

## LEFT-RIGHT SYMMETRY AND CP VIOLATION IN THE B SYSTEM

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We have reanalyzed a version of LR-symmetric models in which the right-handed W-boson could be light. Excluding several fine-tunings, it is shown that, due to constraints from  $\epsilon$ ,  $M_{WR} \gtrsim 5$  TeV, which would render its effects in heavy quark systems small. If fine-tuning is allowed, there are interesting effects in the B system – in particular,  $B_s^0 - \bar{B}_s^0$  mixing can be small, the CP asymmetry in  $B_d \rightarrow \psi K_S$  may be negative, and there is CP violation in Cabibbo allowed  $B_s$  decays.

Although the observed CP violation can be incorporated into the standard model in a satisfactory way, new forces might be responsible for this effect. CP violation has been considered in a variety of extensions of the standard model such as supersymmetry [1,2], extended Higgs models [1,3], and left-right (LR) symmetric theories [1,4]. In LR symmetric theories, the right-handed Cabibbo–Kobayashi–Maskawa (CKM) matrix,  $V^R$ , is usually taken to be equal to the usual left-handed CKM matrix,  $V^L$ . Due to the  $K_L - K_S$  mass difference, this then implies [5] a large mass  $M_R$  for the right-handed charged intermediate vector boson,  $W_R$ , whose effects are then suppressed.

Larger effects are possible if  $M_R$  is small, or, more precisely, if  $\beta_R \equiv (g_R^2/g_L^2)(M_L^2/M_R^2)$  is as large as possible. Here  $g_L$  and  $g_R$  are the left- and right-handed gauge couplings, respectively, and  $M_L$  is the mass of the ordinary W-boson. The effect of the  $W_R$  might then be important in B-meson mixings and decays. Furthermore, because of the large number of phases in  $V^R$ , CP violation could be sizeable in processes where the standard model gives very little contribu-

tion, for instance in Cabibbo allowed  $B_s$  decays such as  $B_s \rightarrow \psi\phi$ .

In order to remove the constraints on  $\beta_R$ , the restriction  $V^R = V^L$  must be relaxed. The right-handed contributions to kaon weak processes are of the form  $C_K^R \beta_R$ , where  $C_K^R$  depends on the elements of the first two columns of  $V^R$  (i.e. those elements which involve the d- and s-quarks). The corresponding expressions for mesons with heavy quarks (D, B) are of the same form, with  $C_K^R$  replaced by  $C_D^R$  (elements involving u- and c-quarks) or  $C_B^R$  (d- (or s-) and b-quarks). Kaon physics puts bounds only on  $C_K^R \beta_R$ ; in order to maximize the effects in heavy quark systems, one must therefore choose  $C_K^R$  as small as possible.

It is well known that  $K^0 - \bar{K}^0$  mixing puts strong constraints on  $\beta_R$  [5]. These come from limiting the contributions to  $\Delta M_K$  of the box diagrams in fig. 1 to the experimental value. These graphs are proportional to  $m_i m_j V_{id}^{R*} V_{js}^R$ , where  $i, j = u, c, t$  are the intermediate quarks. The contributions are clearly small if either  $V_{id}^R \simeq 0$  or  $V_{js}^R \simeq 0$ ;  $i, j = c, t$ . This condition immediately yields the following two forms for  $V^R$ :

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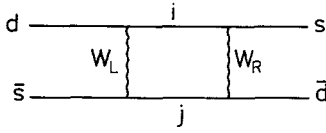


Fig. 1.  $W_L$ - $W_R$  contribution to  $K^0$ - $\bar{K}^0$  mixing. The internal quarks are  $i, j = u, c, t$ . There is also a diagram in which the internal bosons and quarks are interchanged.

$$\text{Model I: } V^R = \begin{pmatrix} e^{i\alpha} & * & * \\ * & ce^{i\sigma} & -se^{i\gamma} \\ * & se^{i\theta} & ce^{i\epsilon} \end{pmatrix}, \quad (1)$$

$$\text{Model II: } V^R = \begin{pmatrix} * & e^{i\alpha} & * \\ ce^{i\sigma} & * & -se^{i\gamma} \\ se^{i\theta} & * & ce^{i\epsilon} \end{pmatrix}. \quad (2)$$

Here  $c \equiv \cos \phi$ ,  $s \equiv \sin \phi$ , and the \*'s denote terms which are  $\ll 1$ . (The values of  $\phi, \alpha, \sigma, \gamma, \theta$ , and  $\epsilon$  need not be the same in the two models, but we use the same symbols for convenience.) Unitarity requires  $\sigma - \theta = \gamma - \epsilon$ . (3)

The long B-lifetime implies  $|\beta_R s| < 0.06$  <sup>#1</sup>. In addition, in Model II, the doubly Cabibbo suppressed charm decays  $c \rightarrow du\bar{s}$  yields  $|c\beta_R| \leq 0.05$ , if they are not observed above the prediction of the standard model <sup>#2</sup>; the strongest limit on such decays of 0.4% for  $D^+ \rightarrow K^+ \pi^+ \pi^-$  [6] gives  $|c\beta_R| \leq 0.06$ . Thus, in Model II,  $\beta_R < \frac{1}{16}$ .  $B_d^0$ - $\bar{B}_d^0$  mixing [7] will constrain  $\beta_R$  even further.

These plausible results have been confirmed recently in a careful study by Langacker and Sankar [8]. They consider four different possibilities for the right-handed neutrino: heavy Majorana, heavy Dirac, intermediate mass (10-100 MeV), and very light. Constraints on  $\beta_R$  are obtained in each case using experimental information from  $\Delta M_K$ ,  $B_d^0$ - $\bar{B}_d^0$  mixing, B decays, neutrinoless double beta decay, universality, nonleptonic kaon decays, muon decay and astrophysics. They find that the weakest limits on  $\beta_R$  occur when the right-handed neutrino is heavy and Dirac. In this case, when reasonable restrictions on fine-tuning are imposed (for example, the \*'s in eqs. (1) and

(2) are allowed to be as large as  $10^{-2}$ ) they obtain

$$\text{Model I: } \beta_R \lesssim 0.04, \quad \frac{g_L M_R}{g_R} \gtrsim 400 \text{ GeV},$$

$$\text{Model II: } \beta_R \lesssim 0.013, \quad \frac{g_L M_R}{g_R} \gtrsim 700 \text{ GeV}. \quad (4)$$

(The smaller value of  $\beta_R$  in Model II is mainly due to the requirement that the LR contribution to  $B_d^0$ - $\bar{B}_d^0$  mixing be no larger than that of the standard model.) However, they do note that if extreme fine-tuning is allowed, the  $W_R$  could still be as light as the  $W_L$ .

The aim of this paper is to further investigate Models I and II and their possible influence on mixing and CP violation in the B system. We will use the limits on  $\beta_R$  given in eq. (4). In addition, the elements  $V_{ij}^R$ , denoted by a \* in eqs. (1), (2), will be written as

$$V_{ij}^R = 10^{-2} X_{ij} \exp(i\phi_{ij}). \quad (5)$$

We begin with the analysis of  $\epsilon$  in the K system. Writing

$$\epsilon = \frac{1}{\sqrt{2}} \frac{\text{Im } M_{12}}{\Delta M_K}, \quad (6)$$

the contribution of the left-right box diagram of fig. 1 to  $\epsilon$  is <sup>#3</sup>

$$\epsilon_{LR} = (1.2 \times 10^6) \beta_R \sum_{i,j=u,c,t} \sqrt{x_i x_j} \eta_{ij} \times \text{Im}(V_{id}^{L*} V_{is}^R V_{jd}^{R*} V_{js}^L) I(x_i, x_j, \beta), \quad (7)$$

where  $x_i = m_i^2/M_L^2$  and  $\beta = M_L^2/M_R^2$ , i.e.  $\beta_R = (g_R^2/g_L^2)\beta$ . In deriving eq. (7), we have used the vacuum saturation approximation ( $B_K^{LR} = 1$ ) and the usual enhancement of 7.7 for the LR matrix element [5]. The  $\eta_{ij}$  are the short-distance QCD corrections, which we will set equal to 1 in the following. (Since, in general,  $\eta_{ij} \gtrsim 1$  [9], their inclusion would even strengthen our results.) The function  $I$  is given by [10]

$$I(x_i, x_j, \beta) = (1 + \frac{1}{4} x_i x_j \beta) I_1(x_i, x_j, \beta) - \frac{1}{4} (1 + \beta) I_2(x_i, x_j, \beta), \quad (8)$$

<sup>#3</sup> In view of the stringent limits we will disregard the mixing between  $W_L$  and  $W_R$ .

<sup>#1</sup> We consider only hadronic B decays since, in order to avoid bounds from muon decay and all mesonic semi-leptonic decays, we assume  $m_{\nu_R} > M_B$ .

<sup>#2</sup> We thank J.-M. Gérard for pointing this out.

where

$$I_1(x_i, x_j, \beta) = \frac{x_i \ln x_i}{(1-x_i)(1-x_i\beta)(x_i-x_j)} + (i \leftrightarrow j) - \frac{\beta \ln \beta}{(1-\beta)(1-x_i\beta)(1-x_j\beta)},$$

$$I_2(x_i, x_j, \beta) = \frac{x_i^2 \ln x_i}{(1-x_i)(1-x_i\beta)(x_i-x_j)} + (i \leftrightarrow j) - \frac{\ln \beta}{(1-\beta)(1-x_i\beta)(1-x_j\beta)}. \quad (9)$$

We will set  $\beta_R \simeq \beta$  in the following; thus both  $\beta$  and  $\beta_R$  are limited by eq. (4). We note that, because  $\beta \ll 1$ ,  $I$  depends on  $\beta$  essentially only through the last term ( $\ln \beta$ ). This  $\beta$  dependence will be kept explicitly in the following. Furthermore, in those graphs in which a t-quark is involved, the explicit dependence of  $\epsilon_{LR}$  on  $m_t$  is linear (ut, ct) or quadratic (tt). Thus the weakest limits on  $M_R$  come for small values of  $m_t$ . We will therefore take  $m_t = 50$  GeV (which is the same value used in ref. [9]), corresponding roughly to its lower bound.

Using the Wolfenstein parametrization of the left-handed CKM matrix [11]

$$V^L = \begin{pmatrix} 1 - \frac{1}{2}\lambda^2 & \lambda & A\rho\lambda^3 e^{-i\delta} \\ -\lambda & 1 - \frac{1}{2}\lambda^2 & A\lambda^2 \\ A\lambda^3(1 - \rho e^{i\delta}) & -A\lambda^2 & 1 \end{pmatrix}, \quad (10)$$

where  $\lambda = 0.22$ ,  $A \simeq 1.0$ , and  $\rho \leq 0.9$  [12], we obtain the following contributions to  $\epsilon_{LR}$  in Model I:

cu:  $0.026(\beta/0.04)c \sin(\sigma - \alpha)$   
 $\times [1 - 0.029 \ln(\beta/0.04)]$ , (11)

tu:  $0.01(\beta/0.04)s [\sin(\theta - \alpha) - \rho \sin(\theta - \alpha - \delta)]$   
 $\times [1 - 0.12 \ln(\beta/0.04)]$ ,

cc:  $0.28(\beta/0.04)X_{cd}c \sin(\sigma - \varphi_{cd})$   
 $\times [1 - 0.032 \ln(\beta/0.04)]$ ,

ct:  $0.13(\beta/0.04)X_{td}c \sin(\sigma - \varphi_{td})$   
 $\times [1 - 0.12 \ln(\beta/0.04)]$ ,

tc:  $0.13(\beta/0.04)X_{cd}s$   
 $\times [\sin(\theta - \varphi_{cd}) - \rho \sin(\theta - \varphi_{cd} - \delta)]$   
 $\times [1 - 0.12 \ln(\beta/0.04)]$ ,

tt:  $0.14(\beta/0.04)X_{td}s$   
 $\times [\sin(\theta - \varphi_{td}) - \rho \sin(\theta - \varphi_{td} - \delta)]$   
 $\times [1 - 0.17 \ln(\beta/0.04)]$ , (11 cont'd)

where we have taken  $m_u = 5.6$  MeV,  $m_c = 1.5$  GeV, and  $m_t = 50$  GeV. In eq. (11), the notation  $q_1 q_2$  indicates that  $i = q_1$  and  $j = q_2$  in eq. (7). The contributions from other combinations of quarks in the loop are much smaller. In Model II the relevant contributions are

uc:  $0.18(\beta/0.013)c \sin(\alpha - \sigma)$   
 $\times [1 - 0.028 \ln(\beta/0.013)]$ ,

ut:  $0.08(\beta/0.013)s \sin(\alpha - \theta)$   
 $\times [1 - 0.1 \ln(\beta/0.013)]$ ,

cc:  $0.09(\beta/0.013)X_{cs}c \sin(\varphi_{cs} - \sigma)$   
 $\times [1 - 0.031 \ln(\beta/0.013)]$ ,

ct:  $0.05(\beta/0.013)X_{cs}s \sin(\varphi_{cs} - \theta)$   
 $\times [1 - 0.1 \ln(\beta/0.013)]$ ,

tc:  $0.05(\beta/0.013)X_{ts}c$   
 $\times [\sin(\varphi_{ts} - \sigma) - \rho \sin(\varphi_{ts} - \sigma - \delta)]$   
 $\times [1 - 0.1 \ln(\beta/0.013)]$ ,

tt:  $0.05(\beta/0.013)X_{ts}s$   
 $\times [\sin(\varphi_{ts} - \theta) - \rho \sin(\varphi_{ts} - \theta - \delta)]$   
 $\times [1 - 0.14 \ln(\beta/0.013)]$ . (12)

We now require  $\epsilon_{LR}$  to be less than the experimental value of  $2.28 \times 10^{-3}$ . This can be achieved in various ways.

(1) No fine-tuning of the elements (including phases) of  $V^R$ . In this case, which is clearly the most natural,  $\beta$  must be sufficiently small so that each individual contribution to  $\epsilon_{LR}$  satisfies the above bound. We obtain, from eqs. (11), (12), as particular examples

cc:  $\beta < 2.81 \times 10^{-4}$ ,  $M_R > 4.8$  TeV,  
 tt:  $\beta < 3.62 \times 10^{-4}$ ,  $M_R > 4.3$  TeV, (13)

for Model I, and

$$\begin{aligned}
 \text{uc: } & \beta < 1.46 \times 10^{-4}, \quad M_R > 6.7 \text{ TeV}, \\
 \text{cc: } & \beta < 2.94 \times 10^{-4}, \quad M_R > 4.7 \text{ TeV}, \\
 \text{tt: } & \beta < 3.98 \times 10^{-4}, \quad M_R > 4.1 \text{ TeV}, \quad (14)
 \end{aligned}$$

for Model II. This result strengthens dramatically the lower limit on  $M_R$  which was thought to be avoided by eqs. (1), (2). It can be easily understood. The bounds in eq. (4) come about (in part) by requiring that the contribution from the right-handed sector to  $\Delta M_K$  be no larger than that of the standard model. However, in this model, the  $W_R$  contributes equally to  $\text{Re}(M_{12})$  and  $\text{Im}(M_{12})$ . Therefore the bound on  $\beta$  decreases by a factor  $\sim 500$ .

(2) Fine-tunings of the  $V_{ij}^R$ . There are several ways to do this. (We discuss here only Model I; Model II is similar.) (a) Cancellations among all the terms in eq. (11). (b) Adjustment of the  $CP$ -violating phases in  $V^R$  so that each term in (11) vanishes. For example, we can set  $\sigma \simeq \alpha \simeq \varphi_{cd} \simeq \varphi_{td}$ . The two pieces of the  $tu$ ,  $tc$ ,  $ct$  and  $tt$  terms can then either vanish separately or cancel each other. In the former case we have  $\theta \simeq \alpha$ ,  $\delta \simeq 0$ , and, from eq. (3),  $\gamma \simeq \epsilon$ . This would imply that all  $CP$  violation resides in the right-handed sector, a rather strange situation. (c) We can set the  $X_{ij} \ll 1$ . Then the  $cu$  and  $tu$  contributions imply that the phases must be ( $O(10\%)$ ), which is a relatively weak assumption. (This fine-tuning is clearly not possible in Model II, since the largest contribution,  $uc$ , is not proportional to an  $X_{ij}$ .) (d) Note that setting  $s \simeq 0$  or  $c \simeq 0$  would still require a small  $\beta$  or one of the above fine-tunings.

Unlike  $\epsilon$ ,  $\epsilon'$  does not much constrain the right-handed sector. The  $s \rightarrow d$  penguin graph in the standard model is proportional to  $\lambda^5 \sin \delta$  (either  $c$ - or  $t$ -quark exchange), while the right-handed contributions are  $\sim 10^{-2} \beta c \sin \sigma$  ( $c$ -quark) and  $\sim 10^{-2} \beta s \times \sin \theta$  ( $t$ -quark). The ratio is therefore roughly given by  $10^{-2} \beta / \lambda^5 \sim 1$ . Only if  $\sin \delta \simeq 0$  are there any constraints on the  $V_{ij}^R$ ; otherwise no useful information can be extracted.

We now turn to the effects of the  $W_R$  in  $B$ -meson physics (there are no sizeable contributions to charm physics). As we have seen, without fine-tuning  $V^R$ , due to the bounds on  $M_R$  (eqs. (13), (14)), the  $W_R$  plays no significant role. We therefore consider the effects when fine-tuned solutions (and a light  $W_R$ ) are allowed.

Probably the most interesting method for seeing  $CP$  violation in the  $B$  system is through hadronic decay asymmetries [13,14]. Because of mixing a state which starts out as a pure  $B^0$  (or  $\bar{B}^0$ ) will evolve in time into a mixture of  $B^0$  and  $\bar{B}^0$ .  $CP$  violation is then manifested by a nonzero value of the asymmetry

$$A_f = \frac{\Gamma(B^0(t) \rightarrow f) - \Gamma(\bar{B}^0(t) \rightarrow \bar{f})}{\Gamma(B^0(t) \rightarrow f) + \Gamma(\bar{B}^0(t) \rightarrow \bar{f})}, \quad (15)$$

where  $f$  is a hadronic final state into which both  $B^0$  and  $\bar{B}^0$  can decay, and  $\bar{f}$  is its  $CP$  conjugate. If eq. (15) is integrated over time, then the asymmetry takes the form

$$A_f = - \frac{2x \text{Im } \lambda_f}{2 + x^2 + x^2 |\rho_f|^2}. \quad (16)$$

Here,  $x$  is the  $B^0$ - $\bar{B}^0$  mixing parameter ( $x = \Delta M / \Gamma$ ),

$$\rho_f = \frac{A(\bar{B}^0 \rightarrow f)}{A(B^0 \rightarrow f)}, \quad (17)$$

and

$$\lambda_f = \frac{q}{p} \rho_f, \quad (18)$$

where

$$\frac{q}{p} = \sqrt{\frac{M_{12}^* - \frac{1}{2} i \Gamma_{12}^*}{M_{12} - \frac{1}{2} i \Gamma_{12}}}. \quad (19)$$

In the standard model,  $\Gamma_{12} \ll M_{12}$  [15], so that  $q/p$  is a pure phase. If the final state is not a  $CP$  eigenstate (e.g.  $B_d \rightarrow D^+ \pi^-$ ,  $B_s \rightarrow D_s^+ \pi^-$ ), then  $A_f$  depends on the hadron dynamics in the  $\rho_f$  term, which makes reliable calculation of the asymmetry very difficult. The most useful final states are those which are  $CP$  eigenstates, in which case  $|\rho_f| = 1$ , and  $A_f$  takes the familiar form \*\*

$$A_f = - \frac{x}{1 + x^2} \text{Im } \lambda_f. \quad (20)$$

In these cases, the standard model makes some definite predictions [14,16]. For Cabibbo allowed  $B_d$  decays,  $A(B_d \rightarrow \psi K_S)$  is expected to be positive. In addition,  $A(B_d \rightarrow \psi K_S)$  should be equal to  $A(B_d \rightarrow \psi \pi^0)$ . In the case of Cabibbo allowed  $B_s$  decays, there is a particularly strong prediction. Both  $A(B_s \rightarrow \psi \phi)$

\*\* If it is possible to do time-dependent measurements, then  $\text{Im } \lambda_f$  may be measured directly.

and  $A(B_s \rightarrow \psi K_S)$  are expected to be  $\simeq 0!$  (For Cabibbo suppressed  $B_d$  and  $B_s$  decays, the standard model allows all values of the asymmetries, so that by themselves, with regards to finding new physics, these processes are somewhat less interesting.)

How might these predictions be influenced by the presence of a light  $W_R$ ? Let us first examine Model I. In this case the possibly relevant four-fermi interactions are

$$b \rightarrow c\bar{c}s, \quad b \rightarrow c\bar{u}d \quad (21)$$

(the transition  $b \rightarrow u$  is suppressed in both models). In Model I, because  $V_{td}^R \simeq 0$ ,  $B_d^0 - \bar{B}_d^0$  mixing is not affected by the presence of the  $W_R$ . Thus, apart from the option  $\delta \simeq 0$  discussed above, the quantity  $q/p$  for  $B_d$ 's is unchanged. (We have checked that, even in the presence of right-handed interactions, the relation  $\Gamma_{12} \ll M_{12}$  still holds.) However, the amplitudes for the decays in eq. (21) are now modified. For the decays  $b \rightarrow c\bar{c}s$  and  $\bar{b} \rightarrow c\bar{c}\bar{s}$  (which correspond to the interesting decay  $B_d \rightarrow \psi K_S$ ), they are

$$A(b \rightarrow c\bar{c}s) \sim \mathcal{M}_L \lambda^2 + \mathcal{M}_R \beta c s e^{i(\gamma-\sigma)},$$

$$A(\bar{b} \rightarrow c\bar{c}\bar{s}) \sim \mathcal{M}_L \lambda^2 + \mathcal{M}_R \beta c \bar{s} e^{i(\gamma-\sigma)}, \quad (22)$$

where  $\mathcal{M}_L$  and  $\mathcal{M}_R$  are the relevant matrix elements of the left- and right-handed operators<sup>#5</sup>. The effect of eq. (22) is to modify the asymmetry in the decay  $B_d \rightarrow \psi K_S$  in an interesting way. In the standard model,  $\rho_f = 1$  for this process. In Model I, setting  $\mathcal{M}_L = \mathcal{M}_R$ , we have

$$\rho_f = \frac{1 - (\beta/\lambda^2) s c e^{i(\gamma-\sigma)}}{1 - (\beta/\lambda^2) \bar{s} c e^{-i(\gamma-\sigma)}}. \quad (23)$$

$\rho_f$  is still a pure phase, and for  $\beta_{sc} \gtrsim \lambda^2$  this phase can be sizeable. (Note that the phase  $\gamma$  is free – it is unaffected by any of the previous fine-tunings.) Therefore  $A(B_d \rightarrow \psi K_S)$  may be significantly altered by the presence of the  $W_R$ ; it can even be negative. Furthermore, the asymmetry  $A(B_d \rightarrow \psi \pi^0)$  is unaffected (since the  $W_R$  does not participate in the quark decay  $b \rightarrow c\bar{c}d$ ). Thus one may have  $A(B_d \rightarrow \psi K_S) \neq A(B_d \rightarrow \psi \pi^0)$  in this model.

<sup>#5</sup> One might worry that there is no interference between  $\mathcal{M}_L$  and  $\mathcal{M}_R$  since, on the quark level, with massless quarks, amplitudes involving left- and right-handed quarks do not interfere. This does not apply on the meson level, as can be easily seen from the fact that the  $\psi$  is a coherent sum of left- and right-handed quarks.

The case of  $B_s$ -mesons is particularly interesting. In addition to the absence of  $CP$  violation in Cabibbo allowed  $B_s$  decays, the standard model also predicts a large value for the  $B_s^0 - \bar{B}_s^0$  mixing parameter,  $x_s$  [17], which would suppress the time-integrated asymmetries in eq. (20). Using eq. (7) (adapted for the  $B$  system), one gets for the off diagonal matrix element of the  $B_s$  mass matrix

$$M_{12} = M_{12}^{\text{st}} [1 - 9.3 s^2 e^{i(\gamma-\theta)} - 10.0 c s e^{i(\epsilon-\theta)}], \quad (24)$$

where  $M_{12}^{\text{st}}$  is the standard model contribution. The dominant left-right contributions are the  $ct$  and  $tt$  intermediate states and  $\beta = 0.04$ ,  $m_t = 50$  GeV and  $m_c = 1.5$  GeV were used (relative to  $M_{12}^{\text{st}}$ , the LR contributions decrease as  $m_t$  increases). Surprisingly,  $x_s = 2 |M_{12}| / \Gamma$  can be considerably smaller than in the standard model if the terms in eq. (24) cancel. (Small values of  $x_s$  are usually thought to be a sign of four generation models [18].) Nonzero  $CP$  asymmetries in Cabibbo allowed  $B_s$  decays are now possible. Not only is  $\rho_f$  in the decay  $B_s \rightarrow \psi \phi$  complex (eq. (24)), but  $q/p$  for the  $B_s$  system (eqs. (19), (24)) is also complex (both are essentially equal to 1 in the standard model). In addition, as in the case of  $B_d$  decays, in general one would expect  $A(B_s \rightarrow \psi \phi) \neq A(B_s \rightarrow \psi K_S)$  since  $\rho_f = 1$  for the latter process.

Due to the quark decay  $b \rightarrow c\bar{u}d$ , the  $W_R$  in Model I will also affect processes such as  $B_d \rightarrow D^+ \pi^-$  and  $B_s \rightarrow D_s^+ \pi^-$ . However, as mentioned above, since these final states are not  $CP$  eigenstates, the values of the  $CP$  asymmetries are very uncertain in the standard model. Thus, even if  $CP$  violation were seen here, it would be very difficult to ascertain whether or not a light  $W_R$  played any role.

In Model II, the possible quark decays are

$$b \rightarrow c\bar{c}d, \quad b \rightarrow c\bar{u}s. \quad (25)$$

The analysis of Model II is similar to that of Model I, although, since  $M_R$  is larger here, the effects are somewhat smaller. First of all, in this case, the phase  $q/p$  for  $B_d$ 's may be changed<sup>#6</sup>, but for the  $B_s$  system the  $W_R$  does not affect  $q/p$  (it remains equal to 1). Secondly,  $\rho_f$  retains its standard model value ( $= 1$ )

<sup>#6</sup> Of course, the elements of  $V^R$  must be chosen so that the observed value of  $x_d$  is reproduced.

for the decays  $B_d \rightarrow \psi K_S$  and  $B_s \rightarrow \psi \phi$ , but, due to eq. (25), may be complex for the processes  $B_d \rightarrow \psi \pi^0$  and  $B_s \rightarrow \psi K_S$ . Thus  $A(B_d \rightarrow \psi K_S)$  may be different from its standard model value, and, as in Model I,  $A(B_d \rightarrow \psi K_S) \neq A(B_d \rightarrow \psi \pi^0)$  in general. Unlike Model I, Model II still gives  $A(B_s \rightarrow \psi \phi) \simeq 0$ , although  $A(B_s \rightarrow \psi K_S)$  may be nonzero.

In conclusion, we have shown that, in the absence of fine-tuning, it is not possible to have a light right-handed  $W$ . Although one can evade the constraints from  $\Delta M_K$  by taking  $V^R \neq V^L$  and choosing a particular form for  $V^R$ , constraints from  $\epsilon$  will, in general, require  $M_R \gtrsim 5$  TeV. If fine-tuned solutions are allowed, then not only can the  $W_R$  be light, but there may be interesting effects in the  $B$  system. In one model,  $B_s^0 - \bar{B}_s^0$  mixing can be smaller than  $B_d^0 - \bar{B}_d^0$  mixing. Also, the pattern of  $CP$  asymmetries predicted by the standard model may be altered. The asymmetry in Cabibbo allowed  $B_s$  decays (e.g.  $B_s \rightarrow \psi \phi$ ) may be nonzero;  $A(B_d \rightarrow \psi K_S)$  may be negative; and the predicted relations  $A(B_d \rightarrow \psi K_S) = A(B_d \rightarrow \psi \pi^0)$  and  $A(B_s \rightarrow \psi \phi) = A(B_s \rightarrow \psi K_S)$  may be violated.

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