STUDY OF PHOTOPRODUCTION ON HYDROGEN IN A STREAMER CHAMBER WITH TAGGED PHOTONS FOR 1.6 GeV < $E_\gamma$ < 6.3 GeV
Topological and reaction cross sections

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We have studied photoproduction using a 1 m streamer chamber at DESY and a tagged photon beam with an energy range of 1.6 GeV < $E_\gamma$ < 6.3 GeV. We analysed approximately 30 000 events and report topological, channel and resonance production cross sections for a large number of reactions with three and five outgoing charged particles.

1. Introduction

Photoproduction cross sections for multiparticle processes have been determined in a number of experiments [1–5]. However, in most of the previous experiments

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there was the difficulty of having a photon beam with a wide energy spectrum and no possibility to measure the photon energy for individual events. Therefore the photon energy could be determined only for reactions with no neutrons in the final state (from 3-constraint kinematic fits to the final-state energies and momenta), while for channels with one (or more) neutrons the photon energy was unknown and, since the photon flux depended on energy, no cross sections could be given. Other experiments [3,5] partly overcame this difficulty by using a beam with a narrow energy spectrum, but these measurements were made at only a few discrete energies.

To amend this situation, and to study systematically the energy dependence of the various cross sections, we have undertaken a comprehensive study in which we used an energy tagged broad band photon beam, together with a 1 m long streamer chamber with a built-in hydrogen target, to detect all charged particles in the final state. The lab beam energy range covered was 1.6 GeV < \( E_\gamma \) < 6.3 GeV. The photons were produced by bremsstrahlung from monochromatic positrons in a thin radiator, and the momentum of the scattered positrons was measured in a magnetic field with a counter hodoscope to an accuracy of ±30 MeV. This was amply sufficient for a clean kinematical separation of events with zero, or more than one neutral particle in the final state.

In sect. 2 we describe the experiment, and in sect. 3 the results for topological and channel cross sections are presented as well as for resonance production as obtained from maximum likelihood fits to the mass distributions.

2. Experimental procedure

2.1. Photon beam

A monochromatic positron beam of energy 6.5, 4.3, 3.5 or 2.9 GeV and an energy width of 0.5% was hitting a 1.2 mm Al radiator, producing bremsstrahlung. The recoil positrons were momentum-analyzed with a C-magnet of 21 kG and detected...
in a hodoscope of 12 scintillation counters, overlapping each other (photon tagging system, TAG), fig. 1. To ensure a photon was emitted, electron pair production was vetoed by detecting the electron on the other side in the counters V3 and V6, or, if the electron had a too low energy, by detecting the second, more energetic positron in the veto counter V4 at the end of the tagging hodoscope. The veto counter on the electron side excluded also events with a more energetic knock-on electron. Photons outside the beam were vetoed by a shower counter with a hole of 3 cm diameter (V5) through which the beam was passing.

Measurements with a total absorption photon counter in the γ beam showed that in 92% of the cases a count in the tagging system including the veto counters were associated with a high energy photon.

The remaining 8% of the tagging counts are due to an incomplete coverage of the background processes by the various veto counters (V1–V5). Because this fraction (8%) is not related to photons in the beam it does not contribute to event triggers. Only on the level of accidental coincidences these counters could introduce a bias, but this was found to be completely neglible.

By detecting the recoil positron in the momentum analyzing magnet the photon energy is known within ±1%. By triggering the streamer chamber on e+e− pairs we could independently measure the energy of the photons. This thus determined energy was in 92% of all triggers associated with an high energy photon, not more than 90 MeV lower than the value given by the tagging system.

2.2. The streamer chamber

The double gap streamer chamber [6] with a sensitive volume of 100 × 60 × (2 × 16) cm³ was filled with a helium neon mixture (70% Ne, 30% He) at atmospheric pressure. By adding a small amount (~10⁻⁷) of electronegative SF₆, the memory time was reduced to 2 µsec. A 400 kV, 10 nsec pulse was applied; it was generated with a 14 stage Marx generator and a 0.8 m coaxial Blumlein system. The streamer chamber was operated in a nearly homogenous magnetic field of 21 kG.

Pictures were taken with 3 cameras with a stereo angle of 18°. The average demagnification was 38, a 35 mm focal length system with f number 2 and Kodak Tri-X Aerographic film SO265 were used.

2.3. The trigger system

The photons passed through a liquid hydrogen target of 3.8 cm length inside the streamer chamber, and were then counted in a totally absorbing shower counter S of 11 rad lengths (fig. 2). The target was surrounded by a cylindrical scintillation counter T with a window at the entrance of the beam. This counter counted the particles coming out of the target and simultaneously served as a vacuum container for the target. To veto e⁺e⁻ pair production we used two counters (O, U in fig. 2) in a plane through the target and perpendicular to the magnetic field.

The trigger condition for hadronic events was TAG · T · S · (O + U), for e⁺e⁻ pairs TAG · T · O · U and the number of "tagged" photons was obtained as the counting rate TAG · S.
2.4. Scanning and measuring procedure

The pictures showed so few background tracks that it was possible to scan and measure the pictures in one step. We took 870,000 pictures from which 14% showed a hadronic event produced in the hydrogen or the target counter. Part of the film was scanned twice from which a scanning efficiency of greater than 99% was found. Since for 9% of the events one of the charged particles was stopped inside the target scintillator, we measured events with a total charge of the outgoing visible particles \( Q = 0 \) or 1. The events were measured on conventional bubble chamber film measuring devices and in part on SMP's (Scanning and Measuring Projectors). Geometric reconstruction and kinematic fits were done using the THRESH and GRIND [7] program chain. Badly measured events were measured twice. Finally 2% of the events remain unmeasurable.

For each particle with momentum below 1 GeV/c for a given mass assignment the ionization predicted from the momentum was checked on the scanning table. The accuracy of the momentum and angle measurements was determined by the average track residual, a measure of the standard deviation of the point coordinate measurement error. It was 7 \( \mu \)m on the film corresponding to 275 \( \mu \)m in real space. Part of the \( e^+e^- \) pairs was also measured on a flying spot digitizer [8]. Here we obtained an average track residual of 3.5 \( \mu \)m corresponding to 140 \( \mu \)m.

Before entering the kinematic program GRIND the invisible vertex is reconstructed in order to separate events originating in the hydrogen target. For this reconstruction at least two visible tracks are needed which precludes an analysis of one-prong events.
The accuracy of the reconstruction is 0.05 cm in the plane perpendicular to the optical axis and 0.5 cm in the direction parallel to the optical axis. The momenta and angles of the outgoing particles are corrected for energy loss and multiple scattering inside the scintillation counter.

Most of the hadronic events originate from photon interactions in the trigger scintillation counters. Due to the excellent vertex reconstruction accuracy the events not coming from the hydrogen target could be separated. A remaining contamination from non-hydrogen events is less than 2%.

Finally we obtain a sample of 29 748 events produced in hydrogen and evenly distributed over the photon energy range from 1.6 GeV to 6.3 GeV.

2.5. Determination of cross sections

In this experiment we measure the cross sections for events with at least two outgoing charged particles. The cross sections are determined by counting the events produced in the hydrogen target and dividing by the measured photon flux.

![Energy dependence of the topological cross sections. All cross sections except the total 1-prong cross section are normalized to expression (1) given in subsect. 2.5 (dashed line). E_γ is the photon energy in the lab system.](image)

Fig. 3. Energy dependence of the topological cross sections. All cross sections except the total 1-prong cross section are normalized to expression (1) given in subsect. 2.5 (dashed line). E_γ is the photon energy in the lab system.
For determining the total cross sections several corrections are necessary:

(i) Part of the beam (20%) did not go through the hydrogen target.
(ii) Due to double bremsstrahlung 6% of the events are vetoed by the shower counter.
(iii) Corrections are also necessary for the deadtime of the shower counter. In the 6.5 GeV run this correction is large (34%) because the shower counter is counting not only the tagged photons (4.1 GeV < \( E_\gamma < 6.3 \) GeV) but all photons above its threshold.

The results for the total photoproduction cross section corrected for one-prong events are within errors in agreement with published data [3,9] over the whole energy range covered (fig. 3). However, since our systematic uncertainties are of the order of 15% we prefer to normalize our data to the published total cross sections, or rather to a smooth fit to them.

The expression we use is

\[
\sigma_{\text{tot}} - \sigma_{\text{1 prong}} = \left( 98.7 \, \mu\text{b} + \frac{64.9 \, \mu\text{b}}{\sqrt{E_\gamma}} \right) - \frac{80 \, \mu\text{b}}{E_\gamma},
\]

where \( E_\gamma \) is measured in GeV. The first two terms are taken from ref. [10] and the last one is a fit to the one-prong cross section [3], which was not analysed in this experiments. The last term also determines the error of this normalization to be 5% independent of energy. This error is not accounted for in the partial cross sections given below.

3. Results

3.1. Topological cross sections

In order to determine the topological cross sections we use all measured events with a total charge of the outgoing visible tracks \( Q = 0 \) or 1 and which have their fitted vertex inside the hydrogen target. The 2% of unmeasurable events are taken to be a random sample and added accordingly for each topology. This number of events must still be corrected for losses due to the veto counters. To do this, each event is rotated around the beam axis by steps of 1°; if a particle hits one of the veto counters this step is marked. The ratio of marked over unmarked steps gives a weight factor for each event. The resulting corrections are of the order of 20% for two prongs and 15% for five prongs. There is, however, a class of events in which one particle goes nearly in the forward direction (\( \theta < 2^\circ \)) (\( \theta = \) angle between outgoing particle and beam); these events are always vetoed and cannot be corrected by the method mentioned above. To correct these losses we plot \( \cos \theta \) for all particles. The particles missing near \( \cos \theta = 1 \) define a correction of 2%.

In our high energy run (\( E_\gamma > 4.0 \) GeV) we used a target counter of 3 mm scintil-
Table 1
Corrections and systematic uncertainties for calculating the topological cross sections

<table>
<thead>
<tr>
<th>Event Description</th>
<th>Uncertainty</th>
</tr>
</thead>
<tbody>
<tr>
<td>Scanning and measuring of events with total charge on outgoing visible track ( Q = 0 ) or ( 1 ) only</td>
<td>( 3 \pm 1% )</td>
</tr>
<tr>
<td>Scanning losses</td>
<td>( \pm 1% )</td>
</tr>
<tr>
<td>Veto weight for events with tracks having ( \theta &gt; 2^\circ )</td>
<td>( 16 \pm 2% )</td>
</tr>
<tr>
<td>Veto weight for events with tracks having ( \theta &lt; 2^\circ )</td>
<td>( 2 \pm 2% )</td>
</tr>
<tr>
<td>Inefficiency of target counter for ( E_\gamma &gt; 4.0 ) GeV and two-prong events</td>
<td>( 46 \pm 5% )</td>
</tr>
<tr>
<td>Inefficiency of target counter for ( E_\gamma &gt; 4.0 ) GeV and events with more than two tracks</td>
<td>( 10 \pm 2% )</td>
</tr>
</tbody>
</table>

The numbers so corrected are added and normalized to the total cross section from formula (1).

In table 1 we summarize the corrections and uncertainties of the topological cross sections. In tables 2 and fig. 3 the topological cross sections are shown. Within the errors they agree with the results from other experiments [2–5,19]. The last row in table 2 gives the cross section for all events with a visible decay (\( V \) or kink) of a charged or neutral strange particle. These cross sections are not included in the prong cross section. It should be noted, however, that the cross sections for events with visible strange particle decays are experiment-dependent since no corrections have been made due to decays outside the visible volume of the chamber or within the vertex reconstruction accuracy.

3.2. Channel cross sections

In this section we discuss the determination of cross sections for four-constraint (4C) events (i.e. events with no outgoing neutral particle), for one-constraint (1C) events (with one neutral particle (\( \pi^0 \), n) or, in the case of an even number of outgoing charged particles, events where the \( \pi^+ \) or p are stopping inside the target counter.

With the kinematic reconstruction program GRIND the following processes are fitted: \( m = 1, 2, 3 \)

\[
\gamma p \rightarrow p \pi^+ \pi^- m \pi^-
\]  
(a)
Table 2
Topological cross sections (μb)

<table>
<thead>
<tr>
<th>Beam energy $E_γ$ (GeV)</th>
<th>1.6–1.9</th>
<th>1.9–2.1</th>
<th>2.1–2.3</th>
<th>2.3–2.6</th>
<th>2.6–3.25</th>
<th>3.25–4.0</th>
<th>4.0–5.0</th>
<th>5.0–6.3</th>
</tr>
</thead>
<tbody>
<tr>
<td>3 prong</td>
<td>93.5 ± 3.8</td>
<td>95.1 ± 4.0</td>
<td>97.1 ± 4.3</td>
<td>94.1 ± 3.2</td>
<td>92.8 ± 3.1</td>
<td>87.1 ± 3.6</td>
<td>78.2 ± 5.0</td>
<td>73.4 ± 5.3</td>
</tr>
<tr>
<td>5 prong</td>
<td>3.3 ± 0.5</td>
<td>3.6 ± 0.5</td>
<td>3.2 ± 0.5</td>
<td>6.4 ± 0.5</td>
<td>10.0 ± 0.7</td>
<td>14.0 ± 1.1</td>
<td>20.6 ± 1.3</td>
<td>25.5 ± 1.6</td>
</tr>
<tr>
<td>7 prong</td>
<td>0.1 ± 0.1</td>
<td>0.2 ± 0.1</td>
<td>0.6 ± 0.2</td>
<td>1.1 ± 0.2</td>
<td>2.1 ± 0.3</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>With visible strange particle decay</td>
<td>5.2 ± 0.6</td>
<td>5.9 ± 0.7</td>
<td>5.9 ± 0.7</td>
<td>6.9 ± 0.6</td>
<td>6.5 ± 0.5</td>
<td>9.1 ± 0.8</td>
<td>8.4 ± 0.8</td>
<td>8.7 ± 0.9</td>
</tr>
</tbody>
</table>

The cross sections for events with visible strange particles are not included in the prong cross sections. It should be noted that these cross sections are experiment-dependent.
Table 3
Channel cross sections (mb) of reactions with 3, 5 and 7 outgoing tracks

<table>
<thead>
<tr>
<th>Beam energy $E_{\gamma}$ (GeV)</th>
<th>1.6–1.9</th>
<th>1.9–2.1</th>
<th>2.1–2.3</th>
<th>2.3–2.6</th>
<th>2.6–3.25</th>
<th>3.25–4.0</th>
<th>4.0–5.0</th>
<th>5.0–6.3</th>
</tr>
</thead>
<tbody>
<tr>
<td>3 prongs</td>
<td></td>
<td></td>
<td></td>
<td></td>
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<td></td>
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<td></td>
</tr>
<tr>
<td>$p n^+\pi^-$</td>
<td>41.7 ± 2.3</td>
<td>39.7 ± 2.4</td>
<td>38.5 ± 2.4</td>
<td>33.8 ± 1.7</td>
<td>28.1 ± 1.6</td>
<td>23.4 ± 1.2</td>
<td>22.5 ± 2.0</td>
<td>19.5 ± 1.8</td>
</tr>
<tr>
<td>$pn^+\pi^-\pi^0$</td>
<td>25.9 ± 1.7</td>
<td>25.0 ± 1.8</td>
<td>26.0 ± 2.1</td>
<td>23.6 ± 1.3</td>
<td>23.2 ± 1.3</td>
<td>18.8 ± 1.4</td>
<td>18.0 ± 1.6</td>
<td>14.4 ± 1.5</td>
</tr>
<tr>
<td>$n2\pi^+\pi^-$</td>
<td>8.0 ± 0.8</td>
<td>11.4 ± 1.1</td>
<td>9.1 ± 1.0</td>
<td>9.5 ± 0.7</td>
<td>11.3 ± 0.8</td>
<td>9.8 ± 0.9</td>
<td>7.9 ± 1.3</td>
<td>7.7 ± 1.3</td>
</tr>
<tr>
<td>$pn^+\pi^- (&gt;2\pi^0)$</td>
<td>17.9 ± 1.1</td>
<td>19.6 ± 1.3</td>
<td>23.6 ± 1.7</td>
<td>27.2 ± 1.3</td>
<td>30.2 ± 1.4</td>
<td>35.0 ± 1.9</td>
<td>29.8 ± 2.3</td>
<td>31.8 ± 2.4</td>
</tr>
<tr>
<td>$n2\pi^+\pi^- (&gt;1\pi^0)$</td>
<td></td>
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<td></td>
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</tr>
<tr>
<td>5 prongs</td>
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<td></td>
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<td></td>
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<td></td>
</tr>
<tr>
<td>$p2\pi^+\pi^-$</td>
<td>3.0 ± 1.0</td>
<td>2.9 ± 0.8</td>
<td>2.0 ± 0.6</td>
<td>3.4 ± 0.6</td>
<td>4.5 ± 0.6</td>
<td>4.4 ± 0.5</td>
<td>5.5 ± 0.5</td>
<td>5.4 ± 0.4</td>
</tr>
<tr>
<td>$p2\pi^+\pi^-\pi^0$</td>
<td>0.3 ± 0.2</td>
<td>0.6 ± 0.2</td>
<td>1.4 ± 0.3</td>
<td>2.7 ± 0.5</td>
<td>4.0 ± 0.5</td>
<td>5.7 ± 0.6</td>
<td>7.4 ± 0.6</td>
<td>7.4 ± 0.6</td>
</tr>
<tr>
<td>$n3\pi^+\pi^-$</td>
<td>0.1 ± 0.1</td>
<td>0.2 ± 0.2</td>
<td>0.3 ± 0.1</td>
<td>0.5 ± 0.2</td>
<td>1.5 ± 0.3</td>
<td>2.3 ± 0.3</td>
<td>2.2 ± 0.3</td>
<td>2.2 ± 0.3</td>
</tr>
<tr>
<td>$p2\pi^+\pi^- (&gt;2\pi^0)$</td>
<td>0.3 ± 0.3</td>
<td>0.3 ± 0.2</td>
<td>0.4 ± 0.2</td>
<td>1.3 ± 0.4</td>
<td>2.3 ± 0.5</td>
<td>4.1 ± 0.6</td>
<td>7.1 ± 0.9</td>
<td>10.5 ± 1.1</td>
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<tr>
<td>$n3\pi^+\pi^- (&gt;1\pi^0)$</td>
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<td></td>
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</tr>
<tr>
<td>7 prongs</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$p3\pi^+\pi^-\pi^0$</td>
<td>0.1 ± 0.1</td>
<td>0.3 ± 0.1</td>
<td>0.5 ± 0.1</td>
<td>0.5 ± 0.1</td>
<td>0.1 ± 0.1</td>
<td>0.4 ± 0.1</td>
<td>0.7 ± 0.2</td>
<td>0.2 ± 0.1</td>
</tr>
<tr>
<td>$n4\pi^+\pi^-\pi^0$</td>
<td>0.1 ± 0.1</td>
<td>0.1 ± 0.1</td>
<td>0.1 ± 0.1</td>
<td>0.1 ± 0.1</td>
<td>0.1 ± 0.1</td>
<td>0.1 ± 0.1</td>
<td>0.7 ± 0.2</td>
<td>0.2 ± 0.1</td>
</tr>
</tbody>
</table>
\[ \gamma p \rightarrow \rho n^{+}n^{-}\pi^{0} \quad (b) \]
\[ \gamma p \rightarrow n(m + 1)\pi^{+}\pi^{-} \quad (c) \]

(i) 4C events

Events which give a 4C-fit are accepted if the fit probability was \( P(\chi^2) > 0.01 \) and if the missing mass squared was zero within the limits

\[ |M^{2}| < 3 \cdot \Delta M^{2} \, . \]

Each event is checked for the correct ionization. Additional 1C-fits are disregarded. The number of fitted events is corrected for acceptance losses (see subsect. 3.1).

(ii) 1C events with one unmeasured charged particle

If a proton or \( \pi^{+} \) stops inside the target counter, the reaction \( \gamma p \rightarrow p(n\pi^{+})(n\pi^{-}) \) \((m \geq 1)\) gives a one-constraint fit. In these cases we check whether the calculated momentum of the missing particle is less than 300 MeV for protons or 200 MeV for pions provided the dip angle of the missing particle is \( |\lambda| < 0.72 \) rad. For larger dip angles it is possible for the particle to escape through the target enclosure such that larger momenta are possible.

The number of fitted events of reaction (a) is corrected for acceptance losses (~20%). A possible contamination of reaction (a) with other reactions is less than 2%. This error is small compared to the error from the acceptance corrections and therefore neglected.

(iii) 1C events with neutral particles

We now turn to reactions (b) and (c) with one kinematic constraint. A fit is accepted if there is agreement in the observed and calculated ionization, and if the missing mass is correct within two standard deviations

\[ |M^{2} - M_{\pi^{0}(n)}^{2}| < 2\Delta M^{2} \, . \]

If there is more than one accepted fit the hypothesis with the smaller missing mass difference divided by the average error \( \Delta M \) is accepted:

\[ |M^{2} - M_{\pi^{0}}^{2}|/\Delta M_{\pi^{0}}^{2} \quad \text{or} \quad |M^{2} - M_{n}^{2}|/\Delta M_{n}^{2} \, . \]

The estimated uncertainty of this method is 3% for \( \pi^{0} \) and 5% for \( n \) hypotheses.

The distribution of fit probabilities \( P(\chi^2) \) increases below 0.20. This is presumably due to events with two neutrals, giving a spurious (albeit bad) 1C fit. We correct the number of events accordingly by taking the number of events for \( P(\chi^2) > 0.20 \) and multiplying this number by 1.25. The difference of the uncorrected and corrected event numbers is added to the number of unfitted (multineutral) events. The numbers are then corrected for acceptance losses (~2%).

At low squared four-momentum transfer \( t \) from the photon to the \( \pi^{+}\pi^{-}\pi^{0} \) system we lose events in which the proton stops inside the target counter. These losses
are corrected with the help of the $t$ distribution $d\sigma/dt$ for events with $m_{\pi^+\pi^-\pi^0} < 1.0$ GeV; the missing events at low $t$ are corrected and the corresponding number of events is subtracted from the unfitted events with one unobserved track.

Fig. 4. Energy dependence of the total cross section for the reaction $\gamma p \rightarrow p\pi^+\pi^-$.  

Fig. 5. Energy dependence of the total cross sections for the reactions $\gamma p \rightarrow p\pi^+\pi^-\pi^0$ and $\gamma p \rightarrow n\pi^+\pi^+\pi^-$.  

(iv) Unfitted events

Reactions with more than one neutral particle, like

\[ \gamma p \rightarrow p m n^+ m n^- k \pi^0, \quad k \geq 2, \]

\[ \gamma p \rightarrow n (m + 1) n^+ m n^- \ell \pi^0, \quad \ell \geq 1, \]

cannot be fitted. For these events we require the missing mass to be larger than the mass of the supposedly missing particles (within errors):

\[ |M M^2 + 2 \Delta M M^2| > (2 M_{\pi^0})^2. \]

\[ |M M^2 + 2 \Delta M M^2| > (M_n + M_{\pi^0})^2. \]

Ambiguities between several possible hypotheses cannot be resolved in this case.

The cross sections are given in table 3. Our results are shown in figs. 4—7 together with the cross sections from other experiments.
3.3. Resonance production in the channel $\gamma p \rightarrow p\pi^+\pi^-$

In the following sections we describe the procedure to obtain the resonance production cross sections for reactions having three or five charged particles in the final state. It should be noted that the cross sections depend on the hypothesis taken into account. Therefore systematical errors could be much higher than statistical errors. In our results only statistical errors are given. The channel $\gamma p \rightarrow p\pi^+\pi^-$ is dominated by $\rho^0$ production and at lower energies by $\Delta^+(1236)$ production. Above $E_\gamma = 2.3$ GeV we observe some $f^0$ production. In figs. 8 and 9 we show the distribution of the effective masses for $M_{\pi^+\pi^-}$ and $M_{\pi^+\pi^-}$.

The Dalitz plot shows that the events in the $\rho^0$ region are not equally distributed in the $p\pi^+$ mass. This means that the $\pi^+$ is not isotropic in the $\rho^0$ helicity system but has a decay angular distribution $W(\cos \theta_H, \phi_H) \sim \sin^2 \theta_H$. ($\cos \theta_H, \phi_H$ are the polar and azimuth angle in the helicity system).

The distribution of the momentum transfer $d\sigma/d|t| (\gamma \rightarrow \pi^+\pi^-)$ indicates a peripheral process and could be fitted by an exponential function $d\sigma/d|t| = d\sigma/d|t|_{t=0} \exp(-B|t|), B$ is given in table 4 and in ref. [11].

Taking these characteristics into account we used the following fit function in
order to determine the fractions of $\rho^0$ and $\Delta$ production:

$$L = \sum_{i=1}^{N} g_i \ln \left( \frac{a_{\Delta^{++}} \frac{BW_{\Delta^{++}}}{N_{\Delta^{++}}} e^{-B_{\Delta^{++}} t_{\Delta^{++}}} + a_{\Delta^0} \frac{BW_{\Delta^0}}{N_{\Delta^0}} e^{-B_{\Delta^0} t_{\Delta^0}}}{1 - a_{\rho} - a_{\Delta^{++}} - a_{\Delta^0}} \right) ,$$

with

- $N =$ number of events,
- $g_i =$ weight of event,
- $a_{\Delta^{++}}, a_{\Delta^0}, a_{\rho} =$ fractions of $\Delta^{++}, \Delta^0, \rho$,
- $N_{\Delta^{++}} =$ normalisation integral (same for $N_{\Delta^0}, N_{\rho}, N_{PS}$),
- $t_{\Delta^{++}}, t_{\Delta^0}, t_{\rho} =$ squared four-momentum transfers $p \rightarrow p\pi^+, p \rightarrow p\pi^-, \gamma \rightarrow \pi^+\pi^-$

For the $\Delta(1236)$ we use a shape which agrees with that expected from the $\pi N$ phase.
Fig. 9. Reaction $\gamma p \rightarrow p\pi^+\pi^-$. Distribution of the effective mass $M_{\pi^+\pi^-}$ for (a) $1.6\text{ GeV} < E_\gamma < 2.6\text{ GeV}$, (b) $2.6\text{ GeV} < E_\gamma < 4.0\text{ GeV}$ and (c) $4.0\text{ GeV} < E_\gamma < 6.3\text{ GeV}$ (not corrected for “total losses” (see subsect. 3.1)).

shift $\delta_{33}$:

$$\text{BW}_\Delta = \frac{\sin^2\delta_{33}}{\pi M_\Delta} \frac{M_{\pi^+}}{\Gamma(M_{\pi^+})} \frac{\pi q(M_{\pi^+})}{\Gamma(M_{\pi^+})}.$$  

The values of $\delta_{33}$ have been taken from phase-shift analysis [12], further we use $q(M) = \text{three-momentum of the } \pi^+ \text{ in the rest system of a } p\pi^+ \text{ state with total mass } M$. To take the $\rho^0$ mass shift [2–5,11] into account (fig. 8) we fitted the $\rho^0$ with two models:

(i) The “parametrization”: The relativistic Breit–Wigner [13] function is multiplied by $(M_\rho/M_{\pi^+})^{n(t)}$. This factor was proposed by Ross and Stodosky [14] to account for the diffractive character of the $\rho^0$ production in the frame work of vector dominance:

$$\text{BW}_\rho = \frac{M_{\pi^+}}{\pi q(M_{\pi^+})} \frac{M_\rho \Gamma(M_{\pi^+})}{(M_{\rho}^2 - M_{\pi^+}^2)^2 + M_\rho^2 \Gamma^2(M_{\pi^+})} \left( \frac{M_\rho}{M_{\pi^+}} \right)^{n(t)},$$

$$\Gamma(M_{\pi^+}) = \Gamma_\rho \left( \frac{q(M_{\pi^+})}{q(M_\rho)} \right)^3 \frac{2}{1 + (q(M_{\pi^+})/q(M_\rho))^2}.$$  

Instead of using an exponent of 4, the data are described more precisely if the exponent $n(t)$ is a free parameter depending on the squared four-momentum transfer $t$. The $t$-dependence of $n(t)$ could be described by the straight line fit

$$n(t) = (5.5 \pm 0.5) - (10.1 \pm 2.5)t.$$

For the mass and width we obtain the fitted values

$$M_\rho = (765.1 \pm 1.2)\text{ MeV}, \quad \Gamma_\rho = (147.3 \pm 3.3)\text{ MeV}.$$
Table 4
Reaction $\gamma p \rightarrow p\rho^0$; parameters of the differential cross sections

$$\frac{d\sigma}{d|t|} = \left| \frac{d\sigma}{d|t|} \right|_{t=0} \exp(-B|t|)$$

<table>
<thead>
<tr>
<th>Beam energy $E_\gamma$ (GeV)</th>
<th>&quot;Parametrisation&quot; $B$</th>
<th>Interference model $B$</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>$\mu_b$ (GeV/c)$^2$</td>
<td>(GeV/c)$^2$</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>1.6–2.1</td>
<td>$205 \pm 20$</td>
<td>$7.8 \pm 0.4$</td>
</tr>
<tr>
<td>2.1–2.6</td>
<td>$160 \pm 13$</td>
<td>$6.9 \pm 0.3$</td>
</tr>
<tr>
<td>2.6–3.25</td>
<td>$134 \pm 9$</td>
<td>$7.6 \pm 0.3$</td>
</tr>
<tr>
<td>3.25–4.0</td>
<td>$128 \pm 9$</td>
<td>$8.1 \pm 0.3$</td>
</tr>
<tr>
<td>4.0–6.3</td>
<td>$158 \pm 13$</td>
<td>$8.9 \pm 0.4$</td>
</tr>
</tbody>
</table>
events for unobserved decay modes. The $\pi^+\pi^-$ effective mass and the cross sections for $\rho^0$ and $f^0$ production in backward direction are shown in fig. 12.

3.4. Resonance production in the channel $\gamma p \rightarrow p\pi^+\pi^-\pi^0$

In figs. 13-15 we show $M_{\pi^+\pi^-\pi^0}$, $M_{\pi^+\pi^-\pi^0}$, $M_{\pi^+\pi^-\pi^0}$, $M_{\pi^+\pi^-\pi^0}$, $M_{\pi^+\pi^-\pi^0}$ effective mass distributions of the reaction $\gamma p \rightarrow p\pi^+\pi^-\pi^0$. These distributions are not cor-

![Fig. 10. Energy dependence of the cross section for the reaction $\gamma p \rightarrow p\rho^0$, using fit (i) (see subsect. 3.3).](image)

![Fig. 11. Energy dependence of the cross section for the reactions $\gamma p \rightarrow \Delta^{++}\pi^-$ and $\gamma p \rightarrow \Delta^0\pi^+$.](image)
### Table 5
Reaction cross sections (μb) of the channel γp → pπ⁺π⁻

<table>
<thead>
<tr>
<th>Beam energy $E_\gamma$ (GeV)</th>
<th>1.6–1.9</th>
<th>1.9–2.1</th>
<th>2.1–2.3</th>
<th>2.3–2.6</th>
<th>2.6–3.25</th>
<th>3.25–4.0</th>
<th>4.0–5.0</th>
<th>5.0–6.3</th>
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<tbody>
<tr>
<td>Reaction</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$p\rho^0$ parametrisation</td>
<td>21.8 ± 1.4</td>
<td>22.1 ± 1.7</td>
<td>22.2 ± 1.6</td>
<td>19.7 ± 1.1</td>
<td>18.5 ± 1.1</td>
<td>17.7 ± 1.0</td>
<td>18.9 ± 2.0</td>
<td>17.4 ± 2.0</td>
</tr>
<tr>
<td>$p\rho^0$ interference model</td>
<td>19.2 ± 1.6</td>
<td>20.7 ± 1.9</td>
<td>20.8 ± 1.8</td>
<td>17.0 ± 1.3</td>
<td>17.0 ± 1.3</td>
<td>17.0 ± 1.2</td>
<td>15.2 ± 1.4</td>
<td></td>
</tr>
<tr>
<td>$p\rho^0$ backw (cos $\theta &lt; 0$)</td>
<td>2.8 ± 0.8</td>
<td>1.1 ± 0.5</td>
<td>0.8 ± 0.7</td>
<td>0.7 ± 0.2</td>
<td>0.5 ± 0.2</td>
<td>0.2 ± 0.1</td>
<td>0.1 ± 0.1</td>
<td>0.1 ± 0.1</td>
</tr>
<tr>
<td>$p\rho^0$ backw a) (cos $\theta &lt; 0$)</td>
<td></td>
<td></td>
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<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$\Delta^{++}π^-$</td>
<td>1.3 ± 0.37</td>
<td>0.39 ± 0.13</td>
<td>0.19 ± 0.06</td>
<td>0.1 ± 0.1</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$\Delta^0(→ππ^-)π^+$</td>
<td>6.1 ± 1.0</td>
<td>5.4 ± 0.9</td>
<td>4.2 ± 0.8</td>
<td>3.8 ± 0.6</td>
<td>2.9 ± 0.5</td>
<td>1.7 ± 0.5</td>
<td>1.2 ± 0.2</td>
<td>0.9 ± 0.2</td>
</tr>
<tr>
<td>$Δ^0(→ππ^-)π^+$</td>
<td>0.9 ± 0.6</td>
<td>0.7 ± 0.7</td>
<td>0.2 ± 0.5</td>
<td>0.1 ± 0.2</td>
<td>0.2 ± 0.2</td>
<td>0.1 ± 0.2</td>
<td>0.4 ± 0.1</td>
<td>0.3 ± 0.1</td>
</tr>
</tbody>
</table>

a) Corrected for unobserved decay modes
Fig. 12. Distribution of the effective mass $M_{\pi^+\pi^-}$ for $2.3 \leq E_\gamma \leq 3.25$ and $\cos \theta^* < 0$ and energy dependence of the cross sections for backward produced $\rho^0$ and $\pi^0$.

Fig. 13. Reaction $\gamma p \rightarrow p\pi^+\pi^-\pi^0$. Distribution of the effective masses $M_{\pi^+\pi^-\pi^0}$ and $M_{\pi^+\pi^-}$ for (a) $1.6 \text{ GeV} < E_\gamma < 2.6 \text{ GeV}$, (b) $2.6 \text{ GeV} < E_\gamma < 4.0 \text{ GeV}$ and (c) $4.0 \text{ GeV} < E_\gamma < 6.3 \text{ GeV}$ (not corrected for “total losses” (see subsect. 3.1)).
Fig. 14. Reaction $\gamma p \rightarrow p\pi^+\pi^-\pi^0$. Distribution of the effective masses $M_{\pi^+\pi^-\pi^0}$ and $M_{\pi^-\pi^+\pi^0}$ for (a) $1.6 \text{ GeV} < E_\gamma < 2.6 \text{ GeV}$, (b) $2.6 \text{ GeV} < E_\gamma < 4.0 \text{ GeV}$ and (c) $4.0 \text{ GeV} < E_\gamma < 6.3 \text{ GeV}$ (not corrected for "total losses" (see subsect. 3.1)).

Fig. 15. Reaction $\gamma p \rightarrow p\pi^+\pi^-\pi^0$. Distribution of the effective masses $M_{\pi^+\pi^-\pi^0}$ and $M_{\pi^-\pi^+\pi^0}$ for (a) $1.6 \text{ GeV} < E_\gamma < 2.6 \text{ GeV}$, (b) $2.6 \text{ GeV} < E_\gamma < 4.0 \text{ GeV}$ and (c) $4.0 \text{ GeV} < E_\gamma < 6.3 \text{ GeV}$ (not corrected for "total losses" (see subsect. 3.1)).
Fig. 16. Energy dependence of the cross sections for the reactions $\gamma p \rightarrow p\omega$, $\gamma p \rightarrow p\rho^0\pi^0$, $\gamma p \rightarrow p\rho^+\pi^-$, $\gamma p \rightarrow p\rho^-\pi^+$ and $\gamma p \rightarrow \Delta^{++}\rho^-$. The SBT-Data for the reactions with $\rho$ or $\Delta$ were taken from ref. [18].

Fig. 16. Energy dependence of the cross sections for the reactions $\gamma p \rightarrow p\omega$, $\gamma p \rightarrow p\rho^0\pi^0$, $\gamma p \rightarrow p\rho^+\pi^-$, $\gamma p \rightarrow p\rho^-\pi^+$ and $\gamma p \rightarrow \Delta^{++}\rho^-$. The SBT-Data for the reactions with $\rho$ or $\Delta$ were taken from ref. [18].

rected for events in which the proton is stopped inside the target (giving a two-prong unfitted event) or where one particle has an angle $\theta < 2^\circ$ with respect to the beam axis. Consequently the $\omega$ peak looks smaller at medium energies than at higher energies, due to the different thicknesses of the target counter.

The $\omega$ production cross section is obtained by interpolating the background from below and above the peak mass region. The corrections for acceptance losses are of the order of 15%–30% at different energies. The results are given in table 6 and fig. 16 where an additional correction for unobserved $\omega$ decay modes has been applied. In addition the cross section for backward produced $\omega$ ($\cos \theta_{\text{cms}} < 0$) is given (fig. 17).

The $\eta$ signal is free from background. The $\eta$ production cross section was corrected for acceptance losses and unseen decays of the $\eta$. Besides the reactions $\gamma p \rightarrow p\omega$ and $\gamma p \rightarrow p\eta$, we further observed inelastic production of $\rho^+$, $\rho^0$, $\rho^-$, $\Delta^+$, $\Delta^{++}$ and double resonance production of $\Delta^{++}\rho^-$ and $\Delta^+\rho^0$.

To determine the cross sections for $\rho$, $\Delta$ and $\rho\Delta$ production we use the maximum
Table 6
Cross sections of the channel $\gamma p \rightarrow p\pi^+\pi^-\pi^0$ (\textmu b); quasi two-body reactions are not included in the other corresponding reactions

<table>
<thead>
<tr>
<th>Beam energy $E_\gamma$ (GeV)</th>
<th>1.6–2.1</th>
<th>2.1–2.6</th>
<th>2.6–3.25</th>
<th>3.25–4.0</th>
<th>4.0–5.0</th>
<th>5.0–6.3</th>
</tr>
</thead>
<tbody>
<tr>
<td>Reaction</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$p\omega$</td>
<td>7.6 ± 1.5</td>
<td>5.3 ± 0.5</td>
<td>3.9 ± 0.3</td>
<td>1.8 ± 0.2</td>
<td>2.7 ± 0.5</td>
<td>2.0 ± 0.5</td>
</tr>
<tr>
<td>$p\omega$ backw</td>
<td>2.1 ± 0.5</td>
<td>0.8 ± 0.1</td>
<td>0.13 ± 0.04</td>
<td>0.14 ± 0.05</td>
<td>0.13 ± 0.04</td>
<td></td>
</tr>
<tr>
<td>$p\pi^0\pi^0$</td>
<td>1.1 ± 0.4</td>
<td>1.1 ± 0.4</td>
<td>1.0 ± 0.3</td>
<td>0.3 ± 0.3</td>
<td>0.2 ± 0.3</td>
<td>0.0 ± 0.3</td>
</tr>
<tr>
<td>$pp^+\pi^-$</td>
<td>1.8 ± 0.5</td>
<td>2.0 ± 0.4</td>
<td>2.2 ± 0.4</td>
<td>1.8 ± 0.4</td>
<td>1.2 ± 0.4</td>
<td>1.3 ± 0.3</td>
</tr>
<tr>
<td>$p\rho^0\pi^0$</td>
<td>0.8 ± 0.5</td>
<td>1.9 ± 0.5</td>
<td>1.7 ± 0.4</td>
<td>0.7 ± 0.3</td>
<td>0.8 ± 0.4</td>
<td>0.9 ± 0.3</td>
</tr>
<tr>
<td>$\Delta'^{++}\pi^-\pi^0$</td>
<td>0.5 ± 0.3</td>
<td>0.8 ± 0.5</td>
<td>1.2 ± 0.3</td>
<td>0.8 ± 0.3</td>
<td>0.4 ± 0.2</td>
<td>0.3 ± 0.2</td>
</tr>
<tr>
<td>$\Delta^0(p\pi^0)\pi^+\pi^-$</td>
<td>0.4 ± 0.3</td>
<td>1.2 ± 0.5</td>
<td>1.1 ± 0.3</td>
<td>0.8 ± 0.3</td>
<td>0.0 ± 0.2</td>
<td>0.1 ± 0.2</td>
</tr>
<tr>
<td>$\Delta'^{++}\rho^-$</td>
<td>3.5 ± 0.6</td>
<td>2.8 ± 0.5</td>
<td>0.9 ± 0.4</td>
<td>0.5 ± 0.2</td>
<td>0.4 ± 0.2</td>
<td>0.5 ± 0.2</td>
</tr>
<tr>
<td>$\Delta^0(p\pi^0)\rho^0$</td>
<td>0.3 ± 0.5</td>
<td>0.4 ± 0.4</td>
<td>0.0 ± 0.3</td>
<td>0.0 ± 0.2</td>
<td>0.7 ± 0.2</td>
<td>0.6 ± 0.2</td>
</tr>
</tbody>
</table>

a) Corrected for decays other than $\pi^+\pi^-\pi^0$.

likelihood fit function

$$L = \sum_{i=1}^{N} g_i \ln \left( \sum_{\rho, \Delta, \Delta\rho} a_{\rho} \left( \frac{BW_\rho}{N_\rho} \right) + \sum_{\Delta} a_{\Delta} \left( \frac{BW_\Delta}{N_\Delta} \right) + \sum_{\Delta\rho} a_{\Delta\rho} \left( \frac{BW_{\Delta\rho}}{N_{\Delta\rho}} \right) + \left( 1 - \sum_{\rho, \Delta, \Delta\rho} a_i \right) \frac{1}{N_{PS}} f(t) \right),$$

where

$$\rho = \rho^+, \rho^-, \rho^0, \quad \Delta = \Delta^{++}, \Delta^+, \Delta^0.$$ 

In the fit we use only events outside the $\omega$ region ($M_{\pi\pi\pi} > 0.88$ GeV). $f(t)$ describes

![Fig. 17. Energy dependence of the cross section for backward produced $\omega$ ($\cos \theta_{\text{c.m.s.}} < 0$) in the reaction $\gamma p \rightarrow p\omega$.](image)
Fig. 18. Reaction $\gamma p \rightarrow n2\pi^+\pi^-$. Distribution of the effective masses $M_{\pi^+\pi^-}$ and $M_{n\pi^-}$ for (a) $1.6 \text{ GeV} < E_\gamma < 2.6 \text{ GeV}$, (b) $2.6 \text{ GeV} < E_\gamma < 4.0 \text{ GeV}$ and (c) $4.0 \text{ GeV} < E_\gamma < 6.3 \text{ GeV}$ (not corrected for "total losses" (see subsect. 3.1)).

the $t$ distribution of the background and is taken to be $f(t) = 1/(t - t_{\text{cut}}^2)$. BW$_\rho$ is the relativistic Breit-Wigner function as described in subsect. 3.3 without the factor $(M_{\rho}/M_{\pi\pi})^2 \delta(t)$, and BW$_{\Delta\rho} = \text{BW}_{\rho} \text{BW}_{\Delta}$. For these reactions the corrections for acceptance losses are negligible. The results are summarized in table 6 and fig. 16.

Table 7
Cross sections of the channel $\gamma p \rightarrow n2\pi^+\pi^-$ (µb)

<table>
<thead>
<tr>
<th>Beam energy $E_\gamma$ (GeV)</th>
<th>1.6–2.1</th>
<th>2.1–2.6</th>
<th>2.6–3.25</th>
<th>3.25–4.0</th>
<th>4.0–5.0</th>
<th>5.0–6.3</th>
</tr>
</thead>
<tbody>
<tr>
<td>Reaction</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$n_0^{0,\pi^+}$</td>
<td>0.06 ± 0.05</td>
<td>1.54 ± 0.15</td>
<td>1.32 ± 0.25</td>
<td>0.84 ± 0.24</td>
<td>0.71 ± 0.4</td>
<td>0.95 ± 0.45</td>
</tr>
<tr>
<td>$\Delta^0(-\pi\pi^+)\pi^+\pi^-$</td>
<td>0.02 ± 0.05</td>
<td>0 ± 0.05</td>
<td>0 ± 0.05</td>
<td>0 ± 0.05</td>
<td>0 ± 0.2</td>
<td></td>
</tr>
<tr>
<td>$\Delta^-$($\rightarrow\pi\pi^+\pi^-$)</td>
<td>2.13 ± 0.40</td>
<td>1.60 ± 0.25</td>
<td>1.17 ± 0.30</td>
<td>0.67 ± 0.16</td>
<td>0.24 ± 0.2</td>
<td>0.15 ± 0.15</td>
</tr>
<tr>
<td>$\Delta^+(-\pi\pi^+)\rho^0$</td>
<td>0.02 ± 0.05</td>
<td>0.25 ± 0.10</td>
<td>0.16 ± 0.10</td>
<td>0.21 ± 0.10</td>
<td>0.2 ± 0.2</td>
<td></td>
</tr>
<tr>
<td>nA$_2$ a)</td>
<td></td>
<td></td>
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</tr>
<tr>
<td></td>
<td>0.7 ± 0.3</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td>0.3 ± 0.3</td>
</tr>
</tbody>
</table>

a) Corrected for decays other than $\pi^+\pi^-n^0$. 
Fig. 19. Reaction $\gamma p \rightarrow n\pi^+\pi^-$. Distribution of the effective mass $M_{\pi^+\pi^-}$ for (a) $1.6 \text{ GeV} < E_\gamma < 2.6 \text{ GeV}$, (b) $2.6 \text{ GeV} < E_\gamma < 4.0 \text{ GeV}$ and (c) $4.0 \text{ GeV} < E_\gamma < 6.3 \text{ GeV}$ (not corrected for “total losses” (see subsect. 3.1)).

3.5. Resonance production in the channel $\gamma p \rightarrow n2\pi^+\pi^-$

We show in figs. 18 and 19 the distributions of the effective masses $M_{\pi^+\pi^-}$, $M_{\pi\pi}$, and $M_{\pi^+\pi^-}$ for the reaction $\gamma p \rightarrow n\pi^+\pi^-$. This channel is dominated by production of $\Delta^-$ and $\rho^0$ while production of $\Delta^+$ and the two-body reaction $\gamma p \rightarrow \Delta^+\rho^0$ are unimportant. We use the same fit procedure as described in the previous section. To take the two combinations for the $\rho^0$ into account we add the fitted fractions for each combination.

In the photon energy region above $E_\gamma > 3.25 \text{ GeV}$ we find a small signal for production of the $A_2^-$. In order to get the fraction of $A_2^-$ we include a term $a_A(1/t_{p\rightarrow n})BW_A(\pi^+\pi^-)/N_A$ into our fit function. At lower energies the phase space has its maximum near the $A_2$ mass inhibiting any $A_2$ separation. The cross sections are given in table 7.

3.6. Resonance production in the channel $\gamma p \rightarrow p2\pi^+2\pi^-$

In this channel we consider only $\rho^0$, $\Delta^{++}$, and some $A_2^-$ production (fig. 20). To take the four combinations of $\pi^+\pi^-$ for the $\rho$ into account, and to avoid confusion with the sum of all fractions $a_i$ being less than one we chose the following likelihood function:

$$L = \sum_{i=1}^{N} g_i \ln \left( \sum_{p=1}^{N_{\text{comb}}} \left( \sum_{i=1}^{N_{\text{ch}}} C_i \frac{BW f(t_i)}{N} \right) + \frac{1 - \sum C_i}{N_{PS}} \right).$$

The first sum in the brackets is for the combinations, the second one for the different reactions ($\rho$, $\Delta$, $A_2$). The fractions $a_i$ are then given by $a_i = N_{\text{comb}}C_i$.

For $f(t)$ we use an exponential function $\exp(-b|t|)$ where $b$ is fitted; the results for $b$, averaged over the whole energy range, are $b = 2.3 \pm 0.5$ for $\rho^0$, $b = 1.2 \pm 0.3$ for $\Delta^{++}$ and $b = 1.2 \pm 0.3$ for $A_2^-$ production. The resulting cross sections are shown in fig. 21 and table 8.
Fig. 20. Reaction $\gamma p \rightarrow p2\pi^+2\pi^-$. Distribution of the effective masses $M_{\pi^+\pi^-}$, $M_{\pi^+}$ and $M_{\pi^+\pi^+\pi^-}$ for (a) $1.6\,\text{GeV} < E_\gamma < 4.0\,\text{GeV}$ and (b) $4.0\,\text{GeV} < E_\gamma < 6.3\,\text{GeV}$ (not corrected for "total losses" (see subsect. 3.1)).

Table 8
Cross sections of the channels $\gamma p \rightarrow p2\pi^+2\pi^-$, $\gamma p \rightarrow p2\pi^+2\pi^-\pi^0$ and $\gamma p \rightarrow n3\pi^+2\pi^-$ (mb); quasi-two-body reactions are not included in the other corresponding reactions.

<table>
<thead>
<tr>
<th>Beam energy $E_\gamma$ (GeV)</th>
<th>2.1–2.6</th>
<th>2.6–3.25</th>
<th>3.25–4.0</th>
<th>4.0–5.0</th>
<th>5.0–6.0</th>
</tr>
</thead>
<tbody>
<tr>
<td>Reaction</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$\gamma p \rightarrow p2\pi^+2\pi^-$</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$p\rho^0\pi^+\pi^-$</td>
<td>0.3 ± 0.3</td>
<td>1.4 ± 0.6</td>
<td>2.0 ± 0.7</td>
<td>3.1 ± 0.8</td>
<td>3.3 ± 0.8</td>
</tr>
<tr>
<td>$\Delta^{++}\pi^+\pi^-$</td>
<td>1.9 ± 0.5</td>
<td>1.1 ± 0.5</td>
<td>0.9 ± 0.4</td>
<td>1.5 ± 0.3</td>
<td>0.7 ± 0.2</td>
</tr>
<tr>
<td>$\Delta^{++}A_2$</td>
<td></td>
<td></td>
<td></td>
<td>0.5 ± 0.2</td>
<td></td>
</tr>
<tr>
<td>$\Delta^{++}\rho^0\pi^-$</td>
<td></td>
<td></td>
<td></td>
<td>0.3 ± 0.2</td>
<td></td>
</tr>
<tr>
<td>$\gamma p \rightarrow p2\pi^+2\pi^-\pi^0$</td>
<td></td>
<td></td>
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</tr>
<tr>
<td>$p\pi^+\pi^-\pi^-\pi^-$</td>
<td>0.5 ± 0.2</td>
<td>1.8 ± 0.3</td>
<td>2.0 ± 0.3</td>
<td>1.6 ± 0.2</td>
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<tr>
<td>$p\pi^+\pi^-\pi^-\eta$</td>
<td>1.4 ± 0.3</td>
<td>2.8 ± 0.4</td>
<td>1.0 ± 0.3</td>
<td>1.1 ± 0.4</td>
<td></td>
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<tr>
<td>$pX^0$</td>
<td>0.3 ± 0.15</td>
<td>0.3 ± 0.15</td>
<td>0.3 ± 0.1</td>
<td>0.2 ± 0.1</td>
<td></td>
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<tr>
<td>$p\rho^0\pi^+\pi^-\pi^0$</td>
<td></td>
<td></td>
<td></td>
<td>0.8 ± 0.2</td>
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<tr>
<td>$\Delta^{++}\pi^+\pi^-\pi^0$</td>
<td></td>
<td></td>
<td></td>
<td>1.1 ± 0.3</td>
<td></td>
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<tr>
<td>$\Delta^{++}2\pi^-\pi^-$</td>
<td></td>
<td></td>
<td></td>
<td>1.3 ± 0.3</td>
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</tbody>
</table>

$\gamma p \rightarrow n3\pi^+2\pi^-$

| $\Delta^{-}\pi^+\pi^-$ | 0.4 ± 0.2 | 0.5 ± 0.2 |

a) Corrected for unobserved decay modes.
3.7. Resonance production in the channel $\gamma p \rightarrow p2\pi^+2\pi^-\pi^0$

The mass distributions of this channel show evidence for $\omega$, $\eta$, $X(1865)$, $\rho^0$ and $\Delta^{++}$ production (fig. 22). To calculate the fractions we use the fit procedure described in the previous section. For the shape of the $\omega$ and $\eta$ a Gaussian $G = \exp(-(m - m_0)^2/\sigma^2)$

$$
\gamma p \rightarrow p2\pi^+2\pi^-\pi^0
$$

Fig. 21. Energy dependence of the reactions $\gamma p \rightarrow p\pi^+\pi^-\rho^0$ and $\gamma p \rightarrow \Delta^{++}\pi^+2\pi^-$. 

Fig. 22. Reaction $\gamma p \rightarrow p2\pi^+2\pi^-\pi^0$. Distribution of the effective masses $M_{\pi^+\pi^-}$, $M_{\rho^+}$, $M_{\pi^+\pi^-\pi^0}$ and $M_{\pi^+\pi^-\pi^-\pi^0}$ (with $M_{\pi^+\pi^-\pi^0} < 0.6$ GeV) for (a) $1.6$ GeV $< E_\gamma < 4.0$ GeV and (b) $4.0$ GeV $< E_\gamma < 6.3$ GeV (not corrected for "total losses" (see subsect. 3.1)).
Fig. 23. Energy dependence of the cross sections for the reactions $\gamma p \rightarrow p\pi^+\pi^-\omega$, $\gamma p \rightarrow p\pi^+\pi^-\eta$ and $\gamma p \rightarrow \eta'$. 200 is used. The widths were characterized by the mass resolution $\sigma_0 = 20$ MeV of our experiment. To determine a production cross section for the $X^0$ we plot the $\eta\pi^+\pi^-$ mass using all $\eta$ events. In this distribution the $X^0$ shows up as a peak above the background. The cross sections, for $\omega$, $\eta$ and $X^0$ production corrected for unobserved decay modes, are given in fig. 23 and table 8.

Fig. 24. Reaction $\gamma p \rightarrow n3\pi^+2\pi^-$. Distribution of the effective mass $M_{\pi\pi^-}$ for (a) $1.6 \text{ GeV} < E_\gamma < 4.0 \text{ GeV}$ and (b) $4.0 \text{ GeV} < E_\gamma < 6.3 \text{ GeV}$ (not corrected for "total losses" (see subsect. 3.1)).
3.8. Resonance production in the channel $\gamma p \rightarrow n3\pi^+2\pi^-$

The only significant resonance signal observed in the mass distributions of this channel is the $\Delta$ (fig. 24). The cross section is determined with the fit described in subsect. 3.6 and given in table 8.

3.9. Resonance production in the channel $\gamma p \rightarrow p\pi^+\pi^- (+\text{neutrals})$

In this section we want to look for resonance production in the $\pi^+\pi^-(m\pi^0)$ final state with $m \geq 2$ where the $B^0 \rightarrow \omega\pi^0 \rightarrow \pi^+\pi^-2\pi^0$ could give a peak at 1.235 GeV [3]. In 40% of the no-fit events with three charged outgoing tracks we can distinguish by ionization between events which have a proton or a neutron in the final state but of course we know neither the number of $\pi^0$ nor their momenta. In fig. 25a we show the invariant mass for events with $|t_{p\rightarrow p}| < 0.5$ (GeV/c)$^2$ and 0.34 GeV $< M_{\pi^+\pi^-} < 0.58$ GeV which is the average mass of the two $\pi^+$s from the $\omega$ decay. Because the phase space for events with $E_\gamma < 4.0$ GeV has its maximum near the expected $B^0$ mass we use only the high energy data with $E_\gamma \geq 4.0$ GeV. In fig. 25a one can see an enhancement at 1240 MeV. From Monte-Carlo studies we exclude that the peak at 1240 MeV is a reflection of $\Delta$, $\rho$ or $\omega$ production. In fig. 25b the $\Delta(1236)$ is removed by a cut in the $p\pi^+$ mass. The solid curve is a background obtained from phase-space calculations for final states with 4, 5, 6 and 7 pions and normalized above 1.6 GeV. The mixture of final state pions was taken according to the measured cross sections and multiplied by isospin weights [20]. If the peak above background at 1240 MeV is due to a $B^0$ production we obtain a cross section

![Diagram](image-url)

Fig. 25. (a) Reaction $\gamma p \rightarrow p\pi^+\pi^- (m\pi^0)$, $m \geq 2$. Mass recoiling from proton with $|t| < 0.5$ (GeV/c)$^2$ with selection of 0.34 GeV $< M_{\pi^+\pi^-} < 0.58$ GeV to enhance events with $\pi^+\pi^-$ from $\omega$ decay. (b) The $\Delta(1236)$ is removed by a $M_{p\pi^+} > 1.32$ GeV cut. The solid curve gives the background.
of
\[ \sigma(\gamma p \rightarrow pB^0 \rightarrow p\pi^+\pi^-2\pi^0) = 0.5 \pm 0.2 \ \mu b \]
for \(4.0 \text{ GeV} < E_\gamma < 6.3 \text{ GeV}\).

4. Conclusion

In this experiment we examined the photoproduction on hydrogen over a wide photon energy range (1.6–6.3 GeV). An energy tagged photon beam and a nearly \(4\pi\) trigger on hadronic events in a streamer chamber allowed for recording single interactions and assigning to them the photon energy within 1%. With measured accuracies comparable to those of previous photoproduction experiments with optical detectors we analysed all exclusive final states comprised of 3, 5, 7 charged particles with or without one neutral particle.

We report the energy dependence of topological and reaction cross sections. All reactions exhibit substantial resonance productions, and in particular \(p\) and \(\Delta(1236)\). We applied Maximum-Likelihood fits to most of the reactions. The resonance production cross sections obtained are listed. Those cross sections which are also measured by previous experiments agree within errors with the published data.

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