# DEUTSCHES ELEKTRONEN-SYNCHROTRON DESY

## ATOMIC SPECTROSCOPY WITH SYNCHROTRON RADIATION

by

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Abstract - The continuous spectrum extending from the infrared to the
x-ray region, the high intensity, the time structure and the high degree
of polarization of synchrotron radiation makes electron storage ring sources
unique for atomic spectroscopy. Vacuum ultraviolet photons can excite
loosely bound electrons to high energy continuum states and deeply bound
core electrons to bound states below and continuum states above the
ionization limit. The interaction between the different excitation
channels strongly influences the spectra.' Many-electron correlations
often result in a complete break-down of the independent particle approxi-
mation. The impact of synchrotron radiation on atomic spectroscopy will
be showcased by reviewing the most important recent experimental results
together with the pertinent theoretical models.

PROPERTIES OF SYNCHROTRON RADIATION

Synchrotron radiation is emitted by relativistic electrons circulating in electron synchro-
trons or electron storage rings. The following outstanding properties make synchrotron
radiation one of the most useful sources for spectroscopy (Ref.1 & 2):

1. continuous spectrum from the infrared to the x-ray region
2. collimation of the radiation in a narrow cone around the instantaneous direction of flight
of the electrons
3. linear polarization in the plane of the electron orbit; circular polarization above and
below the orbit

4. time structure with pulse lengths down
to 100 ps
5. absolute calculability of the proper-
ties of the source
6. cleanliness of the source, since
emission takes place in ultra high
vacuum.

As an example, the spectral distribution
of the intensity emitted by the electron
storage ring DORIS is presented in Fig.1.
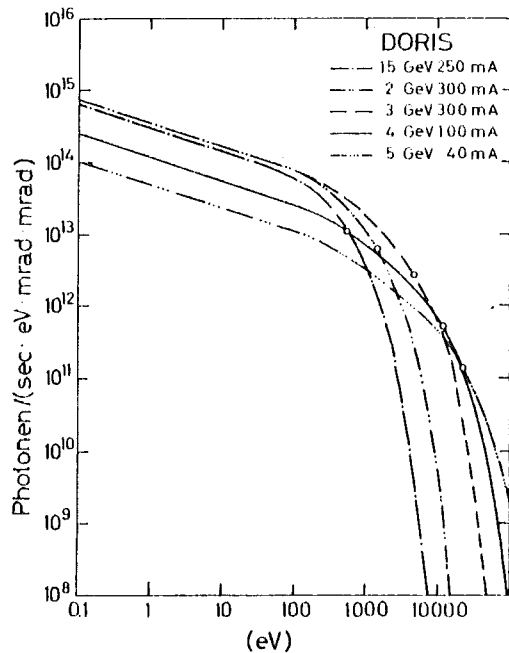
Central potential model

The most characteristic features of the
vacuum-ultraviolet (VUV; 10 eV < $\hbar\omega$ <
1000 eV) spectra of atoms can be describ-
ed qualitatively within the framework of
a central field model based on a realist-
ic potential (Ref. 3&4). The central
potential most widely used with reason-
able success is the Hartree Slater (HS)
potential calculated, for example, by
Herman and Skillmann (5). The non-Coulomb



Fig. 1   Spectral distribution of intensi-
ty in an aperture 1 mrad wide
and 1 mrad high centered at a
tangential direction.

character of the HS-potential for intermediate radii is crucial for the characteristic features of the VUV spectra. Combining the HS-potential U(r) and the centrifugal term $\frac{\ell(\ell+1)}{2r^2}$ results in an effective potential

$$V_{eff} = U(r) + \frac{\ell(\ell+1)}{2r^2}$$

The interplay between the attractive U(r) and the repulsive centrifugal term results in single valley, double valley and repulsive potentials. The double valley potential seen by the Xe f-electrons is depicted in Fig. 2. A pronounced positive barrier separates the inner and the outer valley. The radial wave functions $P_{n,\ell}(r)$ obey the Schrödinger equation

$$\left( -\frac{d}{dr^2} + V_{eff}(r) \right) P_{n,\ell}(r) = \epsilon_{n,\ell} \, P_{n,\ell}(r)$$

For Xe the radial wave function of the bound 4d state and several f-symmetric continuum states are included in Fig. 2. The photoionization cross-section is determined by the matrix element $R_{\ell \pm 1}$ which in the dipole-length form is given by

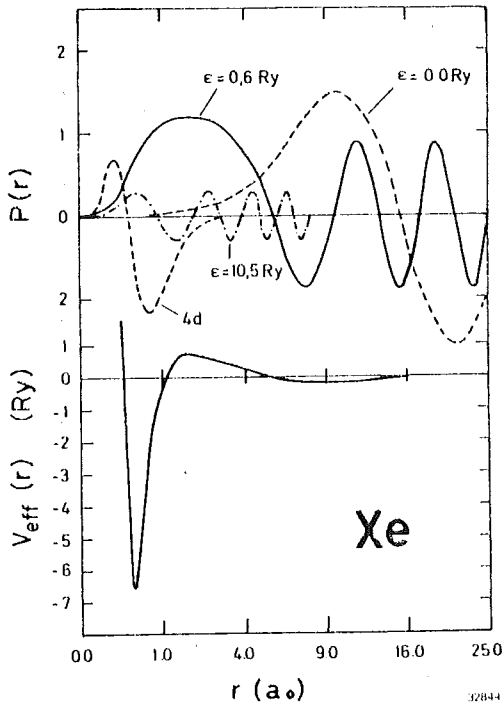$$R_{\ell \pm 1} = \int_0^\infty P_{n,\ell}(r) \, r \, P_{\epsilon,\ell}(r) \, dr$$



Fig. 2 bottom: effective potential $V_{eff}(r)$ for f-electrons of Xe.

top: Xe - 4d $P_{4,d}(r)$ and f continuum $P_{\epsilon,f}(r)$ radial wave-functions for different kinetic energies $\epsilon$.

The Xe 4d photoionization is dominated by transitions into f-symmetric continuum states. The characteristic features of the Xe 4d spectrum shown in Fig. 3 can be directly read off from Fig. 2. At threshold, i.e. for low kinetic energies $\epsilon$ of the outgoing photoelectron, the final state radial wave function is centered in the outer potential valley and hardly overlaps with the 4d wave function.

This explains the delayed onset of absorption at threshold. Towards higher energies the final state wave function penetrates closer to the nucleus, resulting in a larger overlap and a higher transition probability. At $\epsilon = 0.6$ Ry the absolute value of the matrix element peaks, giving rise to the pronounced maximum in the experimental spectrum. Note that due to the different sign of the 4d and $\epsilon$f wave functions in the region of overlap, the matrix element is negative. For still higher energies the first node of the f-symmetric wave function moves into the inner valley. At $\epsilon = 10.5$ Ry the matrix element is zero due to the cancellation of the positive and negative contributions. The zero of the matrix element explains the Cooper minimum found at 150 eV in the experimental spectrum.

Photoionization of closed shell atoms

From Fig. 3 it is obvious that the results of central-potential calculations can only be considered as a guideline. The cross-sections obtained by Hartree-Fock calculations are in far better agreement with the experimental cross-sections than those obtained within the central potential model. In case of the HF calculations the radial wave function of the continuum electron ionized from the $n\ell$-th subshell is obtained by solving the HF equation in the frozen core of the positive ion with an $n\ell$-hole (Ref. 9). This approach is equivalent to taking intrachannel interactions into account (Ref.8). In comparison with experiment the intrachannel interaction over-corrects the central potential calculation. These discrepancies have been resolved by the random phase approximation with exchange (RPAE) (Ref. 10). In RPAE the electric dipole matrix elements are calculated directly treating initial and final state correlations simultaneously. Compared to the HF calculation, the most important improvement results from the inclusion of virtual double-excitations in the ground and ionic states. For closed shell atoms the RPAE cross-sections agree with the experimental cross-sections within less than 10% in most cases (Ref.4&11). Similar agreement between theory
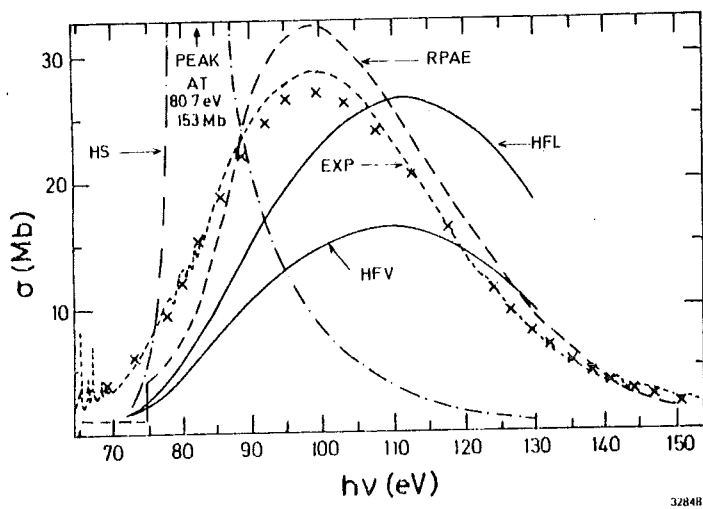
- 3 -

and experiment has been achieved e.g. by multiconfiguration Hartree-Fock (Ref. 12), transit-
ion matrix (Ref. 13), many-body perturbation (Ref. 14, 15), R-matrix (Ref. 15) and density
functional (Ref. 17) calculations. For a discussion of the different theoretical approaches,
their successes and failures, the reader is referred to the excellent reviews by Starace
(Ref. 4, 18).

### Photoionisation of open shell atoms

For open shell atoms our understanding of the VUV photoionisation is far less satisfactory
(Ref. 4, 11, 18, 19). In most cases the preparation of free open shell atoms requires high
temperatures which in combination with the restrictions imposed by VUV optics amounts to non-
trivial experimental difficulties. The great number of channels contributing to photoionizat-
ion causes headaches to the theorists. The experimental set-up used at the Electron Synchro-
tron DESY for the determination of the absorption of high temperature metal vapors is presen-
ted in Fig. 4 (Ref. 20).

### Fig. 4

Experimental set-up at
DESY for the determinat-
ion of high temperature
vapor absorption
spectra.

S1 = incoming synchro-
tron radiation
S = sample pipe,
H = Ta heating pipe
W, M, V = radiation
shields, T = vacuum
tank, Sv = shutter,
F = thin film window



absorption oven          Rowland spectrograph
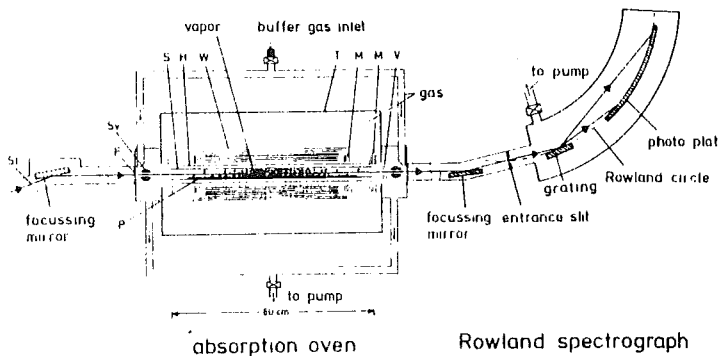
The atomic metals were maintained inside a resistance-heated tubular furnace mounted in front
of a 2 m grazing incidence Rowland-type spectrograph. The term dependent break down of the
subshell concept for the 3p-excitations of atomic 3d metals clearly manifests itself in the
spectrum of Mn presented in Fig. 5. The weak, sharp lines at the 3p threshold are due to

$3p^6 3d^5 4s^2 {}^6S \rightarrow 3p^5 3d^6 {}^6P$ (lines 1-3), ${}^6D$ (line 4) ${}^4P$ (lines 5,6) transitions. The do-
minant asymmetric absorption band is assigned to the LS allowed $3p^6 3d^5 4s^2 {}^6S \rightarrow$

$3p^5 3d^5 4s^2 {}^6P$ transitions. These transitions are strongly coupled to $3p^6 3d^5 4s^2 {}^6S \rightarrow$

$3p^6 3d^4 4s^2 \epsilon f {}^6P$ transitions via the Super-Coster-Kronig decay $3p^5 3d^6 4s^2 6p \rightarrow 3p^6 3d^4 \epsilon f {}^6P$.
The interference between the two channels gives rise to the Fano type line shape (Ref.3, 24)
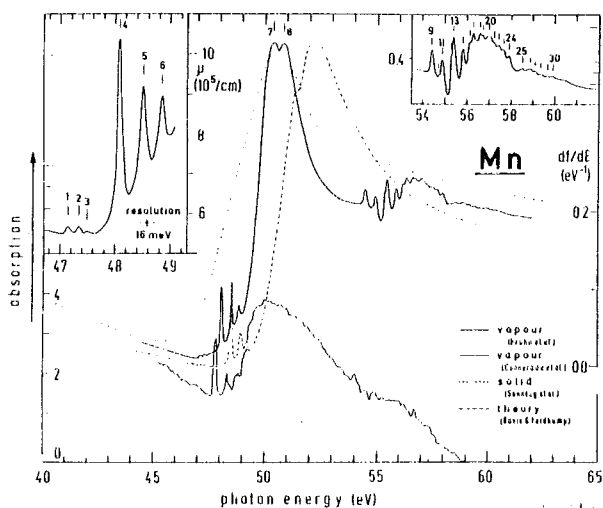
Fig. 5

3p-absorption of atomic and
metallic (Ref. 22) Mn. The
lower solid line gives the den-
sitometer trace reported by
Connerade et al. (Ref. 23).
The absolute absorption
coefficient refers to the
spectrum of metallic Mn. The
oscillator strength df/dE
for atomic Mn calculated by
Davis and Feldkamp (Ref. 24)
is included.

$$\sigma(E) = \sigma_c(E) \frac{\left(q + \frac{E-Er}{\Gamma}\right)^2}{1 + \left(\frac{E-Er}{\Gamma}\right)^2}$$

where $\sigma_c(E)$ gives the 3d → f continuum cross-section in the absence of the interaction with
the 3p → 3d transition, q is the asymmetry parameter, $E_r$ the energy of the resonance and $\Gamma$
the half width. This interpretation of Mn 3p spectrum has been corroborated by recent photo-
emission measurements on Mn atoms (Ref. 25). Fig. 6 shows the 3p absorption spectrum of
atomic Cu (Ref. 20). Since the 3d shell is filled in Cu, there is no strong maximum at thresh-
old. The weak maxima are ascribed to 3p → ns, nd transitions. Davis and Feldkamp (Ref. 26)
have shown that the dip in absorption above the 3p → 4s peaks can be explained by the inter-
ference of 3p → nd, rd and 3d → εf channels. The interaction between the 3p and 3d excit-
ations also manifests itself in the minimum of the 3d cross-section for metallic Cu (Ref.27).

## Resonant photoemission

The analysis of the energy and angular distribution of the outgoing photoelectron allows by
far more stringent tests of theoretical approaches than those based on absorption spectra.
In Fig. 7 an experimental set-up for energy and angular resolved photoemission, in atmosphe-
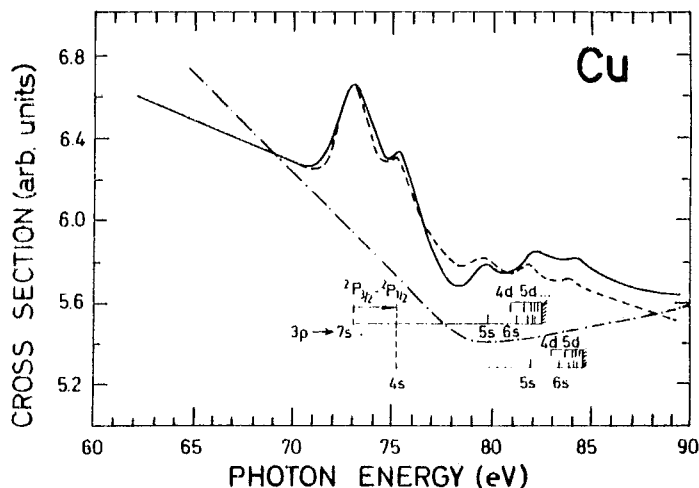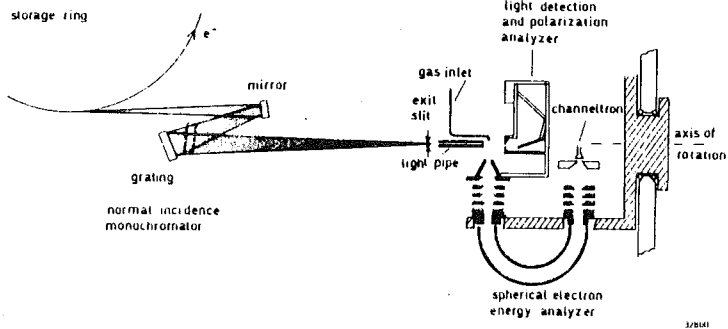ric gases, operated with great success at the NBS is shown (Ref. 28&29).



Fig. 6

Absorption of atomic
Cu at the 3p threshold,
experiment ( ——— )
(Ref. 20), theory
(- - -) (Ref. 26). $\sigma_{3d}$
for metallic Cu
(-.-.-) (Ref. 27).

Fig. 7

Angle resolved photo-
electron spectrometer
coupled to a high
throughput 2 m normal
incidence monochroma-
tor in operation at
SURF-II (Ref. 28 &
29).



In case of photoemission from atomic metals, the requirement to combine a high temperature intense vapor source with an electron spectrometer adds to the experimental difficulties. An experimental arrangement described by Shannon and Codling (Ref. 30) is presented in Fig. 8.
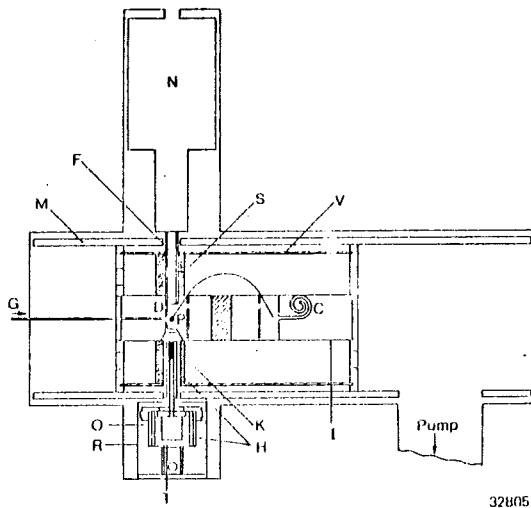


Fig. 8

Cylindrical electron
energy analyser with
oven.
N = liquid $N_2$ reservoir
F = cold finger
M = mu metal
D = cold shield
G = calibration gas
 inlet
P = photon beam
O = oven
R = radiation shields
T = thermocouple
H = heating coils
K = collimator
I = inner cylinder
V = outer cylinder
C = channeltron (Ref.30)

Most of the VUV experiments reported so far have been restricted to systems providing suffi-cient vapor-pressure at temperatures below 1000° C. Recently Chandesris et al. (Ref. 31) succeeded in determining the photoemission of atomic Cu for photon energies between 70 eV and 80 eV. The experimental spectrum is given in Fig. 9. The main line corresponds to the $3d^9$ 4s configuration of $Cu^+$. The five weaker satellite structures have been ascribed to the $3d^8$ 4s ($^1S$, $^1G$, $^3P$, $^1D$, $^3F$) multiplet (Ref. 31). The most interesting result is the reso-nant enhancement of the $^1G$ and $^3F$ lines when tuning the photon energy through the $3p^6$ $3d^{10}$ 4s → $3p^5$ $3d^{10}$ $4s^2$ transition of Cu (see Fig. 6). The variation of the intensity of the $^1G$ and $^3F$ satellite lines between 70 eV and 78 eV is shown in Fig. 10.
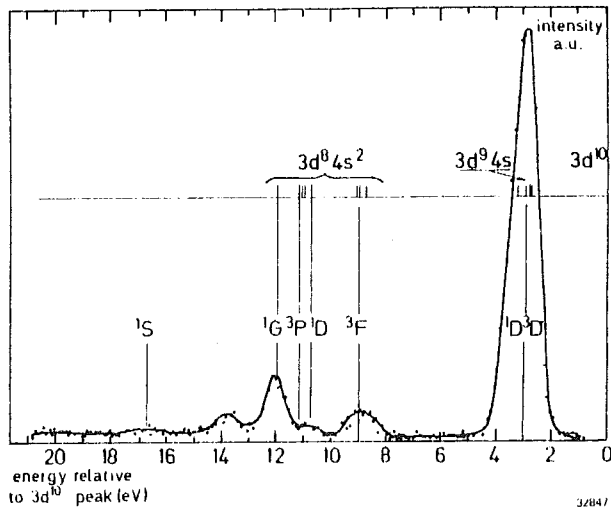
The resonant enhancement of the two electron satellites is due to the super-Coster-Kronig decay of the $3p^3 \, 3d^{10} \, 4s^2 \, ^2P_{1,3}$ state, primarily in the $^1$G multiplet and with lesser amounts in $^3$F and $^1$D of $Cu^+$ $3d^8 \, 4s^2$, $^2$$^2$ The interference between the

$$3p^6 \, 3d^{10} \, 4s \quad \rightarrow \quad 3p^5 \, 3d^{10} \, 4s^2$$

and the two-electron excitation $3p^6 \, 3d^{10} \, 4s \rightarrow 3p^6 \, 3d^8 \, 4s^2 \, \varepsilon f$

via the super Coster-Kronig decay $3p^5 \, 3d^{10} \, 4s^2 \rightarrow 3p^6 \, 3d^8 \, 4s^2 \, \varepsilon f$

is negligible, because of the small oscillator strength of the two-electron excitation. This explains the symmetric Lorentzian type line shape. Note that in the calculations (Ref. 26) the spin orbit splitting of the Cu 3p level has been taken into account. Because of the small probability for the Auger decay $3p^5 \, 3d^{10} \, 4s^2 \rightarrow 3p^6 \, 3d^9 \, 4s \, \varepsilon f$,

the main $3d^9$ 4s line is hardly affected, when tuning the photon energy through the $3p \rightarrow 4s$ resonance.
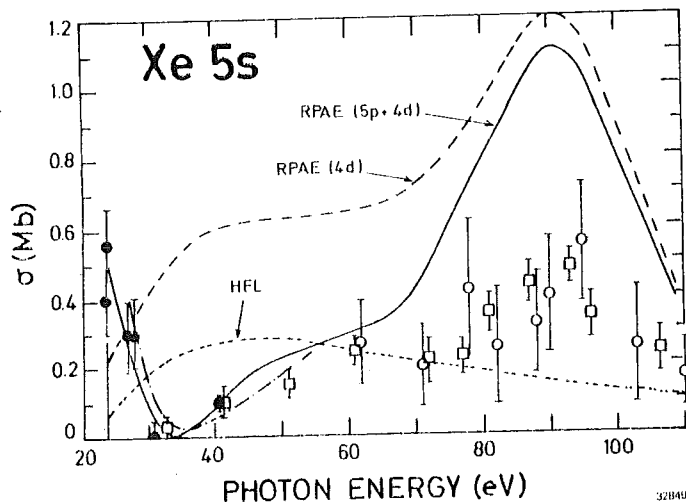
Fig. 11
Xe 5s subshell photo-
ionization cross-section.
Experiment (●) (Ref. 32)
(o) (Ref. 33);
(□) (Ref. 34) theory,
RPAE and HFL (Ref. 10);
RRPA (-·-·-) (Ref. 35).

## Interchannel interaction

The striking effects of interchannel interaction are well showcased for the photoionization
cross-sections of the outer s-subshells of the rare gas atoms. The Xe 5s subshell cross-
section is presented in Fig. 11. In contrast to the Hartree-Fock length (HFL) result, the
experimental curve shows a minimum at 34 eV and a maximum at ∿ 90 eV (Ref. 32, 33, 34). The
minimum mirrors the Cooper minimum in the 5p → εd channel, the maximum the delayed maximum in
the 4d →εf channel. Including the coupling of the 5s, 5p and 4d channels, the main features
of the experimental spectrum are well reproduced by the RPAE calculations by Amusia and
Cherepkov (Ref. 10). The calculations by Johnson and Cheng (Ref. 35) using the relativistic
randomphase approximation RRPA reproduced the experimental results in the region of the mini-
mum above threshold very well. Relativistic effects are responsible for the nonzero of the
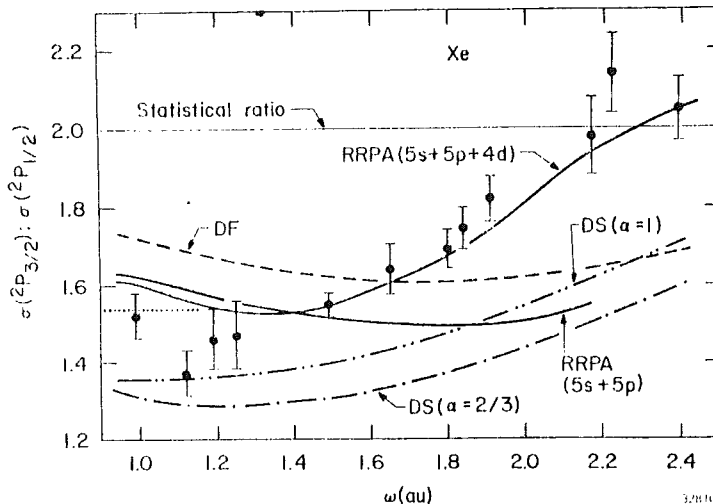cross-section at the minimum.

## Branching ratio

The branching ratio, i.e. the ratio of the photoemission intensity from two subshells split by
the spin-orbit interaction, often considerably deviates from the statistical ratio given by
the occupation numbers of the subshells. Cross-sections varying with photon energy in combi-
nation with the different kinetic energies of the outgoing electrons contribute to these
deviations (Ref. 36). But this effect by no means can explain the experimental results. Rela-
tivistic effects and interchannel interaction play a very important role. This is clearly
demonstrated by the $2P_{3/2}$ : $2P_{1/2}$ branching ratio for the Xe 5p photoemission presented in
Fig. 12. Only the RRPA calculations (Ref. 35) including the coupling of the 5s, 5p and 4d

Fig. 12
$2P_{3/2}$ : $2P_{1/2}$
branching ratio for
Xe 5p.
Experiment: (···)
(Ref. 37);
( ) (Ref. 38);
Theory:
(——) (Ref. 35);
(- - -) (Ref. 39);
(-·-) and (-··-)
(Ref. 38).

channels are able to
reproduce the experi-
mental results.

## Angular resolved photoemission

Angular and energy resolved photoemission measurements form a stringent test for theoretical models, because they yield information on the absolute value and the sign of the matrix element and on the phase of the final state wavefunction (Ref. 4). In LS coupling for closed shell atoms the Cooper Zare model (Ref. 40) holds. The differential photoionisation cross-section for linearly polarized incoming light, in dipole approximation, is given by

$$\frac{d\ ij\ (\varepsilon)}{d\Omega} = \frac{\sigma ij\ (\varepsilon)}{4\pi}\left[1 + \beta ij\ (\varepsilon)\ \frac{1}{2}\ (3\ \cos^2\ \psi- 1)\right]$$

where i, j stand for the quantum numbers of the initial, final state respectively. $\sigma ij\ (\varepsilon)$ is the partial photoionisation cross-section, $\psi$ is the angle between the direction of the outgoing photoelectron and the electric vector of the light. The asymmetry parameter $\beta ij\ (\varepsilon)$ characterizing the angular distribution of the photoelectrons is given by

$$\beta_{n,\ell} = \frac{\ell(\ell-1)R^2_{\ell-1}(\varepsilon) + (\ell+1)(\ell+2)R^2_{\ell+1}(\varepsilon) - 6\ell(\ell+1)R_{\ell-1}(\varepsilon)R_{\ell+1}(\varepsilon)\ \cos\left[\delta_{\ell+1}(\varepsilon) - \delta_{\ell-1}(\varepsilon)\right]}{(2\ell + 1)\left[\ell R^2_{\ell-1}(\varepsilon) + (\ell+1)\ R^2_{\ell+1}(\varepsilon)\right]}$$

where $\delta_\ell$ gives the partial wave phase shift. The second term depends on the matrix elements and the phases of the continuum wave functions. This term represents the interference between the $\ell \rightarrow \ell + 1$ and $\ell \rightarrow \ell - 1$ transitions. Fig. 13 shows the experimental (Ref. 41, 42) and theoretical (Ref. 9, 43) $\beta$ values for the Ar 3p excitation.
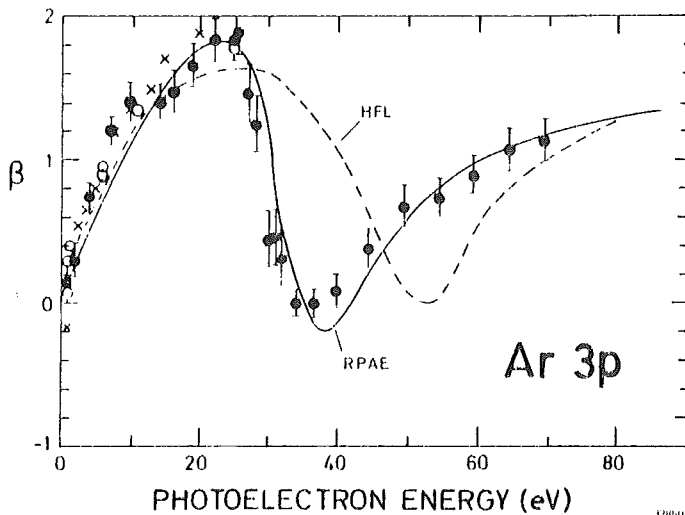


Fig. 13

Asymmetry parameter for the 3p shell of Ar. Experiment: (⊕,0)(Ref. 41); (x) (Ref.42) Theory: HFL (Ref. 9); RPAE (Ref. 43).

The rapid increase of $\beta$ within the first eV above threshold is due to the variation of the phase shift. The Cooper minimum in the 3p → εd channel causes the minimum in the $\beta$ spectrum at ∿ 35 eV. The HFL results (Ref. 43) based on the Cooper Zare model show the characteristic features of the spectrum, though the position of the minimum is at too high energies. Good agreement with the experimental results has been achieved by RPAE calculations (Ref. 43) taking intershell correlations into account. Recent RRPA (Ref. 35) and R-matrix (Ref. 44) calculations give results in close agreement with the RPAE predictions.

## Spin polarisation of photoelectrons

For a complete characterization of a photoionisation process, i.e. for the determination of all matrix elements and phase differences of continuum wave functions involved, the measurement of the total and partial cross-sections and the angular distribution of photoelectrons is not sufficient in general. Additional information can be obtained by the determination of the spin polarisation of the outgoing photoelectrons. Making use of the circular polarisation of the synchrotron radiation above and below the electron orbit, Heinzmann and coworkers (Ref. 45, 46, 47) succeeded in determining the total spin polarisation of the Ar 3p, Kr 4p, Xe 5p photoelectrons in the wavelength range 45 to 100 nm. A schematic diagram of the experimental set-up is shown in Fig. 14. A 10 m plane grating normal-incidence monochromator was used.

Fig. 14

Experimental set-up for the determination of
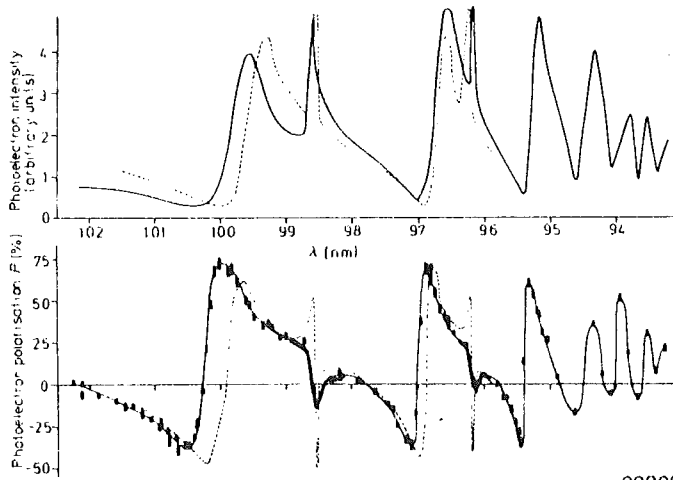the total spin polarisation (from Ref. 46).

The concave mirror formed an image of the
electron beam at the exit slit of the mono-
chromator. Left or right circular polarisation
was selected by the aperture which was movable
perpendicular to the plane of the electron
orbit. The degree of polarisation of the ra-
diation was determined with a four mirror
analyser.

The photoelectrons created at the crossing of
the photon beam and the atomic beam were ex-
tracted by an electric field, focused by
electron optical components and accelerated
to 120 keV for polarisation analysis in a Mott
detector. The experimental results for atomic
Xe are shown in Fig. 15.

The prominent resonance structures above the
$^2P_{3/2}$ ionisation limit (102,2 nm) are due to
the autoionising $5p^6 \to 5p^5$ ($^2P_{1/2}$)nd (broad
structures) $5p^6 \to 5p^5$ ($^2P_{1/2}$)ns (sharp lines)
transitions (see e.g. Ref. 11). The interact-
ion between the discrete and continuum states
gives rise to the asymmetric Fano type line
shapes (Ref. 3). The resonance structure is
also shown by the photoelectron spin polari-
sation. The results of the multichannel
quantum defect theory (MQDT) calculations (Ref.
48) by Lee are well reproducing the characte-
ristic features of the experimental results. An even better agreement between theory and ex-
periment has been achieved by Johnson et al. (Ref. 49) calculating the MQDT parameters within
the relativistic random phase approximation (RRPA).
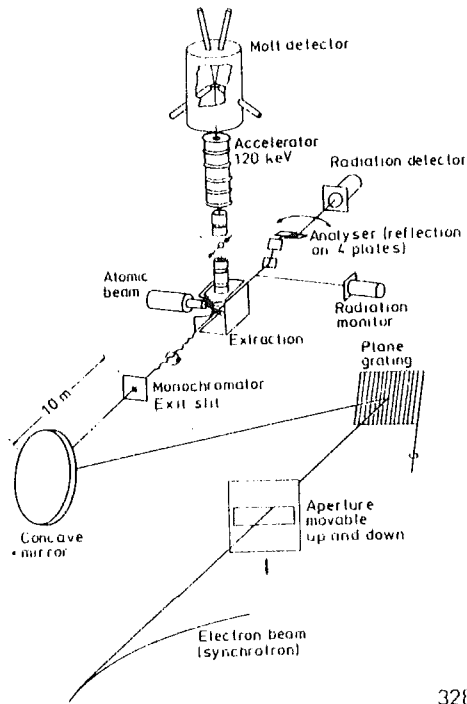


32809



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Fig. 15

Photoionisation of Xe
in the autoionisation
range. Upper part:
cross-section, photo-
electron intensity;
Lower part: total spin
polarisation of photo-
electrons. Experimen-
tal results (——)
(Ref. 46); theory
(- - - -) (Ref. 48).
From Ref. 46).

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