a significant numerical suppression⁴ of the genuine NMSSM contributions w.r.t. the MSSM-like ones for $\lambda < Y_t$. If one demands validity of perturbation theory up to the GUT scale, this relation is always fulfilled, since then λ and κ are bound from above [12] by

$$\lambda^2 + \kappa^2 \lesssim 0.5, \quad (28)$$

so that $\lambda \lesssim 0.7$, where the largest values are only allowed for vanishing κ . The size of the genuine NMSSM contributions will be discussed numerically in the following sections.

3 Incorporation of higher-order contributions

The masses of the \mathcal{CP} -even Higgs bosons are obtained from the complex poles of the full propagator matrix. The inverse propagator matrix for the three \mathcal{CP} -even Higgs bosons h_i

³We discuss here only the Higgs boson self-energies. However, the same line of argument can be made for the tadpole contributions.

⁴For the trilinear couplings in eq. (26), comparing the Higgs singlet with the doublet, an additional potential suppression factor of $\mathcal{O}(m_t/A_t)$ and/or $\mathcal{O}(m_t/\mu_{\text{eff}})$ appears.

from eq. (9) is a 3×3 matrix that reads

$$\Delta^{-1}(k^2) = i \left[k^2 \mathbb{1} - \mathcal{M}_{hh} + \hat{\Sigma}_{hh}(k^2) \right]. \quad (29)$$

Here \mathcal{M}_{hh} denotes the diagonalised mass matrix of the \mathcal{CP} -even Higgs fields at tree level, and $\hat{\Sigma}_{hh}$ denotes their renormalised self-energy corrections⁵. The three complex poles of the propagator in the \mathcal{CP} -even Higgs sector are given by the values of the external momentum k for which the determinant of the inverse propagator-matrix vanishes,

$$\det \left[\Delta^{-1}(k^2) \right]_{k^2=m_{h_i}^2 - i\Gamma_{h_i} m_{h_i}} \stackrel{!}{=} 0, \quad i \in \{1, 2, 3\}. \quad (30)$$

The real parts of the three poles are identified with the the square of the Higgs-boson masses in the \mathcal{CP} -even sector. The renormalised self-energy matrix $\hat{\Sigma}_{hh}$ is evaluated by taking into account the full contributions from the NMSSM at one-loop order and, as an approximation, the MSSM-like contributions at two-loop order of $\mathcal{O}(\alpha_t \alpha_s, \alpha_b \alpha_s, \alpha_t^2, \alpha_t \alpha_b)$ at vanishing external momentum taken over from **FeynHiggs** [21, 29, 41–45], where also the resummation of leading and subleading logarithms from the top/scalar top sector is incorporated [29],⁶

$$\hat{\Sigma}_{hh}(k^2) \approx \hat{\Sigma}_{hh}^{(1L)}(k^2) \Big|_{k^2=0}^{\text{NMSSM}} + \hat{\Sigma}_{hh}^{(2L + \text{beyond})}(k^2) \Big|_{k^2=0}^{\text{MSSM}}. \quad (31)$$

In order to facilitate the incorporation of the MSSM-like two-loop contributions from **FeynHiggs**, the renormalisation scheme chosen for the NMSSM contributions closely follows the **FeynHiggs** conventions as described in [44]. Accordingly, the stop masses are renormalised on-shell. For our numerical evaluation below we employ the MSSM contributions obtained from the version **FeynHiggs** 2.10.2⁷. The poles of the inverse propagator matrix are determined numerically. The algorithm for this procedure is the same as the one described in [54]. For the generation and calculation of the self energies the tools **FeynArts** 3.9 [71, 72] and **FormCalc** 7.4 [73, 74] have been used. The implementation of the NMSSM with real parameters was based on an automatically generated **FeynArts** model file obtained by an early version of **SARAH** [75].

4 Numerical Results

A particular goal of our numerical analysis is to test the kind of approximation in terms of MSSM-type contributions that we have used at the two-loop level. For this purpose a genuine NMSSM scenario will be studied, which gives rise to a SM-like Higgs with a predicted mass at the two-loop level of around 125 GeV and a singlet-like Higgs field with a mass that can be above or below the one of the SM-like state. In order to investigate the influence of the

⁵Details on the calculation of the renormalised self-energy contributions will be presented in a future publication.

⁶In the public version of **FeynHiggs** for the NMSSM also the recent results for momentum-dependent two-loop contributions in the MSSM of [38, 39] will be implemented.

⁷More recent updates of **FeynHiggs** contain additional contributions that are not relevant for our present investigation.

extended Higgs and higgsino sector of the NMSSM compared to the MSSM the parameter λ will be varied. In the limit $\lambda \rightarrow 0$ and constant μ_{eff} all singlet fields decouple from the remaining field spectrum. Increasing the value of λ directly translates to increasing the influence of genuine NMSSM-effects. A detailed study of the one-loop result and the quality of approximations based on partial contributions will be presented here. In order to study the approximation of restricting to MSSM-like contributions beyond one-loop order at $\mathcal{O}(\alpha_t\alpha_s)$, we will compare our result with the public tool `NMSSMCalc` [65], which incorporates the genuine NMSSM-type contributions of $\mathcal{O}(\alpha_t\alpha_s)$ using a hybrid $\overline{\text{DR}}$ /on-shell renormalisation scheme. While for the MSSM various other higher-order corrections are implemented in `FeynHiggs`, the corresponding contributions have not been taken into account in `NMSSMCalc`. We will compare in this context the numerical effect of the NMSSM-type contributions of $\mathcal{O}(\alpha_t\alpha_s)$ as implemented in `NMSSMCalc` with the MSSM-type contributions of this order, and we will investigate the numerical impact of the MSSM-type corrections beyond $\mathcal{O}(\alpha_t\alpha_s)$.

In our numerical discussion below we will just focus on the masses of the two lighter \mathcal{CP} -even states. A more detailed investigation for all states in the Higgs sector and their relevant mixing contributions in different scenarios will be provided in a forthcoming publication.

4.1 Numerical Scenario and Treatment of Input Parameters

The sample scenario for our study is defined by the parameters given in tab. 2. The parameter λ is varied if not stated otherwise. For values $\lambda \gtrsim 0.32$ the mass of the lightest state becomes tachyonic at tree-level for this scenario, and therefore the analyses will be performed only for values of λ up to 0.32. The choice for the top-quark mass in the loop contributions will be the pole mass m_t^{OS} for the comparison with `NMSSMCalc` and $m_t^{\overline{\text{MS}}}(m_t)$ for the remaining studies. Using the $\overline{\text{MS}}$ top-quark mass allows us to include the resummation of leading and next-to-leading logarithms implemented in `FeynHiggs`. The renormalisation scale for the studies in this chapter will be fixed at the used value of the top-quark mass.

The viability of the discussed scenario is tested with the full set of experimental data implemented in the tool `HiggsBounds` 4.1.3 [76–80]. In order to obtain the necessary input for `HiggsBounds` we made use of `NMSSMTools` 4.4.0 [9] and linked it with `HiggsBounds`. While our calculation assumes an on-shell renormalised stop-sector as in [44], the SLHA input file for `NMSSMTools` needs $\overline{\text{DR}}$ -parameters for the stop-sector. Thus a conversion from the on-shell into the $\overline{\text{DR}}$ scheme is necessary for the parameters of the sample scenario given in tab. 2. We only accounted for the dominant effect of these conversions that occurs for $X_t = A_t - \mu_{\text{eff}} \cot \beta$ by applying the on-shell to $\overline{\text{DR}}$ conversion outlined in [81]. We find that the scenario is in agreement with the experimental limits implemented in `HiggsBounds` 4.1.3.

4.2 Full Result at Two-Loop Order

The full results for the tree-level, one- and two-loop Higgs-mass predictions in the sample scenario defined in tab. 2 are shown as a function of λ in fig. 1 for the two lighter \mathcal{CP} -even fields. The term “full result” refers to all one-loop corrections in the NMSSM (including the full momentum dependence and also the reparametrisation of the electromagnetic coupling in terms of the Fermi constant), supplemented with all available contributions of

Higgs sector parameters:

heavy fermion masses:

M_{H^\pm}	$\tan\beta$	μ_{eff}	A_κ	κ	m_t^{OS}	$m_t^{\overline{\text{MS}}}(m_t)$	$m_b^{\overline{\text{MS}}}(m_b)$	m_τ
1000	8	125	-300	0.2	173.2	167.48	4.2	1.78

sfermion- and gaugino-parameters:

$M_{\tilde{q}}$	$M_{\tilde{l}}$	A_t	A_τ, A_b, A_q	A_l	$M_1^{(\text{GUT})}$	M_2	M_3
1500	200	-2000	-1500	-100	≈ 143	300	1500

$M_{\tilde{q}}$	universal squark mass breaking parameter
$M_{\tilde{l}}$	universal slepton mass breaking parameter
$A_{t/b/q}$	trilinear breaking term for stop-/sbottom/the lighter squark-generations
$A_{\tau/l}$	trilinear breaking term for stau/the two lighter slepton-generations
$M_{\{1,2,3\}}$	Gaugino mass breaking parameters for $U(1)_Y$, $SU(2)_L$, $SU(3)_c$.

Table 2: Definition of the analysed sample scenario. All dimensionful parameters are given in GeV. All $\overline{\text{DR}}$ -parameters are defined at $m_t^{\overline{\text{MS}}}(m_t)$. All stop-parameters are on-shell parameters. As indicated by the superscript “(GUT)”, M_1 is related to M_2 by the usual GUT relation, $M_1^{(\text{GUT})} = 5s_w^2/(3c_w^2)M_2$.

$\mathcal{O}(\alpha_t\alpha_s, \alpha_b\alpha_s, \alpha_t^2, \alpha_t\alpha_b)$ from the MSSM, and including the resummation of large logarithms. For this study the parameter λ will be varied between 0.1 and 0.32. The lower limit on the parameter λ has been chosen such that in the considered parameter region a cross-over type behaviour occurs only for the two smaller masses, m_{h_1} and m_{h_2} (for values $\lambda < 0.1$ there is another point with cross-over behaviour of the two larger Higgs-boson masses; however, because of the small values of λ this region is less suitable for studying the behaviour of the genuine NMSSM-corrections, which scale with λ).

The variation of the two masses with λ clearly shows a cross-over type behaviour between the masses, which is correlated to their mixing character w.r.t. the singlet field and the doublet fields. For small values of λ the field h_1 is doublet-like in this scenario and, based on the prediction incorporating all available higher-order corrections, can be identified with the signal that was detected at the LHC at about 125 GeV. The prediction for m_{h_1} varies only very little with λ in this region. The field h_2 , on the other hand, is predominantly singlet-like in this parameter region, and its mass prediction falls steeply with increasing λ . The cross-over occurs at $\lambda_c^{(0)} \approx 0.26$ at tree-level, at $\lambda_c^{(1)} \approx 0.22$ at one-loop order, and at $\lambda_c^{(2)} \approx 0.23$ at two-loop order. Above the cross-over point the behaviour of the two masses and the admixture of the fields h_1 and h_2 in terms of singlet and doublet fields are reversed. The two fields are evenly mixed between singlet- (i.e., genuine NMSSM-type) and doublet-

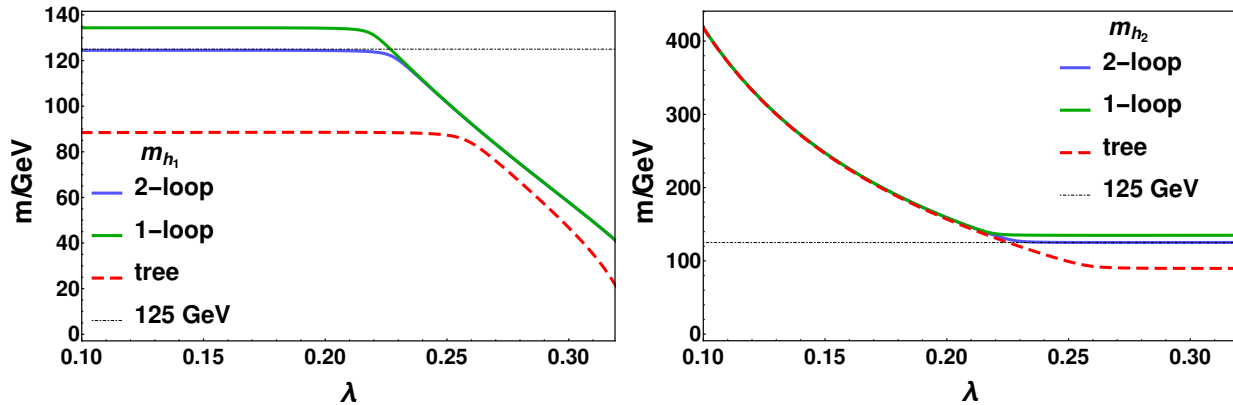


Figure 1: Mass of the lightest and next-to lightest \mathcal{CP} -even Higgs-states, m_{h_1} (left) and m_{h_2} (right), at tree-level, one-loop and two-loop order. At one-loop order all corrections of the NMSSM are included with their momentum-dependence. The two-loop corrections are approximated by the MSSM-type contributions of $\mathcal{O}(\alpha_t\alpha_s, \alpha_b\alpha_s, \alpha_t^2, \alpha_t\alpha_b)$ including the resummation of the leading and next-to-leading logarithms (see text). The dotted line represents 125 GeV. The λ values for which a cross-over behaviour between the masses occurs are at the tree-level $\lambda_c^{(0)} \approx 0.26$, at one-loop order $\lambda_c^{(1)} \approx 0.22$ and at two-loop order $\lambda_c^{(2)} \approx 0.23$.

field (i.e., MSSM-type) components for $\lambda_c^{(n)}$, with $n = 0, 1, 2$. The heaviest \mathcal{CP} -even Higgs field, h_3 , is doublet-like in the depicted interval of λ . As in the MSSM, the larger masses (of doublet-like fields) are affected by higher-order corrections to a lesser extent than the lighter states. Since at $\lambda_c^{(n)}$ the MSSM-type and genuine NMSSM-type contributions enter at equal footing, the SM-like state is most sensitive to genuine NMSSM-type contributions in the region of the cross-over behaviour.

4.3 Numerically leading Contributions at the one-loop Level

For the prediction in the MSSM the top/stop sector contributions are numerically leading. In the studied scenario, given in tab. 2, the genuine NMSSM-corrections are suppressed w.r.t. the corresponding MSSM-like stop-corrections since $\lambda \lesssim 0.32 < Y_t$, see the discussion in sect. 2.4. Thus, the genuine NMSSM corrections from this sector are expected to be sub-leading.

In order to study the impact of the genuine NMSSM contributions we compare the approximation based on the leading MSSM-type one-loop corrections in the gauge-less limit of $\mathcal{O}(Y_t^2)$, labelled as “ t/\tilde{t} -MSSM” in fig. 2, with the one where the genuine NMSSM corrections of $\mathcal{O}(\lambda Y_t, \lambda^2)$ are incorporated. The difference between the mass predictions in the two approximations is plotted as a function of λ for m_{h_1} and m_{h_2} in the left plot of fig. 2.⁸ We find that for the whole range of λ in the plot the impact of the genuine NMSSM corrections of $\mathcal{O}(\lambda Y_t, \lambda^2)$ remains less than 0.5 GeV. The largest difference between the two approximations occurs for the light singlet-like state h_1 at large values of λ close to the upper limit of $\lambda \approx 0.32$ shown in the plot. In fact, for m_{h_1} the difference between the two approximations

⁸The prediction for the heaviest \mathcal{CP} -even state, m_{h_3} , is not shown here since the difference between the two approximations does not exceed 10 MeV in our sample scenario .

is seen to rise sharply for increasing values of λ . On the other hand, at the λ value where the cross-over behaviour occurs, $\lambda_c^{(1)}$, the difference between the two approximations is seen to have a local maximum but remains small, below 0.1 GeV. For the doublet-like state, which has a one-loop mass of more than 130 GeV (see fig. 1), the corrections from genuine NMSSM-contributions remain below the level of 1‰ over the whole range of λ . Thus, the approximation based on the MSSM-type contributions is seen to provide a very accurate prediction for the top/stop sector contributions to the mass of a doublet-like state. For the singlet-like state, where the deviation grows with λ , the deviation reaches $\approx 1\%$ for the one-loop mass of the singlet-like state of ≈ 40 GeV for $\lambda \approx 0.32$.

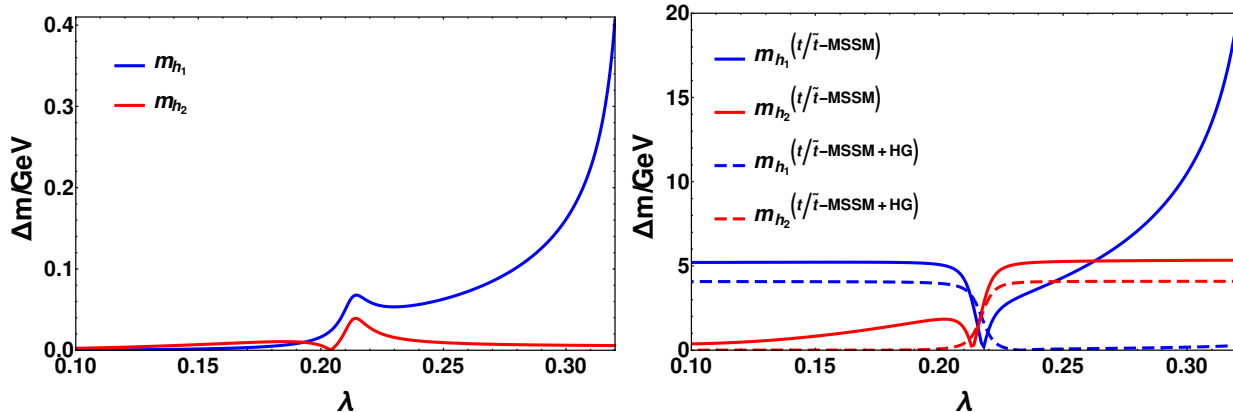


Figure 2: Absolute difference between partial and full results for the one-loop masses of the two lighter \mathcal{CP} -even fields. The value of λ where the cross-over behaviour occurs is $\lambda_c \approx 0.22$. *Left:* Absolute difference between the mass predictions including and excluding the genuine NMSSM contributions from the stops of $\mathcal{O}(\lambda Y_t, \lambda^2)$ for m_{h_1} and m_{h_2} . *Right:* Absolute differences between the mass predictions based on two different one-loop approximations and the full one-loop result. The solid lines, labelled as “ t/\tilde{t} -MSSM”, depict the difference between the full result and the approximation based on the leading MSSM-type contributions from the top/stop sector, $\Delta m_{h_i} = |m_{h_i}^{(1L)} - m_{h_i}^{t/\tilde{t}\text{-MSSM}}|$. The dashed lines, labelled as “ t/\tilde{t} -MSSM + HG”, show the corresponding result where the leading MSSM-type contributions from the top/stop sector are supplemented by the contributions from the Higgs-/higgsino- and gauge-/gaugino-sectors, $\Delta m_{h_i} = |m_{h_i}^{(1L)} - m_{h_i}^{t/\tilde{t}\text{-MSSM+HG}}|$.

The sharp increase of the corrections of $\mathcal{O}(\lambda Y_t, \lambda^2)$ for the highest values of λ that is visible for the light singlet-like field in the left plot of fig. 2 indicates that the approximation for the stop sector of restricting to the MSSM-type contributions becomes questionable for the singlet-like state in this region. However, as shown in the right plot of fig. 2, in this parameter region the stop sector as a whole ceases to provide a reliable approximation of the full one-loop contributions. In the right plot the difference between the full result and the approximation based on the leading MSSM-type contributions from the top/stop sector, $\Delta m_{h_i} = |m_{h_i}^{(1L)} - m_{h_i}^{t/\tilde{t}\text{-MSSM}}|$, is shown together with $\Delta m_{h_i} = |m_{h_i}^{(1L)} - m_{h_i}^{t/\tilde{t}\text{-MSSM+HG}}|$, where in the latter case the leading MSSM-type contributions from the top/stop sector are supplemented by the contribution from the Higgs-higgsino and gauge-/gaugino-sectors. While for the singlet-like state the deviation between the leading contributions from the

top/stop sector and the full one-loop result becomes huge for the largest values of λ , reaching the level of 20 GeV, the deviations stay small, far below the level of 1 GeV, if the leading contributions from the top/stop sector are supplemented by the contributions from the Higgs-/higgsino- and gauge-gaugino-sectors. This result for the singlet-like state can be understood from the fact that the gauge couplings of the singlet-like state are heavily suppressed and that therefore the leading contributions for large λ arise from the Higgs and higgsino sector. Thus, improving on the approximation of MSSM-type contributions in the stop sector requires the incorporation of the contributions from the Higgs and higgsino sector, while the genuine NMSSM contributions in the stop sector are of minor significance in this context.

For the doublet-like state, namely h_1 for values $\lambda \lesssim \lambda_c$ and h_2 for $\lambda \gtrsim \lambda_c$, the difference between the full one-loop result and the result based on the leading contributions from the top/stop sector amounts to a shift of about 5 GeV that is essentially independent of λ except for the region where the cross-over behaviour occurs. This nearly constant shift arises mainly from sub-leading contributions in the top/stop sector. As indicated by the dashed lines, the inclusion of the contributions from the Higgs and the gauge sector reduces the difference to the full one-loop result by about 1 GeV.

As a result of the comparison performed in this section the MSSM-type top/stop sector contributions of $\mathcal{O}(Y_t^2)$ have been verified as the leading one-loop contributions to MSSM-like fields. The genuine NMSSM top/stop sector contributions of $\mathcal{O}(\lambda Y_t, \lambda^2)$ have the largest impact on singlet-like fields for large values of λ , where however an approximation based only on contributions from the fermion/sfermion sector is in any case insufficient. Our analysis at the one-loop level therefore shows that approximating the result for the top/sector by the leading MSSM-type contributions turns out to work well in the parameter regions where the top/stop sector itself yields a reasonable approximation of the full result. These findings provide a strong motivation for applying the same kind of approximation also at the two-loop level.

4.4 Comparison with `NMSSMCalc`

For the comparison of our results with available tools the code `NMSSMCalc` [65] is particularly suitable, since it is the only public tool using also a mixed $\overline{\text{DR}}$ /on-shell renormalisation scheme. In this section the numerical differences between the results for the masses of the two lighter Higgs states from `NMSSMCalc` and our calculation will be discussed at different orders for the scenario given in tab 2. Both codes, `NMSSMCalc` and our calculation, labelled `NMSSM-FeynHiggs` in the following, have been adapted for this comparison. The two codes interpret the input parameters in the stop-sector as defined for on-shell renormalised masses of the stops⁹. Since `NMSSMCalc` uses a different charge renormalisation associated with the value $\alpha(M_Z)$ for the electromagnetic coupling constant, we have reparametrised our result as described in sec. 2.3. The numerical values for $\alpha(M_Z)$ and $\Delta\alpha$ have been taken directly from `NMSSMCalc` for this comparison,

$$\Delta\alpha = \Delta\alpha_{\text{had}}^{(5)} + \Delta\alpha_{\text{lep}} = 5.89188 \cdot 10^{-2}, \quad \alpha(M_Z) = 1/128.962. \quad (32)$$

After the reparametrisation is applied the only difference between the one-loop Higgs-mass predictions of `NMSSM-FeynHiggs` and `NMSSMCalc` stems from the finite contribution of δv used

⁹We thank Kathrin Walz for providing a modified version of `NMSSMCalc` for this feature.

in `NMSSMCalc`. Beyond the one-loop level only MSSM two-loop contributions of $\mathcal{O}(\alpha_t\alpha_s)$ (calculated for on-shell renormalised top- and stop-masses) are considered in `NMSSM-FeynHiggs` for this comparison, as only their NMSSM-counterparts are implemented in `NMSSMCalc`. Two-loop corrections beyond the ones of $\mathcal{O}(\alpha_t\alpha_s)$ as well as the resummation of logarithms, which are incorporated in the default version of `NMSSM-FeynHiggs`, are not included for the analysis in this section (for a discussion of their size see sec. 4.5). For simplicity, we will refer to this reduced set of two-loop contributions as “two-loop order” throughout this section. The remaining differences between the Higgs-mass calculations of `NMSSMCalc` and `NMSSM-FeynHiggs` in this set-up are summarised in tab. 3. The applied modifications ensure that the comparison between the codes will quantify the numerical impact of the genuine NMSSM two-loop corrections of $\mathcal{O}(Y_t\lambda\alpha_s, \lambda^2\alpha_s)$.

NMSSMCalc			NMSSM-FeynHiggs	
one-loop	$\alpha_{\text{em}}(M_Z)$ renormalised	\leftrightarrow	$\alpha_{\text{em}}(M_Z)$ reparametrised	
two-loop	NMSSM $\mathcal{O}(\alpha_t\alpha_s)$	\leftrightarrow	MSSM $\mathcal{O}(\alpha_t\alpha_s)$	

Table 3: Main calculational differences between `NMSSMCalc` and our result (labelled `NMSSM-FeynHiggs`) in the set-up used for the comparison in sec. 4.4. The difference at one-loop order is caused only by the different renormalisation of the electric charge, described in sec. 2.3. At two-loop order the codes in this set-up only differ by the genuine NMSSM contributions of $\mathcal{O}(Y_t\lambda\alpha_s, \lambda^2\alpha_s)$. The two-loop MSSM corrections beyond $\mathcal{O}(\alpha_t\alpha_s)$ and the resummation of logarithms are switched off in `NMSSM-FeynHiggs` for the comparison in sec. 4.4.

We used the SM parameters as specified in the built-in standard input files of `NMSSMCalc` for this comparison. We passed over the input values in the quark- and squark-sectors as on-shell parameters from `NMSSM-FeynHiggs` to `NMSSMCalc`. The pole mass for the top, $m_t = 173.2$ GeV, has been used in the loop contributions in this section, and the renormalisation scale has been chosen as m_t . For the comparison the identical value $\alpha_s^{\overline{\text{MS}}}(m_t^{(\text{OS})}) = 0.1069729$ has been used for both codes (using the evaluation in `NMSSMCalc` with the routines of [82]).

In a first step the one- and two-loop results of `NMSSMCalc` and `NMSSM-FeynHiggs` have been compared in the MSSM-limit, where λ and κ vanish simultaneously. Both the effects of the different renormalisation schemes and the reparametrisation have to vanish in this limit and thus the results have to be identical. The one- and two-loop results for the mass of the lightest \mathcal{CP} -even field obtained in this limit with both codes, 140.742 GeV and 116.902 GeV, respectively, are in agreement with each other with a precision of better than 1 MeV.

This confirms that the MSSM-contributions are treated identically in both calculations. Thus all observed differences between the results for non-vanishing values of λ and κ can be associated to the treatment of the genuine NMSSM-contributions and residual higher-order effects of the different renormalisation of v after the reparametrisation.

For the sample scenario defined in tab. 2 the absolute differences between the two mass predictions are plotted in fig. 3 as functions of λ for the two lighter \mathcal{CP} -even states at one- and two-loop order¹⁰, $\Delta m_{h_i} = m_{h_i}^{\text{NMSSM-FH}} - m_{h_i}^{\text{NMSSMcalc}}$. The left plot in fig. 3 shows the mass

¹⁰The variation of the mass of the heaviest state is smaller than 2 MeV and thus not plotted in fig. 3.

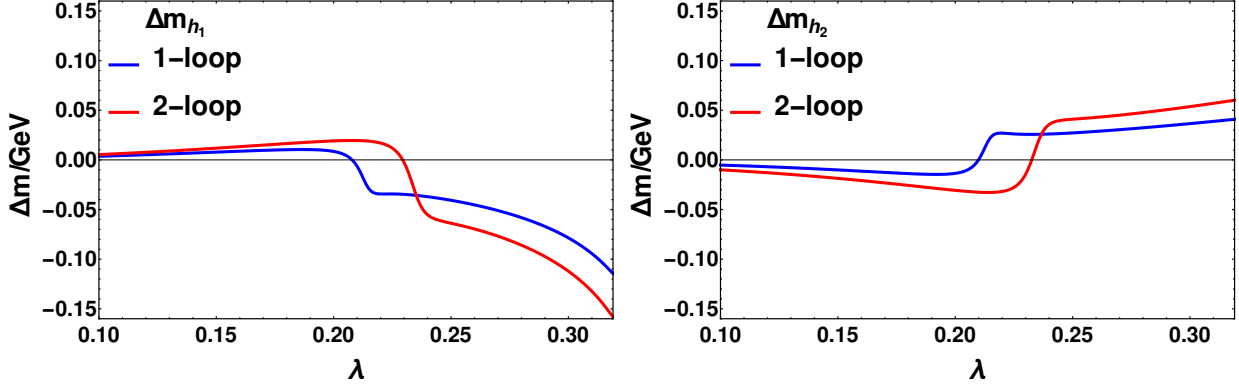


Figure 3: Difference between the mass predictions for the two lighter \mathcal{CP} -even fields h_1 and h_2 from `NMSSMCalc` and `NMSSM-FeynHiggs` at one- and two-loop order, $\Delta m_{h_i} = m_{h_i}^{\text{NMSSM-FH}} - m_{h_i}^{\text{NMSSMcalc}}$. The result of `NMSSM-FeynHiggs` has been reparametrised to $\alpha(M_Z)$. The points where the cross-over behaviour of the fields h_1 and h_2 occurs at one- and two-loop order are $\lambda_c^{(1)} \approx 0.21$ and $\lambda_c^{(2)} \approx 0.24$, respectively.

for the lighter state h_1 , and the mass for the heavier state h_2 is shown in the right plot. The state h_1 behaves doublet-like for values $\lambda \lesssim \lambda_c^{(n)}$ and singlet-like for values $\lambda \gtrsim \lambda_c^{(n)}$. The behaviour of h_2 is the opposite. The values of Δm_{h_i} are seen to be positive for the doublet-like field and negative for the singlet-like field. We find that the difference between the two calculations is small for both mass predictions over the whole range of λ . As expected, the largest differences, reaching about 150 MeV for Δm_{h_1} , occur for the mass of the singlet-like state for the largest values of λ in the plot. The mass of the doublet-like state is affected to a lesser extent by approximating the $\mathcal{O}(\alpha_t \alpha_s)$ correction by the MSSM-type contributions. The relative differences in the cross-over region are found to be less significant than for the largest values of λ . The general shape of the one-loop difference, caused by the different treatment of the charge renormalisation, is seen to be maintained at the two-loop level. The main feature at the two-loop level is the shift in the cross-over points by $\Delta \lambda_c = \lambda_c^{(2)} - \lambda_c^{(1)} \approx 0.03$ between one- and two-loop order, while otherwise the difference in the $\mathcal{O}(\alpha_t \alpha_s)$ contributions is found to have a very small effect. This can be seen for instance by comparing the local and global extrema at $\lambda_c^{(n)}$ and for the largest values of λ . Specifically, for $\lambda = 0.32$ we find that the impact of the genuine NMSSM contributions of $\mathcal{O}(\alpha_t \alpha_s)$ that are implemented only in `NMSSMCalc` amounts to $\Delta m_{h_1}(\lambda_c) \lesssim 50$ MeV for h_1 (for a Higgs mass of $m_{h_1} \approx 40$ GeV) and $\Delta m_{h_2}(\lambda_c) \lesssim 30$ MeV for h_2 (for a Higgs mass of $m_{h_2} \approx 125$ GeV).

These results confirm that the approximation in terms of MSSM-type contributions at the two-loop level induces an uncertainty that is numerically small if $\lambda < Y_t$, as discussed in the previous sections. As expected, the approximation works best for the MSSM-like fields, but the relative effect stays below the level of about 0.13% even for the light singlet mass and large values of λ . The different renormalisation schemes for δv and δZ_e at the one-loop level have a larger, but still small impact on the results in the considered scenario.

4.5 Impact of additional Corrections beyond $\mathcal{O}(\alpha_t\alpha_s)$

While the genuine NMSSM two-loop corrections of $\mathcal{O}(Y_t\lambda\alpha_s, \lambda^2\alpha_s)$ induce a very small effect below 50 MeV, the MSSM two-loop corrections beyond $\mathcal{O}(\alpha_t\alpha_s)$ and the resummation of large logarithms can result in a shift for the mass of the light doublet-like field of several GeV. In order to quantify the impact of the additional MSSM-contributions of $\mathcal{O}(\alpha_t^2, \alpha_b\alpha_s, \alpha_t\alpha_b)$ and the resummation of logarithms, which are incorporated in `NMSSM-FeynHiggs`, the results with and without these corrections are plotted as functions of λ in fig. 4. Here the one-loop

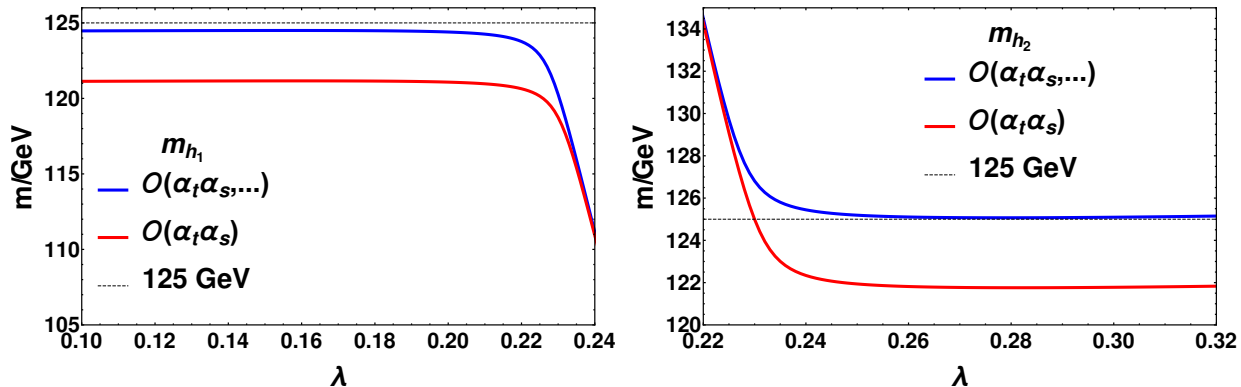


Figure 4: Mass predictions for the two lighter \mathcal{CP} -even fields h_1 and h_2 for different contributions at two-loop order. The blue lines include all MSSM-type corrections of $\mathcal{O}(\alpha_t\alpha_s, \alpha_b\alpha_s, \alpha_t^2, \alpha_t\alpha_b)$ and the resummation of large logarithms as included in `FeynHiggs` 2.10.2, while for the red curves only the MSSM-type corrections of $\mathcal{O}(\alpha_t\alpha_s)$ are included beyond the full one-loop contributions. The thin horizontal line marks 125 GeV.

$\overline{\text{MS}}$ -value of the top-quark, $m_t^{\overline{\text{MS}}}(m_t)$, is used in the loop contributions. A sizeable shift of about 3–4 GeV can be observed for the mass of the doublet-like field. As expected, the impact of the MSSM-type two-loop contributions on the mass prediction for the singlet-like field remains small. In comparison with the contributions discussed in the previous section we find that the effect of the additional corrections beyond $\mathcal{O}(\alpha_t\alpha_s)$ can exceed the numerical impact of the genuine NMSSM-corrections of $\mathcal{O}(Y_t\lambda\alpha_s, \lambda^2\alpha_s)$ by more than two orders of magnitude.

5 Conclusions

We have presented predictions for the Higgs-boson masses in the NMSSM obtained within the Feynman-diagrammatic approach. They are based on the full NMSSM one-loop corrections supplemented with the dominant and sub-dominant two-loop corrections of MSSM-type, including contributions at $\mathcal{O}(\alpha_t\alpha_s, \alpha_b\alpha_s, \alpha_t^2, \alpha_t\alpha_b)$, as well as a resummation of leading and subleading logarithms from the top/scalar top sector. In order to enable a direct comparison with the corresponding results in the MSSM, the renormalisation scheme and all parameters and conventions have been chosen such that the well-known MSSM result of the code `FeynHiggs` is recovered in the MSSM limit of the NMSSM.

In our phenomenological analysis we have investigated a scenario where depending on the value of λ either the lightest or the next-to-lightest neutral Higgs state can be identified with a SM-like Higgs boson at about 125 GeV. As expected, in both cases this state is doublet-like, i.e. it receives only small contributions from the singlet state of the NMSSM. The inclusion of the higher-order contributions which are known for the MSSM is crucial in this context in order to obtain an accurate prediction for the mass spectrum.

We have investigated different approximations at the one-loop level in comparison with our full one-loop result for the NMSSM. We have found that the approximation of the result for the top/stop sector in terms of the leading MSSM-type contributions works well in the parameter regions where the top/stop sector itself yields a reasonable approximation of the full result. It therefore appears to be well motivated to make use of this approximation at the two-loop level. The genuine NMSSM top/stop sector contributions of $\mathcal{O}(Y_t\lambda, \lambda^2)$ can be significant for singlet-like fields if λ is large. For such large values of λ , however, the improvement achieved by including those genuine NMSSM contributions from the top/stop sector is by far overshadowed by the fact that contributions from the Higgs- and higgsino-sector become more and more important for a singlet-like Higgs field.

We have compared our predictions with the public code `NMSSMCalc` for on-shell parameters in the top/stop sector. For the purpose of this comparison we have done an appropriate reparametrisation of the electromagnetic coupling constant, and we have switched off the two-loop corrections beyond the ones of $\mathcal{O}(\alpha_t\alpha_s)$ as well as the resummation of leading and subleading logarithms in our code. After those adaptations the predictions of the two codes only differ in the charge renormalisation at the one-loop level and in the genuine NMSSM top/stop sector contributions of $\mathcal{O}(Y_t\lambda\alpha_s, \lambda^2\alpha_s)$ at the two-loop level. Since these differences arise only from contributions beyond the MSSM, agreement between the predictions of the two codes is expected in the MSSM limit of the NMSSM. We have indeed found that the results obtained with the two codes perfectly agree with each other in this case. For the case of the NMSSM we have compared the predictions of the two codes as a function of λ . We have found that the differences stay small over the whole range of λ , with a maximum difference in the mass of the light singlet-like state of about 150 MeV in the considered scenario. The difference is mainly caused by the different treatment of the charge renormalisation at the one-loop level, while the effect of the genuine NMSSM top/stop sector contributions of $\mathcal{O}(Y_t\lambda\alpha_s, \lambda^2\alpha_s)$ is found to be significantly smaller.

As a final step of our numerical analysis we have investigated the impact of the MSSM-corrections beyond $\mathcal{O}(\alpha_t\alpha_s)$ and the resummation of large logarithms that are incorporated in our code but not in `NMSSMCalc`. While those corrections are small for the mass of the singlet-like state, they amount to an effect of 3 – 4 GeV for the mass of the doublet-like state in the considered scenario. This is more than two orders of magnitude larger than the corresponding effect of the genuine NMSSM-corrections of $\mathcal{O}(Y_t\lambda\alpha_s, \lambda^2\alpha_s)$.

The results presented in this paper will be used as a basis for the extension of the code `FeynHiggs` to the NMSSM.

Acknowledgements

We want to thank Ramona Gröber, Margarete Mühlleitner, Heidi Rzehak, Oscar Stål and Kathrin Waltz for interesting discussions, useful input and interfaces with their codes. We thank Melina Gomez Bock, Rachid Benbrik and Pietro Slavich for helpful communication. The work of S.H. is supported in part by CICYT (grant FPA 2013-40715-P) and by the Spanish MICINN's Consolider-Ingenio 2010 Program under grant MultiDark CSD2009-00064. The authors acknowledge support by the DFG through the SFB 676 "Particles, Strings and the Early Universe". This research was supported in part by the European Commission through the "HiggsTools" Initial Training Network PITN-GA-2012-316704.

References

- [1] ATLAS Collaboration, G. Aad *et al.*, Observation of a new particle in the search for the Standard Model Higgs boson with the ATLAS detector at the LHC, *Phys.Lett.* **B716**, 1 (2012), 1207.7214.
- [2] CMS Collaboration, S. Chatrchyan *et al.*, Observation of a new boson at a mass of 125 GeV with the CMS experiment at the LHC, *Phys.Lett.* **B716**, 30 (2012), 1207.7235.
- [3] K. Tackmann, talk given at *LHCP 2015*, September 2015, St. Petersburg, Russia, see: <https://indico.cern.ch/event/389531/session/31/contribution/50/attachments/1147367/1645479/LHCP2015.pdf>.
- [4] M. Pieri, talk given at *LHCP 2015*, September 2015, St. Petersburg, Russia, see: https://indico.cern.ch/event/389531/session/31/contribution/51/attachments/1147368/1650410/LHCHCP-MarcoPieri_fin.1.pdf.
- [5] H. P. Nilles, Supersymmetry, Supergravity and Particle Physics, *Phys.Rept.* **110**, 1 (1984).
- [6] H. E. Haber and G. L. Kane, The Search for Supersymmetry: Probing Physics Beyond the Standard Model, *Phys.Rept.* **117**, 75 (1985).
- [7] S. Heinemeyer, O. Stal, and G. Weiglein, Interpreting the LHC Higgs Search Results in the MSSM, *Phys.Lett.* **B710**, 201 (2012), 1112.3026.
- [8] K. Jakobs, G. Quast, and G. Weiglein, Higgs-Boson Physics at the LHC, in *The Large Hadron Collider: Harvest of Run 1*, edited by T. Schörner-Sadenius, pp. 195–258, Springer, 2015.
- [9] U. Ellwanger, C. Hugonie, and A. M. Teixeira, The Next-to-Minimal Supersymmetric Standard Model, *Phys.Rept.* **496**, 1 (2010), 0910.1785.
- [10] M. Maniatis, The Next-to-Minimal Supersymmetric extension of the Standard Model reviewed, *Int.J.Mod.Phys.* **A25**, 3505 (2010), 0906.0777.
- [11] J. R. Ellis, J. Gunion, H. E. Haber, L. Roszkowski, and F. Zwirner, Higgs Bosons in a Nonminimal Supersymmetric Model, *Phys.Rev.* **D39**, 844 (1989).

- [12] D. Miller, R. Nevzorov, and P. Zerwas, The Higgs sector of the next-to-minimal supersymmetric standard model, *Nucl.Phys.* **B681**, 3 (2004), hep-ph/0304049.
- [13] S. F. King, M. Muhlleitner, and R. Nevzorov, NMSSM Higgs Benchmarks Near 125 GeV, *Nucl. Phys.* **B860**, 207 (2012), 1201.2671.
- [14] F. Domingo and G. Weiglein, NMSSM interpretations of the observed Higgs signal, (2015), 1509.07283.
- [15] ATLAS, CMS, G. Aad *et al.*, Combined Measurement of the Higgs Boson Mass in pp Collisions at $\sqrt{s} = 7$ and 8 TeV with the ATLAS and CMS Experiments, (2015), 1503.07589.
- [16] P. Z. Skands and D. Wicke, Non-perturbative QCD effects and the top mass at the Tevatron, *Eur. Phys. J.* **C52**, 133 (2007), hep-ph/0703081.
- [17] A. H. Hoang and I. W. Stewart, Top Mass Measurements from Jets and the Tevatron Top-Quark Mass, *Nucl. Phys. Proc. Suppl.* **185**, 220 (2008), 0808.0222.
- [18] A. H. Hoang, The Top Mass: Interpretation and Theoretical Uncertainties, in *7th International Workshop on Top Quark Physics (TOP2014) Cannes, France, September 28-October 3, 2014*, 2014, 1412.3649.
- [19] S. Heinemeyer, W. Hollik, and G. Weiglein, QCD corrections to the masses of the neutral CP - even Higgs bosons in the MSSM, *Phys. Rev.* **D58**, 091701 (1998), hep-ph/9803277.
- [20] S. Heinemeyer, W. Hollik, and G. Weiglein, Precise prediction for the mass of the lightest Higgs boson in the MSSM, *Phys. Lett.* **B440**, 296 (1998), hep-ph/9807423.
- [21] S. Heinemeyer, W. Hollik, and G. Weiglein, The Masses of the neutral CP - even Higgs bosons in the MSSM: Accurate analysis at the two loop level, *Eur.Phys.J.* **C9**, 343 (1999), hep-ph/9812472.
- [22] R.-J. Zhang, Two loop effective potential calculation of the lightest CP even Higgs boson mass in the MSSM, *Phys. Lett.* **B447**, 89 (1999), hep-ph/9808299.
- [23] J. R. Espinosa and R.-J. Zhang, MSSM lightest CP even Higgs boson mass to $O(\alpha(s), \alpha(t))$: The Effective potential approach, *JHEP* **03**, 026 (2000), hep-ph/9912236.
- [24] G. Degrandi, P. Slavich, and F. Zwirner, On the neutral Higgs boson masses in the MSSM for arbitrary stop mixing, *Nucl. Phys.* **B611**, 403 (2001), hep-ph/0105096.
- [25] J. R. Espinosa and R.-J. Zhang, Complete two loop dominant corrections to the mass of the lightest CP even Higgs boson in the minimal supersymmetric standard model, *Nucl. Phys.* **B586**, 3 (2000), hep-ph/0003246.
- [26] A. Brignole, G. Degrandi, P. Slavich, and F. Zwirner, On the $O(\alpha(t)^2)$ two loop corrections to the neutral Higgs boson masses in the MSSM, *Nucl. Phys.* **B631**, 195 (2002), hep-ph/0112177.

- [27] A. Brignole, G. Degrandi, P. Slavich, and F. Zwirner, On the two loop sbottom corrections to the neutral Higgs boson masses in the MSSM, *Nucl. Phys.* **B643**, 79 (2002), hep-ph/0206101.
- [28] S. Heinemeyer, W. Hollik, H. Rzehak, and G. Weiglein, High-precision predictions for the MSSM Higgs sector at $O(\alpha(b) \alpha(s))$, *Eur. Phys. J.* **C39**, 465 (2005), hep-ph/0411114.
- [29] T. Hahn, S. Heinemeyer, W. Hollik, H. Rzehak, and G. Weiglein, High-precision predictions for the light CP-even Higgs Boson Mass of the MSSM, *Phys.Rev.Lett.* **112**, 141801 (2014), 1312.4937.
- [30] P. Draper, G. Lee, and C. E. M. Wagner, Precise estimates of the Higgs mass in heavy supersymmetry, *Phys. Rev.* **D89**, 055023 (2014), 1312.5743.
- [31] G. Lee and C. E. M. Wagner, Higgs Bosons in Heavy Supersymmetry with an Intermediate m_A , (2015), 1508.00576.
- [32] R. Hempfling, Yukawa coupling unification with supersymmetric threshold corrections, *Phys. Rev.* **D49**, 6168 (1994).
- [33] L. J. Hall, R. Rattazzi, and U. Sarid, The Top quark mass in supersymmetric SO(10) unification, *Phys. Rev.* **D50**, 7048 (1994), hep-ph/9306309.
- [34] M. Carena, M. Olechowski, S. Pokorski, and C. E. M. Wagner, Electroweak symmetry breaking and bottom - top Yukawa unification, *Nucl. Phys.* **B426**, 269 (1994), hep-ph/9402253.
- [35] M. Carena, D. Garcia, U. Nierste, and C. E. M. Wagner, Effective Lagrangian for the $\bar{t}bH^+$ interaction in the MSSM and charged Higgs phenomenology, *Nucl. Phys.* **B577**, 88 (2000), hep-ph/9912516.
- [36] D. Noth and M. Spira, Higgs Boson Couplings to Bottom Quarks: Two-Loop Supersymmetry-QCD Corrections, *Phys. Rev. Lett.* **101**, 181801 (2008), 0808.0087.
- [37] D. Noth and M. Spira, Supersymmetric Higgs Yukawa Couplings to Bottom Quarks at next-to-next-to-leading Order, *JHEP* **06**, 084 (2011), 1001.1935.
- [38] S. Borowka, T. Hahn, S. Heinemeyer, G. Heinrich, and W. Hollik, Momentum-dependent two-loop QCD corrections to the neutral Higgs-boson masses in the MSSM, *Eur. Phys. J.* **C74**, 2994 (2014), 1404.7074.
- [39] S. Borowka, T. Hahn, S. Heinemeyer, G. Heinrich, and W. Hollik, Renormalization scheme dependence of the two-loop QCD corrections to the neutral Higgs-boson masses in the MSSM, *Eur. Phys. J.* **C75**, 424 (2015), 1505.03133.
- [40] G. Degrandi, S. Di Vita, and P. Slavich, Two-loop QCD corrections to the MSSM Higgs masses beyond the effective-potential approximation, *Eur. Phys. J.* **C75**, 61 (2015), 1410.3432.

- [41] S. Heinemeyer, W. Hollik, and G. Weiglein, FeynHiggs: A Program for the calculation of the masses of the neutral CP even Higgs bosons in the MSSM, *Comput.Phys.Commun.* **124**, 76 (2000), hep-ph/9812320.
- [42] T. Hahn, S. Heinemeyer, W. Hollik, H. Rzehak, and G. Weiglein, FeynHiggs: A program for the calculation of MSSM Higgs-boson observables - Version 2.6.5, *Comput.Phys.Commun.* **180**, 1426 (2009).
- [43] G. Degrandi, S. Heinemeyer, W. Hollik, P. Slavich, and G. Weiglein, Towards high precision predictions for the MSSM Higgs sector, *Eur.Phys.J.* **C28**, 133 (2003), hep-ph/0212020.
- [44] M. Frank *et al.*, The Higgs Boson Masses and Mixings of the Complex MSSM in the Feynman-Diagrammatic Approach, *JHEP* **0702**, 047 (2007), hep-ph/0611326.
- [45] See: www.feynhiggs.de.
- [46] S. P. Martin, Two-loop scalar self-energies and pole masses in a general renormalizable theory with massless gauge bosons, *Phys.Rev.* **D71**, 116004 (2005), hep-ph/0502168.
- [47] S. P. Martin, Three-loop corrections to the lightest Higgs scalar boson mass in supersymmetry, *Phys.Rev.* **D75**, 055005 (2007), hep-ph/0701051.
- [48] R. Harlander, P. Kant, L. Mihaila, and M. Steinhauser, Higgs boson mass in supersymmetry to three loops, *Phys.Rev.Lett.* **100**, 191602 (2008), 0803.0672.
- [49] P. Kant, R. Harlander, L. Mihaila, and M. Steinhauser, Light MSSM Higgs boson mass to three-loop accuracy, *JHEP* **1008**, 104 (2010), 1005.5709.
- [50] S. Heinemeyer, W. Hollik, and G. Weiglein, Electroweak precision observables in the minimal supersymmetric standard model, *Phys.Rept.* **425**, 265 (2006), hep-ph/0412214.
- [51] O. Buchmueller *et al.*, Implications of Improved Higgs Mass Calculations for Supersymmetric Models, *Eur.Phys.J.* **C74**, 2809 (2014), 1312.5233.
- [52] G. Degrandi and P. Slavich, On the radiative corrections to the neutral Higgs boson masses in the NMSSM, *Nucl.Phys.* **B825**, 119 (2010), 0907.4682.
- [53] F. Staub, W. Porod, and B. Herrmann, The Electroweak sector of the NMSSM at the one-loop level, *JHEP* **10**, 040 (2010), 1007.4049.
- [54] K. Ender, T. Graf, M. Muhlleitner, and H. Rzehak, Analysis of the NMSSM Higgs Boson Masses at One-Loop Level, *Phys.Rev.* **D85**, 075024 (2012), 1111.4952.
- [55] T. Graf, R. Grober, M. Muhlleitner, H. Rzehak, and K. Walz, Higgs Boson Masses in the Complex NMSSM at One-Loop Level, *JHEP* **10**, 122 (2012), 1206.6806.
- [56] W. Porod, SPheno, a program for calculating supersymmetric spectra, SUSY particle decays and SUSY particle production at e+ e- colliders, *Comput. Phys. Commun.* **153**, 275 (2003), hep-ph/0301101.

- [57] W. Porod and F. Staub, SPheno 3.1: Extensions including flavour, CP-phases and models beyond the MSSM, *Comput. Phys. Commun.* **183**, 2458 (2012), 1104.1573.
- [58] M. D. Goodsell, K. Nickel, and F. Staub, Two-loop corrections to the Higgs masses in the NMSSM, *Phys. Rev.* **D91**, 035021 (2015), 1411.4665.
- [59] P. Athron, J.-h. Park, D. Stöckinger, and A. Voigt, FlexibleSUSY - A spectrum generator for supersymmetric models, *Comput. Phys. Commun.* **190**, 139 (2015), 1406.2319.
- [60] U. Ellwanger and C. Hugonie, NMSPEC: A Fortran code for the sparticle and Higgs masses in the NMSSM with GUT scale boundary conditions, *Comput. Phys. Commun.* **177**, 399 (2007), hep-ph/0612134.
- [61] F. Domingo, A New Tool for the study of the CP-violating NMSSM, (2015), 1503.07087.
- [62] B. C. Allanach, SOFTSUSY: a program for calculating supersymmetric spectra, *Comput. Phys. Commun.* **143**, 305 (2002), hep-ph/0104145.
- [63] B. C. Allanach, P. Athron, L. C. Tunstall, A. Voigt, and A. G. Williams, Next-to-Minimal SOFTSUSY, *Comput. Phys. Commun.* **185**, 2322 (2014), 1311.7659.
- [64] B. C. Allanach, A. Bednyakov, and R. Ruiz de Austri, Higher order corrections and unification in the minimal supersymmetric standard model: SOFTSUSY3.5, *Comput. Phys. Commun.* **189**, 192 (2015), 1407.6130.
- [65] J. Baglio *et al.*, NMSSMCALC: A Program Package for the Calculation of Loop-Corrected Higgs Boson Masses and Decay Widths in the (Complex) NMSSM, *Comput. Phys. Commun.* **185**, 3372 (2014), 1312.4788.
- [66] M. Muhlleitner, D. T. Nhung, H. Rzehak, and K. Walz, Two-Loop Contributions of the Order $\mathcal{O}(\alpha_t\alpha_s)$ to the Masses of the Higgs Bosons in the CP-Violating NMSSM, (2014), 1412.0918.
- [67] F. Staub *et al.*, Higgs mass predictions of public NMSSM spectrum generators, (2015), 1507.05093.
- [68] W. Hollik and S. Paßehr, Two-loop top-Yukawa-coupling corrections to the Higgs boson masses in the complex MSSM, *Phys. Lett.* **B733**, 144 (2014), 1401.8275.
- [69] O. Stål, G. Weiglein, and L. Zeune, Improved prediction for the mass of the W boson in the NMSSM, *JHEP* **09**, 158 (2015), 1506.07465.
- [70] F. Domingo and T. Lenz, W mass and Leptonic Z-decays in the NMSSM, *JHEP* **07**, 101 (2011), 1101.4758.
- [71] J. Kublbeck, M. Bohm, and A. Denner, Feyn Arts: Computer Algebraic Generation of Feynman Graphs and Amplitudes, *Comput. Phys. Commun.* **60**, 165 (1990).

- [72] T. Hahn, Generating Feynman diagrams and amplitudes with FeynArts 3, *Comput. Phys. Commun.* **140**, 418 (2001), hep-ph/0012260.
- [73] T. Hahn and M. Perez-Victoria, Automatized one loop calculations in four-dimensions and D-dimensions, *Comput. Phys. Commun.* **118**, 153 (1999), hep-ph/9807565.
- [74] S. Agrawal, T. Hahn, and E. Mirabella, FormCalc 7.5, (2012), 1210.2628, [PoSLL2012,046(2012)].
- [75] F. Staub, SARAH, (2008), 0806.0538.
- [76] P. Bechtle, O. Brein, S. Heinemeyer, G. Weiglein, and K. E. Williams, HiggsBounds: Confronting Arbitrary Higgs Sectors with Exclusion Bounds from LEP and the Tevatron, *Comput. Phys. Commun.* **181**, 138 (2010), 0811.4169.
- [77] P. Bechtle, O. Brein, S. Heinemeyer, G. Weiglein, and K. E. Williams, HiggsBounds 2.0.0: Confronting Neutral and Charged Higgs Sector Predictions with Exclusion Bounds from LEP and the Tevatron, *Comput. Phys. Commun.* **182**, 2605 (2011), 1102.1898.
- [78] P. Bechtle *et al.*, HiggsBounds – 4: Improved Tests of Extended Higgs Sectors against Exclusion Bounds from LEP, the Tevatron and the LHC, *Eur.Phys.J.* **C74**, 2693 (2014), 1311.0055.
- [79] P. Bechtle *et al.*, Recent Developments in HiggsBounds and a Preview of HiggsSignals, *PoS CHARGED2012*, 024 (2012), 1301.2345.
- [80] P. Bechtle, S. Heinemeyer, O. Stal, T. Stefaniak, and G. Weiglein, Applying Exclusion Likelihoods from LHC Searches to Extended Higgs Sectors, *Eur. Phys. J.* **C75**, 421 (2015), 1507.06706.
- [81] K. E. Williams, H. Rzehak, and G. Weiglein, Higher order corrections to Higgs boson decays in the MSSM with complex parameters, *Eur. Phys. J.* **C71**, 1669 (2011), 1103.1335.
- [82] K. G. Chetyrkin, J. H. Kuhn, and M. Steinhauser, RunDec: A Mathematica package for running and decoupling of the strong coupling and quark masses, *Comput. Phys. Commun.* **133**, 43 (2000), hep-ph/0004189.