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Axion-electron decoupling in nucleophobic axion models

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The strongest upper bounds on the axion mass come from astrophysical observations like the neutrino burst duration of SN1987A, which depends on the axion couplings to nucleons, or the white-dwarf cooling rates and red-giant evolution, which involve the axion-electron coupling. It has been recently argued that in variants of DFSZ models with generation-dependent Peccei-Quinn charges an approximate axion-nucleon decoupling can occur, strongly relaxing the SN1987A bound. However, as in standard DFSZ models, the axion remains in general coupled to electrons, unless an *ad hoc* cancellation is engineered. Here we show that axion-electron decoupling can be implemented without extra tunings in DFSZ-like models with three Higgs doublets. Remarkably, the numerical value of the quark mass ratio $m_u/m_d \sim 1/2$ is crucial to open up this possibility.

I. INTRODUCTION

It has been recently argued [1] that in variants of Dine-Fischler-Srednicki-Zhitnitsky (DFSZ) [2, 3] models with two Higgs doublets and generation-dependent Peccei-Quinn (PQ) charges, it is possible to strongly suppress axion couplings to nucleons (axion nucleophobia). This implies that the upper limit on the DFSZ axion mass from the neutrino burst duration of the supernova (SN) SN1987A, which is particularly strong and generally considered ineludible, can in fact be sizeably relaxed.¹ The parameter space region that opens up for nucleophobic axions is, however, only marginal. This is because in DFSZ models the axion also couples to electrons, and then limits from anomalous cooling of white dwarfs and red giants, which are only moderately less restrictive, apply. On the other hand, generation-dependent PQ charges imply that the axion couplings to the mass eigenstate fermions receive corrections from inter-generational mixing. In Ref. [1] this type of effect was invoked to arrange for a tuned cancellation between two contributions to the axion-electron coupling: one proportional to the electron PQ charge, and the other coming from inter-generational mixing between the leptons. This allows the construction of models of nucleophobic *and* electrophobic axions that can evade all the tightest astrophysical bounds (astrophobic axions). Although the tuning of the cancellation required to achieve a significant level of electrophobia is at the level of 10%, astrophobic axion models

constructed in this way are admittedly not particularly elegant. In this short note we put forth a more natural way to achieve astrophobia, which requires extending the scalar sector by a third Higgs doublet, but does not involve any *ad hoc* cancellation between different contributions to the axion-electron coupling. Remarkably, this mechanism implies a strong correlation between the couplings whereby the higher the level of suppression of the axion-nucleon coupling, the more the axion becomes electrophobic. Intriguingly, the mechanism can be implemented thanks to the fact that the light quark mass ratio is close to $m_u/m_d \approx 1/2$.

II. THE CONDITIONS FOR NUCLEOPHOBIA

Let us first recall the conditions for nucleophobia. We define the axion couplings to nucleons via

$$\frac{C_{\mathcal{N}}}{2f_a} \partial_\mu a \bar{\mathcal{N}} \gamma^\mu \gamma_5 \mathcal{N}, \quad (1)$$

with $\mathcal{N} = p, n$, while the fundamental couplings of the axion to quarks C_q , with $q = u, d, \dots$ are defined from a similar expression by replacing $\mathcal{N} \rightarrow q$ and $C_{\mathcal{N}} \rightarrow C_q$. $C_{\mathcal{N}}$ can be expressed in terms of C_q using non-perturbative inputs from nucleon matrix elements [9]. To understand the mechanism behind axion-nucleon decoupling, it is convenient to consider the two linear combinations $C_p \pm C_n$ and express them in terms of the C_q . This yields

$$C_p + C_n = 0.50 (C_u + C_d - 1) - 2\delta_s, \quad (2)$$

$$C_p - C_n = 1.27 (C_u - C_d - f_{ud}), \quad (3)$$

where, in the second line, $f_{ud} = f_u - f_d$, with $f_{u,d} = m_{d,u}/(m_d + m_u)$ the model-independent contributions induced by the axion coupling to gluons, chosen in such a way that the axion does not mix with π^0 . In the

¹ For Kim-Shifman-Vainshtein-Zakharov (KSVZ) [4, 5] axions instead, no suppression mechanism for the axion couplings to nucleons can be enforced, since they are determined in a model-independent way, and yield the often quoted limit $m_a \lesssim 0.02$ eV [6]. Note, however, that recent analyses of the axion emissivity from the SN core hint to a weakening of the bound by a factor of a few [7, 8].

first line, $1 = f_u + f_d$ is an exact number, while $\delta_s = 0.038 C_s + 0.012 C_c + 0.009 C_b + 0.0035 C_t$ is a small $\mathcal{O}(5\%)$ correction dominated by the s -quark contribution. Nucleophobia requires $C_p \pm C_n \approx 0$, which is possible in variant DFSZ models with two Higgs doublets $H_{1,2}$ and non-universal PQ charge assignment [1]. To see this, let us focus on the first generation Yukawa terms

$$\bar{q}_1 u_1 H_1 + \bar{q}_1 d_1 \tilde{H}_2, \quad (4)$$

where $\tilde{H}_2 = i\sigma_2 H_2^*$. The axion couplings to the light quark fields (neglecting flavour mixing, which is assumed to be small throughout this paper²) are

$$C_u = \frac{1}{2N} (\mathcal{X}_{u_1} - \mathcal{X}_{q_1}) = -\frac{\mathcal{X}_1}{2N}, \quad (5)$$

$$C_d = \frac{1}{2N} (\mathcal{X}_{d_1} - \mathcal{X}_{q_1}) = \frac{\mathcal{X}_2}{2N}. \quad (6)$$

Here $\mathcal{X}_{u_1} = \mathcal{X}(u_1)$, etc. denote the PQ charges of the fermion fields while $\mathcal{X}_{1,2} = \mathcal{X}(H_{1,2})$. The coefficient of the PQ colour anomaly is then

$$2N = \sum_{i=1}^3 (\mathcal{X}_{u_i} + \mathcal{X}_{d_i} - 2\mathcal{X}_{q_i}). \quad (7)$$

It is also convenient to define the contribution to the color anomaly from light quarks only:

$$2N_\ell = \mathcal{X}_{u_1} + \mathcal{X}_{d_1} - 2\mathcal{X}_{q_1} = \mathcal{X}_2 - \mathcal{X}_1. \quad (8)$$

The first condition for ensuring approximate nucleophobia then reads (cf. Eq. (2))

$$C_u + C_d = \frac{N_\ell}{N} = 1, \quad (9)$$

i.e. only models in which the color anomaly is determined solely by the light u, d quarks (while the contributions from the two heavier generations cancel or vanish identically) have a chance to be nucleophobic.³ As emphasized in [1], this implies that nucleophobic axion models can be realized only if the PQ charges are generation-dependent.

Assuming that the first condition Eq. (9) is satisfied, the second condition (cf. Eq. (3)) reads

$$C_u - C_d = \frac{-\mathcal{X}_1 - \mathcal{X}_2}{2N} = \frac{\mathcal{X}_1 + \mathcal{X}_2}{\mathcal{X}_1 - \mathcal{X}_2} = f_{ud}, \quad (10)$$

that is,

$$\frac{\mathcal{X}_1}{\mathcal{X}_2} = -\frac{m_d}{m_u}. \quad (11)$$

Finally, by imposing the condition which ensures that the physical axion field is orthogonal to the Goldstone field of hypercharge $U(1)_Y$, i.e. $\mathcal{X}_1 v_1^2 + \mathcal{X}_2 v_2^2 = 0$, we obtain a relation between the ratio of the vacuum expectation values (VEVs) $v_{1,2} = \langle H_{1,2} \rangle$ and the ratio of the quark masses that must be satisfied in order to ensure nucleophobia:

$$\frac{v_2^2}{v_1^2} = -\frac{\mathcal{X}_1}{\mathcal{X}_2} = \frac{m_d}{m_u}. \quad (12)$$

With only two Higgs doublets responsible for breaking the electroweak symmetry and for providing masses to all the fermions, the lepton sector is unavoidably charged under the PQ symmetry and, as mentioned in the introduction, electrophobia can only be enforced by tuning a cancellation between the contribution to the axion electron coupling proportional to the electron PQ charge, and corrections arising from lepton flavour mixing [1]. A possible, and more elegant alternative, is to introduce a third Higgs doublet H_3 with PQ charge \mathcal{X}_3 that couples only to the leptons, and verify if the condition $\mathcal{X}_3 \approx 0$ can be consistently implemented. In this case the whole lepton sector would be approximately neutral under the PQ symmetry, and in particular the axion would decouple from the electrons. This possibility is explored in the remainder of the paper.

III. THE CONDITIONS FOR ELECTROPHOBIA

Let us consider a three-Higgs doublet model (3HDM) wherein $H_{1,2}$ couple to quarks as above, while H_3 couples to the leptons. We want to study if electrophobia can be implemented consistently with nucleophobia. Assuming Eq. (9) is satisfied, we have four additional conditions: orthogonality between the physical axion and the hypercharge Goldstone, the second condition for nucleophobia Eq. (11), and two conditions on the PQ charges that follow from the requirement that the four $U(1)$ rephasing symmetries of the kinetic term of the four scalar fields $H_{1,2,3}$ and ϕ (the latter being the Standard Model (SM) singlet, with $\mathcal{X}_\phi = 1$, responsible for PQ breaking) are broken down to $U(1)_Y \times U(1)_{PQ}$. These last two conditions can be implemented either by coupling the leptonic Higgs doublet H_3 to both hadronic Higgses ($H_{1,2}$), or by coupling one of the two hadronic Higgses to the other two doublets:

$$H_3^\dagger H_1 \phi^m + H_3^\dagger H_2 \phi^n \quad \text{or} \quad H_3^\dagger H_{1,2} \phi^m + H_2^\dagger H_1 \phi^n. \quad (13)$$

For renormalizable operators one has, without loss of generality, $m = 1, 2$ and $n = \pm 1, \pm 2$, where negative values of n mean Hermitian conjugation $\phi^n \equiv (\phi^\dagger)^{|n|}$. All in all,

² In the presence of flavour mixing, $C_q \rightarrow C_q + \Delta C_q$, where ΔC_q involves quark mass diagonalization matrices. We refer the reader to [1] for details.

³ It is worthwhile mentioning that a certain number of models sharing precisely this property were found in a recent study of $U(1)$ flavour symmetry for the quark sector [10].

for the first case in Eq. (13) the four conditions read

$$\frac{\mathcal{X}_1}{\mathcal{X}_2} = -\frac{m_d}{m_u}, \quad (14)$$

$$\mathcal{X}_1 v_1^2 + \mathcal{X}_2 v_2^2 + \mathcal{X}_3 v_3^2 = 0, \quad (15)$$

$$-\mathcal{X}_3 + \mathcal{X}_1 + m = 0, \quad (16)$$

$$-\mathcal{X}_3 + \mathcal{X}_2 + n = 0. \quad (17)$$

To see if there is a consistent charge assignment that allows us to decouple the axion from the leptons, let us set $\mathcal{X}_3 \rightarrow 0$. In this limit, Eq. (15) reduces to the previous condition, Eq. (12), while Eqs. (16)–(17) imply $\mathcal{X}_1/\mathcal{X}_2 = m/n$ which, together with Eq. (14), yields

$$\frac{m_d}{m_u} = -\frac{m}{n}. \quad (18)$$

Hence, with the first choice of operators in Eq. (13), electrophobia can be consistently implemented for the following values of the light quark mass ratio: $m_d/m_u = 2, 1, 1/2$. It is a fortunate coincidence that the actual value $m_u/m_d = 0.48(3)$ is perfectly compatible with the first possibility. This renders it possible to have electrophobia together with nucleophobia by means of a suitable assignment of PQ charges, rather than by tuning of some parameters. By contrast, if the breaking $U(1)^4 \rightarrow U(1)_Y \times U(1)_{PQ}$ is enforced via the second set of operators in Eq. (13), respectively with H_1 or H_2 in the first term, electrophobia would require $m_d/m_u = 1$ or ∞ in the first case, and $m_d/m_u = 1$ or 0 in the latter, implying that for both these cases electrophobia would not be compatible with nucleophobia.

IV. ASTROPHOBIC AXIONS IN 3HDM MODELS

In the previous sections we have spelled out which conditions need to be satisfied to enforce axion-nucleon and axion-electron decoupling. Clearly, in a realistic scenario we expect that these conditions are realized only at some level of approximation, so that $C_{p,n,e}$, rather than vanish, will just be suppressed. We will now study more quantitatively the interrelation between nucleophobia and electrophobia, and the conditions to realize astrophobia with different levels of accuracy.

According to the results of the previous section, let us assume that the scalar potential contains the following terms:

$$H_3^\dagger H_1 \phi^2 + H_3^\dagger H_2 \phi^\dagger. \quad (19)$$

This corresponds to take $m = 2$ and $n = -1$ in Eq. (13) (first case). For the quarks we assume a $2 + 1$ structure with the PQ charges for the first generation equal to the ones of the second generation, as in model (i_1) in [1]. It is then sufficient to list the Yukawa operators involving just the second and third generations:

$$\begin{aligned} \bar{q}_2 u_2 H_1, \quad \bar{q}_3 u_3 H_2, \quad \bar{q}_2 u_3 H_1, \quad \bar{q}_3 u_2 H_2, \\ \bar{q}_2 d_2 \tilde{H}_2, \quad \bar{q}_3 d_3 \tilde{H}_1, \quad \bar{q}_2 d_3 \tilde{H}_2, \quad \bar{q}_3 d_2 \tilde{H}_1. \end{aligned} \quad (20)$$

We now assume that the leptons couple to a third Higgs doublet with the same charges for all generations:

$$\bar{\ell}_i e_j \tilde{H}_3. \quad (21)$$

Eqs. (16)–(17) imply $\mathcal{X}_1 = \mathcal{X}_3 - 2$ and $\mathcal{X}_2 = \mathcal{X}_3 + 1$. Neglecting flavour mixings, the diagonal axion couplings to quarks and leptons read

$$\begin{aligned} C_{u,c} &= \frac{2}{3} - \frac{\mathcal{X}_3}{3}, & C_t &= -\frac{1}{3} - \frac{\mathcal{X}_3}{3}, \\ C_{d,s} &= \frac{1}{3} + \frac{\mathcal{X}_3}{3}, & C_b &= -\frac{2}{3} + \frac{\mathcal{X}_3}{3}, \\ C_{e,\mu,\tau} &= \frac{\mathcal{X}_3}{3}. \end{aligned} \quad (22)$$

The nucleophobic condition in Eq. (10) then reads

$$\mathcal{X}_3 = \frac{1}{2} - \frac{3}{2} f_{ud} \approx -0.03, \quad (23)$$

which, as already anticipated, automatically yields a suppressed coupling to electrons: $C_e \approx 0.01$ (for comparison, in DFSZ models with $v_2 = v_1$ one has $C_e = 1/6$). The SN bound can be expressed as a constraint on the quantity $C_N = \sqrt{C_p^2 + C_n^2}$ [6, 11] that, according to Eqs. (2)–(3), has a lowest value $C_N \approx 0.019$ which is determined by the correction δ_s in Eq. (2) (for comparisons in KSVZ axion models $C_N \approx 0.48$).⁴ To identify the parameter space regions corresponding to a sizeable suppression of the couplings, and to show the parametric correlation between nucleophobia and electrophobia, it is convenient to parameterize the VEVs as

$$v_1 = v c_1 c_2, \quad v_2 = v s_1 c_2, \quad v_3 = v s_2, \quad (24)$$

where $s_i = \sin \beta_i$ and $c_i = \cos \beta_i$, and plot the value of C_N and C_e as a function of the angles $\beta_{1,2}$ rather than in terms of the VEVs ratios $\tan \beta_1 = v_2/v_1$ and $\tan \beta_2 = \sqrt{v_3^2/(v_2^2 + v_1^2)}$. Although the latter are the relevant physical parameters, this has the virtue of zooming in on the regions in which the values of the VEVs are not strongly hierarchical ($\tan \beta_{1,2} \sim O(1)$), and highlighting the correlation between electrophobia and nucleophobia. In the parametrization of Eq. (24), the orthogonality condition in Eq. (15) reads $\mathcal{X}_3 = (3c_1^2 - 1)c_2^2$. The requirement that the Yukawa couplings in the 3HDM remain perturbative restricts the allowed region in the (β_1, β_2) plane. A conservative limit is obtained by imposing the tree-level unitarity bound on the $2 \rightarrow 2$ fermion scattering, $|\text{Re } a_{J=0}| < 1/2$, in the 3HDM theory involving Yukawas at $\sqrt{s} \gg M_{H_{1,2,3}}$. Ignoring running effects, which would make the bound somewhat stronger, and taking into account group theory factors (see e.g. [12, 13])

⁴ An extra tuning with flavour mixings in Eq. (22) can in principle compensate for δ_s and further reduce the value of C_N , see [1] for details.

we get: $y_{t,b}^{3\text{HDM}} < \sqrt{16\pi/3}$ (from $Q_L \bar{u}_R \rightarrow Q_L \bar{u}_R$, with the initial and final states prepared into an $SU(3)_c$ singlet) and $y_\tau^{3\text{HDM}} < \sqrt{4\sqrt{2}\pi}$ (from $Q_L \bar{Q}_L \rightarrow u_R \bar{u}_R$, with the initial state prepared into an $SU(2)_L$ singlet). The label 3HDM reminds us that these are not the Yukawa couplings of the SM. The latter are related to the former via: $y_t = y_t^{3\text{HDM}} s_1 c_2$, $y_b = y_b^{3\text{HDM}} c_1 c_2$, $y_\tau = y_\tau^{3\text{HDM}} s_2$. The unitarity bounds on $y_{t,b,\tau}^{3\text{HDM}}$ can be now translated into a perturbativity bound in the (β_1, β_2) plane, and this results in the hatched region in Fig. 1. Contour lines for different values of C_N and C_e are also plotted in Fig. 1, and show how electrophobia and nucleophobia occur in overlapping regions, so that a single choice of the values of the relevant parameters simultaneously realizes both properties. It should be also noted that while for small values of β_2 the region with suppressed couplings is rather narrow, and astrophobia requires some tuning of the ratio v_2/v_1 to values sufficiently close to $\sqrt{2}$ ($\beta_1 \approx 0.95$), at larger values $\beta_2 \sim \mathcal{O}(1)$ the region opens up and less tuning is required to simultaneously decouple the axion from nucleons and electrons.

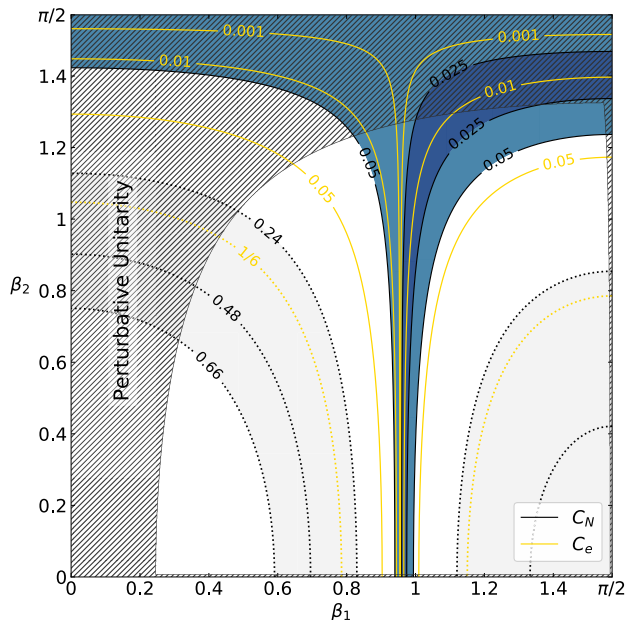


FIG. 1. Contour lines for $C_N = \sqrt{C_p^2 + C_n^2}$ (black) and C_e (yellow) in the (β_1, β_2) plane for the astrophobic model. For reference, contour lines corresponding to the values of C_N and C_e for the KSVZ and the DFSZ axion models are also plotted: $0.48 \rightarrow C_N^{\text{KSVZ}}$ (dotted line), $[0.24, 0.66] \rightarrow [C_{N,\text{min}}^{\text{DFSZ}}, C_{N,\text{max}}^{\text{DFSZ}}]$ (grey region) and $1/6 \rightarrow C_{e,(v_1=v_2)}^{\text{DFSZ}}$ (dotted yellow line) [6].

We recall here for completeness that since nucleophobia requires generation-dependent PQ charges, axion couplings to quarks are in general flavour-violating. As discussed in [1], limits on FCNCs such as $K \rightarrow \pi a$ yield stringent constraints on nucleophobic models which can be complementary to astrophysics bounds.

A final remark about the axion coupling to photons is in order. The coupling is defined by the interaction term

$$\frac{\alpha}{8\pi} \frac{C_\gamma}{f_a} a F_{\mu\nu} \tilde{F}^{\mu\nu}, \quad (25)$$

where $C_\gamma = E/N - 1.92(4)$, with E denoting the coefficient of the electromagnetic anomaly. In astrophobic models there is no particular reason for which C_γ should be suppressed. In the present model the contributions of the quarks and leptons are respectively $E_Q/N = 8/3 - 2\mathcal{X}_3$ and $E_L/N = 2\mathcal{X}_3$, so that their sum is $E/N = 8/3$, a value which is often encountered also in other axion models [14, 15].

V. CONCLUSIONS

Astrophobic axion models, wherein the axion couplings to nucleons and electrons can be simultaneously suppressed well below the values suggested by well-known benchmark models, can be elegantly implemented in a variant of the DFSZ model in which the PQ charges of the quarks are generation-dependent, and the scalar sector contains three Higgs doublets, one of which couples to the leptons and the other two to the quarks. While consistent astrophobic axion models were first constructed in Ref. [1], in the original scenario axion decoupling from the electrons was achieved by means of a tuned cancellation between two different contributions to the axion-electron coupling, one proportional to the electron PQ charge, and the other generated by the mixing of the electron with the leptons of the heavier generations. The virtue of the 3HDM construction presented here is that it avoids the need for this cancellation, and enforces a strong correlation between the suppressions of the axion couplings to nucleons and electrons, in such a way that nucleophobia and electrophobia are simultaneously realized in the same region of parameter space. This renders less contrived the possibility that axions might exhibit astrophobic properties.

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