

Inflation from High-Scale Supersymmetry Breaking

Valerie Domcke^{a,*} and Kai Schmitz^{b,†}

^a *Deutsches Elektronen-Synchrotron (DESY), 22607 Hamburg, Germany*

^b *Max-Planck-Institut für Kernphysik (MPIK), 69117 Heidelberg, Germany*

Abstract

Supersymmetry breaking close to the scale of grand unification can explain cosmic inflation. As we demonstrate in this paper, this can be achieved in strongly coupled supersymmetric gauge theories, such that the energy scales of inflation and supersymmetry breaking are generated dynamically. As a consequence, both scales are related to each other and exponentially suppressed compared to the Planck scale. As an example, we consider a dynamical model in which gauging a global flavor symmetry in the supersymmetry-breaking sector gives rise to a Fayet-Iliopoulos D term. This results in successful D-term hybrid inflation in agreement with all theoretical and phenomenological constraints. The gauged flavor symmetry can be identified with $U(1)_{B-L}$, where B and L denote baryon and lepton number, respectively. In the end, we arrive at a consistent cosmological scenario that provides a unified picture of high-scale supersymmetry breaking, viable D-term hybrid inflation, spontaneous $B-L$ breaking at the scale of grand unification, baryogenesis via leptogenesis, and standard model neutrino masses due to the type-I seesaw mechanism.

*valerie.domcke@desy.de

†kai.schmitz@mpi-hd.mpg.de

Contents

1	Introduction: GUT-scale SUSY breaking as the origin of inflation	2
2	Model: Strong dynamics and gauged $B-L$ in the Jordan frame	5
2.1	Preliminary remarks on hybrid inflation in supergravity	5
2.2	Ingredients for a unified model of D-term inflation	7
2.3	SUSY-breaking dynamics in the hidden sector	16
2.4	Effective Polonyi model and embedding into supergravity	25
2.5	Scalar potential in the inflaton sector	29
3	Phenomenology: A viable scenario of D-term hybrid inflation	34
3.1	D-term inflation in global SUSY	34
3.2	Analytical description of the inflationary phase	35
3.3	Scan of the parameter space and numerical results	39
3.4	Initial conditions	41
4	Discussion: Particle spectrum and cosmology after inflation	43
4.1	Particle spectrum	44
4.2	The cosmology of a $B-L$ phase transition	46
4.3	Particle candidates for dark matter	47
4.4	Topological defects	48
5	Conclusions: A unified model of the early Universe	49
A	Technicalities: Supergravity in the Einstein/Jordan frame	53
A.1	Bosonic action	54
A.2	Scalar potential	56
A.3	Scalar mass parameters	58
A.4	Slow-roll parameters	60

1 Introduction: GUT-scale SUSY breaking as the origin of inflation

Supersymmetry (SUSY) is an elegant and well-motivated extension of the *standard model* (SM). In recent years, the experimental data collected at the *Large Hadron Collider* (LHC) has, however, put increasing pressure on conventional SUSY scenarios with superpartner masses around the electroweak scale. No evidence for supersymmetric particles has been found thus far; see, e.g., the recent SUSY searches by the LHC experiments ATLAS [1] and CMS [2]. Therefore, if supersymmetry exists in nature, the *superpartners of the SM particles* (sparticles) must have masses of at least $\mathcal{O}(1)$ TeV, if not much higher. The idea of heavy particles is also corroborated by the measured value of the Higgs boson mass [3, 4]. In the *Minimal Supersymmetric Standard Model* (MSSM), a 125 GeV Higgs boson [5] can only be explained by means of large radiative corrections [6–10]. This points towards a large SUSY-breaking mass splitting between the top quark and its scalar partners, the stop squarks.

If realized around the electroweak scale, supersymmetry provides a natural solution to the large hierarchy problem in the standard model. For decades, this observation has reinforced the paradigm of low-scale supersymmetry that would be testable in collider experiments. In the present experimental situation, the null results at the LHC, however, bring about the little hierarchy problem. Sparticles with masses of at least $\mathcal{O}(1)$ TeV can only be reconciled with the $\mathcal{O}(100)$ GeV value of the electroweak scale at the cost of fine-tuning. One is therefore led to adopt one of two possible attitudes. Either one gives up on supersymmetry as a well-motivated extension of the standard model, or one challenges the concept of naturalness and accepts a certain degree of fine-tuning. In this paper, we shall take the latter approach. Our understanding of naturalness may be flawed and, for some reason or another, not apply to the physics of the electroweak scale. Moreover, dismissing supersymmetry altogether would do injustice to supersymmetry's other merits. One must not forget that, irrespective of its relation to the electroweak scale, supersymmetry also (i) provides a natural particle candidate for dark matter, (ii) facilitates the unification of the SM gauge coupling constants at a high energy scale, and (iii) sets the stage for the *ultraviolet* (UV) completion of the standard model in string theory.

In fact, supersymmetry broken at a high scale [11–13] has received significant interest in recent years. Many authors have proposed models of high-scale SUSY breaking and its mediation to the visible sector, including scenarios such as universal high-scale supersymmetry [14], split supersymmetry [15–17], mini-split supersymmetry [18], minimal split supersymmetry [19], spread supersymmetry [20, 21], and pure gravity mediation [22–24] (see also [25]). Another intriguing feature of these models is that a high SUSY-breaking scale implies a very heavy gravitino. The gravitino, thus, decays very fast in the early Universe, which solves the cosmological gravitino problem [26–29]. In addition, large sfermion masses help reduce the tension with constraints on the SUSY parameter space from flavor-changing neutral currents and CP violation [30]. For these reasons, we consider supersymmetry broken at a high energy scale to be a leading candidate for new physics beyond the standard model.

In this paper, we will take the idea of high-scale SUSY breaking to the extreme and consider SUSY-breaking scales Λ_{SUSY} as large as the scale of gauge coupling unification in typical *grand unified theories* (GUTs), $\Lambda_{\text{SUSY}} \sim \Lambda_{\text{GUT}} \sim 10^{16}$ GeV. Electroweak naturalness is then certainly lost. But at the same time, another intriguing possibility emerges which is out of reach in low-scale supersymmetry. If Λ_{SUSY} is large enough, cosmic inflation in the early Universe [31–34] can be driven by the vacuum energy density associated with the spontaneous breaking of supersymmetry, $\langle V \rangle \supset \Lambda_{\text{SUSY}}^4$. This represents a remarkable connection between particle physics and cosmology. Inflation is a pillar of the cosmological standard model. Not only does inflation explain the large degree of homogeneity and isotropy of our Universe on cosmological scales, it is also the origin of the primordial fluctuations that eventually seed structure formation on galactic scales (see, e.g., [35, 36] for reviews on inflation). At present, there is, however, no consensus on how to make contact between inflation and particle physics. Against this background, the unification of inflation with the dynamics of spontaneous SUSY breaking provides an elegant and economical embedding of inflation into a microscopic theory.

The interplay between inflation and SUSY breaking has been studied from different angles in the past (see, e.g., [37–39]). The first unified model that illustrates how inflation and SUSY breaking in the visible sector may originate from the same dynamics has been presented in [40]. In this model,

supersymmetry is broken dynamically by the nonperturbative dynamics in a strongly coupled supersymmetric gauge theory. *Dynamical SUSY breaking* (DSB) first occurs in the hidden sector and is then mediated to the MSSM. More recently, a number of related models has been constructed in [41–43].¹ All these models have in common that the energy scales of inflation and SUSY breaking end up being related to the dynamical scale Λ_{dyn} of the strong dynamics. The scale Λ_{dyn} is generated via dimensional transmutation, analogously to the scale of *quantum chromodynamics* (QCD) in the standard model. That is, at energies around Λ_{dyn} , the gauge coupling constant in the hidden sector formally diverges. The unified models in [40–43] therefore do not require any dimensionful input parameters to explain the origin of the energy scales of inflation and SUSY breaking. The generation of Λ_{dyn} is, in particular, a nonperturbative effect in the *infrared* (IR). This explains the exponential hierarchy between Λ_{SUSY} and Λ_{inf} on the one hand and the Planck scale M_{Pl} on the other hand. Meanwhile, several perturbative models of inflation and SUSY breaking have recently been discussed in the literature [50–52]. These models also draw a unified picture of inflation and SUSY breaking. But in contrast to strongly coupled models, they depend on dimensionful input parameters which need to be put in by hand. They, thus, fail to provide a dynamical explanation for the separation of scales.

In this paper, we shall revisit our model in [42], which gives rise to a viable scenario of *D-term hybrid inflation* (DHI) [53, 54] in the context of high-scale SUSY breaking.² Hybrid inflation [59, 60] is an interesting scenario on general grounds, as it establishes another connection between particle physics and cosmology. In hybrid inflation, the inflationary era ends in a rapid second-order phase transition, the so-called waterfall transition, which can be identified with the spontaneous breaking of a local gauge symmetry in models of grand unification. As shown in [42], this symmetry can be chosen to correspond to $U(1)_{B-L}$, where B and L denote baryon and lepton number, respectively. Inflation therefore ends in what is referred to as the $B-L$ phase transition [61–68]. That is, the end of inflation coincides with the spontaneous breaking of $B-L$ in the visible sector. This can be used to generate L -violating Majorana masses for a number of sterile right-handed neutrinos. These neutrinos then lead to baryogenesis via leptogenesis [69] and generate the SM neutrino masses via the seesaw mechanism [70–74]. The model in [42], thus, provides a consistent picture of particle physics and early Universe cosmology. It unifies the dynamics of inflation, high-scale SUSY breaking, and spontaneous $B-L$ breaking. Remarkably enough, all of these phenomena occur at energies close to the GUT scale.

The discussion in [42] mostly focused on model building aspects. We gave a brief summary of our model construction and only touched upon phenomenology. The purpose of the present paper is therefore threefold. We will (i) review the construction of our model in more detail, including many aspects that were left out in [42] (see Sec. 2). We will (ii) perform a more comprehensive scan of parameter space (see Sec. 3). In particular, we will identify new regimes of successful inflation that were overlooked in [42]. And finally, we will (iii) provide a much broader phenomenological discussion,

¹Besides, there is a more general class of models, sometimes referred to as dynamical inflation, where inflation is a consequence of dynamical SUSY breaking in a hidden sector. In these models, the breaking of supersymmetry during inflation is, however, not responsible for the breaking of supersymmetry in the MSSM at low energies (see, e.g., [44–49]).

²This model has recently been employed in a supersymmetric realization of the relaxion mechanism [55]. For other models of hybrid inflation and high-scale SUSY breaking, see [56, 57]. For more recent work on D-term inflation, see [58].

including the implications of our model for the MSSM particle spectrum, the $B-L$ phase transition, dark matter, and cosmic strings (see Sec. 4). In the last section of this paper, we will conclude and give an outlook on how our main observation—the fact that SUSY breaking close to the GUT scale might be the key to a unified picture of particle physics and cosmology—could lead to a new understanding of SUSY’s role in nature (see Sec. 5). In the appendix, as a supplement to Secs. 2 and 3, we collect various technical formulas that help to translate between the Einstein-frame and Jordan-frame formulations of *supergravity* (SUGRA) (see Appendix A). This also includes a detailed comparison of our Jordan/Einstein-frame expressions for the inflationary slow-roll parameters.

2 Model: Strong dynamics and gauged $B-L$ in the Jordan frame

We begin by reviewing the model constructed in [42]. This will also allow us to introduce our notation and conventions. The starting point of our analysis is the idea to build a viable SUGRA model of hybrid inflation that ends in the spontaneous breaking of $B-L$, i.e., in the $B-L$ phase transition.

2.1 Preliminary remarks on hybrid inflation in supergravity

In the absence of supersymmetry, hybrid inflation is incompatible with the statistical properties of the temperature fluctuations in the *cosmic microwave background* (CMB). Nonsupersymmetric hybrid inflation predicts the primordial scalar CMB power spectrum to be blue-tilted, i.e., it predicts a scalar spectral index n_s greater than one [59,60]. This needs to be compared with the recent measurement by the PLANCK collaboration, $n_s^{\text{obs}} = 0.9677 \pm 0.0060$ [75]. Nonsupersymmetric hybrid inflation is, thus, ruled out with a statistical significance of more than 5σ . This conclusion serves as an independent motivation to introduce supersymmetry, in addition to supersymmetry’s other advantages (see Sec. 1).

In supersymmetry, hybrid inflation is understood to be a consequence of (temporary) spontaneous SUSY breaking, which can be accomplished either by a nonvanishing F term [76,77] or D term [53,54]. In the following, we will outline both scenarios and explain why we will eventually focus on D-term inflation. In both cases, the scalar inflaton σ is contained in a chiral multiplet S that transforms as a singlet under all gauge symmetries. S couples to charged chiral multiplets in the superpotential W_{inf} ,

$$W_{\text{inf}} \supseteq \kappa S \Phi \bar{\Phi}, \quad (1)$$

where κ is a dimensionless Yukawa coupling. Φ and $\bar{\Phi}$ denote the so-called waterfall fields, which transform in conjugate representations of a gauge group G . We shall identify G with $U(1)_{B-L}$ and assign $B-L$ charges $+q$ and $-q$ to Φ and $\bar{\Phi}$. This sets the stage for the $B-L$ phase transition at the end of inflation. Any self-interaction of S can be forbidden by invoking R symmetry. If we assign R charges such that $[S]_R = 2$ and $[\Phi \bar{\Phi}]_R = 0$, terms such as S^2 and S^3 are not allowed. The Yukawa coupling in Eq. (1) does not suffice to break supersymmetry. This is, however, necessary to obtain a nonvanishing vacuum energy density that can drive inflation. In *F-term hybrid inflation* (FHI), one therefore equips S with an F term, $|F_S| = \mu_S^2$. Supersymmetry is then broken à la O’Raifeartaigh [78] during inflation. In D-term inflation, one assumes instead a nonzero *Fayet-Iliopoulos* (FI) D term in the

D-term scalar potential V_D . This breaks supersymmetry during inflation via the FI mechanism [79]. F-term and D-term inflation are then characterized by the following expressions for W_{inf} and V_D ,

$$\begin{aligned} \text{FHI:} \quad W_{\text{inf}} &= \kappa S \Phi \bar{\Phi} + \mu_S^2 S, & V_D &= \frac{g^2}{2} \left[q \left(|\phi|^2 - |\bar{\phi}|^2 \right) \right]^2, \\ \text{DHI:} \quad W_{\text{inf}} &= \kappa S \Phi \bar{\Phi} & , \quad V_D &= \frac{g^2}{2} \left[q_0 \xi - q \left(|\phi|^2 - |\bar{\phi}|^2 \right) \right]^2. \end{aligned} \quad (2)$$

The gauge coupling constant g belongs to the gauge group G . In our case, g consequently denotes the $B-L$ gauge coupling. The gauge charge q_0 is factored out of the FI parameter ξ for later convenience.

In both F-term and D-term inflation, the field S parametrizes a completely flat direction in the scalar potential, at least at tree level and in global supersymmetry. This explains why it is natural to identify S with the chiral inflaton field. At large field values of S , the Yukawa coupling in Eq. (1) induces large S -dependent masses for the waterfall fields. Φ and $\bar{\Phi}$ can therefore be integrated out, which results in a logarithmic effective potential for S . This singles out the origin in field space, $S = 0$, as the unique vacuum in the quantum theory. Inflation is, thus, characterized by the slow-roll motion of S from large field values towards the origin in field space. The SUSY-breaking parameters μ_S (FHI) and ξ (DHI) induce a mass splitting between the scalar components of Φ and $\bar{\Phi}$. Below a certain critical value of the inflaton field, this results in two (FHI) or one (DHI) scalar waterfall field(s) becoming unstable. This triggers the $B-L$ phase transition. Inflation ends and the system approaches a ground state in which $B-L$ is spontaneously broken and supersymmetry restored. As we will discuss in Sec. 4.2, this can be used to generate Majorana masses for the right-handed neutrinos N_i in the seesaw extension of the MSSM. All we have to do is to choose appropriate gauge charges and introduce Yukawa couplings between Φ and three generations of sterile neutrinos, $W \supset \frac{1}{2} h_{ij} \Phi N_i N_j$.

Hybrid inflation is sensitive to gravitational corrections in supergravity [80, 81]. In the case of F-term inflation, spontaneous R breaking leads, in particular, to a SUGRA term in the F-term scalar potential V_F that is linear in the complex inflaton field $s \subset S$ [39, 82–85]. To see this, recall that R symmetry breaking can be accounted for by introducing a constant term in the superpotential, $w \subset W$. This term ultimately sets the gravitino mass $m_{3/2}$ in the low-energy vacuum, $w \propto m_{3/2} M_{\text{Pl}}^2$ (where M_{Pl} denotes the reduced Planck mass, $M_{\text{Pl}} \simeq 2.44 \times 10^{18}$ GeV). In F-term inflation, the inflaton field itself possesses a nonzero F term, $|F_S| = \mu^2$. This F term couples to w in the SUGRA scalar potential,

$$V_F \supset \frac{\mu_S^2 w^*}{M_{\text{Pl}}^2} \left(K^{ss^*} K_{s^*} - 3s \right) + \text{h.c.} \quad (3)$$

Here, K denotes the Kähler potential, K_{s^*} stands for the derivative of K w.r.t. s^* , and K^{ss^*} is the ss^* entry in the inverse of the Kähler metric. For a canonical Kähler potential, $K \supset S^\dagger S$, one obtains

$$V_F \supset -\frac{2\mu_S^2 w^*}{M_{\text{Pl}}^2} s + \text{h.c.} \quad (4)$$

This tadpole term breaks the rotational invariance in the complex inflaton plane and, hence, complicates the analysis of the inflationary dynamics significantly. In fact, the term in Eq. (3) renders F-term inflation a two-field model [85], which needs to be treated with special care. Depending on the size of $m_{3/2}$, the tadpole term potentially spoils slow-roll inflation. In addition, it generates a false vacuum at large field values, which limits the set of viable initial conditions for inflation in phase space.

For these reasons, we will restrict ourselves to D-term inflation in this paper. A dynamical realization of F-term inflation that avoids the tadpole problem can be found in [41]. The model in [41] also establishes a connection between inflation and dynamical SUSY breaking around the scale of grand unification. In [41], there is, however, no $U(1)$ symmetry that could be identified with $U(1)_{B-L}$. Moreover, inflation does not end in a phase transition in the waterfall sector. Together, these features of [41] eliminate the possibility to unify inflation with the dynamics of the $B-L$ phase transition. A dynamical model of F-term inflation that ends in the $B-L$ phase transition will be presented elsewhere.

2.2 Ingredients for a unified model of D-term inflation

The absence of the linear tadpole term in D-term inflation tends to make SUGRA corrections more manageable. In particular, the issue of initial conditions appears more favorable compared to F-term inflation (however, see also Sec. 3.4). Nonetheless, D-term inflation still faces a number of challenges. In this section, we will discuss these challenges one by one and outline how they are respectively met in our model. This serves the purpose to explain the bigger physical picture behind our specific setup. In Sec. 2.3, we will then become more explicit and present the details of our construction.

Dynamical generation of the FI term in the strongly coupled SUSY-breaking sector

First of all, the origin of the FI term and its embedding into supergravity are subtle issues that have been the subject of a long debate in the literature. At this point, it is important to distinguish between genuine FI terms and effective FI terms. The former refer to field-independent FI parameters ξ_a that parametrize constant shifts in the auxiliary D_a components of Abelian vector multiplets V_a . The latter denote field-dependent FI parameters ξ_a that depend on the *vacuum expectation values* (VEVs) of dynamical scalar modulus fields ψ_i . Genuine FI terms, $\xi_a = \text{const}$, are FI terms in the original sense. That is, they preserve the underlying gauge symmetry and are compatible with massless vector multiplets. By contrast, in the case of effective FI terms, $\xi_a = \xi_a(\langle\psi_i\rangle)$, the underlying gauge symmetry is always spontaneously broken by the modulus VEVs $\langle\psi_i\rangle$. Effective FI terms are therefore FI terms only in a slightly more general sense. The embedding of genuine FI terms into supergravity always requires an exact global continuous symmetry [86, 87]. This is problematic from the viewpoint of quantum gravity. As can be shown on very general grounds, quantum gravity is likely to violate any global symmetry [88]. Coupling genuinely constant FI terms to gravity, thus, appears to be impossible. Effective FI terms promise to offer a possible way out of this problem. Effective FI terms are frequently encountered in string theory [89, 90], where they arise in consequence of the Green-Schwarz mechanism of anomaly cancellation [91]. However, such constructions typically suffer from the presence of a shift-symmetric modulus field [92]. This modulus field needs to be adequately stabilized [93]. Otherwise, it will absorb the effective FI term in its VEV or cause a cosmological modulus problem [94, 95].

To avoid all of the problems listed above, we will assume that the FI term responsible for inflation is dynamically generated in the strongly coupled SUSY-breaking sector. That is, we will not resort to string theory, but work in the context of field theory. To be precise, we will employ the dynamical mechanism devised in [96]. A dynamical FI term generated via this mechanism is automatically an

effective field-dependent FI term that is controlled by the VEVs of moduli in the hidden sector,

$$\xi = \langle \bar{\psi}\bar{\psi}^* \rangle - \langle \psi\psi^* \rangle \sim \Lambda_{\text{dyn}}^2. \quad (5)$$

Here, ψ and $\bar{\psi}$ belong to chiral multiplets Ψ and $\bar{\Psi}$ that carry $B-L$ charges $+q_0$ and $-q_0$, respectively. This ansatz complies with our philosophy outlined in the introduction (see Sec. 1). Being a dynamically generated quantity, the FI parameter ξ does not need to be added by hand. Instead, it is related to the dynamical scale Λ_{dyn} in the hidden sector which is generated via dimensional transmutation. Let us identify the UV embedding scale of our theory with the Planck scale, $\Lambda_{\text{UV}} = M_{\text{Pl}}$. The *renormalization group* (RG) running of the hidden-sector gauge coupling g_{hid} then results in the following relation,

$$\Lambda_{\text{dyn}} = M_{\text{Pl}} \exp \left[-\frac{1}{b_{\text{hid}}} \frac{8\pi^2}{g_{\text{hid}}^2(M_{\text{Pl}})} \right], \quad (6)$$

where b_{hid} is the coefficient of the hidden-sector RG beta function. This relation explains why Λ_{dyn} and, hence, ξ end up being exponentially suppressed compared to the Planck scale (which is the only available mass scale in our setup). The advantage of our approach is that it comes with a built-in mechanism for modulus stabilization. As usual, the generation of ξ results in a shift-symmetric modulus field. In our case, this will be a linear combination of Ψ and $\bar{\Psi}$ (see Sec. 2.3). However, as the FI parameter ξ is generated in the SUSY-breaking sector, the shift-symmetric modulus couples to *degrees of freedom* (DOFs) involved in the dynamical breaking of supersymmetry. The F term of the SUSY-breaking Polonyi field therefore induces a mass for the modulus field. This stabilizes all dangerous directions in field space and prevents us from running into any modulus problem.

Spontaneous $B-L$ breaking in the hidden sector before the end of inflation

The anticipated $B-L$ phase transition at the end of D-term inflation is accompanied by the production of topological defects in the form of cosmic strings [97,98] (for reviews on cosmic strings, see [99,100]). Such cosmic strings can leave an imprint in the CMB temperature anisotropies, the spectrum of *gravitational waves* (GWs), and in the *diffuse gamma-ray background* (DGRB). Cosmic string decays can also affect outcome of *big bang nucleosynthesis* (BBN). However, no signs of cosmic strings have been detected thus far. Recent upper limits on the properties of cosmic strings can be found in [101,102] (CMB), [103–105] (GWs), and [106] (DGRB and BBN). These bounds allow to put severe constraints on the parameter space of hybrid inflation [107,108]. In fact, the minimal scenario of D-term inflation is already ruled out by the nonobservation of cosmic strings [109]. A possible way out of this problem is to consider scenarios in which $B-L$ is spontaneously broken, in one way or another, already during inflation. Cosmic strings then form at early times and are sufficiently diluted before the end of inflation.

Fortunately, the dynamical generation of ξ in the hidden sector (see Eq. (5)) provides the ideal starting point for implementing this solution to the cosmic string problem. The modulus VEVs $\langle \psi \rangle$ and $\langle \bar{\psi} \rangle$ spontaneously break $B-L$ in the hidden sector already during inflation. Therefore, to prevent the formation of cosmic strings in the waterfall sector at the end of inflation, all we have to do is to communicate the breaking of $B-L$ in the hidden sector to the waterfall fields. This is readily done by adding marginal couplings between the two sectors in the superpotential or Kähler potential that are otherwise irrelevant for the dynamics of inflation [55]. We will come back to this issue in Sec. 4.4.

Sequestered sectors in Jordan-frame supergravity

A notorious problem of any model of D-term inflation is that additional charged scalar fields, other than the waterfall fields Φ and $\bar{\Phi}$, threaten to destabilize the FI term during inflation. Without any additional physical assumption, there is no reason why Φ and $\bar{\Phi}$ should be the only fields charged under the $U(1)$ symmetry whose FI term drives inflation. In general, one should rather expect a whole set of N charged pairs, $\{\Phi_i, \bar{\Phi}_i\}$, with the inflaton only coupling to a subset of M such pairs,

$$W \supset \sum_{i=1}^N \kappa_i S \Phi_i \bar{\Phi}_i, \quad \kappa_i \begin{cases} \neq 0 & ; \quad \forall i \leq M \\ = 0 & ; \quad \forall i > M \end{cases}. \quad (7)$$

In this case, there are $N - M$ pairs that are not sufficiently stabilized by an inflaton-induced mass during inflation. At the same time, these fields also enter into the D-term scalar potential, where they threaten to absorb the FI parameter ξ in their VEVs. In our scenario based on $U(1)_{B-L}$, the role of these dangerous scalar directions is played by the scalar partners of the MSSM quarks and leptons. The squarks \tilde{q}_i and sleptons $\tilde{\ell}_i$ are also charged under $B-L$, but do not couple to the inflation field. Accounting for the presence of these fields, the D-term scalar potential needs to be rewritten as follows,

$$V_D = \frac{g^2}{2} \left[q_0 \xi - q \left(|\phi|^2 - |\bar{\phi}|^2 \right) - \sum_i q_{q_i} \left(|\tilde{q}_i|^2 - |\bar{\tilde{q}}_i|^2 \right) - \sum_i q_{\ell_i} \left(|\tilde{\ell}_i|^2 - |\bar{\tilde{\ell}}_i|^2 \right) \right]^2. \quad (8)$$

The squarks and sleptons therefore acquire D-term-induced masses proportional to $m_D = g |q_0 \xi|^{1/2}$. As evident from the sign relations in Eq. (8), half of these masses end up being tachyonic (see also [110]). This renders the corresponding directions in field space tachyonically unstable. The inflationary trajectory, thus, decays into a vacuum in which $B-L$ is broken by nonvanishing sfermion VEVs.

To avoid this problem, one needs to stabilize the MSSM sfermions by means of additional mass contributions during inflation. Here, the simplest solution is to make use of the soft scalar masses induced by the spontaneous breaking of supersymmetry in the hidden sector. Let us assume that these soft masses are all more or less close to a common value m_0 . Then, to stabilize the MSSM sfermions during inflation, we must require that $m_0 \gg m_D$. This is, however, too strong a condition if SUSY breaking is communicated to the visible sector only via ordinary gravity mediation in the Einstein frame (for a review on gravity mediation, see [111]). In gravity mediation, we expect the soft scalar masses to be of the order of the gravitino mass, $m_0 \sim m_{3/2}$. This soft mass is universal such that also the waterfall fields obtain soft masses of $\mathcal{O}(m_{3/2})$. As a consequence, the stabilization of the MSSM sfermions also stabilizes the waterfall fields. This is an unwanted but unavoidable side effect. In such a scenario, the waterfall fields would never become unstable and inflation would never end.

A possible solution to this problem is to presume a separation of scales of the following form,

$$m_{3/2} \ll m_D \ll m_0. \quad (9)$$

In this case, the MSSM sfermions remain stabilized at all times, while the waterfall fields can become unstable at the end of inflation. Parametrically large soft sfermion masses can, e.g., be achieved by adding a direct coupling between the visible and the hidden sector in the Kähler potential,

$$K \supset \frac{a_{ij}}{M_*^2} Q_i^\dagger Q_j X^\dagger X. \quad (10)$$

Here, Q_i and X stand for a generic MSSM matter field and the SUSY-breaking Polonyi field, respectively. M_* denotes the mass scale at which the effective operator in Eq. (10) is generated. The constants a_{ij} are dimensionless Wilson coefficients that are expected to be of $\mathcal{O}(1)$. Any speculations regarding the underlying UV physics are left for future work. In this paper, we will content ourselves with the observation that Eq. (10) results in soft masses that can be parametrically large compared to $m_{3/2}$. Provided that the cut-off scale is sufficiently below the Planck scale, $M_* \ll M_{\text{Pl}}$, one finds

$$m_0 \sim \frac{M_{\text{Pl}}}{M_*} m_{3/2} \gg m_{3/2}. \quad (11)$$

Now, however, we need a conspiracy among certain parameters. Successful inflation is only possible as long as the parameters g , q_0 , ξ , $m_{3/2}$, and M_* conspire in order to satisfy the following relation,

$$\text{Einstein frame:} \quad 1 \ll \frac{m_D}{m_{3/2}} \ll \frac{M_{\text{Pl}}}{M_*}. \quad (12)$$

We do not see any compelling argument why this relation should be automatically fulfilled. For this reason, we will go one step further and solve the MSSM sfermion problem in a more elegant way.

Let us assume that the canonical description of hybrid inflation in supergravity corresponds to an embedding into a (specific) Jordan frame rather than an embedding into the Einstein frame [112, 113]. At this point, recall that every Jordan-frame formulation of supergravity is characterized by a specific choice for the so-called frame function Ω . The frame function is an arbitrary function of the complex scalar fields in the theory, $\Omega = \Omega(\phi_i, \phi_i^*)$. For given Ω , the metric tensor in the Jordan frame, $g_{\mu\nu}^J$, is related to the metric tensor in the Einstein tensor, $g_{\mu\nu}$, via the following Weyl rescaling,

$$g_{\mu\nu}^J = \mathcal{C}^2 g_{\mu\nu}, \quad \mathcal{C} = \left(-\frac{3M_{\text{Pl}}^2}{\Omega} \right)^{1/2}, \quad (13)$$

Here, \mathcal{C} denotes what we will refer to as the conformal factor. We emphasize that the Weyl transformation in Eq. (13) does not change the physical predictions of the theory. The physical content of the Jordan frame is equivalent to the physical content of the Einstein frame, even at the quantum level [114, 115]. In what follows, we will simply assume that the SUGRA embedding of hybrid inflation is most conveniently described in the Jordan frame. More details on the conversion between the Einstein-frame and Jordan-frame formulations of supergravity can be found in Appendix A.

Given the freedom in defining the frame function Ω , there is, in principle, an infinite number of possible Jordan frames. In the following, we will, however, focus on one particular choice which stands out for several reasons. In this frame, the frame function Ω is determined by the Kähler potential K ,

$$\Omega = -3M_{\text{Pl}}^2 \exp \left[-\frac{K}{3M_{\text{Pl}}^2} \right]. \quad (14)$$

This relation is understood to hold in superspace, such that the frame function Ω becomes a function of chiral multiplets, $\Omega = \Omega(\Phi_i, \Phi_i^\dagger)$. This choice for Ω is motivated by the curved superspace approach to old minimal supergravity in the Einstein frame [116, 117]. In this derivation of the SUGRA action, the function Ω as defined in Eq. (14) is identified as the generalized kinetic energy on curved superspace. Meanwhile, Ω is also a meaningful quantity in the derivation of the Einstein-frame action based on

local superconformal symmetry [118, 119]. In this approach to old minimal supergravity, the function Ω is identified as the prefactor of the kinetic term of the chiral compensator superfield. For our purposes, the advantage of the choice in Eq. (14) is that it sets the stage for canonically normalized kinetic terms for the complex scalar fields in the Jordan frame. Indeed, to obtain canonically normalized kinetic terms, the defining relation in Eq. (14) needs to be combined with the following ansatz for Ω [112],

$$\Omega = -3M_{\text{Pl}}^2 + F, \quad F = \delta_{\bar{i}j} \Phi_i^\dagger \Phi_j + [J(\Phi_i) + \text{h.c.}] , \quad (15)$$

Here, we have introduced F as the *kinetic function* of the chiral matter fields. The additional $-3M_{\text{Pl}}^2$ in Ω accounts for the kinetic term of the gravitational DOFs. J is an arbitrary holomorphic function.

We mention in passing that the relations in Eqs. (14) and (15) also provide the basis for a class of SUGRA models known as *canonical superconformal supergravity* (CSS) models [113]. In these models, the pure supergravity part of the total action is invariant under local Poincaré transformations as usual. At the same time, the matter and gauge sectors of the theory can be made invariant under a local superconformal symmetry by setting the holomorphic function J to zero. This larger set of symmetry transformations renders CSS models particularly simple. In the Jordan frame, one obtains canonical kinetic terms for all fields. Moreover, one finds that the Jordan-frame scalar potential coincides with the scalar potential in global supersymmetry. In our scenario, we will, however, break the superconformal symmetry via the holomorphic function J to a large degree (see Eq. (27) below). For this reason, one should not regard our model to be of the CSS type. A model of D-term inflation based on the idea of superconformal symmetry has been constructed in [120]. This model employs a constant FI term that does not depend on the inflaton field value in the Einstein frame. Our model will by contrast involve an effective FI term that does not depend on the inflaton field value in the Jordan frame (see Sec. 2.5). In [120], the dynamics of inflation are moreover described by a two-field model, whereas we will only deal with a single inflaton field. Interestingly enough, the model in [120] reproduces the predictions of Starobinsky inflation [31] in the limit of large inflaton field values [121].

Together with Eq. (14), the ansatz in Eq. (15) results in the following Kähler potential,

$$K = -3M_{\text{Pl}}^2 \ln \left[1 - \frac{F}{3M_{\text{Pl}}^2} \right] . \quad (16)$$

This is an important result. If we choose the kinetic function F or, equivalently, the holomorphic function J appropriately, this Kähler potential can be readily used to sequester the different sectors of our model. In fact, Eq. (16) turns into a Kähler potential of the sequestering type [122] if the function F can be split into separate (canonical) contributions from the hidden, visible, and inflation sector,

$$K = -3M_{\text{Pl}}^2 \ln \left[1 - \frac{F_{\text{hid}} + F_{\text{vis}} + F_{\text{inf}}}{3M_{\text{Pl}}^2} \right] . \quad (17)$$

Kähler potentials of this form have been derived in the context of extra dimensions [122] as well as in strongly coupled *conformal field theories* (CFTs) [123–126]. They are also similar to the Kähler potential in models of no-scale supergravity [127–129] that can be derived from string theory [130].³ If

³In no-scale supergravity, the kinetic term of the gravitational DOFs depends on a dynamical modulus field T . This is accounted for by replacing the 1 inside the logarithm in Eq. (17) by a field-dependent quantity: $1 \rightarrow (T + T^\dagger)/M_{\text{Pl}}$.

the various sectors do not couple to each other in the superpotential, the Kähler potential in Eq. (17) leads to vanishing soft scalar masses at tree level in all sectors except for the hidden sector.

The possibility to sequester different sectors is a crucial property of Eq. (16) which we will use to solve the MSSM sfermion problem. Altogether, we will choose the function F in our model as follows,

$$F \quad \rightarrow \quad F_{\text{tot}} = F_{\text{hid}} + F_{\text{vis}} + F_{\text{inf}} + \frac{a_{ij}}{M_*^2} Q_i^\dagger Q_j X^\dagger X. \quad (18)$$

From now on, we will refer to the total kinetic function as F_{tot} and reserve the symbol F for the kinetic function of the inflaton field S (see further below). We will also assume that the holomorphic function J in Eq. (15) is a function of S only. That is, the kinetic functions F_{hid} , F_{vis} , and F_{inf} are supposed to consist of standard canonical terms for all fields except for S . The kinetic function F_{tot} as defined in Eq. (18) combines two important features. (i) It leads to a sequestering between the visible sector and the inflaton sector. The waterfall fields consequently obtain no soft masses at tree level. This is necessary to be able to trigger the $B-L$ phase transition at the end of inflation, irrespective of the size of the gravitino mass. (ii) The MSSM sfermions are stabilized thanks to higher-dimensional operators in F_{tot} that couple the visible sector to the SUSY-breaking sector. At this point, we stick to the mechanism that we already discussed in the case of the Einstein frame (see Eq. (10)). Together, these two features allow us to realize successful inflation and solve the MSSM sfermion problem.

Our solution of the MSSM sfermion problem in the Jordan frame is conceptually different from the solution in the Einstein frame discussed around Eq. (12). Now, as the waterfall fields do not acquire a soft mass at tree level, the requirement in Eq. (12) turns into the following two conditions,

$$\text{Jordan frame:} \quad 0 \ll \frac{m_D}{m_{3/2}} \ll \frac{M_{\text{Pl}}}{M_*}. \quad (19)$$

The first inequality is a consequence of our decision to work in a Jordan frame with canonical kinetic terms. It is trivially fulfilled. We are, thus, left with only one sensible physical condition, $M_* \ll m_{3/2} M_{\text{Pl}} / m_D$. To satisfy this condition, we no longer have to rely on a conspiracy among different parameter values. Instead, we simply have to deal with an upper bound on the scale M_* which derives from the requirement that all dangerous scalar directions in field space must be sufficiently stabilized during inflation. We therefore manage to solve the MSSM sfermion problem in $B-L$ D-term inflation by means of model-building decisions rather than by resorting to a specific part of parameter space.

In the following, we will remain agnostic as to the UV origin of F_{tot} in Eq. (18). We settle for the observation that, apart from additional Planck-suppressed interactions, Eq. (18) can be motivated by demanding canonically normalized kinetic terms in the (standard) Jordan frame. This is the reason why we will formulate parts of our analysis in the language of Jordan-frame supergravity. Beyond that, it might be possible to embed our model into extra dimensions, strongly coupled CFTs, no-scale supergravity and/or string theory. But such a task is beyond the scope of this paper and left for future work. For our purposes, the formalism of Jordan-frame supergravity simply provides a convenient technical framework. We shall not speculate about the underlying physics at higher energies.

Shift symmetry in the direction of the inflaton field

Working in the Jordan frame not only helps to protect the waterfall fields against large soft masses. In ordinary gravity mediation in the Einstein frame, also the inflaton acquires a soft mass of the order of the gravitino mass. This results in the notorious eta problem in supergravity [76, 131]. To see this, recall that the gravitino mass is related to the F term of the SUSY-breaking Polonyi field as follows,

$$m_{3/2} = \frac{\langle |F_X| \rangle}{\sqrt{3}M_{\text{Pl}}}. \quad (20)$$

At the same time, the Hubble rate during D-term inflation is controlled by the size of the FI term,

$$H_{\text{inf}} = \frac{\langle V_D \rangle^{1/2}}{\sqrt{3}M_{\text{Pl}}} = \frac{\langle D \rangle}{\sqrt{6}M_{\text{Pl}}} = \frac{gq_0\xi}{\sqrt{6}M_{\text{Pl}}}. \quad (21)$$

General arguments in supergravity indicate that D terms are always accompanied by an F term which is at least as large or even larger [132, 133]. In our case, we intend to dynamically generate the FI term in conjunction with the Polonyi F term in the SUSY-breaking sector. On general grounds, we, thus, expect that $\langle |F_X| \rangle \gtrsim \langle D \rangle$. Therefore, if the inflaton indeed obtained a soft mass of $\mathcal{O}(m_{3/2})$, we would immediately encounter a eta problem, i.e., a slow-roll parameter η much larger than one,

$$\eta = M_{\text{Pl}}^2 \frac{V''}{V} \sim \left(\frac{m_{3/2}}{H_{\text{inf}}} \right)^2 \gg 1, \quad (22)$$

where V'' denotes the second derivative of the scalar potential w.r.t. the inflaton field. This serves as an additional motivation for our specific Jordan frame. There, the soft mass of the inflaton vanishes (at least as long as $F = S^\dagger S$ and $J = 0$), which renders the most dangerous contribution to η zero.

This is, however, not the end of the story. To fully solve the eta problem, we need to work a bit harder. In the Jordan frame, the complex scalars are nonminimally coupled to the Ricci scalar R_J via the frame function Ω . This follows from the Jordan-frame equivalent of the Einstein-Hilbert action,

$$S \supset \frac{1}{2} \int d^4x \sqrt{-g_J} \left(-\frac{\Omega_{\text{tot}}}{3} \right) R_J = \frac{1}{2} \int d^4x \sqrt{-g_J} \left(M_{\text{Pl}}^2 - \frac{F_{\text{tot}}}{3} \right) R_J, \quad (23)$$

which contains the nonminimal term $-F_{\text{tot}}/3 R_J$. This coupling yields additional mass contributions for the scalar fields. Consider, e.g., the canonical terms in the total kinetic function, $F_{\text{tot}} \supset \delta_{\bar{i}j} \Phi_i^\dagger \Phi_j$,

$$S \supset - \int d^4x \sqrt{-g_J} \sum_i \zeta_i R_J |\phi_i|^2, \quad \zeta_i = \zeta = \frac{1}{6}. \quad (24)$$

which describes the special case of a set of conformally coupled scalars. Each complex scalar with a canonical term in the kinetic function F_{tot} therefore acquires a universal gravity-induced mass m_R ,

$$m_R^2 = \zeta R_J = 2H_J^2, \quad (25)$$

where H_J denotes the Hubble parameter in the Jordan frame and where we used the relation between Ricci scalar and Hubble parameter in exact de Sitter space, $R_J = 12H_J^2$. This gravitational mass correction spoils slow-roll inflation as long as it is not sufficiently suppressed. That is, an inflaton kinetic function that only consists of a canonical term, $F = S^\dagger S$, results in too large an η parameter,

$$\eta \sim \frac{m_R^2}{3H_J^2} = \frac{2}{3}. \quad (26)$$

Thus, to fully solve the eta problem, we have to make use of the holomorphic function J in Eq. (15). The freedom in defining J allows us to realize an approximate shift symmetry in the direction of the inflaton field. Such a shift symmetry is a common tool in SUGRA models of inflation, as it allows to suppress the most dangerous SUGRA contributions to the inflaton potential [134]. In our case, an approximate shift symmetry is realized for the following kinetic function of the inflaton field,

$$F = S^\dagger S + [J(S) + \text{h.c.}] , \quad J(S) = -\frac{1}{2}(1 - 2\chi)S^2 . \quad (27)$$

Here, χ is a positive shift-symmetry-breaking parameter which we will assume to be small, $0 < \chi \ll 1$. To see that Eq. (27) indeed features a shift symmetry, it is convenient to rewrite F as follows,

$$F = \frac{1}{2}\chi(S^\dagger + S)^2 - \frac{1}{2}(1 - \chi)(S^\dagger - S)^2 = \chi\sigma^2 + (1 - \chi)\tau^2 , \quad S = \frac{1}{\sqrt{2}}(\sigma + i\tau) . \quad (28)$$

This form of F illustrates that, for $\chi \ll 1$, the kinetic function is approximately invariant under shifts in σ , i.e., the real scalar part of the inflaton field S . Conversely, χ values close to one, $1 - \chi \ll 1$, lead to an approximate shift symmetry in τ , i.e., the imaginary scalar component of S . In the following, we will focus w.l.o.g. on the first of these two cases. In passing, we also mention that the trivial case $\chi = \chi_{\text{CSS}} = 1/2$ (which renders the holomorphic function J vanishing) corresponds to an inflaton field that is conformally coupled to the Ricci scalar. This choice for the parameter χ would allow to construct a SUGRA model that is invariant under local superconformal symmetry (see the discussion below Eq. (15)). However, as argued above, we would then fail to solve the eta problem (see Eq. (26)). For this reason, we need to break the superconformal symmetry. In fact, by choosing $\chi \ll \chi_{\text{CSS}}$, we break the superconformal symmetry in a maximal sense in favor of an approximate shift symmetry.

Given the kinetic function in Eq. (28), it is straightforward to solve the eta problem. In consequence of the approximate shift symmetry, all contributions to the inflaton mass m_σ end up being suppressed by χ . This follows from an explicit computation of m_σ in the Einstein frame (see Eq. (116) in Sec. 2.5),

$$m_\sigma^2 \approx 2\chi \left[m_R^2 - (1 - 2\chi)m_{3/2}^2 \right] . \quad (29)$$

As expected, m_σ reduces to m_R in the limit $\chi \rightarrow 1/2$. On the other hand, if χ is chosen small enough, m_σ becomes suppressed, so that the slow-roll parameter η remains sufficiently small during inflation.⁴

Explicit breaking of the shift symmetry

An exact shift symmetry is out of reach in our model, as the Yukawa coupling in the superpotential, $W_{\text{inf}} = \kappa S \Phi \bar{\Phi}$, breaks any inflaton (or waterfall field) shift symmetry explicitly. Therefore, while χ may be zero at tree level, a nonvanishing value of the shift-symmetry-breaking parameter χ is always generated via radiative corrections. To see this, let us consider the *one-particle-irreducible* (1PI) effective action in global supersymmetry. The superpotential does not receive any quantum corrections

⁴Imposing an approximate shift symmetry in the direction of the inflaton field would also allow to solve the eta problem in the Einstein frame. There, the inflaton mass also vanishes in the limit of an exact shift symmetry. From this perspective, our solution to the eta problem does actually not serve as an additional motivation to work in the Jordan frame. However, our arguments regarding the MSSM sfermion problem remain unchanged. This problem is best solved in the Jordan frame (see the discussion around Eq. (19)). We will therefore continue to work in the Jordan frame.

in consequence of the SUSY nonrenormalization theorem [135]. The renormalization of the Kähler potential is, however, nontrivial and results in a one-loop effective Kähler potential $K_{1\ell}$ [136–139]. Along the inflationary trajectory, $\Phi = \bar{\Phi} = 0$, a calculation in the $\overline{\text{MS}}$ renormalization scheme yields

$$K_{1\ell} = 2\chi_{1\ell} \left[1 - \frac{1}{2} \ln \left(\frac{\kappa^2 S^\dagger S}{\bar{\mu}^2} \right) \right] S^\dagger S, \quad \chi_{1\ell} = \frac{\kappa^2}{16\pi^2}, \quad (30)$$

where $\bar{\mu}$ denotes the $\overline{\text{MS}}$ renormalization scale. Note that this result for $K_{1\ell}$ corresponds to a wavefunction renormalization of the inflaton field S . Next, let us embed the effective Kähler potential in Eq. (30) into supergravity. In the Einstein frame, the relevant quantity is the total Kähler potential K_{tot} , which simply follows from adding $K_{1\ell}$ to the tree-level Kähler potential, $K_{\text{tot}} = K_{\text{tree}} + K_{1\ell}$. In the Jordan frame, we are by contrast interested in the total frame function, $\Omega_{\text{tot}} = \Omega_{\text{tree}} + \Omega_{1\ell}$. One can show that the one-loop correction to the tree-level frame function is related to $K_{1\ell}$ as follows,

$$\Omega_{1\ell} = \Omega_{\text{tree}} \left(\exp \left[-\frac{K_{1\ell}}{3M_{\text{Pl}}^2} \right] - 1 \right) = K_{1\ell} + \mathcal{O}(M_{\text{Pl}}^{-2}). \quad (31)$$

Here, the higher-order terms correspond to Planck-suppressed radiative corrections which are negligibly small. Together, Eqs. (28), (30), and (31) allow us to determine the effective χ parameter that is induced by the breaking of shift symmetry in the superpotential. Along the direction of the real inflaton component, $\tau = 0$, we obtain the following one-loop kinetic function for the inflaton field,

$$F_{1\ell} \simeq K_{1\ell} \xrightarrow{\tau=0} \frac{1}{2} \chi_{\text{eff}} \left(S^\dagger + S \right)^2, \quad \chi_{\text{eff}} = \chi_{1\ell} \left[1 - \frac{1}{2} \ln \left(\frac{\kappa^2 S^\dagger S}{\bar{\mu}^2} \right) \right] \sim \chi_{1\ell}. \quad (32)$$

In the absence of any tree-level contribution, the shift-symmetry-breaking parameter χ is therefore expected to be of the order of $\kappa^2 / (16\pi^2)$. This is an important result which was overlooked in [42]. There, we simply varied χ as a free parameter for fixed κ . Of course, this is a valid procedure, given the fact that χ can very well receive further tree-level contributions (or further radiative corrections from inflaton couplings to extra heavy states). In this case, χ is simply the sum of various contributions, $\chi = \chi_{\text{tree}} + \chi_{1\ell}$, which can take any arbitrary value. But the case $\chi = \chi_{1\ell}$ —which we had neglected thus far—is special, as it corresponds to a scenario with minimal field content and number of free parameters. We will study this scenario in more detail in Sec. 3.3. This will represent one of the main results of this paper and a significant step forward beyond our analysis in [42]. In particular, we will find that $\chi = \chi_{1\ell}$ leads to inflation in new parts of parameter space that we had dismissed before.

Finally, we point out that the fact that we are unable to realize an exact shift symmetry is rather a virtue than a shortcoming of our model. A slightly broken shift symmetry allows us to get a handle on the scalar spectral index n_s which we would otherwise lack in the case of an exact shift symmetry. The prediction for n_s in standard D-term inflation in global supersymmetry roughly corresponds to

$$n_s = 1 + 2\eta - 6\varepsilon \simeq 1 + 2\eta \gtrsim 1 - \frac{1}{N_e} \simeq 0.98, \quad (33)$$

where N_e denotes the number of e-folds between the end of inflation and the time t_{CMB} when the CMB pivot scale, $k_{\text{CMB}} = 0.05 \text{ Mpc}^{-1}$, exists the Hubble horizon during inflation. The prediction in Eq. (33) exceeds the current best-fit value, $n_s^{\text{obs}} = 0.9677 \pm 0.0060$ [75], by at least 2σ . This puts some phenomenological pressure on the simplest version of D-term inflation. To improve on the predicted

value of n_s , various SUGRA models have been proposed in the literature [120, 121, 140–143]. However, in our scenario, no extra effort is needed to enhance the absolute value of the slow-roll parameter η and, thus, reproduce the best-fit value for n_s . The inflaton mass in Eq. (29) approximately results in

$$\eta \sim -\frac{2\chi}{3} \left(\frac{m_{3/2}}{H_J} \right)^2. \quad (34)$$

Therefore, to realize n_s values around $n_s \simeq 0.96$, all we have to do is to choose χ small enough,

$$n_s \simeq 0.96 \quad \Rightarrow \quad \eta \sim -0.02 \quad \Rightarrow \quad \chi \sim 0.03 \left(\frac{H_J}{m_{3/2}} \right)^2. \quad (35)$$

In this sense, the approximate shift symmetry in the kinetic function of the inflaton field automatically provides a possibility to achieve a scalar spectral index consistent with the observational data.

Three physical assumptions to solve five problems of D-term inflation

So far, we have mainly outlined the ingredients of our construction in physical and less technical terms. We hope that this part of our discussion will be accessible also to readers without a strong background in SUGRA model building. A more technical description of our model will be given in the next three sections (see Secs. 2.3, 2.4, and 2.5). Readers less interested in the technical aspects of our model and more interested in its phenomenological implications may directly skip to Sec. 3.

Before entering the technical part of our discussion, let summarize our insights up to this point. On the one hand, we showed that D-term inflation faces a number of challenges. We discussed the following five problems: (i) The generation of the FI term in the D-term scalar potential and its embedding into supergravity, (ii) the production of dangerous cosmic strings at the end of inflation, (iii) the stabilization of dangerous MSSM sfermion directions in the scalar potential during and after inflation, (iv) the eta problem in supergravity, and (v) the tension between the lower bound on n_s in D-term inflation and the current best-fit value. On the other hand, we argued that all of these five problems can be solved if one makes the following three assumptions: (i) The FI term is dynamically generated in the hidden SUSY-breaking sector. (ii) The canonical description of D-term inflation in supergravity corresponds to the embedding into the (standard) Jordan frame with canonically normalized kinetic terms for all scalar fields. (iii) The kinetic function of the inflaton field exhibits a slightly broken shift symmetry. Our model therefore turns out to be a viable SUGRA realization of $B-L$ D-term inflation that is consistent with all theoretical and phenomenological constraints.

2.3 SUSY-breaking dynamics in the hidden sector

In the previous section, we summarized our physical ideas how to realize a viable SUGRA model of D-term inflation that (i) unifies the dynamics of supersymmetry breaking and inflation and that (ii) ends in the $B-L$ phase transition at energies around the GUT scale. In the following, we will show how these ideas can be implemented into a specific model of dynamical SUSY breaking: the *Izawa-Yanagida-Intriligator-Thomas* (IYIT) model [144, 145], which represents the simplest vector-like model of dynamical SUSY breaking. Despite this choice, we believe that our general ideas extend beyond

our specific model. In future work, it would be interesting to study alternative DSB models and assess which other models might give rise to unified dynamics of supersymmetry breaking and inflation.

IYIT sector at high and low energies

We begin by reviewing the IYIT model. In its most general form, the IYIT model corresponds to a strongly coupled supersymmetric $Sp(N)$ gauge theory.⁵ At high energies, its charged matter content consists of $N_f = N + 1$ vector-like pairs of quark flavors, where each quark field Ψ_i transforms in the fundamental representation of $Sp(N)$. The theory becomes confining at energies around the dynamical scale Λ_{dyn} which is generated via dimensional transmutation. Below Λ_{dyn} , the dynamical DOFs in the IYIT sector correspond to a set of $N_f(2N_f - 1)$ gauge-invariant composite meson fields M_{ij} ,

$$M_{ij} \simeq \frac{1}{\eta \Lambda_{\text{dyn}}} \langle \Psi_i \Psi_j \rangle, \quad \eta \sim 4\pi, \quad i, j = 1, 2, \dots, 2N_f, \quad (36)$$

where $M_{ji} = -M_{ij}$ and where η denotes a numerical factor of $\mathcal{O}(4\pi)$ that follows from *naive dimensional analysis* (NDA) [146–149]. It turns out to be useful to absorb the NDA factor η in the dynamical scale Λ_{dyn} . In the following, we will therefore work with the reduced dynamical scale Λ ,

$$\Lambda = \frac{\Lambda_{\text{dyn}}}{\eta} \sim \frac{\Lambda_{\text{dyn}}}{4\pi}. \quad (37)$$

At low energies, the scalar meson VEVs parametrize a moduli space of degenerate supersymmetric vacua. This moduli space is subject to a constraint equation, which, in the classical limit, corresponds to the requirement that the Pfaffian of the antisymmetric meson matrix M_{ij} must vanish, $\text{Pf}(M_{ij}) = 0$. This constraint, however, becomes deformed in the quantum theory. There, it reads [150]

$$\text{Pf}(M_{ij}) \simeq \Lambda^{N_f}. \quad (38)$$

To break supersymmetry in the IYIT sector, one needs to lift the flat directions in moduli space. This is readily achieved by coupling the IYIT quarks Ψ^i to a set of $N_f(2N_f - 1)$ singlet fields Z_{ij} ,

$$\text{At high energies:} \quad W_{\text{hid}} = \frac{1}{2} \lambda_{ij} Z_{ij} \Psi_i \Psi_j, \quad (39)$$

where $\lambda_{ij} = -\lambda_{ji}$ are dimensionless coupling constants. At high energies, these couplings are nothing but ordinary Yukawa couplings which do not affect the vacuum structure of the theory. At low energies, the terms in Eq. (39), however, turn into mass terms for the meson and singlet fields M_{ij} and Z_{ij} ,

$$\text{At low energies:} \quad W_{\text{hid}} \simeq \frac{1}{2} \lambda_{ij} \Lambda Z_{ij} M_{ij}. \quad (40)$$

These mass terms single out the origin in field space as the true supersymmetric ground state. The quantum mechanically deformed moduli constraint in Eq. (38), however, prevents the system from reaching the origin in field space. This breaks supersymmetry. The theory is forced to settle in a vacuum away from the origin, $\langle M_{ij} \rangle \neq 0$, where some of the singlet F-term conditions, $F_{Z_{ij}} = 0$, cannot be satisfied. Supersymmetry is, hence, broken à la O’Raifeartaigh by nonvanishing F terms [78].

⁵In our notation, the compact symplectic group $Sp(N)$ is identical to the unitary group over the quaternions, $U(N, \mathbb{H})$. Here, N denotes the dimension of the quaternionic vector space \mathbb{H}^N that $Sp(N)$ acts on in its fundamental representation.

In the following, we shall focus on the minimal $N = 1$ realization of the IYIT model, for simplicity. In this case, the $Sp(1)$ gauge dynamics are equivalent to those of an $SU(2)$ theory, $Sp(1) \cong SU(2)$, and we have to deal with four quark fields Ψ_i and six singlet fields Z_{ij} at high energies. This translates into six meson fields M_{ij} (and six singlet fields Z_{ij}) at low energies. As we will see shortly, it turns out to be convenient to label the fields in the low-energy theory in a suggestive manner. To do so, we first note that Eq. (39) exhibits a global $U(1)_A$ flavor symmetry that corresponds to an axial quark phase rotation. The $U(1)_A$ charges of the two quark flavors at high energies can be chosen as follows,

$$[\Psi_1]_A = [\Psi_2]_A = +\frac{q_0}{2}, \quad [\Psi_3]_A = [\Psi_4]_A = -\frac{q_0}{2}. \quad (41)$$

This normalization ensures that the charged meson fields at low energies carry $U(1)_A$ charges $\pm q_0$,

$$[M_{12}]_A = +q_0, \quad [M_{34}]_A = -q_0, \quad [M_{13}]_A = [M_{14}]_A = [M_{23}]_A = [M_{24}]_A = 0, \quad (42)$$

and similarly for the Z_{ij} . In the second step, we relabel all fields according to their $U(1)_A$ charges,

$$\begin{aligned} M_{12} &\rightarrow M_+, & M_{34} &\rightarrow M_-, & M_{13} &\rightarrow M_0^1, & M_{14} &\rightarrow M_0^2, & M_{23} &\rightarrow M_0^3, & M_{24} &\rightarrow M_0^4, \\ Z_{12} &\rightarrow Z_-, & Z_{34} &\rightarrow Z_+, & Z_{13} &\rightarrow Z_0^1, & Z_{14} &\rightarrow Z_0^2, & Z_{23} &\rightarrow Z_0^3, & Z_{24} &\rightarrow Z_0^4. \end{aligned} \quad (43)$$

In this notation, the low-energy superpotential in Eq. (40) takes the following form,

$$W_{\text{hid}} \simeq \Lambda (\lambda_+ M_+ Z_- + \lambda_- M_- Z_+ + \lambda_0^1 M_0^1 Z_0^1 + \lambda_0^2 M_0^2 Z_0^2 + \lambda_0^3 M_0^3 Z_0^3 + \lambda_0^4 M_0^4 Z_0^4), \quad (44)$$

where we also relabeled the λ_{ij} . Meanwhile, the constraint in Eq. (38) can now be written as follows,

$$\text{Pf}(M_{ij}) = M_+ M_- - M_0^1 M_0^4 + M_0^2 M_0^3 \simeq \Lambda^2. \quad (45)$$

Together, Eqs. (44) and (45) allow to explicitly calculate the VEVs in the SUSY-breaking vacuum. As it turns out, the location of the true ground state in meson field space depends on the hierarchy among three geometric means of Yukawa couplings, $\lambda = (\lambda_+ \lambda_-)^{1/2}$, $\lambda_0^{14} = (\lambda_0^1 \lambda_0^4)^{1/2}$, $\lambda_0^{23} = (\lambda_0^2 \lambda_0^3)^{1/2}$,

$$\begin{aligned} \lambda < \min \{ \lambda_0^{14}, \lambda_0^{23} \} &\Rightarrow \langle M_+ M_- \rangle \simeq \Lambda^2, & \langle M_0^1 M_0^4 \rangle &= 0, & \langle M_0^2 M_0^3 \rangle &= 0, \\ \lambda_0^{14} < \min \{ \lambda, \lambda_0^{23} \} &\Rightarrow \langle M_+ M_- \rangle = 0, & \langle M_0^1 M_0^4 \rangle &\simeq \Lambda^2, & \langle M_0^2 M_0^3 \rangle &= 0, \\ \lambda_0^{23} < \min \{ \lambda, \lambda_0^{14} \} &\Rightarrow \langle M_+ M_- \rangle = 0, & \langle M_0^1 M_0^4 \rangle &= 0, & \langle M_0^2 M_0^3 \rangle &\simeq \Lambda^2. \end{aligned} \quad (46)$$

We will assume that the first of these three cases is realized, $\lambda < \min \{ \lambda_0^{14}, \lambda_0^{23} \}$. In this case, it is the charged meson fields that obtain a nonzero VEV, $\langle M_+ M_- \rangle \simeq \Lambda^2$. This case is special in the sense that the global $U(1)_A$ flavor symmetry becomes spontaneously broken at low energies. In the two other cases, the flavor symmetry remains unbroken even in the SUSY-breaking vacuum.

Properties of the low-energy vacuum

Let us now discuss the properties of the $U(1)_A$ -breaking vacuum in a bit more detail. In this vacuum, all neutral fields are stabilized by their supersymmetric masses in Eq. (44). The relevant terms in the superpotential and Pfaffian constraint are therefore only those involving charged fields,

$$W_{\text{hid}} \simeq \Lambda (\lambda_+ M_+ Z_- + \lambda_- M_- Z_+), \quad \text{Pf}(M_{ij}) = M_+ M_- \simeq \Lambda^2. \quad (47)$$

The constraint is most easily accounted for by adding a Lagrange multiplier term to the superpotential,

$$W_{\text{hid}} \simeq \Lambda (\lambda_+ M_+ Z_- + \lambda_- M_- Z_+) + \lambda_T T (M_+ M_- - \Lambda^2), \quad (48)$$

where the field T represents the actual Lagrange multiplier. The physical nature of the field T depends on strong-coupling effects in the Kähler potential. If it acquires a nonperturbative kinetic term from the strong gauge dynamics, T becomes physical. On the other hand, if no kinetic term is generated, T is merely an auxiliary field that remains unphysical. Unfortunately, it is unknown which of these cases is realized, as the Kähler potential for T in the strong-coupling regime is uncalculable. At any rate, the difference between the two cases is mostly irrelevant for our purposes. All effects in the case of a physical Lagrange multiplier field T are suppressed by powers of $\lambda/(4\pi)$ [151]. Thus, as long as we stay in the perturbative regime, $\lambda \ll 4\pi$, our results will not be affected by the physical status of the field T . In the following, we will therefore assume that T remains unphysical, for simplicity. In practice, this means that we will take the limit $\lambda_T \rightarrow \infty$ wherever possible. For discussions of the IYIT model based on the assumption of a physical Lagrange multiplier field T , see, e.g., [41, 152].

Given the superpotential in Eq. (48) (and taking the limit $\lambda_T \rightarrow \infty$ at the end of the calculation), one can easily show that the vacuum energy density is minimized for the following meson VEVs,

$$\langle M_{\pm} \rangle = \frac{\lambda}{\lambda_{\pm}} \Lambda. \quad (49)$$

These meson VEVs induce SUSY-breaking F terms for the singlet fields Z_{\pm} . To determine the total F-term SUSY breaking scale μ , it is useful to transform the fields M_{\pm} and Z_{\pm} to a new basis,

$$\begin{pmatrix} A \\ M \end{pmatrix} = \frac{1}{f_A} \begin{pmatrix} \langle M_+ \rangle & -\langle M_- \rangle \\ \langle M_- \rangle & \langle M_+ \rangle \end{pmatrix} \begin{pmatrix} M_+ \\ M_- \end{pmatrix}, \quad \begin{pmatrix} X \\ Y \end{pmatrix} = \frac{1}{\sqrt{2}} \begin{pmatrix} 1 & 1 \\ 1 & -1 \end{pmatrix} \begin{pmatrix} Z_+ \\ Z_- \end{pmatrix}, \quad (50)$$

where we introduced f_A to denote the total energy scale of spontaneous $U(1)_A$ breaking,

$$f_A = (\langle M_+^2 \rangle + \langle M_-^2 \rangle)^{1/2} = \left(\frac{\lambda_+}{\lambda_-} + \frac{\lambda_-}{\lambda_+} \right)^{1/2} \Lambda. \quad (51)$$

In the new field basis, the fields M and T share a supersymmetric Dirac mass term, $m_{MT} = \lambda_T f_A$, that formally diverges in the limit $\lambda_T \rightarrow \infty$. This allows us to identify M as the meson field that becomes eliminated by the Pfaffian constraint. The remaining meson DOFs are then described by the orthogonal linear combination, i.e., by the field A . Note that this automatically implies that the field A plays the role of the chiral Goldstone multiplet of spontaneous $U(1)_A$ breaking. From this perspective, the energy scale f_A may also be regarded as the Goldstone decay constant. To obtain the superpotential describing the low-energy dynamics of A , X , and Y , we proceed as follows: (i) We perform the field rotation in Eq. (50), (ii) shift the meson fields A and M by their nonvanishing VEVs,

$$A \rightarrow \frac{1}{f_A} (\langle M_+^2 \rangle - \langle M_-^2 \rangle) + A, \quad M \rightarrow \frac{2}{f_A} \langle M_+ \rangle \langle M_- \rangle + M, \quad (52)$$

and (iii) integrate out the heavy fields M and T . This results in the following superpotential,

$$W_{\text{hid}} \simeq \mu^2 X - m_F Y A + \frac{1}{2} \lambda_X X A^2. \quad (53)$$

Here, μ denotes the total F-term SUSY breaking scale,

$$\mu = [(\lambda_+^2 \langle M_+^2 \rangle + \lambda_-^2 \langle M_-^2 \rangle) \Lambda^2]^{1/4} = 2^{1/4} \lambda^{1/2} \Lambda. \quad (54)$$

By construction, the singlet field X is the only field with a nonzero F term, $\langle |F_X| \rangle = \mu^2$. It can therefore be identified with the SUSY-breaking Polonyi field. The orthogonal field Y shares a Dirac mass term with the $U(1)_A$ Goldstone field A which is given in terms of the mass scales μ and f_A ,

$$m_F = \frac{\mu^2}{f_A} = \rho \lambda \Lambda, \quad \rho = \left[\frac{1}{2} \left(r_\lambda + \frac{1}{r_\lambda} \right) \right]^{-1/2}, \quad r_\lambda = \frac{\lambda_+}{\lambda_-}. \quad (55)$$

Here, ρ measures the degeneracy between λ_+ and λ_- . For $\lambda_+ \rightarrow \lambda_-$, the parameter ρ approaches one, $\rho \rightarrow 1$. For $\lambda_+ \ll \lambda_-$ or $\lambda_- \ll \lambda_+$, it goes to zero, $\rho \rightarrow 0$. In the following, we will assume that both λ_+ and λ_- are sufficiently small, so that we always stay in the perturbative regime. For definiteness, let us require that both couplings are always at least half an order of magnitude smaller than 4π .

$$\lambda_\pm < \lambda_{\text{pert}} = 4 \simeq 10^{-1/2} 4\pi. \quad (56)$$

This translates into a lower bound on the hierarchy parameter ρ in dependence of $\lambda = (\lambda_+ \lambda_-)^{1/2}$,

$$\lambda_\pm < \lambda_{\text{pert}} \quad \Rightarrow \quad \rho > \rho_{\text{pert}} = \left[\frac{1}{2} \left(r_{\text{pert}} + \frac{1}{r_{\text{pert}}} \right) \right]^{-1/2}, \quad r_{\text{pert}} = \frac{\lambda_+ \lambda_-}{\lambda_{\text{pert}}^2}. \quad (57)$$

Moreover, to simplify our analysis, we will replace ρ by its expectation value $\bar{\rho}$ in the following. We compute $\bar{\rho}$ by averaging ρ over all possible values of λ_\pm , varying both couplings on a linear scale,

$$\bar{\rho} = \frac{1}{\lambda_{\text{pert}}^2} \int_0^{\lambda_{\text{pert}}} \int_0^{\lambda_{\text{pert}}} \rho d\lambda_+ d\lambda_- \simeq 0.80. \quad (58)$$

Note that this result is independent of the concrete value of λ_{pert} . With ρ fixed at this value, the perturbativity constraint in Eq. (57) turns into an upper bound on the Yukawa coupling λ ,

$$\lambda_\pm < \lambda_{\text{pert}}, \quad \rho = \bar{\rho} \quad \Rightarrow \quad \lambda < \left[1 - (1 - \bar{\rho}^4)^{1/2} \right]^{1/2} \frac{\lambda_{\text{pert}}}{\bar{\rho}} \simeq 0.60 \lambda_{\text{pert}} \simeq 2.41. \quad (59)$$

This yields in turn an upper bound on the F-term-induced mass in the superpotential, $m_F \lesssim 1.94 \Lambda$. The lesson from this analysis is the following: From now on, we will work with $\rho \simeq 0.80$ and $\lambda \lesssim 2.41$. The Yukawa couplings λ_\pm are then guaranteed to assume ‘‘typical values’’ (in the sense of the average in Eq. (58)) which are, at the same time, consistent with the requirement of perturbativity, $\lambda < \lambda_{\text{pert}}$.

Similar to the mass m_F , also the Yukawa coupling λ_X in Eq. (53) is given in terms of μ and f_A ,

$$\lambda_X = \left(\frac{\mu}{f_A} \right)^2 = \left(\frac{m_F}{\mu} \right)^2 = \frac{\rho^2 \lambda}{\sqrt{2}}. \quad (60)$$

This Yukawa coupling between the Polonyi field X and the Goldstone field A is a direct consequence of the $T M_+ M_-$ term in Eq. (48). Similar couplings also exist between X and the neutral meson fields. This is shown explicitly in Appendix A of [152] (see also [151]). Together, these Yukawa couplings result in an effective Polonyi mass $m_{1\ell}$ at the one-loop level. An explicit calculation yields [152]

$$m_{1\ell} = c_{1\ell} \lambda^2 \Lambda, \quad c_{1\ell} = \left(\frac{2 \ln 2 - 1}{32\pi^2} n_M^{\text{eff}} \right)^{1/2}. \quad (61)$$

Here, n_M^{eff} denotes the effective number of meson loops contributing to the Polonyi mass. Let us assume that all neutral mesons share the same Yukawa coupling, $\lambda_0^{1,2,3,4} \equiv \lambda_0$. In this case, n_M^{eff} can be brought into the following compact form (the full expression is complicated and can be found in [152]),

$$n_M^{\text{eff}} = \rho^6 + 4\ell_0, \quad (62)$$

where $\ell_0 = \ell(\lambda/\lambda_0)$ is a loop function that can be approximated by a simple quadratic power law,

$$\ell(x) = \frac{1}{2 \ln 2 - 1} \left[\frac{1}{2} \left(1 + \frac{1}{x^2}\right)^2 \ln(1+x^2) - \frac{1}{2} \left(1 - \frac{1}{x^2}\right)^2 \ln(1-x^2) - \frac{1}{x^2} \right] \approx x^2. \quad (63)$$

In the following, we will set $\lambda_0 = 4\pi$ to account for the presence of heavy composite states with masses around the dynamical scale, $m_{\text{heavy}} = \lambda_0 \Lambda \sim \Lambda_{\text{dyn}}$. Just like in QCD, such heavy resonances are expected to appear in the spectrum. Our perturbative language, however, does not suffice to capture their dynamics at low energies. For this reason, we will instead follow an effective approach and mimic the effect of additional heavy states by means of a particular choice for λ_0 . For a Yukawa coupling λ of $\mathcal{O}(1)$, the one-loop coefficient $c_{1\ell}$ in Eq. (61) is then roughly given by $c_{1\ell} \simeq 0.02$. In global supersymmetry, the Polonyi field X correspond to a tree-level flat direction (see Eq. (53)). The loop-induced Polonyi mass $m_{1\ell}$ is therefore crucial to stabilize the SUSY-breaking vacuum against gravitational corrections in supergravity [151]. We will discuss this issue in more detail in Sec. 2.4.

Dynamical generation of an effective FI term

The IYIT model can also be used to dynamically generate an effective FI term. This was pointed out for the first time in [96]. In this paper, we will make use of this mechanism to generate the effective FI term required for $B-L$ D-term inflation. All we have to do now is to promote the global $U(1)_A$ flavor symmetry in the IYIT superpotential (see Eq. (48)) to a local $U(1)_{B-L}$ gauge symmetry. The $B-L$ gauge interactions then result in the following D-term scalar potential in the IYIT sector,

$$V_D = \frac{g^2 q_0^2}{2} \left(|m_+|^2 - |m_-|^2 + |z_+|^2 - |z_-|^2 \right)^2. \quad (64)$$

Here and in the following, lower-case characters (m_{\pm} , z_{\pm} , etc.) denote the complex scalar components of the corresponding chiral multiplets (M_{\pm} , Z_{\pm} , etc.). The charged mesons M_{\pm} acquire nonzero VEVs as a result of the dynamical breaking of supersymmetry (see Eq. (49)). These VEVs spontaneously break $B-L$ which leads to the following effective FI term,

$$\xi = \langle M_-^2 \rangle - \langle M_+^2 \rangle. \quad (65)$$

This FI parameter is exactly of the form that we anticipated in Eq. (5) in Sec. 2.2. In particular, we now see that, in our dynamical model, the role of the moduli Ψ and $\bar{\Psi}$ is played by the mesons M_{\pm} . To evaluate the expression in Eq. (65), it is, in principle, necessary to account for the backreaction of the D-term scalar potential in Eq. (64) on the meson VEVs in Eq. (49). In the following, we will, however, restrict ourselves to the weakly gauged limit, $|gq_0| \lesssim \lambda$, where this backreaction is negligible. In this case, we can simply continue to work with our results in Eq. (49), such that Eq. (65) turns into

$$\xi = \left(\frac{\lambda_+}{\lambda_-} - \frac{\lambda_-}{\lambda_+} \right) \Lambda^2 = \frac{2(1-\rho^4)^{1/2}}{\rho^2} \Lambda^2. \quad (66)$$

Here, we assumed w.l.o.g. that $\lambda_+ > \lambda_-$ such that the FI parameter is always positive, $\xi > 0$. Once we set the parameter ρ to its expectation value, $\bar{\rho} \simeq 0.80$, we obtain the following simple relation,

$$\xi^{1/2} \simeq 0.88 f_A \simeq 1.54 \Lambda. \quad (67)$$

In Sec. 2.5, we will use this result as a key ingredient in our construction of the inflaton potential. However, before we are able to do so, we need to make sure that the FI parameter ξ is not “eaten up” by the charged singlet fields Z_{\pm} in the IYIT sector. To this end, let us rewrite Eq. (64) as follows,

$$V_D = \frac{g^2 q_0^2}{2} (\xi - xy^* - x^*y)^2, \quad (68)$$

where we integrated out the meson fields and replaced the fields Z_{\pm} by the Polonyi field X and the stabilizer field Y . From Eq. (68), it is evident that ξ results in a mass mixing between X and Y ,

$$\Delta m_{xy}^2 = -g^2 q_0^2 \xi. \quad (69)$$

At the same time, X obtains an effective mass $m_{1\ell}$ at the one-loop level, while Y acquires a tree-level mass m_F from the superpotential. Taken as a whole, this results in the following two mass eigenvalues,

$$(m_{xy}^{\pm})^2 = \frac{m_F^2 + m_{1\ell}^2}{2} \pm \left[\left(\frac{m_F^2 - m_{1\ell}^2}{2} \right)^2 + \Delta m_{xy}^4 \right]^{1/2}. \quad (70)$$

In the limit of vanishing mass mixing, $\Delta m_{xy} \rightarrow 0$, these mass eigenvalues reduce to $m_{1\ell}$ and m_F , respectively. For too large mass mixing, the eigenvalue m_{xy}^- can, however, become tachyonic. In this case, one singlet mass eigenstate becomes unstable and absorbs ξ in its VEV. To prevent this from happening, the absolute value of Δm_{xy} needs to be smaller than the geometric mean of $m_{1\ell}$ and m_F ,

$$m_{xy}^- > 0 \quad \Rightarrow \quad |\Delta m_{xy}| < (m_{1\ell} m_F)^{1/2}. \quad (71)$$

This requirement translates into an upper bound on the gauge coupling constant g ,

$$g < g_{\max} = \frac{1}{|q_0|} \left(\frac{c_{1\ell}}{2} \right)^{1/2} \frac{(\rho\lambda)^{3/2}}{(1-\rho^4)^{1/4}}. \quad (72)$$

For $\rho = \bar{\rho}$ and $\lambda \ll \lambda_{\text{pert}}$, we hence obtain $|g_{\max} q_0| \simeq 7.8 \times 10^{-2} \lambda^{3/2}$. In Fig. 1, we plot the upper bound on $|gq_0|$ as a function of λ and ρ . This figure illustrates that the stability condition in Eq. (72) is always stronger than the mere requirement of a weak gauge coupling, $|gq_0| \lesssim \lambda$. The constraint in Eq. (72) is therefore a sufficient condition to justify our analysis in the weakly gauged limit.

Modulus stabilization and mass spectrum at low energies

The dynamically generated FI term in Eq. (65) is an effective FI term that depends on the VEVs of the meson fields M_{\pm} . As shown in [92], such FI terms are typically accompanied by a shift-symmetric modulus field (see Sec. 2.2). Our dynamical model is no exception to this statement. In our case, the role of the modulus field is played by the B - L Goldstone multiplet A which contains all meson DOFs after imposing the Pfaffian constraint in Eq. (47). The field A is a chiral multiplet. It, hence,

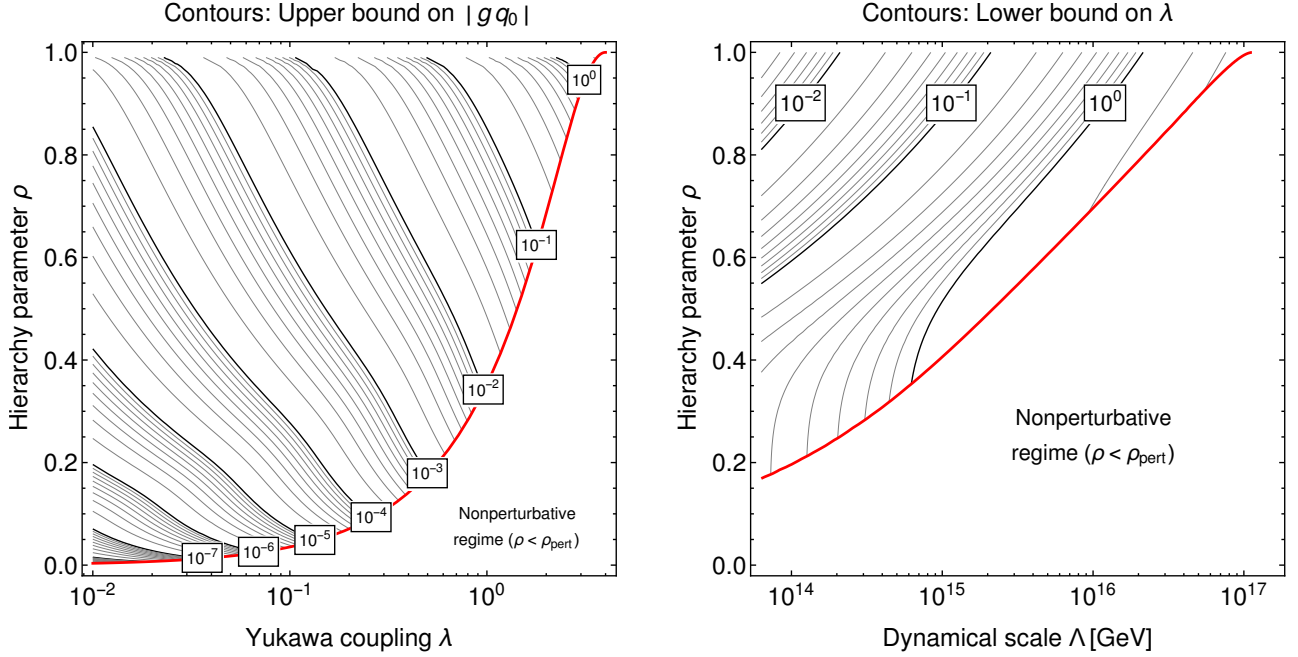


Figure 1: Bounds on the gauge coupling g (**left panel**) and the Yukawa coupling λ (**right panel**). The upper bound on g ensures that the IYIT singlets X and Y do not absorb ξ in their VEVs (see Eq. (72)). Similarly, the lower bound on λ guarantees that the VEV the Polyni field is located in the quadratic part of the effective potential (see Eq. (102)). Both bounds need to be satisfied to sufficiently stabilize the SUSY-breaking vacuum in the IYIT sector. In both plots, the solid red line indicates where in parameter space the perturbativity constraint in Eq. (57) becomes violated.

consists of a real scalar c , a real pseudoscalar φ , and a Weyl fermion \tilde{a} . In analogy to supersymmetric models of the QCD axion, these particles may also be referred to as the saxion c , axion φ , and axino \tilde{a} (see, e.g., [152]). In our model, the pseudoscalar φ corresponds to the Goldstone boson of spontaneous $B-L$ breaking. It remains massless and exhibits a derivative coupling to the $B-L$ vector boson A_μ . To see this, we have to apply the field transformation in Eq. (50) to the kinetic terms of the scalar meson fields. The kinetic part of the Lagrangian then ends up containing the following terms,

$$-\mathcal{L}_{\text{kin}} \supset \frac{1}{4} (\partial_\mu A_\nu - \partial_\nu A_\mu) (\partial^\mu A^\nu - \partial^\nu A^\mu) + \frac{1}{2} (\partial_\mu \varphi + m_V A_\mu) (\partial^\mu \varphi + m_V A^\mu). \quad (73)$$

Note that this is nothing but the Stückelberg Lagrangian of an Abelian gauge field with mass m_V ,

$$m_V = \sqrt{2} g q_0 f_A. \quad (74)$$

In view of Eq. (73), the Goldstone boson φ can also be regarded as the Stückelberg field of spontaneous $B-L$ breaking. This is consistent with the fact that the $B-L$ Higgs multiplet — represented by the meson field M — decouples once we insist on the Pfaffian constraint in Eq. (47) being satisfied exactly.

After spontaneous $B-L$ breaking, the pseudoscalar φ parametrizes the longitudinal polarization state of the massive $B-L$ vector boson A_μ . It is “eaten up” by A_μ and does not cause any further problems. At the same time, the real scalar c may become problematic, as it threatens to destabilize the FI parameter ξ . This is the notorious modulus problem in the presence of an effective FI term [92]. In our model, this problem is, however, absent. The scalar c and the fermion \tilde{a} are automatically stabilized by the F-term-induced mass m_F in the superpotential (see Eq. (53)). To make this statement more precise, let us now review the mass spectrum in the IYIT sector at low energies (see also [96, 152]).

The relevant superfields at low energies are the Polonyi field $X = (x, \tilde{x})$, the stabilizer field $Y = (y, \tilde{y})$, the Goldstone field $A = (a, \tilde{a})$, and the vector field $V = (\lambda, A_\mu)$. Here, x , y , and a are complex scalars. The complex scalar a contains the Goldstone boson and its scalar partner, $a = 2^{-1/2}(c + i\varphi)$. The fields \tilde{x} , \tilde{y} , \tilde{a} , and λ are Weyl fermions, where λ denotes the $B-L$ gaugino. A_μ is the $B-L$ vector boson. To determine the mass spectrum for these fields, we work in the weakly gauged limit where Δm_{xy} in Eq. (69) is negligible. A standard calculation in global supersymmetry then yields

$$\begin{aligned} m_x^2 &= m_{1\ell}^2, & m_y^2 &= m_F^2, & m_c^2 &= 2m_F^2 + m_V^2, & m_\varphi &= 0, \\ m_{\tilde{x}}^2 &= 0, & m_{\tilde{y}}^2 &= m_F^2 + m_V^2, & m_{\tilde{a}}^2 &= m_F^2 + m_V^2, & m_\lambda &= 0. \end{aligned} \quad (75)$$

Here, the indices refer to the respective mass eigenstates which are not necessarily identical to the corresponding ‘‘flavor’’ eigenstates (see, e.g., \tilde{y} , \tilde{a} , and λ). As expected, we find that the Goldstone boson φ remains massless, $m_\varphi = 0$. Similarly, also the fermionic component of the Polonyi field X remains massless, $m_{\tilde{x}} = 0$. This is because \tilde{x} corresponds to the goldstino field of spontaneous supersymmetry breaking. It is absorbed by the gravitino field in supergravity. Finally, also the $B-L$ gaugino λ remains massless (however, see also Eq. (77)). This has the following reason. The original Weyl fermion λ shares a Dirac mass with the axino, $\mathcal{L} \supset i m_V \lambda \tilde{a}$. One would, thus, think that λ ends up forming a Dirac fermion with the axino, i.e., the fermionic component of the $B-L$ Goldstone multiplet. The axino, however, also shares a Dirac mass with the fermionic component of the stabilizer field, $\mathcal{L} \supset m_F \tilde{a} \tilde{y}$, that is parametrically larger, $m_F \gg m_V$, in the weakly gauged limit. \tilde{y} therefore ‘‘steals’’ the axino from the gaugino, so that the gaugino no longer has a mass partner to form a Dirac fermion. In more technical terms, this goes back to the fact that the diagonalization of two Dirac masses for three Weyl fermions necessarily results in one massive Dirac fermion and one massless Weyl fermion. For our purposes, the most important lesson from Eq. (75) is that the superpartners of the Goldstone boson, the saxion c and the axino \tilde{a} , are indeed stabilized. Both fields obtain masses from the gauge sector⁶ as well as from the F-term-induced mass in the superpotential. This solves the modulus problem and assures us that ξ is a viable input for the construction of our inflation model.

Up to now, our discussion only dealt with the properties of the IYIT model in global supersymmetry. The next important step is to embed the IYIT model into supergravity. As discussed in Sec. 2.2, we especially intend to work in Jordan-frame supergravity with canonically normalized kinetic terms. However, before going into any details, let us briefly discuss the implications of supergravity for the low-energy mass spectrum. On general grounds, we essentially expect two effects: (i) In supergravity, R symmetry is broken to ensure the vanishing of the *cosmological constant* (CC) in the true vacuum. The order parameter of R symmetry breaking is the gravitino mass $m_{3/2}$. We therefore expect that supergravity leads to corrections to the various mass eigenvalues of $\mathcal{O}(m_{3/2})$. This should, in particular, also hold true if all other sectors are sequestered from the hidden SUSY-breaking sector. (ii) As a consequence of R symmetry breaking, the Polonyi field X acquires a nonzero VEV that is typically

⁶This follows from the super-Higgs mechanism. In consequence of spontaneous $B-L$ breaking, the massless vector multiplet V (one Weyl fermion, one massless vector boson) absorbs an entire chiral multiplet (one complex scalar, one Weyl fermion), so that it eventually contains the DOFs of a massive vector multiplet (one real scalar, one Dirac fermion, one massive vector boson). In the absence of supersymmetry breaking, all these DOFs would have a common mass m_V .

parametrically larger than the gravitino mass, $\langle X \rangle \propto m_{3/2} / (c_{1\ell}^2 \lambda^3)$ (see Sec. 2.4). This induces an effective Majorana mass for the Goldstone multiplet A in the superpotential (see Eq. (53)),

$$m_A = \lambda_X \langle X \rangle. \quad (76)$$

The Majorana mass m_A breaks some of the mass degeneracies in Eq. (75) and helps to make sure that the $B-L$ gaugino λ acquires a nonzero mass after all. To illustrate the effect of nonzero m_A , we compute the fermion masses in the limit of vanishing gravitino mass, $m_{3/2} \rightarrow 0$, and small Majorana mass, $m_A \ll m_F$. This exercise leads to the following mass eigenvalues (in the Jordan frame),

$$m_\lambda \simeq \frac{2 m_V m_F}{m_F^2 + m_V^2} m_V \sin \theta, \quad m_{\tilde{a}, \tilde{y}}^2 \simeq m_F^2 + m_V^2 \pm (m_A - m_\lambda) (m_F^2 + m_V^2)^{1/2}, \quad (77)$$

and again $m_{\tilde{x}} = 0$. Now, the vector boson mass m_V also receives contributions from the Polonyi VEV,

$$m_V \rightarrow m_V = \sqrt{2} g q_0 v_A, \quad v_A = (f_A^2 + \langle X^2 \rangle)^{1/2}, \quad (78)$$

where we parametrize the two contributions from f_A and $\langle X \rangle$ to v_A in terms of a mixing angle θ ,

$$\cos \theta = \frac{f_A}{v_A}, \quad \sin \theta = \frac{\langle X \rangle}{v_A}. \quad (79)$$

Eq. (77) demonstrates that, for $\langle X \rangle \neq 0$, the gaugino λ indeed obtains a nonvanishing mass. Moreover, we recognize that the Dirac fermion (\tilde{y}, \tilde{a}) splits into two nondegenerate Majorana fermions. Making the same assumptions as before, we also compute the scalar masses for a nonvanishing Polonyi VEV,

$$m_{y_-}^2 = \frac{1}{2} (A - B^{1/2}), \quad m_{y_+}^2 = m_F^2 + m_A^2, \quad m_c^2 = \frac{1}{2} (A + B^{1/2}), \quad (80)$$

where

$$\begin{aligned} A &= 3 m_F^2 + m_A^2 + m_V^2, \\ B &= m_F^4 + m_A^4 + m_V^4 + 6 m_A^2 m_F^2 + 2 m_V^2 [(m_F^2 + m_A^2) \cos(2\theta) - 2 m_A m_F \sin(2\theta)], \end{aligned} \quad (81)$$

and $m_x = m_{1\ell}$ and $m_\varphi = 0$. For a dominant F-term-induced mass, $m_A, m_V \ll m_F$, this simplifies to

$$m_{y_-}^2 \simeq m_F^2 - m_A^2, \quad m_{y_+}^2 = m_F^2 + m_A^2, \quad m_c^2 \simeq 2 m_F^2 + 2 m_A^2 + m_V^2. \quad (82)$$

We, thus, find that the Majorana mass m_A breaks the degeneracy among the two real scalar components of Y and shifts the saxion mass to even larger values. This concludes our analysis of the IYIT mass spectrum. We will now discuss the embedding into Jordan-frame supergravity in more detail.

2.4 Effective Polonyi model and embedding into supergravity

In global supersymmetry, the Polonyi field X is stabilized at the origin in field space, $\langle X \rangle = 0$, by its one-loop effective mass $m_{1\ell}$ (see Eq. (61)). Gravitational corrections in supergravity, however, threaten to destabilize this vacuum solution. We shall now explain why this is a serious problem. At field values

larger than some critical value, $|x| \gtrsim x_c$, the one-loop effective potential for the complex Polonyi field x changes from a quadratic to a logarithmic behavior (see, e.g., [41] for an explicit calculation),

$$V_{1\ell}(x) \simeq \begin{cases} m_{1\ell}^2 |x|^2 & ; \quad |x| \ll x_c \\ V_{1\ell}^0 \ln |x/x_c| & ; \quad |x| \gg x_c \end{cases}, \quad V_{1\ell}^0 \sim \frac{m_F^4}{16\pi^2}. \quad (83)$$

Here, $V_{1\ell}^0$ denotes the height of the logarithmic plateau at large field values. The critical field value x_c is reached once the Polonyi field induces effective masses for the quarks in the IYIT sector of $\mathcal{O}(\Lambda_{\text{dyn}})$. The Yukawa interactions of the Polonyi field with the IYIT quarks follow from Eqs. (39) and (50),

$$W_{\text{hid}} \supset \frac{X}{\sqrt{2}} (\lambda_+ \Psi_1 \Psi_2 + \lambda_- \Psi_3 \Psi_4). \quad (84)$$

This allows us to estimate x_c . For definiteness, we will work with $x_c = \sqrt{2} \Lambda_{\text{dyn}}/\lambda$ in the following. At $|x| \gtrsim x_c$, the IYIT quarks decouple perturbatively, which gives rise to the logarithmic corrections in Eq. (83). Dangerous SUGRA corrections can shift the Polonyi VEV from the origin in field space towards the logarithmic plateau at large field values. Once this happens, the Polonyi field is no longer stabilized and the system settles in a completely different vacuum at field values of $\mathcal{O}(M_{\text{Pl}})$. In the following, we will illustrate where in parameter space this unwanted conclusion can be avoided. This will, in particular, provide us with a useful lower bound on the Yukawa coupling λ (see Eq. (102)).

For the purposes of this section, it will suffice if we exclusively focus on the Polonyi field X and integrate out the heavier fields A and Y . The low-energy superpotential in Eq. (53) then turns into

$$W_{\text{hid}} = \mu^2 X + w. \quad (85)$$

Here, w denotes a constant contribution to the superpotential that we added by hand. w is meaningless in global supersymmetry. In supergravity, it accounts for the fact that R symmetry must be broken to ensure a vanishing CC in the true vacuum. In the presence of the constant w , Eq. (85) is nothing but the superpotential of the standard Polonyi model of spontaneous supersymmetry breaking [153]. In this sense, the IYIT model can be regarded as a UV completion of the Polonyi model that offers a dynamical explanation for the origin of the SUSY-breaking scale μ . This is expected as the IYIT model is, after all, just a dynamical realization of spontaneous supersymmetry breaking à la O’Raifeartaigh. The IYIT model does not explain the UV origin of the constant w . In this paper, we will not speculate about this issue any further. That is, we do not have anything new to say about the CC problem.

Eq. (85) needs to be supplemented by the following Kähler potential (see Eqs. (16) and (28)),

$$K_{\text{tot}} \supset -3M_{\text{Pl}}^2 \ln \left[1 - \frac{F_{\text{hid}} + F_{\text{inf}}}{3M_{\text{Pl}}^2} \right], \quad F_{\text{hid}} = X^\dagger X, \quad F_{\text{inf}} = F, \quad (86)$$

where we set all terms to zero that are irrelevant for the present discussion. The functions in Eq. (85) and (86) allow us to calculate the total SUGRA potential for the Polonyi field in the Jordan frame,

$$V_{\text{hid}}^J(x) = \mu^4 + V_{1\ell}^J(x) - \frac{|3w + 2\mu^2 x|^2}{(1-f)3M_{\text{Pl}}^2} + m_R^2 |x|^2. \quad (87)$$

Here, the second term on the right-hand side, i.e., the Jordan-frame one-loop effective potential $V_{1\ell}^J$, is equivalent to the global-SUSY expression $V_{1\ell}$ in Eq. (83). The third term on the right-hand side

corresponds to a tree-level SUGRA correction in the Jordan frame, while the last term represents the gravity-induced mass discussed around Eq. (25). The function f in Eq. (87) is defined as follows,

$$f = \frac{1}{3M_{\text{Pl}}^2} (F - F_S F_{S^\dagger}) , \quad (88)$$

which may be regarded as a dimensionless measure for the amount of superconformal symmetry breaking in the kinetic function of the inflaton field. In the following, we will refer to f as the *reduced kinetic function* of the inflaton field. Given our choice for F in Eq. (28), the function f evaluates to

$$f = \frac{1 - 2\chi}{3M_{\text{Pl}}^2} [\chi \sigma^2 - (1 - \chi) \tau^2] . \quad (89)$$

As expected, this expression vanishes for $\chi \rightarrow \chi_{\text{CSS}} = 1/2$. The imaginary component of the complex inflaton field will be stabilized during inflation, $\tau = 0$. During inflation, we therefore have to deal with

$$f = (1 - 2\chi) z , \quad z = \frac{\chi \sigma^2}{3M_{\text{Pl}}^2} . \quad (90)$$

The constant w controls the value of the CC. To ensure that inflation ends in a Minkowski vacuum with vanishing CC, we need to impose the following two conditions after inflation, i.e., for $f = 0$,

$$V_{\text{hid}}^J(x) = 0, \quad \frac{d}{dx} V_{\text{hid}}^J(x) = 0 \quad \text{for } f = 0, \quad x = \langle X \rangle, \quad w = w_0 . \quad (91)$$

These two conditions can be solved for the two unknowns $\langle X \rangle$ and w_0 . Let us focus on w_0 for now,⁷

$$w_0 = \left(1 - \frac{4}{3k}\right)^{1/2} \frac{\mu^2 M_{\text{Pl}}}{\sqrt{3}} . \quad (92)$$

Here, k is a convenient measure for the relative importance of the SUGRA corrections in Eq. (87),

$$k = \frac{m_{1\ell}^2 + m_R^2}{\mu^4/M_{\text{Pl}}^2} . \quad (93)$$

The definition of k is chosen such that it mimics the effect of a higher-dimensional operator in F_{hid} ,

$$F_{\text{hid}} \supset X^\dagger X - \frac{k}{(2!)^2} \frac{(X^\dagger X)^2}{M_{\text{Pl}}^2} , \quad (94)$$

that induces a mass correction $\Delta m_k^2 = m_{1\ell}^2 + m_R^2$ in the SUGRA potential. Large values of k , thus, indicate that the Polonyi field is strongly stabilized by its one-loop effective mass, $\Delta m_k^2 \gg m_{3/2}^2$.

Given the result for the constant w_0 in Eq. (92), we can go one step back and determine the time-dependent Polonyi VEV during inflation. To do so, we just need to solve one equation,

$$\frac{d}{dx} V_{\text{hid}}^J(x) = 0 \quad \text{for } f \neq 0, \quad x = \langle X \rangle, \quad w = w_0 . \quad (95)$$

Assuming that $\langle X \rangle$ is located in the quadratic part of the potential, Eq. (95) has the following solution,

$$\langle X \rangle = \frac{(k - 4/3)^{1/2}}{[(1 - f)k - 4/3] k^{1/2}} \frac{2M_{\text{Pl}}}{\sqrt{3}} . \quad (96)$$

⁷The Kähler potential in Eq. (86) turns the usual e^{K/M_{Pl}^2} term in the SUGRA potential into a simple rational function (see Appendix A). Our Jordan-frame formulation of supergravity therefore allows us to solve the two conditions in Eq. (91) in a closed form. Note that this is not possible for the Polonyi model in standard Einstein-frame supergravity.

Indeed, in the limit of a large one-loop effective mass, $k \gg 1$, the Polonyi field remains stabilized close to the origin, $\langle X \rangle \ll M_{\text{Pl}}$. For $f = 0$, Eq. (96) turns into the solution of Eq. (91). Both the constant w_0 and the Polonyi VEV $\langle X \rangle$ break R symmetry. This is because both the superpotential W as well as the IYIT singlets Z_{\pm} carry R charge 2. We can therefore use our results in Eqs. (92) and (96) to determine the order parameter of R symmetry breaking, i.e., the gravitino mass in the Jordan frame,

$$m_{3/2} = \frac{\langle W \rangle}{M_{\text{Pl}}^2} = \frac{\mu^2 \langle X \rangle + w_0}{M_{\text{Pl}}^2} = \left(1 - \frac{4}{3k}\right)^{1/2} \frac{(1-f)k + 2/3}{(1-f)k - 4/3} \frac{\mu^2}{\sqrt{3}M_{\text{Pl}}}. \quad (97)$$

This result allows us to write the total mass of the Polonyi field in the Jordan frame, m_x^J , as follows,

$$(m_x^J)^2 = \left[1 - \frac{4}{3(1-f)k}\right] (m_{1\ell}^2 + m_R^2) = \frac{3k}{(1-f)(k-4/3)} \frac{[(1-f)k - 4/3]^3}{[(1-f)k + 2/3]^2} m_{3/2}^2. \quad (98)$$

In the following, we will restrict ourselves to the large- k limit. This is justified because k is typically at least of $\mathcal{O}(10)$ in the part of parameter space that we are interested in (see Eqs. (54) and (61)),

$$k \approx \frac{m_{1\ell}^2}{\mu^4/M_{\text{Pl}}^2} = \frac{1}{2} \left(\frac{c_{1\ell} \lambda M_{\text{Pl}}}{\Lambda}\right)^2 \simeq 47 \left(\frac{c_{1\ell}}{0.02}\right)^2 \left(\frac{\lambda}{1}\right)^2 \left(\frac{5 \times 10^{15} \text{ GeV}}{\Lambda}\right)^2. \quad (99)$$

In the large- k limit, the Polonyi VEV in Eq. (96) can be approximately written as follows,

$$\langle X \rangle \approx \frac{2\sqrt{3} m_{3/2}^2}{(1-f)(m_x^J)^2} M_{\text{Pl}} \approx \frac{2\sqrt{2}}{1-f} \frac{m_{3/2}}{c_{1\ell}^2 \lambda^3}, \quad (100)$$

confirming that $\langle X \rangle$ is parametrically enhanced compared to the gravitino mass, $\langle X \rangle \propto m_{3/2}/(c_{1\ell}^2 \lambda^3)$. For large values of k , also the relations between w_0 , μ , and $m_{3/2}$ become significantly simpler,

$$k \gg 1 \quad \Rightarrow \quad w_0 \approx \frac{\mu^2 M_{\text{Pl}}}{\sqrt{3}} \approx m_{3/2} M_{\text{Pl}}^2. \quad (101)$$

In the remainder of this paper, we will restrict ourselves to working with these approximate expressions.

We derived the result in Eq. (100) under the assumption that the leading term in the one-loop effective potential is an effective mass term, $V_{1\ell}^J = m_{1\ell}^2 |x|^2 + \mathcal{O}(x^4)$. The derivation of Eq. (100) is therefore only self-consistent and valid as long as $\langle X \rangle \lesssim x_c$ (see Eq. (83)). This implies a lower bound on the Yukawa coupling λ that depends on the energy scale Λ as well as on the hierarchy parameter ρ . We plot this lower bound λ_{min} as a function of Λ and ρ in the right panel of Fig. 1. The exact numerical result shown in this figure is well approximated by the following analytical expression,

$$\lambda_{\text{min}} \simeq \min \left\{ \frac{16\pi\sqrt{2}}{\sqrt{3}(2\ln 2 - 1)\rho^6} \frac{\Lambda}{M_{\text{Pl}}}, \left[\frac{4\pi\sqrt{2}\lambda_0^2}{\sqrt{3}(2\ln 2 - 1)} \frac{\Lambda}{M_{\text{Pl}}} \right]^{1/3} \right\}. \quad (102)$$

λ_{min} is sensitive to ρ at large values of ρ where n_M^{eff} in Eq. (62) is dominated by ρ rather than the neutral meson contribution $4\ell_0$. At small ρ values, where $n_M^{\text{eff}} \approx 4\ell_0$, the ρ dependence disappears. In addition to the lower bound λ_{min} , we also require that λ must remain perturbative, $\lambda < \lambda_{\text{pert}} = 4$. In the following, we will eliminate λ from our analysis and set it to the following value, for simplicity,

$$\bar{\lambda} = (\lambda_{\text{min}} \lambda_{\text{pert}})^{1/2}. \quad (103)$$

That is, we fix λ just at the central value of the allowed range of values, $\lambda_{\min} < \lambda < \lambda_{\text{pert}}$. Together with our choice for the hierarchy parameter, $\rho = \bar{\rho} \simeq 0.80$, this removes all dimensionless parameters from the IYIT sector, so that the only remaining free parameter is the scale Λ . We then obtain for $\bar{\lambda}$,

$$\bar{\lambda} \simeq 1.78 \left(\frac{\Lambda}{5 \times 10^{15} \text{ GeV}} \right)^{1/2}. \quad (104)$$

At the same time, λ must not be larger than $\lambda \simeq 2.41$, since otherwise λ_+ or λ_- will exceed λ_{pert} (see Eq. (59)). This results in an upper bound on the dynamical scale, $\Lambda \lesssim 10^{16} \text{ GeV}$. The relation in Eq. (104) enables us to express all mass scales in the IYIT sector in terms of Λ . For $\lambda = \bar{\lambda}$ and $\rho = \bar{\rho}$ and making use of Eqs. (54), (55), and (97), we find (in addition to the relations in Eq. (67))

$$\begin{aligned} \mu &\simeq 7.94 \times 10^{15} \text{ GeV} \left(\frac{\Lambda}{5 \times 10^{15} \text{ GeV}} \right)^{5/4}, \\ m_F &\simeq 7.15 \times 10^{15} \text{ GeV} \left(\frac{\Lambda}{5 \times 10^{15} \text{ GeV}} \right)^{3/2}, \\ m_{3/2} &\simeq 1.51 \times 10^{13} \text{ GeV} \left(\frac{\Lambda}{5 \times 10^{15} \text{ GeV}} \right)^{5/2}. \end{aligned} \quad (105)$$

The relations in Eqs. (67) and (105) are the main result of this chapter. They demonstrate how the dynamical breaking of supersymmetry in the IYIT sector generates all mass scales relevant for our model via dimensional transmutation. Our model, thus, does not require any hard dimensionful input parameters. Moreover, Eq. (105) illustrates that supersymmetry breaking close to the GUT scale results in a large gravitino mass. As expected, our model therefore predicts a very heavy sparticle spectrum (see Sec. 4.1). Eqs. (67) and (105) now set the stage for our model of D-term inflation.

2.5 Scalar potential in the inflaton sector

We now have all ingredients at our disposal to construct our inflationary model. In a first step, we add the usual superpotential of D-term inflation (see Eq. (2)) to the Polonyi superpotential in Eq. (85),

$$W_{\text{tot}} \supset \kappa S \Phi \bar{\Phi} + \mu^2 X + w_0. \quad (106)$$

The inflaton S as well as the waterfall fields Φ and $\bar{\Phi}$ belong to a separate sector that is sequestered from the IYIT sector. The relevant Kähler potential is of the following form (see Eqs. (16) and (28)),

$$K_{\text{tot}} \supset -3M_{\text{Pl}}^2 \ln \left[1 - \frac{F_{\text{hid}} + F_{\text{inf}}}{3M_{\text{Pl}}^2} \right], \quad F_{\text{hid}} = X^\dagger X, \quad F_{\text{inf}} = F + \Phi^\dagger \Phi + \bar{\Phi}^\dagger \bar{\Phi}. \quad (107)$$

The waterfall fields Φ and $\bar{\Phi}$ carry $B-L$ charges $+q$ and $-q$, respectively. They, thus, appear in the D-term scalar potential, together with the dynamically generated FI parameter ξ (see Eq. (65)),

$$V_D^J = \frac{g^2}{2} \left[q_0 \xi - q \left(|\phi|^2 - |\bar{\phi}|^2 \right) \right]^2. \quad (108)$$

V_D^J denotes the D-term scalar potential in the Jordan frame which is identical to the D-term scalar potential in global supersymmetry, V_D^0 . In addition, the total tree-level scalar potential V_{tree}^J also receives an F-term contribution V_F^J which can be computed by making use of Eqs. (106) and (107),

$$V_F^J = V_F^0 + \Delta V_F^J. \quad (109)$$

Here, the first contribution, V_F^0 , denotes the usual F-term scalar potential in global supersymmetry,

$$V_F^0 = \mu^4 + m_{\text{eff}}^2 \left(|\phi|^2 + |\bar{\phi}|^2 \right) + \kappa^2 |\phi|^2 |\bar{\phi}|^2, \quad (110)$$

while the second term, ΔV_F^J , corresponds to the tree-level SUGRA correction in the Jordan frame,

$$\Delta V_F^J = -\frac{\mu^4}{1-f} + (\delta m_{\text{eff}}^2)^* \phi \bar{\phi} + \delta m_{\text{eff}}^2 \phi^* \bar{\phi}^* + \delta \kappa^2 |\phi|^2 |\bar{\phi}|^2. \quad (111)$$

For more details on the computation of ΔV_F^J , see Appendix A. In Eqs. (110) and (111), we introduced the masses squared m_{eff}^2 and δm_{eff}^2 as well as the quartic coupling $\delta \kappa^2$. These are defined as follows,

$$m_{\text{eff}}^2 = \kappa^2 |s|^2, \quad \delta m_{\text{eff}}^2 = -\frac{1-2\chi}{1-f} m_{3/2} \kappa s, \quad \delta \kappa^2 = -\frac{(1-2\chi)^2 \kappa^2 |s|^2}{1-f} \frac{1}{3M_{\text{Pl}}^2}. \quad (112)$$

Note that all three parameters are field-dependent. The real mass parameter m_{eff}^2 denotes the effective inflaton-dependent mass that stabilizes the waterfall fields during inflation. The complex mass parameter δm_{eff}^2 is a bilinear mass that originates from the interference between the supersymmetric mass of the waterfall fields in the superpotential, $\kappa \langle S \rangle$, and the gravitino mass $m_{3/2}$. This so-called B term is, hence, a consequence of R symmetry breaking in the superpotential. It is only generated for the scalar waterfall fields and not for the corresponding fermions, which is why it breaks supersymmetry. Just like the usual A terms in models of broken supersymmetry, the B term results in a soft breaking of supersymmetry. The coupling $\delta \kappa^2$ will be irrelevant for our purposes as it constitutes just a small correction to κ^2 , i.e., the quartic coupling of the waterfall fields in global supersymmetry.

During inflation, the waterfall fields are stabilized at their origin, $\langle \phi \rangle = \langle \bar{\phi} \rangle = 0$. Along the inflationary trajectory, the tree-level scalar potential in the Jordan frame therefore reads as follows,

$$V_{\text{tree}}^J = \frac{1}{2} D_0^2 - \frac{f}{1-f} F_0^2, \quad D_0 = g q_0 \xi, \quad F_0 = \mu^2. \quad (113)$$

Here, $D_0^2/2$ denotes the contribution to the vacuum energy density from the D-term scalar potential. The large F-term contribution, $V_F^0 \supset +F_0^2$, is cancelled by the contribution from R symmetry breaking that is contained in the SUGRA correction to the scalar potential, $\Delta V_F^J \supset -F_0^2$. This explains why the vacuum energy density during inflation is dominated by the D-term contribution in our model. During the $B-L$ phase transition at the end of inflation, the D term is absorbed by the VEV of one of the waterfall fields. In the true vacuum after inflation, all contributions to the CC therefore approximately cancel. In the next section, we will perform a standard slow-roll analysis of our inflationary model. This is most easily done in terms of the usual slow-roll parameters in the Einstein frame. To compute these parameters, we need to convert the potential in Eq. (113) from the Jordan frame to the Einstein frame. This is achieved by rescaling V_{tree}^J by the fourth power of the conformal factor \mathcal{C} (see Eq. (13)),

$$V_{\text{tree}} = \mathcal{C}^4 V_{\text{tree}}^J = \left(-\frac{3M_{\text{Pl}}^2}{\Omega} \right)^2 \left[\frac{1}{2} D_0^2 - \frac{f}{1-f} F_0^2 \right]. \quad (114)$$

On the inflationary trajectory, this can be rewritten as a function of the parameter z (see Eq. (90)),

$$V_{\text{tree}} = \frac{1}{(1-z)^2} \left[\frac{1}{2} D_0^2 - \frac{(1-2\chi)z}{1-(1-2\chi)z} F_0^2 \right], \quad z = \frac{\chi \sigma^2}{3M_{\text{Pl}}^2}. \quad (115)$$

The second derivative of V_{tree} w.r.t. the field σ provides us with the mass parameter m_σ^2 (see Eq. (29)),

$$m_\sigma^2 = 2\chi \left[\frac{D_0^2}{3M_{\text{Pl}}^2} - (1 - 2\chi) \frac{F_0^2}{3M_{\text{Pl}}^2} \right], \quad \frac{D_0^2}{3M_{\text{Pl}}^2} \approx m_R^2, \quad \frac{F_0^2}{3M_{\text{Pl}}^2} \approx m_{3/2}^2. \quad (116)$$

As anticipated, m_σ is suppressed by the shift-symmetry-breaking parameter χ . By appropriately choosing χ , we will therefore be able to adjust the scalar spectral index n_s so that it matches the observed best-fit value. We also note that the mass parameter m_σ is not a physical mass eigenvalue in the actual sense. This is because the scalar inflaton field σ is not properly normalized. The mass of the canonically normalized inflaton field $\hat{\sigma}$ is instead given in terms of the slow-roll parameter η in the Einstein frame, $m_{\hat{\sigma}}^2 = 3\eta H^2 \sim m_\sigma^2$ (see Sec. 3.2). Moreover, m_σ is just a tree-level parameter, whereas the scalar potential also receives important contributions at the one-loop level.

The radiative corrections are encoded in the one-loop effective Coleman-Weinberg potential [154],

$$V_{1\ell}^J = \frac{Q_J^4}{64\pi^2} \text{STr} \left[\frac{\mathcal{M}_J^4}{Q_J^4} \left(\ln \frac{\mathcal{M}_J^2}{Q_J^2} - C \right) \right], \quad C = \frac{3}{2}. \quad (117)$$

Here, $\text{STr}[\cdot]$ stands for the supertrace over a (matrix-valued) function of the total tree-level mass matrix squared \mathcal{M}_J^2 in the Jordan frame. We evaluate $V_{1\ell}^J$ in the $\overline{\text{MS}}$ renormalization scheme and only consider contributions from scalars and fermions. This fixes the numerical constant C in Eq. (117) to $C = 3/2$ (see, e.g., [155]). The energy scale Q_J denotes the $\overline{\text{MS}}$ renormalization scale. To determine the radiative corrections to the inflaton potential, it is sufficient to focus on the inflaton-dependent masses in the waterfall sector. From Eqs. (24), (108), (110), and (111), we find for the scalar fields,

$$V_{\text{tree}}^J \supset \frac{1}{2} \begin{pmatrix} \phi^* \\ \bar{\phi}^* \\ \phi \\ \bar{\phi} \end{pmatrix}^T \begin{pmatrix} m_\phi^2 & 0 & 0 & \delta m_{\text{eff}}^2 \\ 0 & m_{\bar{\phi}}^2 & \delta m_{\text{eff}}^2 & 0 \\ 0 & (\delta m_{\text{eff}}^2)^* & m_\phi^2 & 0 \\ (\delta m_{\text{eff}}^2)^* & 0 & 0 & m_{\bar{\phi}}^2 \end{pmatrix} \begin{pmatrix} \phi \\ \bar{\phi} \\ \phi^* \\ \bar{\phi}^* \end{pmatrix}, \quad m_{\phi, \bar{\phi}}^2 = m_{\text{eff}}^2 + m_R^2 \mp q m_D^2. \quad (118)$$

where the mass parameters m_D^2 , m_R^2 , m_{eff}^2 , and δm_{eff}^2 are respectively defined below Eq. (8) as well in Eqs. (25) and (112). In addition to these tree-level masses, the scalar waterfall fields also obtain gauge-mediated masses at the loop level. This is because supersymmetry breaking in the IYIT sector results in a mass splitting among the components of the massive $B-L$ vector multiplet (see Eq. (75)) [156]. Including these one-loop masses into Eq. (117) would result in a two-loop contribution to the effective potential. For this reason, we will ignore the effect of *gauge-mediated supersymmetry breaking* (GMSB) for now. We will come back to this issue in Sec. 4.1. In the next step, we diagonalize the mass matrix in Eq. (118). This results in two complex mass eigenstates ϕ_\pm with inflaton-dependent mass eigenvalues,

$$m_\pm^2 = m_{\text{eff}}^2 + m_R^2 \pm (1 + \delta^4)^{1/2} q m_D^2, \quad \delta^4 = \frac{|\delta m_{\text{eff}}^2|^4}{q^2 m_D^4}. \quad (119)$$

Here, δ is related to the rotation angle $\beta_{\phi\bar{\phi}}$ that diagonalizes the scalar mass matrix, $\delta^2 = \tan(2\beta_{\phi\bar{\phi}})$. We note that the parameter δ depends on the inflaton field value, which makes it a time-dependent quantity. For this reason, the mass eigenstates ϕ_\pm do not coincide with the charge eigenstates $\phi, \bar{\phi}$ during inflation. The mass parameters m_R^2 , m_D^2 , and δm_{eff}^2 in Eq. (119) arise from various effects in

the scalar sector of our model: the conformal coupling to the Ricci scalar in Eq. (24), the D-term scalar potential in Eq. (108), and the soft B term in Eq. (111). None of these effects is relevant for the fermions in the waterfall sector. The two Weyl fermions in Φ and $\bar{\Phi}$ simply from a Dirac fermion $\tilde{\phi}$ with Jordan-frame mass $m_{\tilde{\phi}} = m_{\text{eff}}$. No further SUGRA corrections arise in the Jordan frame [112].

We are now ready to evaluate $V_{1\ell}^J$ in Eq. (117). Our final result can be written as follows,

$$V_{1\ell}^J = \frac{Q_J^4}{16\pi^2} L(x, \alpha), \quad L(x, \alpha) = \frac{1}{4} \text{STr} \left[\frac{\mathcal{M}_J^4}{Q_J^4} \left(\ln \frac{\mathcal{M}_J^2}{Q_J^2} - \frac{3}{2} \right) \right], \quad (120)$$

where L is a one-loop function that takes the same form in the Jordan frame as in the Einstein frame,

$$L(x, \alpha) = \frac{1}{2} \sum_{\pm} (x \pm 1)^2 \left[\ln(x \pm 1) - \frac{3}{2} \right] - (x - \alpha)^2 \left[\ln(x - \alpha) - \frac{3}{2} \right], \quad (121)$$

and where the variable x , the parameter α , and the renormalization scale Q_J are introduced such that

$$x = \frac{m_{\text{eff}}^2 + m_R^2}{Q_J^2}, \quad \alpha = \frac{m_R^2}{Q_J^2}, \quad Q_J^2 = (1 + \delta^4)^{1/2} q m_D^2. \quad (122)$$

All of these quantities depend on the inflaton field value by virtue of the parameters m_{eff}^2 , m_R^2 , and δ . In the following, we will, however, neglect the field dependence of m_R^2 and approximate it instead by the constant expression in Eq. (116). The fact that Q_J is field-dependent does not pose any problem for our model. Recall that one usually encounters a field-independent renormalization scale Q_J in the Jordan frame and a field-dependent renormalization scale $Q = \mathcal{C} Q_J$ in the Einstein frame—or vice versa. In our model, the renormalization scale is, by contrast, field-dependent in both frames. This is *a priori* a perfectly valid choice. Independent of whether Q_J is field-dependent or not, we merely have to make sure that our final results are not overly sensitive to our particular choice for Q_J . This is a requirement that we will have to check *a posteriori* as part of our slow-roll analysis (see Sec. 3). The main field dependence of Eq. (120) is encoded in x which may also be written as follows,

$$x = \frac{m_+^2 + m_-^2}{m_+^2 - m_-^2} = \frac{2 m_{\text{eff}}^2}{m_+^2 - m_-^2} + \alpha. \quad (123)$$

$x = 1$ therefore corresponds to the critical point along the inflationary trajectory at which m_- vanishes,

$$x = 1 \quad \Leftrightarrow \quad \sigma = \sigma_c \quad \Leftrightarrow \quad m_- = 0. \quad (124)$$

At this point in field space, the mass eigenstate ϕ_- becomes tachyonically unstable which triggers the $B-L$ waterfall transition. We also note that Eq. (123) illustrates the physical meaning of α . The parameter α represents a shift in the field variable x compared to the situation in global supersymmetry where one simply has $x_0 = 2 m_{\text{eff}}^2 / (m_+^2 - m_-^2)$. As evident from Eq. (122), this shift results from the fact that the waterfall scalars obtain a gravity-induced mass m_R , while the waterfall fermion does not.

To convert Eq. (120) into the one-loop effective Coleman-Weinberg potential in the Einstein frame, we need to multiply again by \mathcal{C}^4 , just like in the case of the tree-level scalar potential (see Eq. (114)),

$$V_{1\ell} = \mathcal{C}^4 V_{1\ell}^J = \frac{Q^4}{16\pi^2} L(x, \alpha), \quad Q = \mathcal{C} Q_J. \quad (125)$$

The Weyl transformation from the Jordan frame to the Einstein frame therefore corresponds to nothing but a rescaling of the Q_J^4 factor in Eq. (120). The loop function L remains unchanged. This is consistent with the fact that the Weyl transformation in Eq. (13) only affects dimensionful parameters. A mass scale m_J in the Jordan frame is, e.g., mapped onto $m = \mathcal{C} m_J$ in the Einstein frame. Dimensionless ratios of mass parameters, thus, remain invariant under the Weyl transformation [114,115]. In passing, we also mention that the effective scalar potential $V_{1\ell}$ in Eq. (125) cannot be derived from the effective Kähler potential $K_{1\ell}$ in Eq. (30). The reason for this is that, in D-term inflation, the effective Kähler potential $K_{1\ell}$ can enter into the total scalar potential only via the D-term scalar potential,

$$K_{\text{tot}} \rightarrow K_{\text{tot}} + K_{1\ell} \quad \Rightarrow \quad V_D \supset -gq D_0 \left(\phi \frac{\partial}{\partial \phi} K_{1\ell} - \bar{\phi} \frac{\partial}{\partial \bar{\phi}} K_{1\ell} \right). \quad (126)$$

This, however, only constitutes a contribution to the one-loop effective potential for the waterfall fields which we are not interested in. The one-loop effective potential for the inflaton field in Eq. (125) has a different origin. This can be explicitly seen in the superspace formulation of global supersymmetry. There, Eq. (125) does not follow from the effective potential for the chiral multiplets S , Φ , and $\bar{\Phi}$, i.e., from the effective Kähler potential $K_{1\ell}$, but from the effective potential for the auxiliary D component of the vector field V [136]. This quantity is less often discussed in the literature. Alternatively, Eq. (125) can also be derived in a superspace language that applies to models of softly broken global supersymmetry [139]. In this approach, one first integrates out the heavy vector multiplet V such that supersymmetry is softly (and explicitly) broken in the effective theory at low energies. Then, one calculates the radiative corrections to the soft SUSY-breaking terms in the Lagrangian. This allows one to recover Eq. (125) as the one-loop renormalization of the so-called soft Kähler potential \tilde{K} . In an explicit calculation, we convince ourselves that Eq. (125) indeed satisfies the relation $V_{1\ell} = -\tilde{K}_{1\ell}$. It is interesting to note that this result differs from the situation in F-term inflation. There, the effective Kähler potential directly contributes to the effective inflaton potential via the F-term scalar potential.

The total inflaton potential follows from the combination of our results in Eqs. (114) and (125),

$$V = \frac{V^J}{(1-z)^2}, \quad V^J = \left[\frac{1}{2} + (1 + \delta^4) \frac{g^2 q^2}{16\pi^2} L(x, \alpha) \right] D_0^2 - \frac{(1-2\chi)z}{1-(1-2\chi)z} F_0^2 \quad (127)$$

The individual parameters and functions appearing in this potential can be found in the following equations: z in Eq. (90), D_0 and F_0 in Eq. (113), δ in Eq. (119), and L in Eq. (121). The potential in Eq. (127) is one of the main results in this paper and the starting point of our phenomenological study of the inflationary dynamics (see Sec. 3). In conclusion, let us summarize the main differences between Eq. (127) and the inflaton potential of ordinary D-term inflation in global supersymmetry,

$$V_0 = \left[\frac{1}{2} + \frac{g^2 q^2}{16\pi^2} L(x_0, 0) \right] D_0^2, \quad x_0 = \frac{m_{\text{eff}}^2}{q m_D^2}. \quad (128)$$

Compared to this potential, our total inflaton potential V receives four different SUGRA corrections: (i) The total potential is rescaled by \mathcal{C}^4 to account for the transition from the Jordan frame to the Einstein frame. (ii) The approximate shift symmetry in the inflaton kinetic function in combination with F-term SUSY breaking in the IYIT sector results in a small contribution from the F-term scalar

potential. (iii) The soft B term mass δm_{eff}^2 modifies the prefactor of the one-loop effective potential as well as the definition of the field variable x . (iv) The gravity-induced mass m_R gives rise to the parameter α . All of these effects vanish in the global-SUSY limit, such that $V \rightarrow V_0$. The main claim of our paper is that the SUGRA corrections in Eq. (127) are instrumental in realizing a viable scenario of D-term inflation that is in agreement with all theoretical and phenomenological constraints.

3 Phenomenology: A viable scenario of D-term hybrid inflation

In the previous section, we introduced a supergravity embedding of the IYIT model of dynamical supersymmetry breaking with the following properties: (i) by promoting a $U(1)$ flavour symmetry of the DSB model to the gauged $U(1)_{B-L}$ symmetry, we connect the scales of supersymmetry and $B-L$ breaking and simultaneously generate an effective FI term for the $U(1)_{B-L}$ symmetry. We demonstrated that all mass scales, including the FI term, the $B-L$ breaking scale and the supersymmetry breaking scale, are all set by the dynamical scale Λ , see Eqs. (67) and (105). (ii) The effective FI term generates a D-term scalar potential which can be used to implement DHI. Besides the usual one-loop contribution from integrating out the waterfall fields in the limit $M_{\text{Pl}} \rightarrow \infty$, our construction entails several (calculable) supergravity corrections. The final result for the one-loop effective scalar potential is given in Eq. (127). (iii) The requirement of perturbativity and the necessity to stabilize the Polonyi field leads to constraints on the parameters of the DSB model, see Fig. 1.

In this section we turn to the phenomenology of the resulting DHI model, outlined in Sec. 2.1. This will essentially fix the only remaining free parameter of our DSB sector, the dynamical scale Λ . After briefly reviewing the standard picture in global supersymmetry, we proceed to an analytical study of the parameter space, highlighting the most important effects of the different contributions to the scalar potential calculated in the previous section. We then present a full numerical study of the relevant parameter space, supplemented by a discussion on the initial conditions in different parts of the parameter space.

3.1 D-term inflation in global SUSY

The key ingredients of globally supersymmetric DHI are the superpotential and D-term potential given in Eq. (2). The waterfall fields $\Phi, \bar{\Phi}$ obtain masses which depend on the scalar component s of the chiral multiplet S , which stabilize them for values of the inflaton field above the critical value $|s_c^{\text{glob}}|^2 = g^2 q q_0 \xi / \kappa^2$. These field-dependent masses result in a Coleman-Weinberg one-loop contribution to the effective potential of the inflaton, so that the scalar potential for the inflaton above the critical field value is given by Eq. (128). At the critical field value (corresponding to $x_0 = 1$) one of the waterfall fields acquires a nonvanishing vacuum expectation value, absorbing the FI term ξ .

Identifying the inflaton field as the radial component of s , $\varphi = |s|/\sqrt{2}$, its classical evolution during inflation is described by the slow-roll equation,

$$V(\varphi) \varphi'(N) = V'(\varphi), \quad (129)$$

where $N = -\int H dt$ counts the number of remaining e-folds N to the end of inflation (with $N = 0$ at the end of inflation). This is an accurate description of the inflationary dynamics as long as the slow-roll parameters,

$$\varepsilon(\varphi) = \frac{M_{\text{Pl}}^2}{2} \left(\frac{V'(\varphi)}{V(\varphi)} \right)^2, \quad \eta(\varphi) = M_{\text{Pl}}^2 \frac{V''(\varphi)}{V(\varphi)}, \quad (130)$$

are much smaller than one. The CMB observables, describing the statistical properties of vacuum quantum fluctuation during inflation, can be expressed in terms of these variables as

$$A_s = \frac{V}{24\pi^2 \varepsilon M_{\text{Pl}}^4}, \quad n_s = 1 - 6\varepsilon + 2\eta, \quad r = 16\varepsilon, \quad (131)$$

evaluated at $N_* \simeq 55$ e-folds before the end of inflation.

DHI ends at the critical field value φ_c or even earlier, when the second slow-roll parameter η becomes large, $\varphi_\eta^2 = (g^2 q^2 M_{\text{Pl}}^2)/(16\pi^2)$, depending on the size of φ_η/φ_c . For $\varphi_\eta/\varphi_c \gg 1$, i.e., if the slow-roll condition is violated before the critical point, the value of φ at N_* e-folds before the end of inflation is given by $\varphi_*^2 \simeq (g^2 q^2 N_* M_{\text{Pl}}^2)/(4\pi^2)$. The amplitude of the scalar spectrum is mainly controlled by the FI parameter, $A_s \simeq (q_0^2 N_* \xi^2)/(3q^2 M_{\text{Pl}}^4)$, and its spectral index, governed by the second slow-roll parameter η , is obtained as $n_s \simeq 1 - 1/N_* \simeq 0.98$ in the limit of $gq \ll 4\pi$. For values of ξ around the GUT scale, this yields the correct scalar amplitude, albeit with a somewhat too large spectral index, disfavoured by about 2σ by the current data [75].

On the other hand, if the slow-roll conditions are satisfied all the way up to the critical field value, we find $\varphi_* \simeq \varphi_c$. The small value of the inflaton coupling κ in this region of parameter space implies that the field excursion during $N_* \simeq 55$ e-folds of inflation is typically small compared to the field value at the endpoint of inflation φ_c . The observed value of the scalar amplitude fixes $A_s^{\text{obs}} = A_s = (4\pi^2 q_0^3 \xi^3)/(3q^2 \kappa^2 M_{\text{Pl}}^6)$, enabling lower values of ξ for smaller values of κ . The spectral index in this region is found to be $n_s \simeq 1$, excluded at more than 5σ by the PLANCK data [75].

Despite its simplicity and obvious connection to particle physics, this model has several major short-comings, as discussed in Sec. 2.2. These are connected to the origin of the FI mass scale in supergravity, the stability of scalar fields during inflation, gravitational corrections to the inflaton trajectory in supergravity, and phenomenological constraints from CMB observations. In the following, we demonstrate how all these shortcomings can simultaneously be overcome in our setup.

3.2 Analytical description of the inflationary phase

Inflationary dynamics in SUGRA

In the following we implement DHI with the dynamically generated FI term of Sec. 2.3, supplemented by the assumption of an approximate shift symmetry in the direction of the inflaton field. As discussed in Section 2.2, this shift symmetry is broken by one-loop effects in the scalar potential and Kähler potential. The interplay of these two small contributions will enable us to identify regions in parameter space which comply with all experimental constraints.⁸

⁸This includes the nonobservation of cosmic strings, as will be demonstrated in Sec. 4.4.

The dynamics of inflation is determined by the scalar potential (127), which contains all relevant supergravity and one-loop contributions. Our choice of kinetic function F (see Eq. (28)) with $\chi \ll 1$ ensures that σ , the real part of the complex scalar s , plays the role of the inflaton. The supergravity version of Eq. (129) in the Einstein frame reads

$$\mathcal{K}_{ss^*}(\sigma) V(\sigma) \sigma'(N) = V'(\sigma). \quad (132)$$

where $V = \mathcal{C}^4 V^J$ is the Einstein-frame scalar potential and $\mathcal{K}_{ss^*} = \partial^2 K / (\partial s \partial s^*)$ is the prefactor of the kinetic term for the inflaton. The initial condition (i.e., the end of inflation) is given by $\sigma(N=0) = \max(\sigma_c, \sigma_\eta)$. This enables us to evaluate the (Einstein-frame) slow-roll parameters $\varepsilon(\hat{\sigma})$ and $\eta(\hat{\sigma})$ and hence the CMB observables at $N_* = 55$ e-folds before the end of inflation. Evaluating the slow-roll parameters requires derivatives of the scalar potential with respect to the canonical normalized field $\hat{\sigma}$, which we perform by exploiting $\partial \hat{\sigma} / \partial \sigma = \sqrt{\mathcal{K}_{ss^*}}$, as follows from the canonically normalization of the kinetic terms in the Einstein frame,

$$\frac{1}{2} \mathcal{K}_{ss^*} \partial_\mu \sigma \partial^\mu \sigma \simeq \frac{1}{2} \mathcal{C}^4 (1-f) \partial_\mu \sigma \partial^\mu \sigma = \frac{1}{2} \partial_\mu \hat{\sigma} \partial^\mu \hat{\sigma}. \quad (133)$$

For convenience, we recall here a few key quantities (evaluated along the inflationary trajectory) introduced earlier (see Eqs. (13), (15), (28) and (90))

$$\mathcal{C}^2 = -\frac{3M_{\text{Pl}}^2}{\Omega}, \quad \Omega = -3M_{\text{Pl}}^2 + F, \quad F = \chi \sigma^2, \quad f = (1-2\chi)z, \quad z = \frac{\chi \sigma^2}{3M_{\text{Pl}}^2}. \quad (134)$$

For more details on translating between the Einstein and Jordan frame, see App. A.

The results of the numerical analysis are shown in Fig. 2. Before discussing them in detail, we will give an analytical analysis of the parameter space in the vicinity of the globally supersymmetric limit. This will prove instructive for interpreting the numerical results.

Slow-roll parameters

The slow-roll parameters in the Einstein frame can be expressed in terms of derivatives of the scalar potential and of the kinetic function in the Jordan frame as (see Appendix A.4),

$$\varepsilon = \frac{1}{\mathcal{N}^2} \left(\varepsilon_J^{1/2} - 2\xi_J^{1/2} \right)^2, \quad (135)$$

$$\eta = \frac{1}{\mathcal{N}^2} \left(\eta_J + 12\xi_J - 8(\varepsilon_J \xi_J)^{1/2} - 2\zeta_J - 2\nu^{1/2} \left(\varepsilon_J^{1/2} - 2\xi_J^{1/2} \right) \right), \quad (136)$$

with $\mathcal{N} \equiv \mathcal{K}_{s^\dagger s}^{1/2} = \mathcal{C}^2(1-f)^{1/2}$ and

$$\begin{aligned} \varepsilon_J &\equiv \frac{M_{\text{Pl}}^2}{2} \left(\frac{V_\sigma^J}{V^J} \right)^2, & \eta_J &\equiv M_{\text{Pl}}^2 \frac{V_{\sigma\sigma}^J}{V^J}, \\ \xi_J^{1/2} &\equiv \frac{M_{\text{Pl}}}{\sqrt{2}} \frac{\Omega_\sigma}{\Omega}, & \zeta_J &\equiv M_{\text{Pl}}^2 \frac{\Omega_{\sigma\sigma}}{\Omega}, & \nu &\equiv \frac{M_{\text{Pl}}^2}{2} \left(\frac{\mathcal{N}_\sigma}{\mathcal{N}} \right)^2. \end{aligned} \quad (137)$$

These expressions are equivalent to those found in Appendix A of Ref. [157]. In the following, we will use Eqs. (135) and (136) to analyze the inflationary predictions, since this format enables us to nicely disentangle the different contributions in various parts of the parameter space.

With the definitions above, simplified expressions for the *Jordan-frame slow-roll parameters* ε_J and η_J can be obtained by approximating the Coleman-Weinberg one-loop potential for $x \gg 1$ and $\alpha \ll 1$ as

$$V_{1\ell}^J = \frac{Q_J^4}{16\pi^2} \left[\ln x + \mathcal{O}(\alpha x) \right]. \quad (138)$$

with x , α and Q_J given in Eq. (122). As in the globally supersymmetric case, $x = 1$ denotes the critical point. Eq. (138) is a good approximation as long as $1 \ll x \ll 1/\alpha$, which will hold in most of the parameter regime of interest. We then find

$$\varepsilon_J \simeq \left(\frac{M_{\text{Pl}}}{\sigma/\sqrt{2}} \right)^2 \left[(1 + \delta_\varepsilon^4) \frac{q^2 g^2 D_0^2}{16\pi^2 V^J} - \frac{f}{(1-f)^2} \frac{F_0^2}{V^J} \right]^2, \quad (139)$$

$$\eta_J \simeq - \left(\frac{M_{\text{Pl}}}{\sigma/\sqrt{2}} \right)^2 \left[(1 - \delta_\eta^4) \frac{q^2 g^2 D_0^2}{16\pi^2 V^J} + \frac{f(1+3f)}{(1-f)^3} \frac{F_0^2}{V^J} \right], \quad (140)$$

with f given in Eq. (90) and

$$\delta_\varepsilon \equiv \left(\ln x + \frac{1}{2} \right)^{1/4} \delta, \quad \delta_\eta \equiv \left(\ln x + \frac{1}{2} + \frac{2 + \delta^4}{1 + \delta^4} \right)^{1/4} \delta, \quad (141)$$

where δ was introduced in Eq. (119) and F_0 and D_0 denote the F- and D-term contributions from global supersymmetry, respectively. For both ε_J and η_J , the term proportional to D_0^2 stems from the Coleman-Weinberg one-loop potential whereas the term proportional to F_0^2 is a supergravity effect, induced by the noncanonical terms in the Kähler potential. Moreover, we note that the Coleman-Weinberg term splits into the expression familiar from global supersymmetry (indicated by the “1” in the parenthesis) and the supergravity contribution to the waterfall field sector, parametrized by $\delta_{\varepsilon,\eta}^4$. Note that, as in global supersymmetry, ε_J is suppressed compared to η_J .

Eqs. (139) and (140) illustrate the main effect of the F-term SUGRA corrections in our model. For $f \ll 1$ and $V^J \simeq D_0^2/2$, the second term in Eq. (140) yields

$$\Delta\eta_J \simeq -\frac{4}{3}(1-2\chi)\chi \frac{F_0^2}{D_0^2}, \quad (142)$$

indicating that the supergravity contributions from the tree-level F-term scalar potential can induce the desired lowering of the spectral index ($\Delta\eta \sim -0.01$) compared to the result of global supersymmetry if $\chi \simeq 7.5 \times 10^{-3} D_0^2/F_0^2$.⁹ This small value of χ indicates the presence of an approximate shift symmetry.

Turning to the effects of a small, positive value for χ on the first slow-roll parameter, see Eq. (139), we note that positive χ will lead to a decrease in ε . The one-loop and SUGRA contributions may even cancel each other, indicating the presence of a hilltop or a saddle point in the scalar potential. We will come back to the consequences of such a scenario below.

The explicit expressions for the remaining auxiliary Jordan-frame slow-roll parameters are

$$\xi_J^{1/2} = - \left(\frac{M_{\text{Pl}}}{\sigma/\sqrt{2}} \right) \frac{z}{1-z}, \quad \zeta_J = - \left(\frac{M_{\text{Pl}}}{\sigma/\sqrt{2}} \right)^2 \frac{z}{1-z}, \quad \nu^{1/2} = \left(\frac{M_{\text{Pl}}}{\sigma/\sqrt{2}} \right) \frac{(1+2\chi-f)z}{2(1-z)(1-f)} \quad (143)$$

⁹For $\chi = 1/2$, we have $\Delta\eta_J = 0$, which corresponds to the absence of a $m_{3/2}^2$ term for the inflaton field due to the sequestering Kähler potential. One might thus expect a second solution, $\chi = 1/2 - |\delta\chi|$ with $|\delta\chi| \ll 1$, to produce $\Delta\eta \sim -0.01$. However in this case the corresponding gravity-induced mass for the inflaton, see Eq. (144), is too large.

Here ζ_J captures the gravity-induced mass of the inflaton and emphasizes once more the need for an approximate shift symmetry ($\chi \ll 1$) for the inflaton field: for $\chi \simeq 1/2$, the inflaton picks up a gravity-induced mass just as all the other scalars do,

$$\chi \simeq \frac{1}{2} \quad \Rightarrow \quad m_\sigma^2 \simeq m_R^2. \quad (144)$$

with $m_R^2 \simeq D_0^2/(3M_{\text{Pl}}^2)$. This implies a contribution to the slow-roll parameter η of $\Delta\eta_\zeta \simeq 2/3$ (see Eq. (26)) and, hence, leads to an η problem. A pure canonical term in the inflaton kinetic function, $F \simeq S^\dagger S$, is therefore not viable in our model. The approximate shift symmetry resolves the problem, suppressing this contribution as $\Delta\eta_\zeta \simeq 4\chi/3$. Of course, Eq. (142) and (144) directly correspond to the second and first term of Eq. (116), respectively. Due to $F_0 > D_0$, the contribution from Eq. (142) will always dominate for $\chi \ll 1$.

Inserting these results into Eqs. (135) and (136), we find to leading order ($z \ll 1$, $D_0/F_0 \ll 1$):

$$\varepsilon \simeq \left(\frac{M_{\text{Pl}}}{\sigma/\sqrt{2}} \right)^2 \left[(1 + \delta_\varepsilon^4) \frac{q^2 g^2 D_0^2}{16\pi^2 V^J} - f \frac{F_0^2}{V^J} \right]^2, \quad (145)$$

$$\eta \simeq - \left(\frac{M_{\text{Pl}}}{\sigma/\sqrt{2}} \right)^2 \left[(1 - \delta_\eta^4) \frac{q^2 g^2 D_0^2}{16\pi^2 V^J} + f \frac{F_0^2}{V^J} \right]. \quad (146)$$

Viable parameter space

Starting from Eqs. (145) and (146) and the results of D-term hybrid inflation in global supersymmetry, we can analytically assess the viable parameter space in the vicinity of the globally supersymmetric results. Comparing the global SUSY DHI results with the observed value for n_s , we conclude that the supergravity contributions must enhance $|\eta|$ by (at least) an $\mathcal{O}(1)$ factor. At the same time, requiring $V'(\hat{\sigma}) > 0$ implies an upper bound on these contributions (see Eq. (145)):

$$(1 - \delta_\eta^4) \frac{q^2 g^2 D_0^2}{16\pi^2 V^J} \lesssim f \frac{F_0^2}{V^J} < (1 + \delta_\varepsilon^4) \frac{q^2 g^2 D_0^2}{16\pi^2 V^J}, \quad (147)$$

for $\sigma = \sigma_*$. This implies a lower bound on δ (governing both the size of δ_ε and δ_η). At the same time, δ_η yields a positive contribution to η and a too large value will lead to an enhancement of the spectral index n_s . Together this implies $\delta \sim \mathcal{O}(0.1 \cdots 1)$, where to leading order $\delta^4 \simeq \kappa^2 \sigma^2 m_{3/2}^2 / (2q_0^2 q^2 g^4 \xi^2)$. We can estimate δ by exploiting the analytical results for σ_* in globally supersymmetric D-term hybrid inflation, see Sec. 3.1. In addition, we note that the requirement that the tree-level supergravity term contributes $\Delta\eta \sim -0.01$ implies

$$-\Delta\eta \simeq \frac{2\chi}{3} \left(\frac{m_{3/2}}{H_J} \right)^2 \simeq 0.01 \quad \rightarrow \quad \chi \simeq 10^{-4} \left(\frac{g}{0.1} \right)^2 \left(\frac{10^{15} \text{ GeV}}{\sqrt{\xi}} \right). \quad (148)$$

where we have inserted the relations (67) and (105).

In the regime of large κ (and taking for simplicity $|q| \sim |q_0| \sim 1$), the constraints on δ thus roughly fix the parameter combination $\kappa^2 \sqrt{\xi}/g^2$. Using Eq. (148) we immediately see that the correct spectral index can be obtained for

$$\chi \simeq 3.5 \times 10^{-4} \left(\frac{0.1}{\delta^4} \right) \left(\frac{\kappa}{0.1} \right)^2 \left(\frac{N_*}{55} \right). \quad (149)$$

The amplitude of the scalar power spectrum A_s is mainly dependent on ξ , see Sec. 3.1. This essentially fixes $\xi \simeq 10^{-5} M_{\text{Pl}}^2$, and determines the preferred range of the gauge coupling, e.g. $g \sim 0.1$ for $\kappa = 0.1$. Note that this constraint can be circumvented if one allows inflation to begin very close to the hilltop of the scalar potential, $\varepsilon_* \simeq 0$, which can be obtained by tuning the contributions in Eq. (145). From Eq. (131) we see that in this case, we can in principle arbitrarily lower ξ . However, this corresponds to a very tuned situation and we will not focus on this regime of the parameter space.

In the regime of small κ we note from the expressions of the globally supersymmetric limit that $\sigma_* \simeq \sigma_c$ and $n_s \simeq 1$. This indicates that (i) the leading order term in the expansion of V_{CW} in $1/x$ becomes a poor approximation and (ii) to obtain the correct spectral index, we must rely nearly exclusively on the supergravity terms in η . As a result of the first point, the lower bound on δ in fact becomes irrelevant when using the full expression for the one-loop potential. We are thus left with $\xi^{3/2}/g^2 \lesssim 8.5 \times 10^{-3} M_{\text{Pl}}^3/2\delta^4$. Imposing the observed value for A_s and approximating σ_* by the corresponding expression in globally supersymmetric DHI, this yields

$$\xi \simeq 5.5 \times 10^{-6} M_{\text{Pl}}^2 \left(\frac{\kappa}{10^{-3}} \right)^{2/3}. \quad (150)$$

Inserting this into Eq. (148), we find

$$\chi \simeq 0.1 g^2 \left(\frac{\kappa}{10^{-3}} \right)^{-1/3}. \quad (151)$$

Both Eq. (149) and Eq. (151) point to small values of χ , i.e., an approximate shift symmetry. For $\kappa = 0.1$, Eq. (149) indicates a value of χ which is larger than obtained only by integrating out the waterfall fields, $\chi_{1\ell} \simeq \kappa^2/(16\pi^2) = 6 \times 10^{-5} (\kappa/0.1)^2$, see Eq. (30). On the other hand, for smaller values of κ , the symmetry breaking induced by the waterfall fields can be sufficient to generate the correct spectral index for accordingly small values of the gauge coupling g , see Eq. (151). We will confirm these results with a dedicated numerical analysis below.

3.3 Scan of the parameter space and numerical results

In this section we present our results for a numerical scan of the parameter space, focusing on the regions identified analytically in the previous section. Starting from the full scalar potential (127) and the equation of motion (132), we determine the slow-roll parameters (130) and consequently the inflationary observables (131) at $N_* = 55$ e-folds before the end of inflation. Fixing the charges $|q_0| = 1$ and $|q| = 2$, we for each parameter point in the (κ, g, χ, ξ) plane (i) determine the end-point of inflation, (ii) solve the slow-roll equation of motion and (iii) determine for fixed (κ, g, χ) the value of ξ which reproduces the observed amplitude of the scalar power spectrum. We also explicitly check that our results are not sensitive to the precise choice of the renormalization scale Q_J .

Our results are depicted in Fig. 2, for $\kappa = 0.1$ (left panel) and $\kappa = 10^{-3}$ (right panel), as well as in Fig. 3 where we have imposed the additional relation $\chi = \chi_{1\ell} = \kappa^2/(16\pi^2)$, see Eq. (30). In all figures, the green band indicates the region of parameter space in accordance with all constraints. In the parameter space of interest, we find values for the tensor-to-scalar ratio r of $\mathcal{O}(10^{-6} \dots 10^{-4})$, far below the current bounds. The numerical results for the inflationary observables agree excellently with

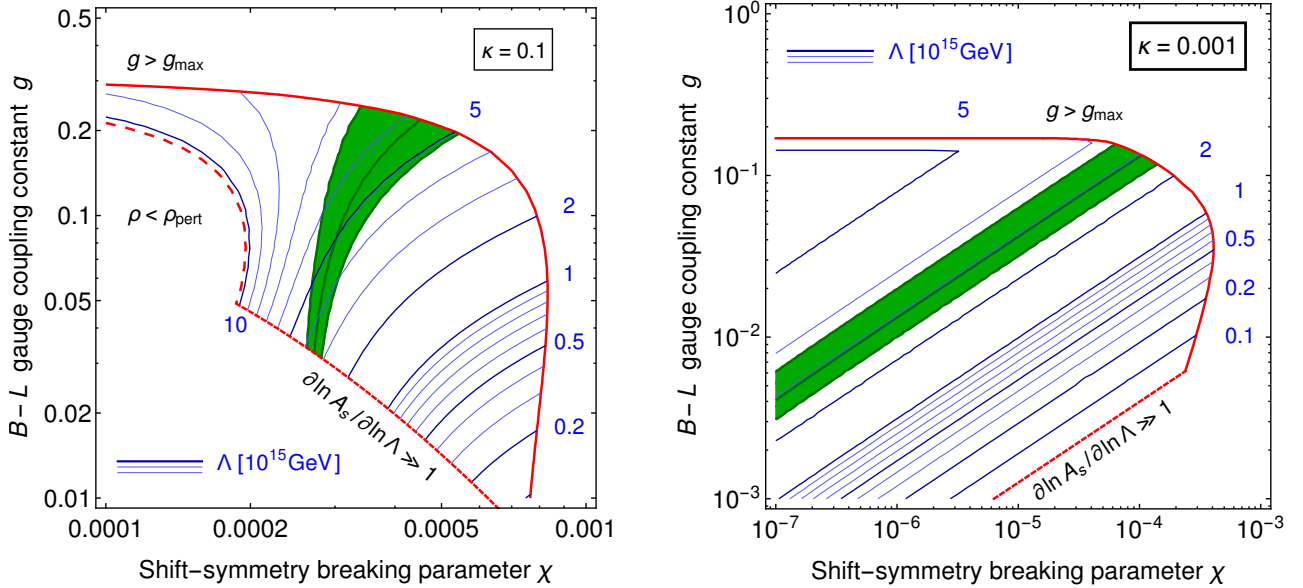


Figure 2: CMB observables and viable parameter space for two representative, fixed values of the superpotential coupling, $\kappa = 0.1$ and $\kappa = 0.001$. The red boundaries show constraints enforcing perturbativity ($\rho > \rho_{\text{pert}}$, see Eq. (57)), the stabilization of the Polyni field ($g < g_{\text{max}}$, see Eq. (72)) and limiting the amount of fine-tuning in the model parameters (quantified by $\partial A_s / \partial \ln \Lambda$, see discussion below Eq. (149)), blue lines indicate contour lines for the dynamical scale Λ which reproduce the observed amplitude of the scalar spectrum. The green band indicates values of the spectral index in agreement at 95% CL with the current data, $n_s = 0.9677 \pm 0.006$ [75].

results obtained from our analytical expressions for the slow-roll parameters, Eq. (145) and Eq. (146), as well as with our estimates for the shift-symmetry-breaking parameter χ in Eqs. (149) and (151). This underlines that although our numerical analysis takes into account all contributions to the scalar potential, the most relevant contribution to lower the spectral index is the shift-symmetry-suppressed soft mass for the inflaton, leading to Eq. (142).

Our choices for the coupling κ are designed to cover the relevant aspects of the parameter space, while focusing on particularly interesting benchmark points. Responsible for explicit shift symmetry breaking in the superpotential, we expect $\kappa \lesssim 1$. In the left panel of Fig. 2, we consider $\kappa = 0.1$. This enables us to reproduce the observed CMB observables (in particular n_s) with loop and SUGRA contributions of comparable size, leading to $\chi \sim 10^{-4}$. In global-SUSY DHI the parameter space splits into two regimes, characterized by the size of $|\sigma_\eta / \sigma_c|$ and consequently by different parameter dependencies of s_* , see Sec. 3.1. The value of $\kappa = 0.1$ falls into the regime of $\sigma_\eta \gg \sigma_c$. In the right panel of Fig. 2 we turn to the opposite regime, $\sigma_\eta \ll \sigma_c$. To reproduce the observed spectral index, we here need to require the SUGRA contributions to clearly dominate over the one-loop contributions. Note that for even smaller values of κ , the critical value σ_c can take super-Planckian values, enabling a phase of ‘sub-critical hybrid inflation’ after the inflation field has passed σ_c [158, 159].

In Fig. 3 we impose $\chi = \chi_{1\ell} = \kappa^2 / (16\pi^2)$ (Eq. (30)), thus reducing the parameter space of our model by one dimension. Interestingly and nontrivially, we find solutions which obey all constraints if $\kappa \sim g = \mathcal{O}(10^{-3})$. Hence the minimal model setup with shift symmetry breaking only through the coupling of the waterfall fields in the superpotential can reproduce the observed CMB observables,

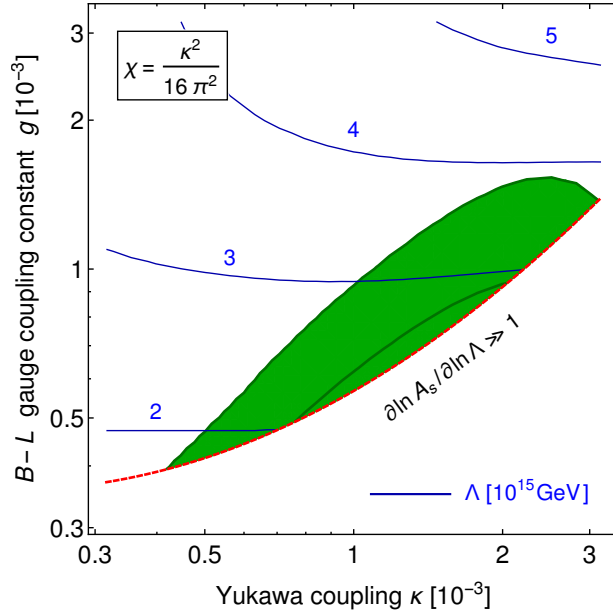


Figure 3: CMB observables and viable parameter space for shift symmetry breaking exclusively through the superpotential coupling of the waterfall fields, $\chi = \chi_{1\ell} = \kappa^2/(16\pi^2)$. Color code as in Fig. 2.

thereby essentially determining all model parameters: the superpotential coupling κ , the gauge coupling g and the mass scale Λ . The value of the gauge coupling g is small compared to the expectation in GUTs, but interestingly, the relation $\kappa \sim g$ is precisely the relation predicted in $N = 2$ supersymmetric hybrid inflation [160].

3.4 Initial conditions

In the viable parameter space, inflation occurs either near a hilltop (i.e., a local maximum in the scalar potential) or near an inflection point, depending on the exact values of χ and g . In Fig. 4 we depict these two possibilities (for $\kappa = 0.1$), together with the decomposition of the total scalar potential into its dominant components. The solid line shows the full scalar potential, the dashed lines with label (i) indicate the following components: (1) leading-order term in the Coleman-Weinberg potential in the global-SUSY limit, (2) supplemented with the leading supergravity terms to the inflaton F-term potential and to the waterfall mass spectrum and (3) in addition supplemented with the next-to-leading order term in the expansion of the Coleman-Weinberg potential (see Eq. (138)), $V_{1\ell}^{J,NLO} = Q_J^4/(8\pi^2)\alpha x \ln(x)$. The latter term becomes relevant as $x(\sigma)$ increases to $x \sim 1/\alpha$. The remaining discrepancy to the full scalar potential (in the left panel) is mainly due to the σ -dependence of the D-term potential in the Einstein frame, induced by the conformal factor.

Implementing inflation in the left panel of Fig. 4 requires some fine-tuning in the initial conditions, to ensure the correct vacuum is reached. However, we point out two further observations: (i) in all the parameter space of interest, we find $H_*/(2\pi) \lll (\sigma_{\max} - \sigma_*)$, i.e., if (by accepting some tuning), the initial conditions are in the desired regime, they are at least stable against quantum fluctuations. (ii) lowering the $B-L$ gauge coupling g , the energy level of the false minimum is raised compared to

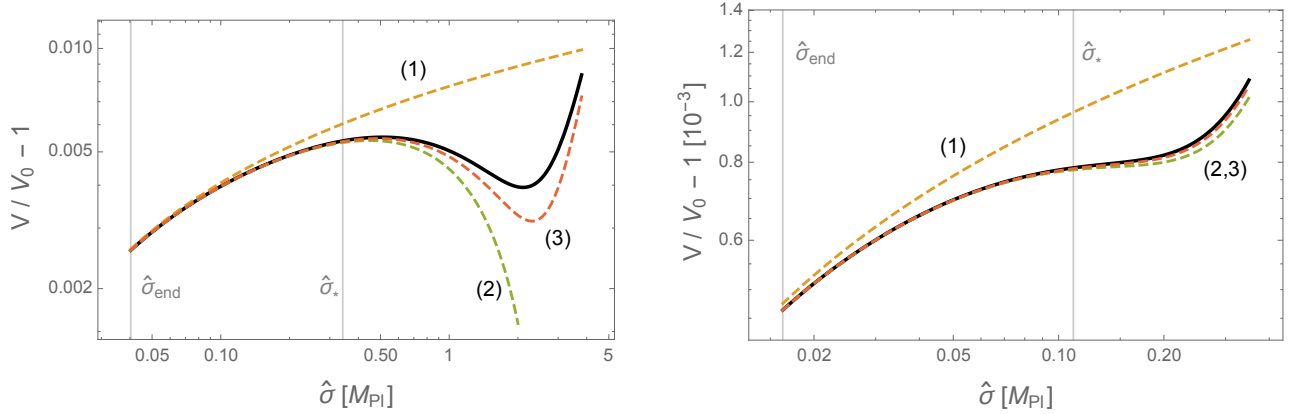


Figure 4: Contributions to the scalar potential (for $\kappa = 0.1$). The total scalar potential is shown in solid black, the dashed curves mark the following contributions: (1) global-SUSY one-loop potential, (2) + leading SUGRA effects, (3) + gravity-induced effects in the one-loop potential. For details see text. The parameter values are chosen as $g = 0.13$, $\chi = 3.5 \times 10^{-4}$, $\xi = 10^{-5} M_{\text{Pl}}^2$ (left panel) and $g = 0.05$, $\chi = 2.8 \times 10^{-4}$, $\xi = 6.3 \times 10^{-6} M_{\text{Pl}}^2$ (right panel).

$V(\sigma_*)$. An interesting (albeit fine-tuned) situation arises if the vacuum energy density of the false minimum lies just a tiny bit above $V(\sigma_*)$, allowing for a phase of eternal inflation, followed by N_* e-folds of inflation arising once the inflaton field tunnels through the potential barrier.

On the other hand, in the right panel of Fig. 4 inflation can start at large field values, avoiding an initial condition problem. There is however some degree of tuning required in the model parameters to ensure this shape of the potential. For $\kappa = 0.1$, this becomes particularly relevant for small values of g , when large SUGRA contributions to the slow-roll parameters need to be carefully balanced. This results in the ‘fine-tuning’ constraint on the parameter space in Fig. 2. An overview of these different regions in parameter space is given in Fig. 5 for the cases of $\kappa = 0.1$ and $\chi = \kappa^2/(16\pi^2)$, in both cases focusing on the region of parameter space which reproduces the correct CMB observables.

Note that for very large field values, $\sigma^2 \sim 3M_{\text{Pl}}^2/\chi \sim 10^4 M_{\text{Pl}}^2$, both the conformal factor \mathcal{C} and the F-term potential exhibit a pole (see Eqs. (149) and (114)):

$$\Omega = 0 \rightarrow (\sigma_{\mathcal{C}}^{\infty})^2 \simeq \frac{1}{\chi}(3M_{\text{Pl}}^2), \quad f = 1 \rightarrow (\sigma_F^{\infty})^2 = \frac{3M_{\text{Pl}}^2}{\chi(1-2\chi)}. \quad (152)$$

After canonical normalization of the inflaton field, the pole in the conformal factor will be pushed to infinity. The pole in the F-Term potential is always at larger field values and is hence never reached.¹⁰ However, for $\chi \ll 1$, σ_F^{∞} approaches $\sigma_{\mathcal{C}}^{\infty}$ and the F-term potential begins to dominate the tree-level potential already for $\sigma < \sigma_{\mathcal{C}}^{\infty}$. This can generate a false, negative valued vacuum at large field values. In the regions of parameter space where the inflaton field reaches values of order M_{Pl} , this can impact the vacuum structure. However at these large field values, $\sigma \gg M_{\text{Pl}}$, higher order operators may significantly modify the scalar potential.

For $\kappa = 10^{-3}$, we find that inflation typically occurs in a small field region in the vicinity of a hilltop, accompanied by a false, often negative-valued vacuum at large field values. The amplitude of this vacuum is lifted as g and χ are decreased, until at values of $g \lesssim 5 \times 10^{-4}$ inflation occurs close

¹⁰The pole in the conformal factor implies that in the field space of the canonically normalized field $\hat{\sigma}$, the scalar potential asymptotes to $\lim_{\hat{\sigma} \rightarrow \infty} V(\hat{\sigma}) = V(\sigma_{\mathcal{C}}^{\infty})$ and is thus always bounded from below.

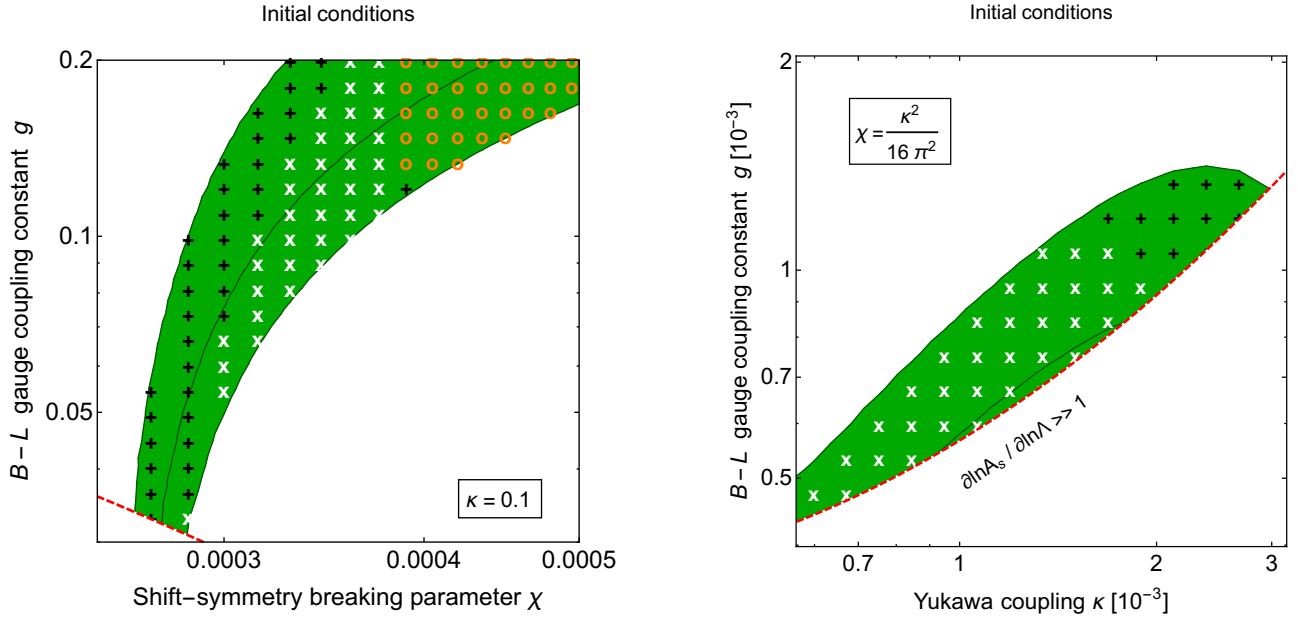


Figure 5: Initial conditions for $\kappa = 0.1$ (**left panel**) and $\chi = \kappa^2/(16\pi^2)$ (**right panel**). The three different possibilities for the structure of the scalar potential are (i) inflection point inflation (black ‘+’-symbol, situation as in the right panel of Fig. 4), (ii) hilltop inflation with a local minimum at $\sigma \gg \sigma_*$ (white ‘x’-symbol, situation as in left panel of Fig. 4) and (iii) hilltop inflation without a local minimum (red ‘o’-symbol). This last situation arises due to the effect described below Eq. (152), and requires tuning the initial conditions. As in Figs. 2 and 3, the green band indicates that the scalar spectral index lies within the 2σ band.

to an inflection point. The shape of the potential is well described by the D-term potential, $\mathcal{C}^4 D_0^2/2$, supplemented by the full globally supersymmetric one-loop potential (not truncated at $\mathcal{O}(1/x)$) and the leading order SUGRA contribution from the F-term potential.

4 Discussion: Particle spectrum and cosmology after inflation

During inflation, supersymmetry is broken through F- and D-term contributions. After inflation, when the D-term is absorbed into the VEV of the waterfall field, only F-term supersymmetry breaking remains. This is communicated to the particles of the MSSM through (i) higher dimensional terms in the Kähler potential (*Planck-scale-mediated supersymmetry breaking*, PMSB) (ii) *anomaly-mediated supersymmetry breaking* (AMSB) and (iii) couplings to the $B-L$ multiplet which receives a supersymmetry breaking mass splitting at tree level (*gauge-mediated supersymmetry breaking*, GMSB), see e.g. [161] for an overview. While PMSB will play a crucial role for the SM squarks and sleptons and for the mass parameters of the Higgs sector, the standard model gauginos will only receive a loop suppressed AMSB contribution. At low energies, the particle spectrum thus resembles the results obtained in pure gravity mediation (PGM) [19, 22–24],¹¹ with the overall scale of the spectrum determined by the inflationary observables (which determine the value of the FI-parameter ξ), see Eqs. (67) and (105). In this section, we discuss the mass spectrum of our model during and after inflation, and discuss consequences for early universe cosmology, including reheating, leptogenesis, dark matter and

¹¹See also Ref. [110] for a related discussion.

the production of topological defects.

4.1 Particle spectrum

Stabilization of squarks and sleptons during and after inflation

The total scalar mass of an MSSM matter field Q_i with gauge charge q_i is given by

$$m_{0,i}^2 = \mathcal{C}^2 \left[-q_i m_D^2 - a_{ii} \Delta m_0^2 + q_i^2 m_{\text{gm}}^2 + m_R^2 \right], \quad (153)$$

where the first term denotes the D-term induced mass present only during inflation, the second term is a tree-level supergravity contribution induced by higher-dimensional operators in the Kähler potential, the third term is the gauge-mediated SUSY breaking contribution and the fourth term is the gravity-induced mass (present only during inflation). Assuming that the MSSM sector couples to the supersymmetry breaking sector via higher-dimensional operators in the Jordan frame (see Eq. (18)),

$$\Omega \supset X^\dagger X + Q_i^\dagger Q_i + \frac{a_{ii}}{M_*^2} Q_i^\dagger Q_i X^\dagger X + \mathcal{O}(M_*^{-4}), \quad (154)$$

yields

$$V_F^J \supset -a_{ii} \frac{\mu^4}{M_*^2} |\tilde{q}_i|^2 = -3 a_{ii} \frac{m_{3/2}^2 M_{\text{Pl}}^2}{M_*^2} |\tilde{q}_i|^2, \quad (155)$$

and hence $\Delta m_0^2 = 3 m_{3/2}^2 M_{\text{Pl}}^2 / M_*^2$. The quantities m_D and m_R have been introduced in Eqs. (8) and Eq. (25), respectively. m_{gm} denotes the mass contribution obtained through gauge mediation, with the dominant (one-loop) effect arising due to the mass splitting within the $B-L$ gauge multiplet [156]

$$m_{\text{gm}}^2 \simeq \frac{g^2}{32\pi^2} m_V^2 \ln \left(\frac{m_c^2 m_V^6}{m_a^8} \right), \quad (156)$$

with m_V , m_c and m_a given in section 2.3. This contribution is clearly sub dominant compared to the tree-level D-term contribution during inflation. The stabilization of the MSSM scalars during inflation ($m_{0,i}^2 \gg H^2$) requires $a_{ii} < 0$ and

$$|a_{ii}| \Delta m_0^2 \gg q_i m_D^2 - q_i^2 m_{\text{gm}}^2 - H_J^2 \simeq q_i m_D^2 \quad (157)$$

which for $|q_i| \simeq |q_0| \simeq |a_{ii}| \simeq 1$ implies

$$M_* \ll \frac{\sqrt{3} m_{3/2} M_P}{m_D} \sim 5 \times 10^{16} \text{ GeV} \left(\frac{0.1}{g} \right), \quad (158)$$

a value close to the dynamical scale Λ .

After the end of inflation, only the second and third term in Eq. (153) remain, leading to very heavy MSSM squarks and sleptons,

$$m_{0,i} \simeq (-a_{ii})^{1/2} \Delta m_0 > 10^{14} \text{ GeV} \left(\frac{g}{0.1} \right) \left(\frac{\sqrt{\xi}}{10^{15} \text{ GeV}} \right). \quad (159)$$

MSSM gauginos

Similar to the squarks and sleptons of the previous subsection, the μ and B parameters of the MSSM receive tree-level supergravity contributions. Consequently, the heavy Higgs scalars and the higgsinos obtain masses of $\mathcal{O}(m_{3/2})$. For the MSSM gauginos on the other hand tree-level supergravity contributions are strongly suppressed (since our supersymmetry breaking field X is not a total singlet of the SM) [19, 22–24]. The dominant contributions are thus obtained at one loop through anomaly mediation and (in the case of binos and winos) through higgsino threshold effects. As detailed in Ref. [24] in the context of PGM, these are generically both of the same order ($\sim g_a^2 m_{3/2}/(16\pi^2)$), where g_a is the respective SM gauge coupling. Depending on the size of the higgsino threshold effects, either the wino or the bino can take the place of the lightest neutral MSSM particle¹² – and hence of the dark matter candidate. In the following we will focus on the case where the higgsino threshold contributions do not dominated over the AMSB contribution, rendering the wino the lightest supersymmetric particle (LSP). The motivation for this is two-fold. Firstly, this is the more likely scenario in PGM [24]. Secondly, due to its smaller annihilation cross section, a thermal bino LSP population with $m_{\tilde{b}} \gtrsim 300$ GeV leads to the overproduction of dark matter [162, 163]. In combination with the bounds set by CMS [2] and ATLAS [1], this excludes a thermal bino as a viable dark matter candidate.

A particularly interesting situation arises if the two contributions to the wino mass are tuned to very similar values, leading to a cancellation of these two terms and hence to a wino mass which can be arranged to be much lighter than its generic mass scale $m_{3/2}/(16\pi^2)$. For example, in the notation of Ref. [24] this is achieved for $-\mu_H \simeq -2B \simeq m_{3/2}$ (for $\tan\beta = v_u/v_d \simeq 1$). Such a fine tuning might be justified from the anthropological requirement of dark matter, see Sec. 4.3. Additional contributions to the gaugino masses may arise from threshold and anomaly-mediated corrections from heavy vector matter multiplets charged under $SU(2)_L$ and/or threshold corrections from the F terms of flat directions in KSVZ-type axion models [164]. In this case, these contributions would also play a role in tuning the wino mass.

Particles beyond the MSSM

The masses of all remaining degrees of freedom are set by the dynamical scale Λ , effectively decoupling these particles from low energy physics. The $B-L$ gauge multiplet features a tree-level mass splitting due to its direct coupling to the supersymmetry breaking sector, as discussed towards the end of Sec. 2.3. All degrees of freedom of the gauge multiplet obtain large masses of order m_F or m_V , except for the $B-L$ gaugino whose mass is suppressed by $\langle X \rangle/v_A$. We note that as for the MSSM gauginos, the latter will obtain an additional loop-suppressed AMSB mass.

Turning to the supersymmetry breaking sector, the only degree of freedom which is present in the low-energy effective theory of the IYIT model is the pseudomodulus X , which acts as the Polonyi field of SUSY breaking, see Sec. 2.4. The dominant mass contribution after the end of inflation arises from its one-loop effective potential,

$$m_X \simeq 0.02 \lambda^2 \Lambda \sim 10^{14} \text{ GeV}. \quad (160)$$

¹²Due to their larger gauge coupling at low energy scales, the gluinos are typically significantly heavier.

The masses of the scalar fields of the inflation sector can be obtained from the scalar potential in Eq. (127). For $q/(q_0\xi) > 0$ the field ϕ obtains a VEV of $\langle|\phi|^2\rangle = q_0/q\xi$ after the end of inflation.¹³ In this vacuum, the masses of the scalar degrees of freedom are given as

$$m_\phi = m_s = 10^{14} \text{ GeV} \left(\frac{q_0}{q}\right)^{1/2} \left(\frac{\kappa}{0.1}\right) \left(\frac{\sqrt{\xi}}{10^{15} \text{ GeV}}\right), \quad (161)$$

$$m_{|\phi|} = 10^{14} \text{ GeV} (q_0 q)^{1/2} \left(\frac{g}{0.1}\right) \left(\frac{\sqrt{\xi}}{10^{15} \text{ GeV}}\right), \quad (162)$$

where $m_{|\phi|}$ denotes the mass of the radial degree of freedom of ϕ in the true vacuum. The fermionic degrees contained in S and $\bar{\Phi}$ form a Dirac spinor with a mass term $W_{\bar{\phi}s} = \kappa\langle\phi\rangle$. If the IYIT sector is fully sequestered from the inflaton sector, the angular degree of freedom of ϕ and the fermion $\tilde{\phi}$ remain massless. The reason for this is that although $B-L$ is spontaneously broken by $\langle m_\pm \rangle \neq 0$, there is a remaining accidental global $U(1)$ symmetry in the superpotential, associated with $\phi \mapsto \exp(i\alpha)\phi$, $\bar{\phi} \mapsto \exp(-i\alpha)\bar{\phi}$. This global symmetry is spontaneously broken at the end of inflation, when ϕ acquires a VEV. The angular degree of freedom of ϕ is the Goldstone boson of this spontaneously broken symmetry. In the true vacuum after the end of inflation D-term supersymmetry breaking is absent, and assuming a full sequestering between the IYIT sector and the inflation sector, the F-term supersymmetry breaking contained in the IYIT sector is not communicated to the Φ multiplet. The fermionic degree $\tilde{\phi}$ is consequently massless, too. The spontaneous breaking of an $U(1)$ symmetry at the end of inflation would lead to the formation of cosmic strings (see Sec. 4.4), in contradiction with observations. The discussion above however immediately reveals how to resolve this issue: if we drop the assumption of a complete sequestering between the IYIT and the inflaton sector, both $B-L$ breaking and supersymmetry breaking can be communicated to the Φ multiplet, rendering all its degrees of freedom massive. In Sec. 4.4 we will achieve this by introducing higher dimensional operators in the Kähler potential coupling Φ to Z_- and/or M_- . These operators will come with small coefficients (respecting the level of sequestering necessary prevent the waterfall fields from obtaining too large masses) and will explicitly break the global $U(1)$ symmetry (in agreement with general arguments that no exact global symmetries should exist in any theory of quantum gravity [88]). As we will see below, this leads to masses for the angular degree of freedom of ϕ and for $\tilde{\phi}$ of the order of the Hubble parameter.

Note that this situation is crucially different than in standard DHI, where the VEV of the waterfall field ϕ spontaneously breaks a local $U(1)$ symmetry at the end of inflation, triggering the super-Higgs-mechanism: the angular degree of freedom is ‘eaten’ by the $U(1)$ gauge boson, providing the longitudinal degree of freedom for the massive vector field while $\tilde{\phi}$ forms a Dirac fermion with the $U(1)$ gaugino. In our case however, the $U(1)_{B-L}$ multiplet is already massive, having absorbed the corresponding degrees of freedom from the meson multiplets.

4.2 The cosmology of a $B-L$ phase transition

D-term hybrid inflation ends in a phase transition in which the waterfall field ϕ , charged under $B-L$, obtains a vacuum expectation value. Assigning $B-L$ charge $q = -2$ to Φ , it can couple to

¹³If q and $q_0\xi$ have opposite signs, the roles of ϕ and $\bar{\phi}$ are inverted.

the right-handed neutrinos N_i (which carry $B-L$ charge $+1$) in the seesaw extension of the MSSM, $W \supset h_{ij}/2\Phi N_i N_j$. In fact, when gauging $B-L$, the introduction of three right-handed neutrinos is the simplest way to ensure anomaly cancellation. Once the waterfall field ϕ obtains a VEV, this generates the Majorana mass matrix for the right-handed neutrinos, $M_{ij} = h_{ij}\langle\phi\rangle$.

A very similar cosmological phase transition was studied in the case of F-term hybrid inflation in Refs. [61–63,67]. It was shown that this phase transition can set the initial conditions for the hot early universe: With the energy initially stored in oscillations of the waterfall field (as well as in degrees of freedom created in tachyonic preheating), this energy is transferred to the thermal bath through the decay into right-handed neutrinos (which obtain their mass from the coupling to $B-L$ breaking waterfall field). In the course of this process, both thermal and nonthermal processes generate a lepton asymmetry, which, after conversion into a baryon asymmetry through sphaleron processes, can explain the baryon asymmetry observed today. Using a coupled set of Boltzmann equations, Refs. [61–63,67] provide a time-resolved picture of the entire reheating and leptogenesis process.

We expect this overall picture to hold also in our model. There are however a few differences in the details of the phase transition. Contrary to [61–63,67], in the DHI model presented here (i) $B-L$ is broken already during inflation, (ii) there is a tree-level mass splitting in the $B-L$ multiplet, (iii) supersymmetry is broken in the true vacuum with $m_{3/2} \sim 10^{12} \dots 10^{13}$ GeV (iv) there is an additional chiral multiplet in the waterfall sector¹⁴, which in the analysis of [63] plays the role of the $B-L$ Goldstone multiplet and (v) we allow here for smaller values of the $B-L$ gauge coupling. Consequently, no (local) cosmic strings are formed at the end of inflation, the $B-L$ multiplet is not produced in tachyonic preheating and the gravitino is too heavy to be a dark matter candidate as in [63]. Hence while we expect the same sequence of events as in [61–63,67], leading to successful leptogenesis for a mass of the lightest right-handed neutrino above about 10^{10} GeV and a reheating temperature of about $T_{RH} \gtrsim 10^8$ GeV, the above mentioned differences require a detailed study to verify these expectations. This is beyond the scope of the current paper.

4.3 Particle candidates for dark matter

The high reheating temperature expected in our model (see above) implies an abundant production of gravitinos [165]. Since these gravitinos are very heavy, their decay temperature

$$T_{3/2} \simeq 1.5 \times 10^8 \text{ GeV} \left(\frac{g_*(T_{RH})}{80} \right)^{-1/4} \left(\frac{m_{3/2}}{10^{12} \text{ GeV}} \right)^{3/2}, \quad (163)$$

is much larger than the temperature of BBN (\sim MeV). The gravitinos will thus decay into MSSM gauginos (the lightest particles in our MSSM spectrum) before the onset of BBN, a well known solution to the classical gravitino problem [27,166,167]. If one of the gauginos (in our setup the wino, see Sec. 4.1) is sufficiently light, so that its freeze-out temperature, $T_f \sim m_{\tilde{w}}/28$, is lower than the gravitino decay temperature $T_{3/2}$, then its relic abundance will be set by the usual thermal

¹⁴The light degrees of freedom in the additional chiral multiplet in the waterfall sector have a decay rate into right-handed neutrinos of $\Gamma \simeq h^2/(4\pi)H^2 = \mathcal{O}(\text{GeV})$ for typical values of the Yukawa coupling of $h \simeq 10^{-5}$. They thus decay into the SM thermal bath before the onset of BBN and do not create any cosmological problems.

freeze-out contribution.¹⁵ This occurs for $m_{\tilde{w}} \lesssim 4 \times 10^9 \text{ GeV} (m_{3/2}/(10^{12} \text{ GeV}))^{3/2}$, with the correct relic density obtained for $m_{\tilde{w}} \simeq 2.7 \text{ TeV}$ [170, 171]. This value is much smaller than the generic gaugino mass scale $m_{3/2}/(16\pi^2)$, but may be achieved by fine tuning the anomaly mediation and higgsino threshold corrections (see Sec. 4.1). Without such fine tuning, the strongly enhanced LSP abundance would lead to an overclosure of the Universe. Such a fine tuning may therefore be justified by anthropological arguments. Alternatively, one can take the gauginos to be at their natural scale $m_{3/2}/(16\pi^2)$ and invoke R-parity breaking to ensure a sufficiently fast decay of the LSP into the SM degrees of freedom [172]. In this case, the question of the nature of dark matter candidate remains open and may be addressed e.g. by the QCD axion.

4.4 Topological defects

In standard DHI, the angular degree of freedom of the waterfall field ϕ is massless, protected by the $U(1)$ gauge symmetry of DHI. Consequently, cosmic strings are formed at the end of standard DHI. This is known as the cosmic string problem of DHI, since the nonobservation of cosmic strings in the CMB [101], together with constraints on the spectral index, essentially exclude the entire parameter space. The setup we propose here is crucially different. The $U(1)_{B-L}$ symmetry is already broken during inflation by the meson VEVs $\langle m_{\pm} \rangle \neq 0$, and no local cosmic strings are formed at the end of inflation. The angular degree of ϕ merely exhibits an accidental global symmetry which is not expected to be exact, see Sec. 4.1. We can express this by adding higher dimensional operators¹⁶ in the Kähler potential of the type $M_{\text{Pl}} K \supset \epsilon_{ZZ}^K Z_-^2 \Phi$, $\epsilon_{MM}^K M_-^2 \Phi$, $\epsilon_{MZ}^K M_- Z_- \Phi$, all supplemented by their complex conjugate. Here the parameters ϵ_{IJ}^K are expected to be exponentially small, respecting the sequestering between the inflation and the IYIT sector. By means of a Kähler transformation these holomorphic terms can be equivalently considered as terms in the superpotential, $W \supset W_0 \epsilon_{ZZ}^K Z_-^2 \Phi / M_{\text{Pl}}^3$, etc. Taking into account the vacuum expectation values for the scalar and auxiliary (F-term) components in $Z_{\pm}, M_{\pm}, \bar{\Phi}, \Phi$ and S , this leads to linear terms in the scalar potential for the waterfall fields. Schematically,

$$V = V_0 - c(\phi + \phi^*) + \tilde{m}^2 |\phi|^2 + \frac{\tilde{\lambda}}{4} |\phi|^4, \quad (164)$$

with $\tilde{\lambda} = 2g^2 q^2$ denoting the self-coupling of the waterfall field, \tilde{m}^2 its (inflaton-dependent mass) and $c \sim \epsilon_{IJ}^K \Lambda^3 m_{3/2} / M_{\text{Pl}}$ determined by the higher dimensional operators mentioned above.

To study cosmic string formation,¹⁷ we consider the system close to the end of inflation, just when Eq. (164) develops a local maximum. At this point, the local minimum of the potential is given by $|\phi| = 2(c/\tilde{\lambda})^{1/3}$. The phase of the local minimum is set by the phase of c and we will take it to be zero in the following. The mass of the canonically normalized radial degree of freedom α in this local

¹⁵On the other hand, if $T_f > T_{3/2}$ the LSP abundance will be dominated by the nonthermal contribution from gravitino decay. The gravitino abundance in turn receives contributions from thermal production, production from the decay of the Polonyi field and production through oscillations of a field in the inflaton sector [165]. In particular the thermal production [168] and the decay of ϕ to two gravitinos through a supergravity coupling present when $\langle K_{\phi} \rangle \simeq \langle \phi \rangle \neq 0$ [169] yield large gravitino abundances and thus overclose the universe for the the large LSP masses consistent with $T_f > T_{3/2}$.

¹⁶Here we have assumed $q_0 = -1$. Similar terms (involving also the inflaton field) can be written down for $q_0 = -2$.

¹⁷We thank the authors of Ref. [55] for very helpful discussions on this point.

minimum is given by $m_\alpha^2 = \frac{1}{2}(c^2\tilde{\lambda})^{1/3}$.

To avoid the production of cosmic strings, we require that quantum fluctuations of the angular degree of freedom (see e.g. [173]) cannot overcome the barrier at $\alpha/(\sqrt{2}\langle\phi\rangle) = \pi$, i.e.,

$$\langle\delta a^2\rangle = \frac{H}{3m_\alpha} \left(\frac{H}{2\pi}\right)^2 \ll 2\langle\phi\rangle^2\pi^2. \quad (165)$$

This leads to

$$c^{1/3} \gg 0.05 \tilde{\lambda}^{1/6} H, \quad (166)$$

In this paper, we will consider

$$\tilde{c} \equiv c/H^3 \gtrsim 1, \quad (167)$$

safely satisfying Eq. (166) but also ensuring that the fluctuations in the radial direction are small compared to the position of the local minimum and that the decay rate of angular component α in the true vacuum is not significantly smaller than the decay rate of the radial component. For the couplings in the Kähler and/or superpotential, this implies

$$\epsilon_{IJ}^K \gtrsim \left(\frac{H}{\Lambda}\right)^3 \sim \left(\frac{g\Lambda}{M_{\text{Pl}}}\right)^3 \sim g^3 10^{-9}, \quad W_0 \epsilon_{IJ}^K/M_{\text{Pl}}^3 \sim \epsilon_{IJ}^K \left(\frac{m_{3/2}}{M_{\text{Pl}}}\right) \sim g^3 10^{-16}, \quad (168)$$

in good agreement with our sequestering ansatz.

However, scenarios with a richer phenomenology are possible. For example, imagine that a term such as $K \supset \Phi Z_- Z_-/M_{\text{Pl}}$ is forbidden by an additional discrete symmetry, which in turn is explicitly broken by Planck suppressed operators of even higher dimension. If this explicit breaking is of a suitable size, unstable domain walls will form [174–176]. A similar situation has been discussed for the QCD axion [177, 178], see also [179–181]. The decaying domain walls will emit energy in the form of gravitational waves. The resulting gravitational wave spectrum depends mainly on two parameters, the tension σ of the domain walls and their annihilation temperature T_{ann} . For the high energy scales present in our model, the resulting stochastic gravitational wave background might be within the sensitivity reach of upcoming advanced LIGO runs [182, 183], depending on the details of the discrete symmetry (breaking).

5 Conclusions: A unified model of the early Universe

In this paper, we constructed a phenomenologically viable SUGRA model of hybrid inflation in which reheating proceeds via the $B-L$ phase transition. We focused on the case of D-term inflation to avoid the notorious complications associated with the inflaton tadpole term in F-term inflation (see Eq. (3)). This tadpole term turns F-term inflation into a two-field model, potentially spoils the slow-roll motion of the inflaton field, and creates a false vacuum at large field values. D-term inflation does, by contrast, not involve any inflaton tadpole term, which prevents one from running into these problems.

The first part of our paper contains the details of our model-building effort (see Sec. 2). To meet all theoretical and phenomenological constraints, our model combines the following three features:

(i) The vacuum energy driving D-term inflation is provided by a *Fayet-Iliopoulos* (FI) D term. We assume that this D term is dynamically generated in the hidden SUSY-breaking sector [96].

Our construction involves two steps. First, we suppose that SUSY breaking in the hidden sector is accomplished by the dynamics of a strongly coupled supersymmetric gauge theory. To be specific, we employ the *Izawa-Yanagida-Intriligator-Thomas* (IYIT) model [144,145], which represents the simplest vector-like model of dynamical SUSY breaking. Thanks to the strong interactions in the IYIT sector, our model does not require any hard dimensionful input scales. All mass scales (including the SUSY breaking scale itself) turn out to be related to the dynamical scale in the IYIT sector, Λ_{dyn} . The dynamical scale Λ_{dyn} is in turn generated via the quantum effect of dimensional transmutation, just like the confinement scale of QCD. The second step in our construction consists in promoting a global axial $U(1)_A$ flavor symmetry in the IYIT sector to a weakly gauged local $U(1)_{B-L}$ symmetry. The SUSY-breaking dynamics in the IYIT sector then result in an effective FI parameter ξ that is determined by the vacuum expectation values of certain moduli in the effective theory at low energies.

Our dynamically generated FI term has a number of interesting properties. (1) Being an effective field-dependent FI parameter, it can be consistently coupled to supergravity. In this sense, it differs from genuinely constant FI parameters whose coupling to supergravity always requires an exact global continuous symmetry. (2) The generation of field-dependent FI parameters typically results in dangerous flat directions in the scalar potential. In our case, all moduli are, however, automatically stabilized by a large mass term in the superpotential that is induced by the SUSY-breaking F term. (3) The generation of effective FI parameters is always accompanied by the spontaneous breaking of the underlying Abelian gauge symmetry. This is also the case in our model where the generation of ξ spontaneously breaks $B-L$ in the IYIT sector. We use this fact to our advantage and communicate the breaking of $B-L$ to the visible sector via marginal couplings in the superpotential. This allows us to prevent the formation of dangerous cosmic strings during the $B-L$ phase transition at the end of inflation. (4) The magnitude of the FI parameter and, hence, the energy scale of inflation are related to the SUSY breaking scale. This unifies the dynamics of inflation and SUSY breaking. The energy scales of both phenomena derive from the dynamical scale, $\Lambda_{\text{dyn}} = e^{-S_{\text{inst}}/b_{\text{hid}}} M_{\text{Pl}}$, which is generated via nonperturbative dynamics in the infrared.¹⁸ This explains the exponential hierarchy between the energy scales of inflation and SUSY breaking on the one hand and the Planck scale on the other hand.

(ii) We assume that the natural SUGRA description of our model corresponds to an embedding into the standard Jordan frame with canonically normalized kinetic terms for all complex scalar fields. From the Einstein-frame perspective, this corresponds to a noncanonical Kähler geometry based on a Kähler potential of the sequestering type. This sequestering structure allows us to control the soft masses in the visible MSSM sector independently of the corresponding soft masses in the inflation sector. In fact, thanks to our choice of the Kähler potential, the inflation sector sequesters from the IYIT sector such that none of the fields in the inflation sector obtains a large soft mass. This is a crucial requirement for a successful $B-L$ phase transition. Otherwise, i.e., without sequestering, large soft masses in the inflation sector would keep the waterfall fields stabilized at the origin and, thus, remove the tachyonic instability in the scalar potential. At the same time, we introduce a higher-dimensional coupling between the visible MSSM sector and the IYIT sector in the Kähler potential

¹⁸Here, $S_{\text{inst}} = 8\pi^2/g_{\text{hid}}^2$ denotes the nonperturbative instanton action in the IYIT sector (see Eq. (6)). g_{hid} and b_{hid} stand for the gauge coupling constant and the beta function coefficient of the IYIT gauge group, respectively.

to stabilize all MSSM sfermions during and after inflation. Again, this is an important ingredient of our model. Without any extra stabilization mechanism, the MSSM sfermions would destabilize the FI term in the D-term scalar potential and inflation would prematurely end in the wrong vacuum. For the purposes of this paper, we do not specify the high-energy origin of the additional coupling between the visible MSSM sector and the IYIT sector in the Kähler potential. However, it would be interesting to study different scenarios for the possible origin of these operators in future work.

We caution that one should not attribute too much meaning to our choice to work in Jordan-frame supergravity. The formulation of our model in the language of Jordan-frame supergravity should rather be regarded as a placeholder for a hypothetical completion of our model at high energies. Possible candidates for an ultraviolet completion of our model that feature an appropriate Kähler geometry include models of extra dimensions, strongly coupled conformal field theories, no-scale supergravity, and string theory. Again, any further speculations into this direction are left for future work.

(iii) Our third and final assumption consists in an approximate shift symmetry in the direction of the inflaton field in the Kähler potential. Such an approximate shift symmetry is a popular tool in many SUGRA models of inflation. As usual, it helps us to suppress dangerously large SUGRA corrections to the inflaton mass and, hence, solve the SUGRA eta problem. In our case, the most dangerous such correction, $m_R^2 = R_J/6$, stems from the nonminimal coupling between the inflaton field to the Ricci scalar in the Jordan frame, R_J . This effect can be completely suppressed by an exact shift symmetry — which is, however, not feasible in our model, since the superpotential of D-term inflation inherently breaks any shift symmetry. But this is not a problem. As we are able to show, also an approximate shift symmetry manages to adequately suppress all dangerous SUGRA corrections. On top of that, we can use the fact that the inflaton shift symmetry must be slightly broken to adjust our prediction for the scalar spectral index n_s . The amount of shift symmetry breaking in the Kähler potential is quantified by a parameter χ . By choosing this additional parameter appropriately, we can reach agreement between our prediction for n_s and the current best-fit value reported by PLANCK. Here, an interesting special case arises if χ is zero at tree level and only radiatively generated because of the shift-symmetry-breaking Yukawa coupling in the superpotential, $\chi = \chi_{1\ell} = \kappa^2 / (16\pi^2)$. We are able to demonstrate that even this minimal scenario allows to successfully reproduce the CMB data. In this case, the constraints $A_s \simeq A_s^{\text{obs}}$ and $n_s \simeq n_s^{\text{obs}}$ fix all free parameters of our model (see Fig. 3),

$$\Lambda \sim 3 \times 10^{15} \text{ GeV}, \quad \kappa \sim 10^{-3}, \quad g \sim 10^{-3}, \quad \chi_{1\ell} \sim 10^{-8}. \quad (169)$$

In summary, we conclude that the above three assumptions allow us to solve five problems of $B-L$ D-term inflation: (i) Our FI term can be consistently coupled to supergravity; (ii) we avoid the formation of cosmic strings at the end of inflation; (iii) all MSSM sfermions are sufficiently stabilized during and after inflation; (iv) we do not encounter any SUGRA eta problem; and (v) our prediction for n_s is in agreement with the PLANCK data. This is a highly nontrivial success of our model.

A further outcome of our model is a unified picture of the early Universe (see Secs. 3 and 4). Provided that we include the right couplings in the superpotential, the $B-L$ phase transition at the end of inflation generates large Majorana masses for a number of right-handed neutrinos. This sets the stage for baryogenesis via leptogenesis as well as for the generation of small standard model neutrino

masses via the seesaw mechanism. In the end, our model therefore unifies the scales of dynamical SUSY breaking, inflation, and spontaneous $B-L$ breaking. All of these scales derive from the dynamical scale $\Lambda_{\text{dyn}} = 4\pi\Lambda$ in the IYIT sector. We also find that, in order to reproduce the amplitude of the scalar power spectrum, the reduced dynamical scale Λ must take a value close to the GUT scale,

$$\Lambda_{\text{SUSY}} \sim \Lambda_{\text{inf}} \sim \Lambda_{B-L} \sim \Lambda \sim 5 \times 10^{15} \text{ GeV} \sim \Lambda_{\text{GUT}}. \quad (170)$$

This is another highly nontrivial result of our analysis. Before confronting our model with the experimental CMB data, we did not need to make any assumption about the numerical value of Λ . All of the above scales only become fixed once we require that our model yields the correct value for the scalar spectral amplitude. This leads to the interesting physical question which scale in Eq. (170) actually corresponds to a fundamental scale and which scale is only a derived quantity. Is there, e.g., an anthropic reason for the observed scalar spectral amplitude which then determines the SUSY breaking scale? Or is the SUSY breaking scale rather determined by the scale of R symmetry breaking in the superpotential and the requirement of a nearly vanishing cosmological constant? Or should one instead regard the GUT scale as the most fundamental scale which then fixes all other scales? All of these questions are beyond the scope of this work. But we feel that our model provides an interesting starting point for further studies in this direction. An important task would especially be to embed our model into a full-fledged GUT scenario that explains the occurrence of the GUT scale in Eq. (170).

A central prediction of our model is that supersymmetry is broken at a high energy scale. The naturalness of the electroweak scale is therefore lost. This sacrifice is, however, compensated for by the unification of the dynamics of SUSY breaking and inflation. One of our key messages therefore is that pushing the SUSY breaking scale to very high values is not necessarily just a loss. A high SUSY breaking scale also represents an opportunity for novel ideas such as those presented in this paper. In the end, supersymmetry might play a different role in nature than previously expected. Following the arguments presented in this paper, it is conceivable that supersymmetry's actual purpose is not to ensure the stability of the electroweak scale, but to provide the right conditions for successful inflation!

In this paper, we only touched upon the implications of a high SUSY breaking scale for the particle spectrum of the MSSM and more work in this direction is certainly needed. In particular, one should re-evaluate in more detail how the running of the standard model coupling constants can be matched with the coupling constants in the MSSM provided that supersymmetry is broken at energies close to the GUT scale. This matching of the low-energy parameters with their counterparts at high energies is sensitive to important experimental input data, such as the top quark mass m_t and the strong coupling constant α_s . Given the current experimental uncertainty in these observables, we expect that it should actually not pose any problem to successfully match the standard model to our high-scale scenario. On top of that, large threshold corrections because of nonuniversal soft masses at high energies may help us to achieve a successful matching (see [184] for a recent analysis). In fact, given our treatment of the MSSM soft masses (see Eq. (153)), large nondegeneracies in the sparticle mass spectrum at high energies are quite likely. Moreover, one should re-evaluate in more detail under which conditions our high-scale scenario is compatible with the idea of gauge coupling unification. Again, such an analysis would be sensitive to the experimental input data at low energies. In addition, it would also depend on

the details of the anticipated unification scenario. We are, however, confident on general grounds that it should be feasible to realize gauge coupling unification in our model. After all, unification is also possible in entirely nonsupersymmetric scenarios. We therefore expect that supersymmetry, despite the large value of its breaking scale, will only help in achieving gauge coupling unification [185].

In conclusion, we find that our model provides a consistent cosmological scenario that unifies five different phenomena: (i) dynamical supersymmetry breaking at a high energy scale, (ii) viable D-term hybrid inflation in supergravity, (iii) spontaneous $B-L$ breaking at the GUT scale, (iv) baryogenesis via leptogenesis, and (v) standard model neutrino masses due to the type-I seesaw mechanism. Our model is built around a strongly coupled hidden sector, which puts it on a sound theoretical footing. We do not need to make any *ad hoc* assumptions about the dimensionful parameters in our model. Instead, all important mass scales are related to the dynamical scale of the strong interactions in the hidden sector. Thanks to its precise parameter relations, our model is therefore well suited to be used as a basis for further explicit calculations. It would, e.g., be worthwhile to study the reheating process after inflation in greater detail and determine the corresponding implications for the spectrum of gravitational waves. Similarly, a more comprehensive study of the MSSM particle spectrum and its consequences for dark matter would be desirable. The analysis in the present paper should only be regarded as a first step. It served the purpose to illustrate our main point: *the fact that SUSY breaking close to the GUT scale might be the key to a unified picture of particle physics and cosmology.* This is a fascinating observation and we are excited to see where it will lead us in the future. One possibility is that it will eventually cause a paradigm shift in our understanding of SUSY's role in the physics of the early Universe. High-scale SUSY breaking might be the driving force behind inflation!

Acknowledgements

The authors wish to thank T. T. Yanagida for inspiring discussions at Kavli IPMU at the University of Tokyo in the early stages of this project in 2014. The authors are grateful to W. Buchmüller, J. Evans, B. v. Harling, M. Peloso and L. Witkowski for helpful remarks and discussions at various stages of this project. This project has received funding from the European Union's Horizon 2020 research and innovation programme under the Marie Skłodowska-Curie grant agreement No. 674896 (K. S.).

A Technicalities: Supergravity in the Einstein/Jordan frame

Our model is based on a particular embedding into supergravity. We assume that the coupling to gravity is most naturally described in a Jordan frame where all scalar kinetic terms are canonically normalized (see Sec. 2). At the same time, we wish to perform a standard slow-roll analysis of the inflationary dynamics (see Sec. 3), which requires a reformulation of our model in the Einstein frame. To facilitate the transition between these two different frames, this appendix provides a dictionary that allows one to translate back and forth between the two different formulations of our model.

A.1 Bosonic action

In the usual Einstein frame, the purely bosonic action of our model takes the following form,¹⁹

$$S_{\text{bos}} = \int d^4x \sqrt{-g} \left[\frac{1}{2} M_{\text{Pl}}^2 R - \mathcal{K}_{\bar{i}j} g^{\mu\nu} D_\mu \phi_i^* D_\nu \phi_j - \frac{1}{4} F_{\mu\nu} F^{\mu\nu} - V \right]. \quad (171)$$

Here, M_{Pl} denotes the reduced Planck Mass, $M_{\text{Pl}} \simeq 2.44 \times 10^{18}$ GeV; g is the determinant of the Einstein-frame spacetime metric $g_{\mu\nu}$; R is the Ricci scalar constructed from $g_{\mu\nu}$; $g^{\mu\nu}$ stands for the inverse of the metric $g_{\mu\nu}$; the fields ϕ_i represent the complex scalar fields in our model; D_μ denotes the usual gauge-covariant derivative; $F_{\mu\nu}$ is the field strength tensor of the Abelian B - L vector field; and V represents the total scalar potential in the Einstein frame. As evident from Eq. (171), the scalar fields ϕ_i couple to gravity only via the inverse spacetime metric $g^{\mu\nu}$. This corresponds to the case of minimal coupling. At the same time, the scalar fields exhibit a nontrivial (Kähler) geometry in field space. This is accounted for by the Kähler metric \mathcal{K} which multiplies the scalar kinetic terms in Eq. (171). The Kähler metric \mathcal{K} is defined as the Hessian of the real-valued Kähler potential K ,

$$\mathcal{K}_{\bar{i}j} = \frac{\partial^2 K}{\partial \phi_i^* \partial \phi_j}. \quad (172)$$

In our model, the Kähler potential K is not canonical, such that $\mathcal{K}_{\bar{i}j} \neq \delta_{\bar{i}j}$. The scalar kinetic terms (and, hence, the scalar fields themselves) are, thus, not canonically normalized in the Einstein frame.

To obtain the equivalent of Eq. (171) in the Jordan frame, we need to perform a Weyl rescaling,

$$g_{\mu\nu}^J = \mathcal{C}^2 g_{\mu\nu}, \quad g_J^{\mu\nu} = \mathcal{C}^{-2} g^{\mu\nu}, \quad \sqrt{-g_J} = \mathcal{C}^4 \sqrt{-g}, \quad \mathcal{C} = \left(-\frac{3M_{\text{Pl}}^2}{\Omega} \right)^{1/2}, \quad (173)$$

where \mathcal{C} is known as the conformal factor. The frame function Ω is an arbitrary real negative function of the complex scalars, $\Omega = \Omega(\phi_i, \phi_i^*) < 0$. Each choice for Ω defines a separate Jordan frame. In Sec. 2, we make a particular choice for Ω , demanding the following relation to the Kähler potential,

$$\Omega = -3M_{\text{Pl}}^2 \exp\left(-\frac{K}{3M_{\text{Pl}}^2}\right) \quad \Leftrightarrow \quad K = -3M_{\text{Pl}}^2 \ln\left(-\frac{\Omega}{3M_{\text{Pl}}^2}\right). \quad (174)$$

This results in what may be regarded as the standard Jordan frame. In light of the relation in Eq. (174), the frame function Ω has two possible interpretations. In the curved superspace approach to old minimal supergravity [116, 117], Ω can be identified as the generalized kinetic energy on curved superspace, while in the superconformal approach to old minimal supergravity [118, 119], Ω can be identified as the prefactor of the kinetic term of the chiral compensator superfield. Eq. (174) allows to relate the partial derivatives of the Kähler potential to the partial derivatives of the frame function,

$$K_i = \frac{\partial K}{\partial \phi_i} = \mathcal{C}^2 \frac{\partial \Omega}{\partial \phi_i} = \mathcal{C}^2 \Omega_i, \quad K_{\bar{i}} = \frac{\partial K}{\partial \phi_i^*} = \mathcal{C}^2 \frac{\partial \Omega}{\partial \phi_i^*} = \mathcal{C}^2 \Omega_{\bar{i}}. \quad (175)$$

Similarly, we are able to express the Kähler metric \mathcal{K} in terms of derivatives of the frame function,

$$\mathcal{K}_{\bar{i}j} = \mathcal{C}^2 \omega_{\bar{i}j}, \quad \omega_{\bar{i}j} = \Omega_{\bar{i}j} - \frac{\Omega_{\bar{i}} \Omega_j}{\Omega}, \quad \Omega_{\bar{i}j} = \frac{\partial^2 \Omega}{\partial \phi_i^* \partial \phi_j}. \quad (176)$$

¹⁹Some authors in the literature distinguish between Einstein-frame and Jordan-frame quantities by labeling them with indices E and J , respectively. We will, by contrast, not use any particular label for quantities in the Einstein frame and merely label quantities in the Jordan frame with an index J . This will slightly simplify our notation.

Here, we introduced ω as a rescaled field-space metric that is determined by the derivatives of the frame function and that is equivalent to the Kähler metric up to the rescaling factor \mathcal{C}^2 . Eq. (176) automatically implies a similar relation between the respective inverse metrics, \mathcal{K}^{-1} and ω^{-1} ,

$$(\mathcal{K}^{-1})_{i\bar{j}} = \mathcal{C}^{-2} (\omega^{-1})_{i\bar{j}}. \quad (177)$$

We now apply the Weyl transformation in Eq. (173) to the Einstein-frame action in Eq. (171). This yields the purely bosonic action of our model in the Jordan frame (see [112] for more details),

$$S_{\text{bos}}^J = \int d^4x \sqrt{-g_J} \left[\frac{1}{2} \left(-\frac{\Omega}{3} \right) R_J - \Omega_{i\bar{j}} g_J^{\mu\nu} D_\mu \phi_i^* D_\nu \phi_j + \Omega \mathcal{A}_\mu \mathcal{A}^\mu - \frac{1}{4} F_{\mu\nu} F^{\mu\nu} - V^J \right]. \quad (178)$$

In view of this action, several comments are in order:

(i) The frame function Ω depends on the scalar fields of our model. The Einstein-Hilbert term (i.e., the kinetic term for the metric that is proportional to the Ricci scalar R_J) therefore becomes field-dependent. Or in other words, the scalar fields are now nonminimally coupled to gravity.

(ii) The Planck mass squared in Eq. (171) is now replaced by $-\Omega/3$. This indicates that the square root of $-\Omega/3$ should be interpreted as the effective field-dependent Planck mass in the Jordan frame,

$$M_{\text{Pl}}^J = \left(-\frac{\Omega}{3} \right)^{1/2} \quad \Leftrightarrow \quad M_{\text{Pl}} = \mathcal{C} M_{\text{Pl}}^J, \quad (179)$$

which is consistent with the fact that all Jordan-frame mass scales m_J pick a factor \mathcal{C} when transforming from the Jordan frame to the Einstein frame, $m = \mathcal{C} m_J$. From this perspective, the conformal factor \mathcal{C} turns out to be nothing but the ratio of the two respective Planck masses, $\mathcal{C} = M_{\text{Pl}}/M_{\text{Pl}}^J$.

(iii) The Kähler metric \mathcal{K} in Eq. (171) is now replaced by the Hessian of Ω . In our model, we choose Ω such that it only contains canonical as well as purely holomorphic/antiholomorphic terms,

$$\Omega = -3M_{\text{Pl}}^2 + \delta_{i\bar{j}} \phi_i^* \phi_j + [J(\phi_i) + \text{h.c.}], \quad (180)$$

where J is an arbitrary holomorphic function. The canonical terms, $\Omega \supset \delta_{i\bar{j}} \phi_i^* \phi_j$, lead to nonminimal couplings between the complex scalars and the Ricci scalar R_J that are invariant under a classical conformal symmetry. These conformal couplings can be disturbed by a nonzero function J which explicitly breaks the conformal symmetry. Irrespective of whether $J = 0$ or $J \neq 0$, Eq. (180) leads to

$$\Omega_{i\bar{j}} = \delta_{i\bar{j}}. \quad (181)$$

In this case, we obtain the following expressions for the rescaled field-space metric ω and its inverse,

$$\omega_{i\bar{j}} = \delta_{i\bar{j}} - \frac{\Omega_{i\bar{j}} \Omega_j}{\Omega}, \quad (\omega^{-1})_{i\bar{j}} = \delta_{i\bar{j}} + \frac{1}{\varrho} \frac{\Omega_{i\bar{j}} \Omega_j}{\Omega}, \quad \varrho = 1 - \frac{\Omega_{i\bar{k}} \Omega_k}{\Omega}. \quad (182)$$

Here, the dimensionless parameter ϱ functions as a measure for the amount of conformal symmetry breaking in the frame function Ω . In the conformal limit, $J \rightarrow 0$, it simply reduces to the conformal factor squared, $\varrho \rightarrow \mathcal{C}^2$. In this sense, ϱ plays a similar role as the reduced kinetic function of the inflation field, f , defined in Eq. (89). In fact, in our concrete model, one can show that $\varrho = \mathcal{C}^2 (1 - f)$.

(iv) In the Jordan frame, the scalar kinetic terms receive additional contributions from the bosonic part of the auxiliary SUGRA gauge field \mathcal{A}_μ . This is accounted for by the third term on the right-hand side of Eq. (178). The auxiliary field \mathcal{A}_μ can be eliminated after solving its equation of motion,

$$\mathcal{A}_\mu = \frac{1}{\Omega} \text{Im} \{ \Omega_i D_\mu \phi_i \} . \quad (183)$$

This solution illustrates that the \mathcal{A}^2 term in Eq. (178) is only relevant as long as we are interested in the dynamics of angular degrees of freedom, i.e., the complex phases of the complex scalars ϕ_i . This is, however, not the case. In our model, inflation occurs along the real direction of the complex inflation field s . The auxiliary field \mathcal{A}_μ therefore vanishes and the \mathcal{A}^2 term in Eq. (178) can be ignored. Together with Eq. (181), $\mathcal{A}_\mu = 0$ leads to canonically normalized kinetic terms for all complex scalar fields in our model. This is an important result and the main motivation for our ansatz in Eq. (180).

Combining our above results, the action in Eq. (178) can be simplified to the following expression,

$$S_{\text{bos}}^J = \int d^4x \sqrt{-g_J} \left[\frac{1}{2} (M_{\text{Pl}}^J)^2 R_J - \delta_{ij} g_J^{\mu\nu} D_\mu \phi_i^* D_\nu \phi_j - \frac{1}{4} F_{\mu\nu} F^{\mu\nu} - V^J \right] . \quad (184)$$

This is the starting point for the analysis of our model in the Jordan frame. Thus far, we have not commented on the relation between the potentials V and V^J . We will do this now in the next section.

A.2 Scalar potential

The total scalar potential in the Einstein frame, V , has mass dimension four. On general grounds, this implies the following universal relation to the total scalar potential in the Jordan frame, V^J ,

$$V = \mathcal{C}^4 V^J , \quad V^J = \mathcal{C}^{-4} V , \quad (185)$$

which holds at tree level as well as at the loop level. Eq. (185) implies the following useful relations,

$$\begin{aligned} V_i &= \frac{\partial V}{\partial \phi_i} = \mathcal{C}^4 \left(V_i^J - \frac{2}{\Omega} \Omega_i V^J \right) , & V_i^J &= \frac{\partial V^J}{\partial \phi_i} = \mathcal{C}^{-4} \left(V_i + \frac{2}{\Omega} \Omega_i V \right) , \\ V_{ij} &= \frac{\partial^2 V}{\partial \phi_i^* \partial \phi_j} = \mathcal{C}^4 \left[V_{ij}^J - \frac{2}{\Omega} (\Omega_{\bar{i}} V_j^J + \Omega_j V_{\bar{i}}^J) - \frac{2}{\Omega} \left(\omega_{\bar{i}j} - 2 \frac{\Omega_{\bar{i}} \Omega_j}{\Omega} \right) V^J \right] , \\ V_{\bar{i}j}^J &= \frac{\partial^2 V^J}{\partial \phi_i^* \partial \phi_j} = \mathcal{C}^{-4} \left[V_{\bar{i}j} + \frac{2}{\Omega} (\Omega_{\bar{i}} V_j + \Omega_j V_{\bar{i}}) + \frac{2}{\Omega} \left(\omega_{\bar{i}j} + 2 \frac{\Omega_{\bar{i}} \Omega_j}{\Omega} \right) V \right] . \end{aligned} \quad (186)$$

Together, Eqs. (185) and (186) illustrate that a Minkowski vacuum in the Einstein frame ($V = V_i = 0$) also corresponds to a Minkowski vacuum in the Jordan frame ($V^J = V_i^J = 0$), and vice versa.

In the next step, we shall become more specific and discuss the individual contributions to V and V^J , respectively. The Einstein-frame potential consists of the usual F-term and D-term contributions,

$$V = V_F + V_D . \quad (187)$$

To begin with, let us focus on the F-term scalar potential (see [186] for more details),

$$V_F = F_{\bar{i}}^* \mathcal{K}_{\bar{i}j} F_j - 3 \exp \left(\frac{K}{M_{\text{Pl}}^2} \right) \frac{|W|^2}{M_{\text{Pl}}^2} . \quad (188)$$

Here, the F_i and F_i^* stand for the generalized F terms in supergravity and their complex conjugates,

$$F_i = -\exp\left[\frac{K}{2M_{\text{Pl}}^2}\right] (\mathcal{K}^{-1})_{i\bar{j}} (\mathcal{D}W)_{\bar{j}}^*, \quad F_i^* = -\exp\left[\frac{K}{2M_{\text{Pl}}^2}\right] (\mathcal{K}^{-1})_{\bar{i}j}^* (\mathcal{D}W)_j, \quad (189)$$

where $\mathcal{D}W$ denotes the Kähler-covariant derivative of the superpotential on the Kähler manifold,

$$(\mathcal{D}W)_i = \frac{\partial W}{\partial \phi_i} + \frac{\partial K}{\partial \phi_i} \frac{W}{M_{\text{Pl}}^2}. \quad (190)$$

The F-term potential in the Jordan frame is given as $V_F^J = \mathcal{C}^{-4} V_F$. This can be rewritten as follows,

$$V_F^J = \left(W_i - 3W \frac{\Omega_i}{\Omega}\right) (\omega^{-1})_{i\bar{j}} \left(W_{\bar{j}}^* - 3W^* \frac{\Omega_{\bar{j}}}{\Omega}\right) + \frac{9}{\Omega} |W|^2. \quad (191)$$

which underlines the similarity between the role of the inverse metric ω^{-1} in the Jordan frame and the role of the inverse Kähler metric \mathcal{K}^{-1} in the Einstein frame. With our ansatz for the frame function Ω in Eq. (180), V_F^J can be further simplified to the following compact expression (see, e.g., [120]),

$$V_F^J = V_F^0 + \Delta V_F^J, \quad V_F^0 = W_i W_i^*, \quad \Delta V_F^J = \frac{1}{\rho \Omega} |W_i \Omega_i - 3W|^2. \quad (192)$$

Eq. (192) illustrates a remarkable effect. Provided that the scalar kinetic terms in the Jordan frame are canonically normalized, V_F^J splits into two separate contributions — where the first contribution, V_F^0 , is nothing but the ordinary F-term scalar potential in global supersymmetry and the second contribution, ΔV_F^J , represents an additive SUGRA correction. Eq. (192) provides the basis for the calculation of the F-term scalar potential in our model (see Eqs. (110) and (111)). We first calculate the F-term scalar potential in the Jordan frame according to Eq. (192). Then, we convert our result from the Jordan frame to the Einstein frame making use of the general relation in Eq. (185),

$$V_F = \mathcal{C}^4 \left(W_i W_i^* + \frac{1}{\rho \Omega} |W_i \Omega_i - 3W|^2\right). \quad (193)$$

Computing V_F via this detour is considerably easier than a direct calculation starting with Eq. (188).

The SUGRA correction ΔV_F^J in Eq. (192) is directly proportional to the mass scales that appear in the superpotential. In our model, these mass scales correspond to the F-term SUSY breaking scale μ , the effective inflaton-dependent mass of the waterfall fields, $\kappa \langle S \rangle$, and the R -symmetry-breaking constant w_0 (see Eq. (106)). All of these mass scales are responsible for the explicit breaking of superconformal symmetry. Conversely, this means that, if the superpotential does not exhibit any explicit mass scales, the SUGRA correction ΔV_F^J must vanish. This is exactly what happens in the class of *canonical superconformal supergravity* (CSS) models studied in [113]. These models are based on the frame function in Eq. (180) with the holomorphic function J set to zero. Moreover, they exhibit a purely cubic superpotential, such that $\Delta V_F^J = 0$. One generic feature of CSS models therefore is that their Jordan-frame scalar potential coincides with the scalar potential in global supersymmetry,

$$\text{CSS models:} \quad W = \frac{1}{3} \lambda_{ijk} \Phi_i \Phi_j \Phi_k, \quad V_F^J = V_F^0, \quad V_D^J = V_D^0, \quad \Delta V_F^J = 0. \quad (194)$$

Note that this statement applies to the total scalar potential, including the D-term scalar potential.

In our model, the D-term scalar potential in the Einstein frame, V_D , is given by [186]

$$V_D = \frac{1}{2} D^2, \quad (195)$$

where D denotes the auxiliary component of the $B-L$ vector multiplet V . In writing down Eq. (195), we assumed a canonical gauge-kinetic function for the $B-L$ vector field, $f_V = 1$, and absorbed the gauge coupling constant g into the definition of D . On-shell, the auxiliary D field can be replaced by

$$D = -g q_i K_i \phi_i. \quad (196)$$

In the language of Kähler geometry, this is equivalent to the Killing potential of the $U(1)_{B-L}$ isometry of our Kähler manifold. Together, Eqs. (195) and (196) result in the following expression for V_D ,

$$V_D = \frac{g^2}{2} (q_i K_i \phi_i)^2. \quad (197)$$

This result can be easily translated into the Jordan frame by making use of Eqs. (175) and (185),

$$V_D^J = \mathcal{C}^{-4} V_D = \frac{g^2}{2} (q_i \Omega_i \phi_i)^2. \quad (198)$$

In our model, all complex scalars with nonzero gauge charge q_i appear with a canonical term in Ω . Just like in the class of CSS models, V_D^J therefore obtains the same form as in global supersymmetry,

$$q_i \Omega_i = q_i \phi_i^* \quad \Rightarrow \quad V_D^J = \frac{g^2}{2} (q_i |\phi_i|^2)^2 = V_D^0. \quad (199)$$

This means in turn that the D-term scalar potential in the Einstein frame can be written as

$$V_D = \frac{g^2}{2} \mathcal{C}^4 (q_i |\phi_i|^2)^2. \quad (200)$$

Combining all of our above results, we conclude that V and V^J are given as follows in our model,

$$V = \mathcal{C}^4 V^J, \quad V^J = W_i W_i^* + \frac{g^2}{2} (q_i |\phi_i|^2)^2 + \frac{1}{\rho \Omega} |W_i \Omega_i - 3W|^2. \quad (201)$$

This result is the starting point for our calculation of the inflaton potential in Sec. 2.5.

A.3 Scalar mass parameters

Eq. (201) allows us to derive useful expressions for the scalar mass parameters m_{ab}^J in the Jordan frame.²⁰ The scalar mass matrix is given by the Hessian of the scalar potential, $(m_{ab}^J)^2 = V_{ab}^J$. As a consequence of the simple structure of V^J , the scalar masses, thus, split into two contributions: the ordinary masses in global supersymmetry, m_{ab}^0 , as well as additive corrections in supergravity, Δm_{ab} ,

$$(m_{ab}^J)^2 = (m_{ab}^0)^2 + \Delta m_{ab}^2, \quad (m_{ab}^0)^2 = \frac{\partial^2}{\partial z_a \partial z_b} (V_F^0 + V_D^0), \quad \Delta m_{ab}^2 = \frac{\partial^2}{\partial z_a \partial z_b} \Delta V_F^J. \quad (202)$$

²⁰Here, a and b represent collective indices that encompass all scalar fields ϕ_i as well as their complex conjugates ϕ_i^* . In the following, the symbol z_a will therefore either denote the field ϕ_i for some index i or the field ϕ_i^* for some index \bar{i} .

In the case of scalar fields that only appear with a canonical term in the frame function, $\Omega \supset |\phi_i|^2$, the corrections Δm_{ab}^2 take a particularly simple form. Based on our result in Eq. (192), we find

$$\Delta m_{ij}^2 = \frac{(W_{jk}\Omega_{\bar{k}} - 2W_j)(W_{i\bar{\ell}}^*\Omega_{\ell} - 2W_{i\bar{\ell}}^*)}{\rho\Omega}, \quad \Delta m_{ij}^2 = \frac{(W_{ijk}\Omega_{\bar{k}} - W_{ij})(W_{\bar{\ell}}^*\Omega_{\ell} - 3W^*)}{\rho\Omega}, \quad (203)$$

and similarly for the respective conjugate parameters, $\Delta m_{ij}^2 = (\Delta m_{ij}^2)^*$ and $\Delta m_{ij}^2 = (\Delta m_{ij}^2)^*$. The diagonal entries of the scalar mass matrix therefore obtain the following compact form,

$$\Delta m_{ii}^2 = \frac{|W_{ik}\Omega_{\bar{k}} - 2W_i|^2}{\rho\Omega}. \quad (204)$$

In addition to the masses encoded in the scalar potential, the complex scalar fields acquire further, effective masses from their nonminimal coupling to R_J in the Jordan-frame action (see Eq. (178)),

$$(m_{ab}^R)^2 = \zeta R_J \frac{\partial^2 \Omega}{\partial z_a \partial z_b}, \quad \zeta = \frac{1}{6}. \quad (205)$$

All scalar fields with a canonical kinetic function, thus, receive a universal gravity-induced mass m_R ,

$$m_R^2 = \zeta R_J. \quad (206)$$

In summary, the entries of the total effective mass matrix in the Jordan frame, M_J^2 , read as follows,

$$(M_J^2)_{ab} = (m_{ab}^0)^2 + \Delta m_{ab}^2 + (m_{ab}^R)^2. \quad (207)$$

In our model, all scalar fields are canonically normalized by construction. The eigenvalues of the matrix M_J^2 therefore directly correspond to the physical scalar mass eigenvalues in the Jordan frame. The situation is more complicated in the Einstein frame, where the scalar fields parametrize the target space of a non-linear sigma model (see Eq. (171)). There, the scalar fields are *a priori* not canonically normalized which makes it more difficult to find the physical mass eigenvalues. Without reference to the Jordan frame, the computation of the scalar mass spectrum in the Einstein frame requires two steps. First, one has to perform a field transformation that renders all fields canonically normalized. Then, one has to calculate the mass eigenvalues of these canonically normalized fields as usual. Our result in Eq. (207), however, allows us to bypass this complicated procedure. Instead, we can simply make use of the universal scaling behavior of physical mass scales when transforming back and forth between the Jordan frame and the Einstein frame. According to this scaling behavior, we know that total effective scalar mass matrix in the Einstein frame, M^2 , must obtain the following form,

$$M_{ab}^2 = \mathcal{C}^2 (M_J^2)_{ab} = \mathcal{C}^2 \left[(m_{ab}^0)^2 + \Delta m_{ab}^2 + (m_{ab}^R)^2 \right]^2. \quad (208)$$

It would be interesting to check the validity of this result by means of an explicit calculation in the Einstein frame. Such a task is, however, beyond the scope of this paper and left for future work.

More details on the mass parameters for all fields with nonzero spin (i.e., the fermions, vector boson, and gravitino in our model) can be found in the literature. The relevant expressions in the Jordan frame are spelled out in [112], while the standard Einstein-frame results are listed, e.g., in [186].

A.4 Slow-roll parameters

Finally, let us discuss the relation between the inflationary slow-roll parameters in the Einstein frame, ε and η , and their counterparts in the Jordan frame, ε_J and η_J . The results derived in the section will enable us to use our results for the scalar potential in the Jordan frame (see Sec. 2) as input for a standard slow-roll analysis of the inflationary dynamics in the Einstein frame (see Sec. 3).

Let us consider the action of the complex inflaton field s in the Einstein frame (see Eq. (171)),

$$S_{\text{inf}} = - \int d^4x \sqrt{-g} [\mathcal{N}^2 \partial_\mu s^* \partial^\mu s + V(s)] , \quad \mathcal{N} = \mathcal{K}_{s^*s}^{1/2}. \quad (209)$$

As can be seen from this action, the inflaton field is not canonically normalized in the Einstein frame. This is made explicit by the noncanonical normalization factor of the inflaton kinetic term, $\mathcal{N} \neq 1$. However, in our slow-roll analysis, we will have to work with the canonically normalized field \hat{s} . The field \hat{s} can be constructed as a function of the field s by solving the following differential equations,

$$\frac{\partial \hat{\sigma}}{\partial \sigma} = \mathcal{N}(\sigma, \tau) , \quad \frac{\partial \hat{\tau}}{\partial \tau} = \mathcal{N}(\sigma, \tau) , \quad s = \frac{1}{\sqrt{2}}(\sigma + i\tau) , \quad \hat{s} = \frac{1}{\sqrt{2}}(\hat{\sigma} + i\hat{\tau}) . \quad (210)$$

In terms of the canonically normalized field \hat{s} , the action in Eq. (209) obtains its standard form,

$$S_{\text{inf}} = - \int d^4x \sqrt{-g} [\partial_\mu \hat{s}^* \partial^\mu \hat{s} + V(\hat{s})] , \quad V(\hat{s}) \equiv V(s(\hat{s})) . \quad (211)$$

This action is the starting point of our standard slow-roll analysis. The slow-roll parameters in the Einstein frame, ε and η , are defined in terms of the usual partial derivatives of the scalar potential,

$$\varepsilon = \frac{M_{\text{Pl}}^2}{2} \left(\frac{V'}{V} \right)^2 , \quad \eta = M_{\text{Pl}}^2 \frac{V''}{V} , \quad V' = \frac{\partial V}{\partial \hat{\sigma}} , \quad V'' = \frac{\partial^2 V}{\partial \hat{\sigma}^2} . \quad (212)$$

Here, we assumed that inflaton occurs along the real component $\hat{\sigma}$ of the complex inflaton field \hat{s} . In the next step, we rewrite these expressions making use of the chain rule and the relations in Eq. (210),

$$V' = \frac{\partial \sigma}{\partial \hat{\sigma}} \frac{\partial V}{\partial \sigma} = \frac{V_\sigma}{\mathcal{N}} , \quad V'' = \frac{\partial \sigma}{\partial \hat{\sigma}} \frac{\partial V'}{\partial \sigma} = \frac{1}{\mathcal{N}} \left(\frac{V_{\sigma\sigma}}{\mathcal{N}} - \frac{\mathcal{N}_\sigma V_\sigma}{\mathcal{N}^2} \right) , \quad (213)$$

where $V_\sigma = \partial V / \partial \sigma$, $V_{\sigma\sigma} = \partial^2 V / \partial \sigma^2$, and $\mathcal{N}_\sigma = \partial \mathcal{N} / \partial \sigma$. With these definitions and relations, we find

$$\varepsilon = \frac{\tilde{\varepsilon}}{\mathcal{N}^2} , \quad \eta = \frac{\tilde{\eta} - 2(\nu \tilde{\varepsilon})^{1/2}}{\mathcal{N}^2} , \quad (214)$$

where we assumed that $V_\sigma > 0$ and $\mathcal{N}_\sigma > 0$. The parameters $\tilde{\varepsilon}$ and $\tilde{\eta}$ represent what can be referred to as the naive slow-roll parameters in the Einstein frame, i.e., the slow-roll parameters that one would obtain if one ignored the noncanonical normalization factor \mathcal{N} in Eq. (209). Meanwhile, the factor ν is an auxiliary slow-roll parameter that accounts for the field dependence of the factor \mathcal{N} ,

$$\tilde{\varepsilon} = \frac{M_{\text{Pl}}^2}{2} \left(\frac{V_\sigma}{V} \right)^2 , \quad \tilde{\eta} = M_{\text{Pl}}^2 \frac{V_{\sigma\sigma}}{V} , \quad \nu = \frac{M_{\text{Pl}}^2}{2} \left(\frac{\mathcal{N}_\sigma}{\mathcal{N}} \right)^2 . \quad (215)$$

The expressions in Eq. (214) are now well suited to establish a connection to the Jordan frame. The naive slow-roll parameters $\tilde{\varepsilon}$ and $\tilde{\eta}$ can be readily related to the Jordan-frame slow-roll parameters ε_J and η_J by employing the relations for the partial derivatives of the scalar potential in Eq. (186),

$$\tilde{\varepsilon} = \left(\varepsilon_J^{1/2} - 2 \xi_J^{1/2} \right)^2 , \quad \tilde{\eta} = \eta_J + 12 \xi_J - 8 (\varepsilon_J \xi_J)^{1/2} - 2 \zeta_J , \quad (216)$$

where we assumed again a positive potential gradient, $V_\sigma^J > 0$. The Jordan-frame slow-roll parameters ε_J and η_J are defined in terms of the usual partial derivatives of the Jordan-frame scalar potential,

$$\varepsilon_J = \frac{M_{\text{Pl}}^2}{2} \left(\frac{V_\sigma^J}{V^J} \right)^2, \quad \eta_J = M_{\text{Pl}}^2 \frac{V_{\sigma\sigma}^J}{V^J} \quad \text{with} \quad V_\sigma^J = \frac{\partial V^J}{\partial \sigma}, \quad V_{\sigma\sigma}^J = \frac{\partial^2 V^J}{\partial \sigma^2}. \quad (217)$$

In Eq. (216), we also introduced the auxiliary slow-roll parameters ξ_J and ζ_J which account for the field dependence of the frame function Ω . These slow-roll parameters are defined as follows,

$$\xi_J^{1/2} = \frac{M_{\text{Pl}}}{\sqrt{2}} \frac{\Omega_\sigma}{\Omega}, \quad \zeta_J = M_{\text{Pl}}^2 \frac{\Omega_{\sigma\sigma}}{\Omega} \quad \text{with} \quad \Omega_\sigma = \frac{\partial \Omega}{\partial \sigma}, \quad \Omega_{\sigma\sigma} = \frac{\partial^2 \Omega}{\partial \sigma^2}. \quad (218)$$

Unlike in the Einstein frame, we do not have to distinguish between naive and actual slow-roll parameters in the Jordan frame. This is because, in our model, all scalar fields are canonically normalized in the Jordan frame by construction. In the language of Eq. (214), this can be phrased by saying that the normalization factor of the inflaton kinetic term in the Jordan frame is simply trivial, $\mathcal{N}_J = 1$.

Combining our results in Eqs. (214) and (216), we finally obtain the following relations,

$$\begin{aligned} \varepsilon &= \frac{1}{\mathcal{N}^2} \left(\varepsilon_J^{1/2} - 2\xi_J^{1/2} \right)^2, \\ \eta &= \frac{1}{\mathcal{N}^2} \left[\eta_J + 12\xi_J - 8(\varepsilon_J \xi_J)^{1/2} - 2\zeta_J - 2\nu^{1/2} \left(\varepsilon_J^{1/2} - 2\xi_J^{1/2} \right) \right]. \end{aligned} \quad (219)$$

This is an important result that holds in any model with an Einstein-frame action as in Eq. (209). Eq. (219) is the starting point for our computation of the Einstein-frame slow-roll parameters in Sec. 3. We emphasize that computing ε and η according to Eq. (219) is considerably easier than a brute-force calculation in the Einstein frame. In the Einstein frame, we would have to deal with a complicated Kähler potential, a more complicated scalar potential, and a noncanonically normalized inflaton field. Eq. (219) allows us to circumvent these complications and determine the parameters ε and η simply based on the derivatives of the Jordan-frame scalar potential V^J and the frame function Ω .

References

- [1] **ATLAS** Collaboration, M. Aaboud et al., *Search for squarks and gluinos in events with an isolated lepton, jets and missing transverse momentum at $\sqrt{s} = 13$ TeV with the ATLAS detector*, [arXiv:1708.08232](#).
- [2] **CMS** Collaboration, A. M. Sirunyan et al., *Search for supersymmetry in multijet events with missing transverse momentum in proton-proton collisions at 13 TeV*, *Phys. Rev.* **D96** (2017), no. 3 032003, [[arXiv:1704.07781](#)].
- [3] **ATLAS** Collaboration, G. Aad et al., *Observation of a new particle in the search for the Standard Model Higgs boson with the ATLAS detector at the LHC*, *Phys. Lett.* **B716** (2012) 1–29, [[arXiv:1207.7214](#)].
- [4] **CMS** Collaboration, S. Chatrchyan et al., *Observation of a new boson at a mass of 125 GeV with the CMS experiment at the LHC*, *Phys. Lett.* **B716** (2012) 30–61, [[arXiv:1207.7235](#)].

- [5] **ATLAS, CMS** Collaboration, G. Aad et al., *Combined Measurement of the Higgs Boson Mass in pp Collisions at $\sqrt{s} = 7$ and 8 TeV with the ATLAS and CMS Experiments*, *Phys. Rev. Lett.* **114** (2015) 191803, [[arXiv:1503.07589](#)].
- [6] Y. Okada, M. Yamaguchi, and T. Yanagida, *Upper bound of the lightest Higgs boson mass in the minimal supersymmetric standard model*, *Prog. Theor. Phys.* **85** (1991) 1–6.
- [7] Y. Okada, M. Yamaguchi, and T. Yanagida, *Renormalization group analysis on the Higgs mass in the softly broken supersymmetric standard model*, *Phys. Lett.* **B262** (1991) 54–58.
- [8] J. R. Ellis, G. Ridolfi, and F. Zwirner, *Radiative corrections to the masses of supersymmetric Higgs bosons*, *Phys. Lett.* **B257** (1991) 83–91.
- [9] J. R. Ellis, G. Ridolfi, and F. Zwirner, *On radiative corrections to supersymmetric Higgs boson masses and their implications for LEP searches*, *Phys. Lett.* **B262** (1991) 477–484.
- [10] H. E. Haber and R. Hempfling, *Can the mass of the lightest Higgs boson of the minimal supersymmetric model be larger than $m(Z)$?*, *Phys. Rev. Lett.* **66** (1991) 1815–1818.
- [11] G. F. Giudice, M. A. Luty, H. Murayama, and R. Rattazzi, *Gaugino mass without singlets*, *JHEP* **12** (1998) 027, [[hep-ph/9810442](#)].
- [12] J. D. Wells, *Implications of supersymmetry breaking with a little hierarchy between gauginos and scalars*, in *11th International Conference on Supersymmetry and the Unification of Fundamental Interactions (SUSY 2003) Tucson, Arizona, June 5-10, 2003*, 2003. [[hep-ph/0306127](#)].
- [13] J. D. Wells, *PeV-scale supersymmetry*, *Phys. Rev.* **D71** (2005) 015013, [[hep-ph/0411041](#)].
- [14] L. J. Hall and Y. Nomura, *A Finely-Predicted Higgs Boson Mass from A Finely-Tuned Weak Scale*, *JHEP* **03** (2010) 076, [[arXiv:0910.2235](#)].
- [15] N. Arkani-Hamed and S. Dimopoulos, *Supersymmetric unification without low energy supersymmetry and signatures for fine-tuning at the LHC*, *JHEP* **06** (2005) 073, [[hep-th/0405159](#)].
- [16] G. F. Giudice and A. Romanino, *Split supersymmetry*, *Nucl. Phys.* **B699** (2004) 65–89, [[hep-ph/0406088](#)]. [Erratum: *Nucl. Phys.* **B706** (2005) 487–487].
- [17] N. Arkani-Hamed, S. Dimopoulos, G. F. Giudice, and A. Romanino, *Aspects of split supersymmetry*, *Nucl. Phys.* **B709** (2005) 3–46, [[hep-ph/0409232](#)].
- [18] A. Arvanitaki, N. Craig, S. Dimopoulos, and G. Villadoro, *Mini-Split*, *JHEP* **02** (2013) 126, [[arXiv:1210.0555](#)].
- [19] N. Arkani-Hamed, A. Gupta, D. E. Kaplan, N. Weiner, and T. Zorawski, *Simply Unnatural Supersymmetry*, [arXiv:1212.6971](#).

- [20] L. J. Hall and Y. Nomura, *Spread Supersymmetry*, *JHEP* **01** (2012) 082, [[arXiv:1111.4519](#)].
- [21] L. J. Hall, Y. Nomura, and S. Shirai, *Spread Supersymmetry with Wino LSP: Gluino and Dark Matter Signals*, *JHEP* **01** (2013) 036, [[arXiv:1210.2395](#)].
- [22] M. Ibe, T. Moroi, and T. T. Yanagida, *Possible Signals of Wino LSP at the Large Hadron Collider*, *Phys. Lett.* **B644** (2007) 355–360, [[hep-ph/0610277](#)].
- [23] M. Ibe and T. T. Yanagida, *The Lightest Higgs Boson Mass in Pure Gravity Mediation Model*, *Phys. Lett.* **B709** (2012) 374–380, [[arXiv:1112.2462](#)].
- [24] M. Ibe, S. Matsumoto, and T. T. Yanagida, *Pure Gravity Mediation with $m_{3/2} = 10\text{--}100\text{ TeV}$* , *Phys. Rev.* **D85** (2012) 095011, [[arXiv:1202.2253](#)].
- [25] W. Buchmüller, M. Dierigl, F. Ruehle, and J. Schweizer, *Split symmetries*, *Phys. Lett.* **B750** (2015) 615–619, [[arXiv:1507.06819](#)].
- [26] H. Pagels and J. R. Primack, *Supersymmetry, Cosmology and New TeV Physics*, *Phys. Rev. Lett.* **48** (1982) 223.
- [27] S. Weinberg, *Cosmological Constraints on the Scale of Supersymmetry Breaking*, *Phys. Rev. Lett.* **48** (1982) 1303.
- [28] M. Yu. Khlopov and A. D. Linde, *Is It Easy to Save the Gravitino?*, *Phys. Lett.* **138B** (1984) 265–268.
- [29] J. R. Ellis, D. V. Nanopoulos, and S. Sarkar, *The Cosmology of Decaying Gravitinos*, *Nucl. Phys.* **B259** (1985) 175–188.
- [30] F. Gabbiani, E. Gabrielli, A. Masiero, and L. Silvestrini, *A Complete analysis of FCNC and CP constraints in general SUSY extensions of the standard model*, *Nucl. Phys.* **B477** (1996) 321–352, [[hep-ph/9604387](#)].
- [31] A. A. Starobinsky, *A New Type of Isotropic Cosmological Models Without Singularity*, *Phys. Lett.* **91B** (1980) 99–102.
- [32] A. H. Guth, *The Inflationary Universe: A Possible Solution to the Horizon and Flatness Problems*, *Phys. Rev.* **D23** (1981) 347–356.
- [33] A. D. Linde, *A New Inflationary Universe Scenario: A Possible Solution of the Horizon, Flatness, Homogeneity, Isotropy and Primordial Monopole Problems*, *Phys. Lett.* **108B** (1982) 389–393.
- [34] A. Albrecht and P. J. Steinhardt, *Cosmology for Grand Unified Theories with Radiatively Induced Symmetry Breaking*, *Phys. Rev. Lett.* **48** (1982) 1220–1223.
- [35] D. H. Lyth and A. Riotto, *Particle physics models of inflation and the cosmological density perturbation*, *Phys. Rept.* **314** (1999) 1–146, [[hep-ph/9807278](#)].

- [36] A. D. Linde, *Particle physics and inflationary cosmology*, *Contemp. Concepts Phys.* **5** (1990) 1–362, [[hep-th/0503203](#)].
- [37] L. Randall and S. D. Thomas, *Solving the cosmological moduli problem with weak scale inflation*, *Nucl. Phys.* **B449** (1995) 229–247, [[hep-ph/9407248](#)].
- [38] A. Riotto, *Inflation and the nature of supersymmetry breaking*, *Nucl. Phys.* **B515** (1998) 413–435, [[hep-ph/9707330](#)].
- [39] W. Buchmüller, L. Covi, and D. Delepine, *Inflation and supersymmetry breaking*, *Phys. Lett.* **B491** (2000) 183–189, [[hep-ph/0006168](#)].
- [40] K. I. Izawa, *Supersymmetry-breaking models of inflation*, *Prog. Theor. Phys.* **99** (1998) 157–160, [[hep-ph/9708315](#)].
- [41] K. Schmitz and T. T. Yanagida, *Polonyi Inflation: Dynamical supersymmetry breaking and late-time R symmetry breaking as the origin of cosmic inflation*, *Phys. Rev.* **D94** (2016), no. 7 074021, [[arXiv:1604.04911](#)].
- [42] V. Domcke and K. Schmitz, *Unified model of D-term inflation*, *Phys. Rev.* **D95** (2017), no. 7 075020, [[arXiv:1702.02173](#)].
- [43] K. Harigaya and K. Schmitz, *Unified Model of Chaotic Inflation and Dynamical Supersymmetry Breaking*, *Phys. Lett.* **B773** (2017) 320–324, [[arXiv:1707.03646](#)].
- [44] S. Dimopoulos, G. R. Dvali, and R. Rattazzi, *Dynamical inflation and unification scale on quantum moduli spaces*, *Phys. Lett.* **B410** (1997) 119–124, [[hep-ph/9705348](#)].
- [45] K. I. Izawa, M. Kawasaki, and T. Yanagida, *Dynamical tuning of the initial condition for new inflation in supergravity*, *Phys. Lett.* **B411** (1997) 249–255, [[hep-ph/9707201](#)].
- [46] K. Hamaguchi, K.-I. Izawa, and H. Nakajima, *Supersymmetric Inflation of Dynamical Origin*, *Phys. Lett.* **B662** (2008) 208–212, [[arXiv:0801.2204](#)].
- [47] K. Harigaya, M. Ibe, K. Schmitz, and T. T. Yanagida, *Chaotic Inflation with a Fractional Power-Law Potential in Strongly Coupled Gauge Theories*, *Phys. Lett.* **B720** (2013) 125–129, [[arXiv:1211.6241](#)].
- [48] K. Harigaya, M. Ibe, K. Schmitz, and T. T. Yanagida, *Dynamical Chaotic Inflation in the Light of BICEP2*, *Phys. Lett.* **B733** (2014) 283–287, [[arXiv:1403.4536](#)].
- [49] K. Harigaya, M. Ibe, K. Schmitz, and T. T. Yanagida, *Dynamical fractional chaotic inflation*, *Phys. Rev.* **D90** (2014), no. 12 123524, [[arXiv:1407.3084](#)].
- [50] R. Argurio, D. Coone, L. Heurtier, and A. Mariotti, *Sgoldstino-less inflation and low energy SUSY breaking*, *JCAP* **1707** (2017), no. 07 047, [[arXiv:1705.06788](#)].

- [51] I. Antoniadis, A. Chatrabhuti, H. Isono, and R. Knoops, *Inflation from Supersymmetry Breaking*, *Eur. Phys. J.* **C77** (2017), no. 11 724, [[arXiv:1706.04133](#)].
- [52] E. Dudas, T. Gherghetta, Y. Mambrini, and K. A. Olive, *Inflation and High-Scale Supersymmetry with an EeV Gravitino*, [arXiv:1710.07341](#).
- [53] P. Binetruy and G. R. Dvali, *D term inflation*, *Phys. Lett.* **B388** (1996) 241–246, [[hep-ph/9606342](#)].
- [54] E. Halyo, *Hybrid inflation from supergravity D terms*, *Phys. Lett.* **B387** (1996) 43–47, [[hep-ph/9606423](#)].
- [55] J. L. Evans, T. Gherghetta, N. Nagata, and M. Peloso, *Low-scale D-term inflation and the relaxion mechanism*, *Phys. Rev.* **D95** (2017), no. 11 115027, [[arXiv:1704.03695](#)].
- [56] T. Higaki, K. S. Jeong, and F. Takahashi, *Hybrid inflation in high-scale supersymmetry*, *JHEP* **12** (2012) 111, [[arXiv:1211.0994](#)].
- [57] C. Pallis and Q. Shafi, *From Hybrid to Quadratic Inflation With High-Scale Supersymmetry Breaking*, *Phys. Lett.* **B736** (2014) 261–266, [[arXiv:1405.7645](#)].
- [58] K. Kadota, T. Kobayashi, and K. Sumita, *A viable D-term hybrid inflation model*, *JCAP* **1711** (2017), no. 11 033, [[arXiv:1707.00813](#)].
- [59] A. D. Linde, *Axions in inflationary cosmology*, *Phys. Lett.* **B259** (1991) 38–47.
- [60] A. D. Linde, *Hybrid inflation*, *Phys. Rev.* **D49** (1994) 748–754, [[astro-ph/9307002](#)].
- [61] W. Buchmüller, K. Schmitz, and G. Vertongen, *Matter and Dark Matter from False Vacuum Decay*, *Phys. Lett.* **B693** (2010) 421–425, [[arXiv:1008.2355](#)].
- [62] W. Buchmüller, K. Schmitz, and G. Vertongen, *Entropy, Baryon Asymmetry and Dark Matter from Heavy Neutrino Decays*, *Nucl. Phys.* **B851** (2011) 481–532, [[arXiv:1104.2750](#)].
- [63] W. Buchmüller, V. Domcke, and K. Schmitz, *Spontaneous B-L Breaking as the Origin of the Hot Early Universe*, *Nucl. Phys.* **B862** (2012) 587–632, [[arXiv:1202.6679](#)].
- [64] W. Buchmüller, V. Domcke, and K. Schmitz, *WIMP Dark Matter from Gravitino Decays and Leptogenesis*, *Phys. Lett.* **B713** (2012) 63–67, [[arXiv:1203.0285](#)].
- [65] K. Schmitz, *The B-L Phase Transition: Implications for Cosmology and Neutrinos*. PhD thesis, Hamburg U., 2012. [arXiv:1307.3887](#).
- [66] W. Buchmüller, V. Domcke, K. Kamada, and K. Schmitz, *The Gravitational Wave Spectrum from Cosmological B – L Breaking*, *JCAP* **1310** (2013) 003, [[arXiv:1305.3392](#)].

- [67] W. Buchmüller, V. Domcke, K. Kamada, and K. Schmitz, *A Minimal Supersymmetric Model of Particle Physics and the Early Universe*, in *Cosmology and Particle Physics beyond Standard Models* (L. Álvarez-Gaumé, G. S. Djordjević, and D. Stojković, eds.), CERN-Proceedings-2014-001, pp. 47–77. CERN, Geneva, 2014. [arXiv:1309.7788](#).
- [68] V. Domcke, *Matter, Dark Matter and Gravitational Waves from a GUT-Scale U(1) Phase Transition*. PhD thesis, Hamburg U., 2013.
- [69] M. Fukugita and T. Yanagida, *Baryogenesis Without Grand Unification*, *Phys. Lett.* **B174** (1986) 45–47.
- [70] P. Minkowski, $\mu \rightarrow e\gamma$ at a Rate of One Out of 10^9 Muon Decays?, *Phys. Lett.* **67B** (1977) 421–428.
- [71] T. Yanagida, *Horizontal Symmetry and Masses of Neutrinos*, *Conf. Proc.* **C7902131** (1979) 95–99.
- [72] T. Yanagida, *Horizontal Symmetry and Masses of Neutrinos*, *Prog. Theor. Phys.* **64** (1980) 1103.
- [73] M. Gell-Mann, P. Ramond, and R. Slansky, *Complex Spinors and Unified Theories*, *Conf. Proc.* **C790927** (1979) 315–321, [[arXiv:1306.4669](#)].
- [74] R. N. Mohapatra and G. Senjanovic, *Neutrino Mass and Spontaneous Parity Violation*, *Phys. Rev. Lett.* **44** (1980) 912.
- [75] **Planck** Collaboration, P. A. R. Ade et al., *Planck 2015 results. XX. Constraints on inflation*, *Astron. Astrophys.* **594** (2016) A20, [[arXiv:1502.02114](#)].
- [76] E. J. Copeland, A. R. Liddle, D. H. Lyth, E. D. Stewart, and D. Wands, *False vacuum inflation with Einstein gravity*, *Phys. Rev.* **D49** (1994) 6410–6433, [[astro-ph/9401011](#)].
- [77] G. R. Dvali, Q. Shafi, and R. K. Schaefer, *Large scale structure and supersymmetric inflation without fine tuning*, *Phys. Rev. Lett.* **73** (1994) 1886–1889, [[hep-ph/9406319](#)].
- [78] L. O’Raifeartaigh, *Spontaneous Symmetry Breaking for Chiral Scalar Superfields*, *Nucl. Phys.* **B96** (1975) 331–352.
- [79] P. Fayet and J. Iliopoulos, *Spontaneously Broken Supergauge Symmetries and Goldstone Spinors*, *Phys. Lett.* **51B** (1974) 461–464.
- [80] C. Panagiotakopoulos, *Blue perturbation spectra from hybrid inflation with canonical supergravity*, *Phys. Rev.* **D55** (1997) R7335–R7339, [[hep-ph/9702433](#)].
- [81] A. D. Linde and A. Riotto, *Hybrid inflation in supergravity*, *Phys. Rev.* **D56** (1997) R1841–R1844, [[hep-ph/9703209](#)].

- [82] M. U. Rehman, Q. Shafi, and J. R. Wickman, *Supersymmetric Hybrid Inflation Redux*, *Phys. Lett.* **B683** (2010) 191–195, [[arXiv:0908.3896](#)].
- [83] M. U. Rehman, Q. Shafi, and J. R. Wickman, *Minimal Supersymmetric Hybrid Inflation, Flipped $SU(5)$ and Proton Decay*, *Phys. Lett.* **B688** (2010) 75–81, [[arXiv:0912.4737](#)].
- [84] K. Nakayama, F. Takahashi, and T. T. Yanagida, *Constraint on the gravitino mass in hybrid inflation*, *JCAP* **1012** (2010) 010, [[arXiv:1007.5152](#)].
- [85] W. Buchmüller, V. Domcke, K. Kamada, and K. Schmitz, *Hybrid Inflation in the Complex Plane*, *JCAP* **1407** (2014) 054, [[arXiv:1404.1832](#)].
- [86] Z. Komargodski and N. Seiberg, *Comments on the Fayet-Iliopoulos Term in Field Theory and Supergravity*, *JHEP* **06** (2009) 007, [[arXiv:0904.1159](#)].
- [87] K. R. Dienes and B. Thomas, *On the Inconsistency of Fayet-Iliopoulos Terms in Supergravity Theories*, *Phys. Rev.* **D81** (2010) 065023, [[arXiv:0911.0677](#)].
- [88] T. Banks and N. Seiberg, *Symmetries and Strings in Field Theory and Gravity*, *Phys. Rev.* **D83** (2011) 084019, [[arXiv:1011.5120](#)].
- [89] M. Dine, N. Seiberg, and E. Witten, *Fayet-Iliopoulos Terms in String Theory*, *Nucl. Phys.* **B289** (1987) 589–598.
- [90] J. J. Atick, L. J. Dixon, and A. Sen, *String Calculation of Fayet-Iliopoulos d Terms in Arbitrary Supersymmetric Compactifications*, *Nucl. Phys.* **B292** (1987) 109–149.
- [91] M. B. Green and J. H. Schwarz, *Anomaly Cancellation in Supersymmetric $D=10$ Gauge Theory and Superstring Theory*, *Phys. Lett.* **149B** (1984) 117–122.
- [92] Z. Komargodski and N. Seiberg, *Comments on Supercurrent Multiplets, Supersymmetric Field Theories and Supergravity*, *JHEP* **07** (2010) 017, [[arXiv:1002.2228](#)].
- [93] P. Binetruy, G. Dvali, R. Kallosh, and A. Van Proeyen, *Fayet-Iliopoulos terms in supergravity and cosmology*, *Class. Quant. Grav.* **21** (2004) 3137–3170, [[hep-th/0402046](#)].
- [94] G. D. Coughlan, W. Fischler, E. W. Kolb, S. Raby, and G. G. Ross, *Cosmological Problems for the Polonyi Potential*, *Phys. Lett.* **131B** (1983) 59–64.
- [95] J. R. Ellis, D. V. Nanopoulos, and M. Quiros, *On the Axion, Dilaton, Polonyi, Gravitino and Shadow Matter Problems in Supergravity and Superstring Models*, *Phys. Lett.* **B174** (1986) 176–182.
- [96] V. Domcke, K. Schmitz, and T. T. Yanagida, *Dynamical D -Terms in Supergravity*, *Nucl. Phys.* **B891** (2015) 230–258, [[arXiv:1410.4641](#)].
- [97] T. W. B. Kibble, *Topology of Cosmic Domains and Strings*, *J. Phys.* **A9** (1976) 1387–1398.

- [98] R. Jeannerot, J. Rocher, and M. Sakellariadou, *How generic is cosmic string formation in SUSY GUTs*, *Phys. Rev.* **D68** (2003) 103514, [[hep-ph/0308134](#)].
- [99] A. Vilenkin, *Cosmic Strings and Domain Walls*, *Phys. Rept.* **121** (1985) 263–315.
- [100] M. B. Hindmarsh and T. W. B. Kibble, *Cosmic strings*, *Rept. Prog. Phys.* **58** (1995) 477–562, [[hep-ph/9411342](#)].
- [101] **Planck** Collaboration, P. A. R. Ade et al., *Planck 2013 results. XXV. Searches for cosmic strings and other topological defects*, *Astron. Astrophys.* **571** (2014) A25, [[arXiv:1303.5085](#)].
- [102] **Planck** Collaboration, P. A. R. Ade et al., *Planck 2015 results. XIII. Cosmological parameters*, *Astron. Astrophys.* **594** (2016) A13, [[arXiv:1502.01589](#)].
- [103] S. A. Sanidas, R. A. Battye, and B. W. Stappers, *Constraints on cosmic string tension imposed by the limit on the stochastic gravitational wave background from the European Pulsar Timing Array*, *Phys. Rev.* **D85** (2012) 122003, [[arXiv:1201.2419](#)].
- [104] J. J. Blanco-Pillado, K. D. Olum, and X. Siemens, *New limits on cosmic strings from gravitational wave observation*, [[arXiv:1709.02434](#)].
- [105] C. Ringeval and T. Suyama, *Stochastic gravitational waves from cosmic string loops in scaling*, *JCAP* **1712** (2017), no. 12 027, [[arXiv:1709.03845](#)].
- [106] H. F. Santana Mota and M. Hindmarsh, *Big-Bang Nucleosynthesis and Gamma-Ray Constraints on Cosmic Strings with a large Higgs condensate*, *Phys. Rev.* **D91** (2015), no. 4 043001, [[arXiv:1407.3599](#)].
- [107] T. Charnock, A. Avgoustidis, E. J. Copeland, and A. Moss, *CMB constraints on cosmic strings and superstrings*, *Phys. Rev.* **D93** (2016), no. 12 123503, [[arXiv:1603.01275](#)].
- [108] J. Lizarraga, J. Urrestilla, D. Daverio, M. Hindmarsh, and M. Kunz, *New CMB constraints for Abelian Higgs cosmic strings*, *JCAP* **1610** (2016), no. 10 042, [[arXiv:1609.03386](#)].
- [109] R. Battye, B. Garbrecht, and A. Moss, *Tight constraints on F- and D-term hybrid inflation scenarios*, *Phys. Rev.* **D81** (2010) 123512, [[arXiv:1001.0769](#)].
- [110] K. S. Babu, K. Schmitz, and T. T. Yanagida, *Pure gravity mediation and spontaneous B–L breaking from strong dynamics*, *Nucl. Phys.* **B905** (2016) 73–95, [[arXiv:1507.04467](#)].
- [111] H. P. Nilles, *Supersymmetry, Supergravity and Particle Physics*, *Phys. Rept.* **110** (1984) 1–162.
- [112] S. Ferrara, R. Kallosh, A. Linde, A. Marrani, and A. Van Proeyen, *Jordan Frame Supergravity and Inflation in NMSSM*, *Phys. Rev.* **D82** (2010) 045003, [[arXiv:1004.0712](#)].
- [113] S. Ferrara, R. Kallosh, A. Linde, A. Marrani, and A. Van Proeyen, *Superconformal Symmetry, NMSSM, and Inflation*, *Phys. Rev.* **D83** (2011) 025008, [[arXiv:1008.2942](#)].

- [114] M. Postma and M. Volponi, *Equivalence of the Einstein and Jordan frames*, *Phys. Rev.* **D90** (2014), no. 10 103516, [[arXiv:1407.6874](#)].
- [115] A. Yu. Kamenshchik and C. F. Steinwachs, *Question of quantum equivalence between Jordan frame and Einstein frame*, *Phys. Rev.* **D91** (2015), no. 8 084033, [[arXiv:1408.5769](#)].
- [116] K. S. Stelle and P. C. West, *Minimal Auxiliary Fields for Supergravity*, *Phys. Lett.* **74B** (1978) 330–332.
- [117] S. Ferrara and P. van Nieuwenhuizen, *The Auxiliary Fields of Supergravity*, *Phys. Lett.* **74B** (1978) 333.
- [118] E. Cremmer, S. Ferrara, L. Girardello, and A. Van Proeyen, *Yang-Mills Theories with Local Supersymmetry: Lagrangian, Transformation Laws and SuperHiggs Effect*, *Nucl. Phys.* **B212** (1983) 413.
- [119] T. Kugo and S. Uehara, *Improved Superconformal Gauge Conditions in the $N = 1$ Supergravity Yang-Mills Matter System*, *Nucl. Phys.* **B222** (1983) 125–138.
- [120] W. Buchmüller, V. Domcke, and K. Schmitz, *Superconformal D-Term Inflation*, *JCAP* **1304** (2013) 019, [[arXiv:1210.4105](#)].
- [121] W. Buchmüller, V. Domcke, and K. Kamada, *The Starobinsky Model from Superconformal D-Term Inflation*, *Phys. Lett.* **B726** (2013) 467–470, [[arXiv:1306.3471](#)].
- [122] L. Randall and R. Sundrum, *Out of this world supersymmetry breaking*, *Nucl. Phys.* **B557** (1999) 79–118, [[hep-th/9810155](#)].
- [123] M. A. Luty and R. Sundrum, *Supersymmetry breaking and composite extra dimensions*, *Phys. Rev.* **D65** (2002) 066004, [[hep-th/0105137](#)].
- [124] M. Luty and R. Sundrum, *Anomaly mediated supersymmetry breaking in four-dimensions, naturally*, *Phys. Rev.* **D67** (2003) 045007, [[hep-th/0111231](#)].
- [125] M. Ibe, K. I. Izawa, Y. Nakayama, Y. Shinbara, and T. Yanagida, *Conformally sequestered SUSY breaking in vector-like gauge theories*, *Phys. Rev.* **D73** (2006) 015004, [[hep-ph/0506023](#)].
- [126] M. Ibe, K. I. Izawa, Y. Nakayama, Y. Shinbara, and T. Yanagida, *More on conformally sequestered SUSY breaking*, *Phys. Rev.* **D73** (2006) 035012, [[hep-ph/0509229](#)].
- [127] E. Cremmer, S. Ferrara, C. Kounnas, and D. V. Nanopoulos, *Naturally Vanishing Cosmological Constant in $N=1$ Supergravity*, *Phys. Lett.* **133B** (1983) 61.
- [128] J. R. Ellis, A. B. Lahanas, D. V. Nanopoulos, and K. Tamvakis, *No-Scale Supersymmetric Standard Model*, *Phys. Lett.* **134B** (1984) 429.
- [129] A. B. Lahanas and D. V. Nanopoulos, *The Road to No Scale Supergravity*, *Phys. Rept.* **145** (1987) 1.

- [130] E. Witten, *Dimensional Reduction of Superstring Models*, *Phys. Lett.* **155B** (1985) 151.
- [131] E. D. Stewart, *Inflation, supergravity and superstrings*, *Phys. Rev.* **D51** (1995) 6847–6853, [[hep-ph/9405389](#)].
- [132] T. T. Dumitrescu, Z. Komargodski, and M. Sudano, *Global Symmetries and D-Terms in Supersymmetric Field Theories*, *JHEP* **11** (2010) 052, [[arXiv:1007.5352](#)].
- [133] Y. Kawamura, *Limitation on Magnitude of D-components*, *Prog. Theor. Phys.* **125** (2011) 509–520, [[arXiv:1008.5223](#)].
- [134] M. Kawasaki, M. Yamaguchi, and T. Yanagida, *Natural chaotic inflation in supergravity*, *Phys. Rev. Lett.* **85** (2000) 3572–3575, [[hep-ph/0004243](#)].
- [135] M. T. Grisaru, W. Siegel, and M. Rocek, *Improved Methods for Supergraphs*, *Nucl. Phys.* **B159** (1979) 429.
- [136] I. L. Buchbinder, S. Kuzenko, and Z. Yarevskaya, *Supersymmetric effective potential: Superfield approach*, *Nucl. Phys.* **B411** (1994) 665–692.
- [137] M. T. Grisaru, M. Rocek, and R. von Unge, *Effective Kahler potentials*, *Phys. Lett.* **B383** (1996) 415–421, [[hep-th/9605149](#)].
- [138] A. Brignole, *One loop Kahler potential in non renormalizable theories*, *Nucl. Phys.* **B579** (2000) 101–116, [[hep-th/0001121](#)].
- [139] S. Groot Nibbelink and T. S. Nyawelo, *Effective action of softly broken supersymmetric theories*, *Phys. Rev.* **D75** (2007) 045002, [[hep-th/0612092](#)].
- [140] O. Seto and J. Yokoyama, *Hiding cosmic strings in supergravity D-term inflation*, *Phys. Rev.* **D73** (2006) 023508, [[hep-ph/0508172](#)].
- [141] C.-M. Lin and J. McDonald, *Supergravity modification of D-term hybrid inflation: Solving the cosmic string and spectral index problems via a right-handed sneutrino*, *Phys. Rev.* **D74** (2006) 063510, [[hep-ph/0604245](#)].
- [142] J. Rocher and M. Sakellariadou, *D-term inflation in non-minimal supergravity*, *JCAP* **0611** (2006) 001, [[hep-th/0607226](#)].
- [143] W. Buchmüller, V. Domcke, and C. Wieck, *No-scale D-term inflation with stabilized moduli*, *Phys. Lett.* **B730** (2014) 155–160, [[arXiv:1309.3122](#)].
- [144] K.-I. Izawa and T. Yanagida, *Dynamical supersymmetry breaking in vector-like gauge theories*, *Prog. Theor. Phys.* **95** (1996) 829–830, [[hep-th/9602180](#)].
- [145] K. A. Intriligator and S. D. Thomas, *Dynamical supersymmetry breaking on quantum moduli spaces*, *Nucl. Phys.* **B473** (1996) 121–142, [[hep-th/9603158](#)].

- [146] A. Manohar and H. Georgi, *Chiral Quarks and the Nonrelativistic Quark Model*, *Nucl. Phys.* **B234** (1984) 189–212.
- [147] H. Georgi and L. Randall, *Flavor Conserving CP Violation in Invisible Axion Models*, *Nucl. Phys.* **B276** (1986) 241–252.
- [148] M. A. Luty, *Naive dimensional analysis and supersymmetry*, *Phys. Rev.* **D57** (1998) 1531–1538, [[hep-ph/9706235](#)].
- [149] A. G. Cohen, D. B. Kaplan, and A. E. Nelson, *Counting 4 pis in strongly coupled supersymmetry*, *Phys. Lett.* **B412** (1997) 301–308, [[hep-ph/9706275](#)].
- [150] N. Seiberg, *Exact results on the space of vacua of four-dimensional SUSY gauge theories*, *Phys. Rev.* **D49** (1994) 6857–6863, [[hep-th/9402044](#)].
- [151] Z. Chacko, M. A. Luty, and E. Ponton, *Calculable dynamical supersymmetry breaking on deformed moduli spaces*, *JHEP* **12** (1998) 016, [[hep-th/9810253](#)].
- [152] K. Harigaya, M. Ibe, K. Schmitz, and T. T. Yanagida, *Peccei-Quinn Symmetry from Dynamical Supersymmetry Breaking*, *Phys. Rev.* **D92** (2015), no. 7 075003, [[arXiv:1505.07388](#)].
- [153] J. Polonyi, *Generalization of the Massive Scalar Multiplet Coupling to the Supergravity*, Tech. Rep. KFKI-77-93, Hungary Central Research Institute, 1977.
- [154] S. R. Coleman and E. J. Weinberg, *Radiative Corrections as the Origin of Spontaneous Symmetry Breaking*, *Phys. Rev.* **D7** (1973) 1888–1910.
- [155] S. P. Martin, *Two loop effective potential for a general renormalizable theory and softly broken supersymmetry*, *Phys. Rev.* **D65** (2002) 116003, [[hep-ph/0111209](#)].
- [156] K. Intriligator and M. Sudano, *General Gauge Mediation with Gauge Messengers*, *JHEP* **06** (2010) 047, [[arXiv:1001.5443](#)].
- [157] T. Chiba and M. Yamaguchi, *Extended Slow-Roll Conditions and Rapid-Roll Conditions*, *JCAP* **0810** (2008) 021, [[arXiv:0807.4965](#)].
- [158] W. Buchmüller, V. Domcke, and K. Schmitz, *The Chaotic Regime of D-Term Inflation*, *JCAP* **1411** (2014), no. 11 006, [[arXiv:1406.6300](#)].
- [159] W. Buchmüller and K. Ishiwata, *Grand Unification and Subcritical Hybrid Inflation*, *Phys. Rev.* **D91** (2015), no. 8 081302, [[arXiv:1412.3764](#)].
- [160] T. Watari and T. Yanagida, *$N=2$ supersymmetry in a hybrid inflation model*, *Phys. Lett.* **B499** (2001) 297–304, [[hep-ph/0011389](#)].
- [161] S. P. Martin, *A Supersymmetry primer*, *Adv. Ser. Direct. High Energy Phys.* **21** (2010) 1–153, [[hep-ph/9709356](#)]. [*Adv. Ser. Direct. High Energy Phys.* **18** (1998) 1–98].

- [162] K. A. Olive and M. Srednicki, *New Limits on Parameters of the Supersymmetric Standard Model from Cosmology*, *Phys. Lett.* **B230** (1989) 78–82.
- [163] K. Griest, M. Kamionkowski, and M. S. Turner, *Supersymmetric Dark Matter Above the W Mass*, *Phys. Rev.* **D41** (1990) 3565–3582.
- [164] K. Harigaya, M. Ibe, and T. T. Yanagida, *A Closer Look at Gaugino Masses in Pure Gravity Mediation Model/Minimal Split SUSY Model*, *JHEP* **12** (2013) 016, [[arXiv:1310.0643](#)].
- [165] K. S. Jeong and F. Takahashi, *A Gravitino-rich Universe*, *JHEP* **01** (2013) 173, [[arXiv:1210.4077](#)].
- [166] T. Gherghetta, G. F. Giudice, and J. D. Wells, *Phenomenological consequences of supersymmetry with anomaly induced masses*, *Nucl. Phys.* **B559** (1999) 27–47, [[hep-ph/9904378](#)].
- [167] M. Ibe, R. Kitano, H. Murayama, and T. Yanagida, *Viable supersymmetry and leptogenesis with anomaly mediation*, *Phys. Rev.* **D70** (2004) 075012, [[hep-ph/0403198](#)].
- [168] M. Bolz, A. Brandenburg, and W. Buchmüller, *Thermal production of gravitinos*, *Nucl. Phys.* **B606** (2001) 518–544, [[hep-ph/0012052](#)]. [Erratum: *Nucl. Phys.* **B790** (2008) 336–337].
- [169] M. Kawasaki, F. Takahashi, and T. T. Yanagida, *Gravitino overproduction in inflaton decay*, *Phys. Lett.* **B638** (2006) 8–12, [[hep-ph/0603265](#)].
- [170] J. Hisano, S. Matsumoto, M. Nagai, O. Saito, and M. Senami, *Non-perturbative effect on thermal relic abundance of dark matter*, *Phys. Lett.* **B646** (2007) 34–38, [[hep-ph/0610249](#)].
- [171] M. Cirelli, A. Strumia, and M. Tamburini, *Cosmology and Astrophysics of Minimal Dark Matter*, *Nucl. Phys.* **B787** (2007) 152–175, [[arXiv:0706.4071](#)].
- [172] R. Barbier et al., *R-parity violating supersymmetry*, *Phys. Rept.* **420** (2005) 1–202, [[hep-ph/0406039](#)].
- [173] V. F. Mukhanov, H. A. Feldman, and R. H. Brandenberger, *Theory of cosmological perturbations. Part 1. Classical perturbations. Part 2. Quantum theory of perturbations. Part 3. Extensions*, *Phys. Rept.* **215** (1992) 203–333.
- [174] A. Vilenkin, *Gravitational Field of Vacuum Domain Walls and Strings*, *Phys. Rev.* **D23** (1981) 852–857.
- [175] G. B. Gelmini, M. Gleiser, and E. W. Kolb, *Cosmology of Biased Discrete Symmetry Breaking*, *Phys. Rev.* **D39** (1989) 1558.
- [176] S. E. Larsson, S. Sarkar, and P. L. White, *Evading the cosmological domain wall problem*, *Phys. Rev.* **D55** (1997) 5129–5135, [[hep-ph/9608319](#)].

- [177] P. Sikivie, *Of Axions, Domain Walls and the Early Universe*, *Phys. Rev. Lett.* **48** (1982) 1156–1159.
- [178] S. Chang, C. Hagmann, and P. Sikivie, *Studies of the motion and decay of axion walls bounded by strings*, *Phys. Rev.* **D59** (1999) 023505, [[hep-ph/9807374](#)].
- [179] K.-S. Choi, H. P. Nilles, S. Ramos-Sanchez, and P. K. S. Vaudrevange, *Accions*, *Phys. Lett.* **B675** (2009) 381–386, [[arXiv:0902.3070](#)].
- [180] A. G. Dias, A. C. B. Machado, C. C. Nishi, A. Ringwald, and P. Vaudrevange, *The Quest for an Intermediate-Scale Accidental Axion and Further ALPs*, *JHEP* **06** (2014) 037, [[arXiv:1403.5760](#)].
- [181] A. Ringwald and K. Saikawa, *Axion dark matter in the post-inflationary Peccei-Quinn symmetry breaking scenario*, *Phys. Rev.* **D93** (2016), no. 8 085031, [[arXiv:1512.06436](#)]. [Addendum: *Phys. Rev.* **D94** (2016) no.4 049908].
- [182] K. Nakayama, F. Takahashi, and N. Yokozaki, *Gravitational waves from domain walls and their implications*, *Phys. Lett.* **B770** (2017) 500–506, [[arXiv:1612.08327](#)].
- [183] K. Saikawa, *A review of gravitational waves from cosmic domain walls*, *Universe* **3** (2017), no. 2 40, [[arXiv:1703.02576](#)].
- [184] S. A. R. Ellis and J. D. Wells, *High-scale supersymmetry, the Higgs boson mass, and gauge unification*, *Phys. Rev.* **D96** (2017), no. 5 055024, [[arXiv:1706.00013](#)].
- [185] S. A. R. Ellis and J. D. Wells, *Visualizing gauge unification with high-scale thresholds*, *Phys. Rev.* **D91** (2015), no. 7 075016, [[arXiv:1502.01362](#)].
- [186] J. Wess and J. Bagger, *Supersymmetry and supergravity*. Princeton Series in Physics. Princeton University Press, Princeton, New Jersey, second ed., 1992. 259 pages.