Observation of deep inelastic scattering at low $x$

H1 Collaboration

Measurements of the scattered electron energy spectrum and the differential cross sections \( \frac{d\sigma}{d\log(x)} \) and \( \frac{d\sigma}{dQ^2} \) for inclusive neutral current deep inelastic electron–proton scattering are presented. The data were obtained with the H1 detector at HERA during its first running period in which 26.7 GeV electrons collided with 820 GeV protons. The data correspond to an integrated luminosity of 1.3 nb\(^{-1}\) and allow the first studies of the structure of the proton at values of \( x \) down to \( 10^{-4} \) for \( Q^2 > 5 \text{ GeV}^2 \).

1. Introduction

Since the discovery of partons more than 20 years ago [1], deep inelastic lepton scattering experiments [2,3] have provided important information on the structure of the proton and on the nature of the interactions between leptons and quarks. The electron–proton collider HERA allows the extension of this line of research into as yet unexplored kinematic regions.

This paper describes the analysis of data taken with the H1 detector [4,5] in July of 1992, HERA’s first running period. Both the H1 and ZEUS experiments have presented preliminary results from this period [4,6].

The kinematics of the inclusive deep inelastic scattering (DIS) process \( ep \rightarrow eX \) is determined by two independent variables, conventionally chosen to be two of \( x, y \) and \( Q^2 \). These variables may be measured using information from either the scattered lepton or the hadronic system or both. The polar angle \( \theta_e \) of the scattered electron is measured relative to the proton beam direction, termed the forward direction in the following. The angle, \( \theta_e \), and the energy of the scattered lepton, \( E_e' \), determine the above variables through the relations

\[
Q^2 = 4E_eE_p \cos^2(\frac{1}{2} \theta_e),
\]

\[
y = 1 - (E_e'/E_e) \sin^2(\frac{1}{2} \theta_e),
\]

\[x = Q^2/sy,
\]

where the centre of mass energy squared \( s = 4E_eE_p = 87600 \text{ GeV}^2 \), and \( E_e \) and \( E_p \) are the energies of the incoming electron and proton, respectively. Due to the large centre of mass energy, \( x \) values down to \( \sim 10^{-4} \) can be studied in the deep inelastic regime. A salient feature of the kinematics is a peak in the scattered electron energy spectrum at the beam energy \( E_e \) for electrons scattered into the backward region \( \theta_e > 150^\circ \). This peak, termed the kinematic peak in the following, is of particular interest for calibration purposes. The outgoing hadrons are used for a complementary determination of \( y \) using the relation [7]

\[
y_h = \sum_{\text{hadrons}} \frac{E_h - p_{z,h}}{2E_e},
\]

where the \( E_h \) are the energies of the hadrons and the \( p_z \) their momenta in the \( z \) or proton beam direction.

At HERA the electroweak interaction rate is orders of magnitude smaller than the background rate caused by strong interactions of beam protons with either the residual gas in the beampipe or with the material of the beampipe itself. Moreover, at low scattered electron energies, the background rate due to photoproduction events is much larger than the rate of deep inelastic events. The identification of the deep inelastic events is discussed in detail in the following. The data sample is used to derive a first measurement of the neutral current cross section in the new kinematic range.
2. The H1 detector

Fig. 1 shows a deep inelastic scattering event at $x = 0.002$ and $Q^2 = 17 \text{ GeV}^2$ observed in the H1 detector. Most of the detector components important for this analysis are visible. These are

- The tracker: the central tracking detector consists of two large jet drift chamber modules, two $z$ drift chambers and two multiwire proportional chambers for triggering. Its angular acceptance is $15^\circ - 170^\circ$. The forward tracking detector accepts tracks between $7^\circ$ and $25^\circ$. It consists of three modules of drift and multiwire proportional chambers. The backward multiwire proportional chamber (BPC) has four wire planes and an angular acceptance of $155^\circ - 175^\circ$. A superconducting coil provides a uniform magnetic field of 1.2 T in the tracking region.

- The calorimeters: the backward electromagnetic calorimeter (BEMC) is made of 88 lead/scintillator sandwich stacks, each with a depth of 22 radiation lengths, corresponding to about 0.7 interaction lengths, and transverse dimensions of $16 \times 16 \text{ cm}^2$. The liquid argon calorimeter consists of an electromagnetic section with lead absorber (20–30 radiation lengths) and a hadronic section with steel absorber. The total depth of the calorimeter varies between 4.5 and 8 interaction lengths.

- The time of flight (TOF) system, located behind the backward calorimeter, consists of two scintillator planes, each with a time resolution of about 3 ns, and enables the separation of genuine $ep$ events from proton beam-wall and beam-gas interactions upstream of the detector at the trigger level.

- The luminosity detector system described in ref. [8], not visible in fig. 1, is designed to detect the $e^-\gamma$ coincidence from the reaction $e + p \rightarrow e + \gamma + p$. The electron tagger is located 33 m from the interaction region in the backward or $-z$ direction and detects electrons scattered through angles less than 5 mrad with respect to the electron beam direction. The photon tagger is located at $z = -103 \text{ m}$. Both detectors are TlCl/TlBr crystal calorimeters.

At low values of $Q^2$ the scattered electron deposits its energy in the backward electromagnetic calorimeter. The scattering angle is determined using the backward proportional chamber and the reconstructed event vertex and, at smaller $\theta_e$, the drift chambers. The angles and energies of hadronic final state parti-

![Fig. 1. A deep inelastic scattering event at $x = 0.002$ and $Q^2 = 17 \text{ GeV}^2$, observed in the H1 detector. The detector components shown are the electromagnetic (EMC), hadronic (HAC) and backward electromagnetic (BEMC) calorimeters, forward (FT) and central (CT) trackers, backward proportional chamber (BPC), and scintillator hodoscope (TOF).](image-url)
cles are measured with the central and forward tracking systems and with the liquid argon and backward calorimeters. The analysis in this paper is restricted to electrons detected in the backward calorimeter.

3. Calibration and resolution

The energy resolution of the BEMC due to sampling fluctuations is 10%/\sqrt{E}, as has been determined in test beam studies [9]. The average noise per stack was measured to be 150 MeV which implies that the noise contribution to the measurement of a typical scattered electron shower is about 450 MeV. The measured energy has to be corrected for energy loss in the material in front of the BEMC (about 1 X_0), losses in the wavelength shifter regions between the stacks and for leakage. Monte Carlo simulations showed that all these effects combined give a 2.7% energy correction on average with a fluctuation of 1.2% due to inhomogeneities. The energy resolution is further affected by stack to stack intercalibration uncertainties which are estimated to be 3.7%. From these considerations the following energy resolution was derived:  

$$\frac{\sigma_E}{E} = \sigma_{\text{noise}}/E + \sigma_{\text{sampling}}/\sqrt{E} + \sigma_{\text{const}},$$

where \(\sigma_{\text{noise}} = 0.45 \text{ GeV}, \sigma_{\text{sampling}} = 0.1 \text{ GeV}^{1/2}, \sigma_{\text{const}} = 0.04\) and \(E\) is measured in GeV. This results in a width of the simulated kinematic peak, due to the intrinsic width and detector effects, of about 2.2 GeV which agrees with the observed width.

In the kinematic peak region \((E > 22 \text{ GeV})\) a \(\chi^2\) comparison of the observed energy spectrum with the Monte Carlo prediction was used to determine the overall BEMC energy calibration. An additional check was performed by deriving the scattered electron energy from the angles \(\theta_e\) of the electron and \(\theta_h\) of the momentum vector of the hadronic system. The energy calibration has an uncertainty of 2%. For the determination of \(y_h\) from the hadronic final state a combination of well measured tracks in the central region with energy deposits in the calorimeter was used. The calibration of the liquid argon calorimeter is presently known to 2% for the electromagnetic and to 7% for the hadronic energies [10].

For angles between 174° and about 170°, the electron scattering angle \(\theta_e\) is determined by the vertex of the event and the reconstructed hit in the BPC. Events at low \(y\) which contribute to the energy distribution in the kinematic peak may leave no track in the detector. These are included in the electron energy spectrum but not in the \(Q^2\) and \(x\) distributions. For smaller angles (< 170°), \(\theta_e\) can be reconstructed from tracks in the central chambers. The angular resolution \(\delta\theta_e\) depends only weakly on \(\theta_e\) and is about 6 mrad for interactions with a reconstructed vertex.

The four-momentum transfer squared is determined from the energy and angle of the scattered electron. With the exception of extremely large polar angles, the resolution \(\delta Q^2/Q^2\) is dominated by the electron energy resolution and is about 6%. An alternative calculation of \(Q^2\) using the two scattering angles \(\theta_e\) and \(\theta_h\) has a similar resolution, essentially independent of \(Q^2\), and was used as a consistency check. For the determination of \(x = Q^2/sy\) it is advantageous to combine leptonic and hadronic measurements of \(y\). The resolution \(\delta y_e/\sqrt{y_e}\) varies like 1/\(y\) and is 5% at \(y = 0.6\) but deteriorates to 30% for \(y = 0.1\). The \(y_h\) resolution is better than about 30% for \(y_h > 0.025\). Hence, for \(y_e < 0.1\), \(y_h\) was used in preference to \(y_e\). The resulting \(x\) resolution varies between 15% at \(x = 10^{-4}\) and 35% at \(x = 10^{-2}\).

For \(x > 10^{-2}\) and small \(Q^2\) hadrons are lost in the forward beam pipe region and \(x\) measurements are subject to systematic shifts. This will require detailed study in future high statistics analyses.

4. Event selection and background

The data presented here correspond to a total integrated luminosity of 1.3 nb\(^{-1}\), which is known to a precision of 7%. The trigger pertinent to this analysis required that a local energy deposit, or cluster, of more than 4 GeV be identified in the BEMC. Events were rejected if signals in both TOF planes were compatible with particles produced in upstream proton background interactions. The acceptance of this trigger increased from 90% to 99% for electron energies between 5 and 10 GeV and was larger than 99% for electron energies above this. The total number of such triggers recorded was about \(6 \times 10^4\).

Deep inelastic scattering event candidates were identified using the following criteria:

- A cluster of more than 6 GeV was required in the backward calorimeter in association with at least one hit in the adjacent BPC. The radial separation of the
centre of gravity of the cluster and the BPC hit was required to be less than 15 cm. Furthermore, the cluster centre of gravity had to lie outside the range $|x| > 16$ cm around the beam axis.

- For events with a BEMC cluster energy below the kinematic peak region ($E_e < 22$ GeV) it was required that at least one track in the central tracker originate from the transverse beam position. The $z$ coordinate of the vertex had to be within $\pm 50$ cm of the nominal interaction point, compatible with the width of the $z$-vertex distribution of 40 cm (FWHM).

- Out of time proton beam background was further suppressed by restrictive cuts on the signals from the individual TOF scintillator planes.

The resulting sample of 219 events was scanned for remaining beam background and cosmic events, which were removed. The sample of DIS candidates surviving all selection criteria comprised 182 events. In this sample six events were observed with a clear electron tagger signal in coincidence with an energy deposit in the BEMC of less than 10 GeV. These are events where the scattered electron disappears in the beampipe, but hadrons and photons produced in the backward region simulate an electron signal in the BEMC. This implies that the DIS sample contained about 20–40 photoproduction events at this stage of the selection procedure. Further evidence for the presence of this background was provided by a comparison of the hadron and the electron $y$ measurements, shown in fig. 2a. A clear correlation between $y_e$ and $y_h$ is evident in the region in which the $y_e$ resolution is good, $y_e > 0.1$; yet, independent of $y_h$, there is also an accumulation of events at high $y_e$, i.e., low electron energies. Fig. 2b shows a Monte Carlo calculation of $y_h$ and $y_e$, based on the vector dominance model (VDM) [11] for photoproduction. As in the data an accumulation of events at high $y_e$ is seen. Detailed Monte Carlo studies of the photoproduction background using various event generators [11, 12], and resolution considerations, led us to reject events if $y_h < \frac{1}{2} y_e$, for $y_e > 0.6$. The resulting event sample contained 148 events, none of which had a signal in the electron tagger. The remaining photoproduction contamination could be as much as 50% for $E_e^* < 10$ GeV but is estimated to be less than 20% for $10 < E_e^* < 14$ GeV. For $E_e^* > 14$ GeV the photoproduction contamination is negligible. Note that $y = 0.6$ corresponds roughly to $E_e^* = 10$ GeV. The lowest $x$ event in this sample has $x = 6 \times 10^{-5}$ at $Q^2 = 4$ GeV$^2$ while the largest $^{*1}$ $Q^2$ event has a $Q^2 = 82$ GeV$^2$ at $x = 4 \times 10^{-3}$.

The contamination of the DIS sample with proton and electron beam induced background was estimated to be less than 5% for $E_e^* > 10$ GeV, based on studies of the multiplicity of identified low momentum protons and of studies of $e$ and $p$ bunches which have no partner to collide with. Another potential background comes from event pile-up. Due to the high HERA bunch crossing rate of 10 MHz the detector information for an interaction can be distorted by signals resulting from a collision in adjacent bunch crossings.

*1 In the same data taking period five neutral currents events were detected in the liquid argon calorimeter with $Q^2 > 100$ GeV$^2$. 
The number of events affected by pile-up was estimated to be less than 1%.

The energy spectrum of the scattered electron for the accepted data sample is shown in fig. 3. The expected peak of the distribution at $E_e' = E_e$ is clearly visible. The measured spectrum is compared with a Monte Carlo calculation including a full simulation of the H1 detector. The events have been generated using HERACLES 3.1 [13] for the electroweak interaction, which includes first order radiative corrections, followed by LEPTO 5.2 [14] for the simulation of QCD processes. We chose to represent the parton distributions using the MRSD0 parametrization described in ref. [15]. The simulated spectrum in fig. 3 was normalized to the measured luminosity. Between 12 and 30 GeV the spectra agree well with a $\chi^2$ of 7.2 for eight degrees of freedom. The data contain more events in the low energy region than is predicted by the Monte Carlo calculation. This may be due to remaining photoproduction contamination and a low $x$ behaviour of the proton structure functions which is different from that of the MRSD0 parametrization.

5. Differential cross sections

In the Born approximation the deep inelastic scattering cross section at low $Q^2$ is determined by the two structure functions $F_2$ and $2xF_1 = F_2/(1 + R):$

$$\frac{d^2\sigma}{dx dQ^2} = \frac{2\pi\alpha^2}{Q^4x} \left( 2(1 - y) + \frac{y^2}{1 + R} \right) F_2(x, Q^2). \quad (3)$$

In order to reduce sensitivity to the photoproduction background and to the effects of radiative corrections [16,17] the cross section analysis was limited to $y < 0.6^{\#2}$. As discussed above, a lower $y$ limit was set at $y = 0.025$, ensuring that the $y$ resolution was always better than 30%. In addition it was demanded that $Q^2 > 5$ GeV$^2$, $\theta_e < 174^\circ$ and that the $ep$ interaction vertex be reconstructed, thus reducing the sample to 72 events. The rejected events are primarily at high $E_e'$ where for kinematic reasons hadrons are produced with small angles.

The observed distributions were normalized to the measured luminosity and converted into differential cross sections by correcting for the acceptance and finite bin size effects. The average total acceptance corrections varied between 30% and 50% including smearing of the distributions due to finite detector resolution and reconstruction inefficiencies determined from the data. The cross sections $d\sigma/d\log(x)$ and $d\sigma/dQ^2$ are shown in fig. 4. The log($x$) representation was chosen in order to remove the trivial $1/x$ dependence of the cross section [eq. (3)]. The full error bars correspond to the statistical error which is the dominating uncertainty. The systematic errors are shown separately. All points are subject to a common additional uncertainty of 7% due to the luminosity measurement error. In the accessed kinematic range the measured deep inelastic cross section, not corrected for radiative effects, amounts to $\sigma = 92 \pm 11$ (stat.) $\pm 12$ (syst.) nb.

The calculation of the systematic uncertainty included the following error sources: possible shifts of the energy scale by 2% and of $\theta_e$ by 3 mrad; uncertainties in the trigger (2%) and detector (4%) efficiency calculations; electron and proton beam induced background (5%); photoproduction contamination in both the lowest $x$ and $Q^2$ bin (15%); the influence

\#2 Note that the $y_h - y_e$ cut was applied only for $y_e > 0.6$. Thus it served only to remove background in the lower part of the energy distribution and has no effect on the $x, Q^2$ distributions.
Deep inelastic scattering has been observed for the first time in a kinematic region that extends down to \( x = 10^{-4} \) for \( Q^2 \) above 5 GeV\(^2\). The data presented here stem from the first luminosity period at HERA, with collisions of 26.7 GeV electrons on 820 GeV protons. The spectrum of the scattered electron energy has been measured down to \( E' = 6 \) GeV. It exhibits the predicted peak around the electron beam energy and is rather flat at smaller energies. The simultaneous measurement of the inclusive reaction kinematics using the scattered lepton and the hadronic energy and angles has been shown to be an effective means of reducing the large photoproduction background at low scattered electron energies. This also extends the range of \( y \) which can be accurately measured to lower \( y \). A measurement of the \( x \) and the \( Q^2 \) dependent cross sections in the range \( Q^2 > 5 \) GeV\(^2\), \( 0.6 > y > 0.025 \) and \( \theta_e < 174^\circ \) gives \( \sigma = 92 \pm 11 \) (stat.) \( \pm 12 \) (syst.) nb.

**6. Conclusions**

The theoretical calculations include the contribution of higher order radiative corrections which have not been subtracted from the data. The corrections were calculated \[17\] in the measured region and are expected to change the cross sections by about 40% at the lowest \( x \) and \( Q^2 \) values. They are an order of magnitude smaller at the largest \( x \) and \( Q^2 \) values. The derivation of the Born cross sections, and of \( F_2 \), from the measured cross sections requires an iterative procedure, which is left to future analyses with higher statistics.
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References

[4] F. Eisele, First results from the H1 experiment at HERA, in: Proc. 26th Intern. Conf. on High energy physics (Dallas, TX, 1992), to appear, and DESY preprint 92-140 (1992);
A. Akhundov et al., private communication.