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Determination of  $\tan \beta$   
at a Future  $e^+e^-$  LC

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# Outline

- Introduction
- $b\bar{b}A \rightarrow b\bar{b}b\bar{b}$  simulation
- High luminosity:  $2000 \text{ fb}^{-1}$
- $HA \rightarrow b\bar{b}b\bar{b}$  event rate
- H and A width from  $HA \rightarrow b\bar{b}b\bar{b}$
- New aspect:  $H^+H^- \rightarrow t\bar{t}b$
- Conclusions

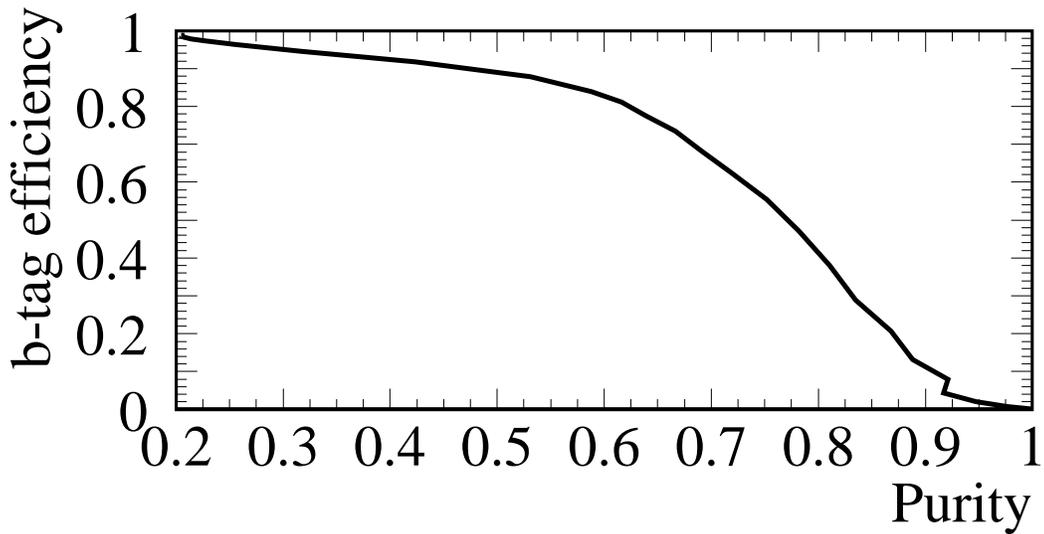
# Introduction

- Framework:  
Two-Higgs Doublet Model or MSSM.
- Production and Decay of A, h, H, and  $H^\pm$ .
- Considered reactions for TESLA:  
strong dependence on  $\tan \beta$ .
- Extrapolation  $b\bar{b}A \rightarrow b\bar{b}b\bar{b}$  for  $100 < m_A < 200$  GeV.
- Estimate of  $HA \rightarrow b\bar{b}b\bar{b}$  event rate.
- Estimate of H and A width determination.
- Estimate of charged Higgs bosons branching ratio and decay width.

# b-tagging

Experimental potential depends strongly on the b-tagging performance.

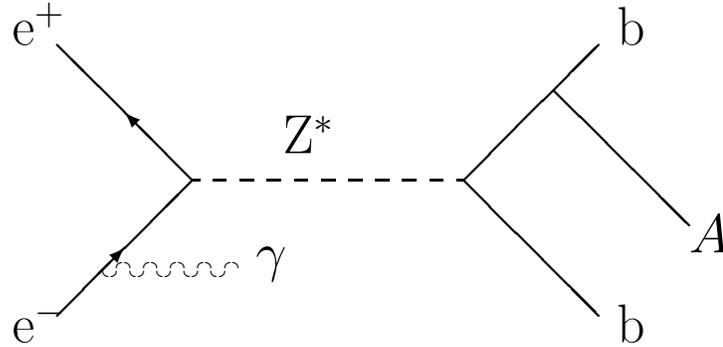
Hadronic events  $e^+e^- \rightarrow q\bar{q}$  (5 flavors).



Efficiency: Ratio of simulated  $b\bar{b}$  events after the selection to all simulated  $b\bar{b}$  events.

Purity: Ratio of simulated  $b\bar{b}$  events after the selection to all selected  $q\bar{q}$  events.

# $b\bar{b}A$ Simulation

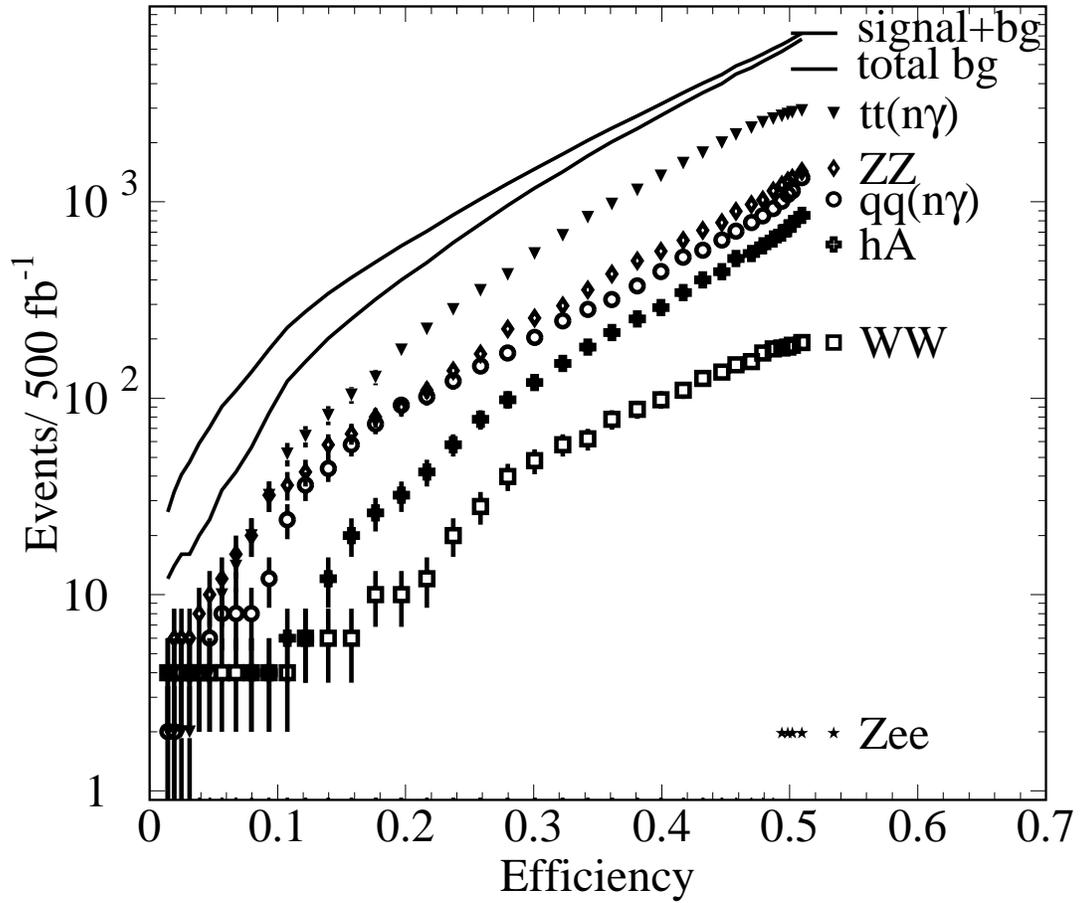


Simulated Higgs boson mass: 100 GeV

Channel	bbA	qq	WW	eW $\nu$	tt	ZZ	eeZ	hA	sum
(in 1000)	50	6250	3500	2500	350	300	3000	50	16000
After Presel.	73%	20991	7481	0	89983	10278	145	12665	141544

Simulated hA rate corresponds to twice the luminosity (maximum cross section in general Two-Higgs Doublet Model).

# Signal and Background



# Interference: $b\bar{b}A \quad hA \rightarrow b\bar{b}b\bar{b}$

Expectation before event selection:

$$\sigma_{b\bar{b}A} \equiv \sigma(e^+e^- \rightarrow b\bar{b}A \rightarrow b\bar{b}b\bar{b})$$

$$\sigma_{hA} \equiv \sigma(e^+e^- \rightarrow hA \rightarrow b\bar{b}b\bar{b})$$

$$\sigma_{b\bar{b}A+hA} \equiv \sigma(e^+e^- \rightarrow b\bar{b}A, hA \rightarrow b\bar{b}b\bar{b})$$

$$\sigma_{\text{interf}} = \sigma_{b\bar{b}A+hA} - \sigma_{b\bar{b}A} - \sigma_{hA}.$$

For  $m_b = 4.62$  GeV:

$$\sigma_{b\bar{b}A} = 1.83 \pm 0.01 \text{ fb}$$

$$\sigma_{hA} = 36.85 \pm 0.10 \text{ fb}$$

$$\sigma_{b\bar{b}A+hA} = 39.23 \pm 0.12 \text{ fb}$$

$$\sigma_{\text{interf}} = 0.55 \pm 0.16 \text{ fb}$$

Positive interference,  
reduction in statistical error.

## Interference: $b\bar{b}A \quad hA \rightarrow b\bar{b}b\bar{b}$

Expectation after event selection:

100  $b\bar{b}A \rightarrow b\bar{b}b\bar{b}$  events

$2 \pm 1$   $hA \rightarrow b\bar{b}b\bar{b}$  events.

Maximum interference magnitude:

$$(10 + 1.4)^2 - 100 - 2 \approx 28$$

Similar ratio of interference to signal 30% before and after event selection.

Interference events:

background-like: small systematic error.

signal-like: large systematic error.

Solution: fit signal and background to data for various  $\tan \beta$ .

Another systematic error is the running b-mass. Higher-order corrections should be very precisely known by the time the LC is constructed.

## $b\bar{b}A$ Results for $500 \text{ fb}^{-1}$

For  $\tan \beta = 50$  and  $m_A = 100 \text{ GeV}$ :

$$\Delta \tan \beta / \tan \beta = 0.07.$$

$$\begin{aligned} \Delta \tan^2 \beta / \tan^2 \beta &= \Delta N_{\text{signal}} / N_{\text{signal}} \\ &= \sqrt{N_{\text{signal}} + N_{\text{background}}} / N_{\text{signal}} = 0.14. \end{aligned}$$

Smaller values of  $\tan \beta$ , the sensitivity decreases rapidly.  $5\sigma$  signal detection for  $\tan \beta = 35$ .

MSSM:  $b\bar{b}h$  would double the number of signal events and have the same  $\tan \beta$  dependence:

$$\Delta \tan^2 \beta / \tan^2 \beta \sim \sqrt{300} / 200 \approx 0.085$$

For  $\tan \beta = 50$  and  $m_A = m_h = 100 \text{ GeV}$ :

$$\Delta \tan \beta / \tan \beta = 0.04.$$

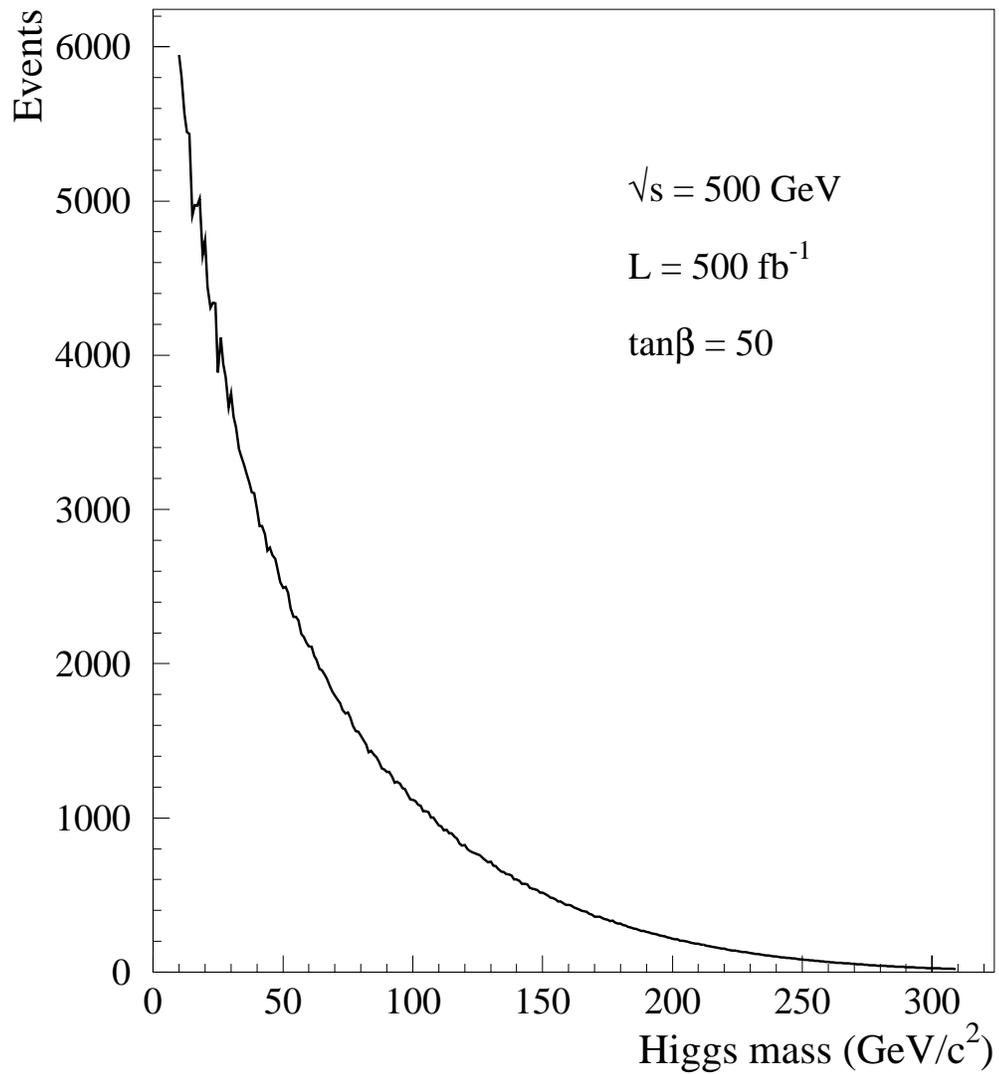
(For heavier  $A$ ,  $b\bar{b}H$  will contribute).

Experimental challenge:

at 10% efficiency,  $\Delta \tan \beta / \tan \beta < 0.05$

requires  $\Delta \epsilon / \epsilon < 0.1$ , thus  $\Delta \epsilon < 1\%$ .

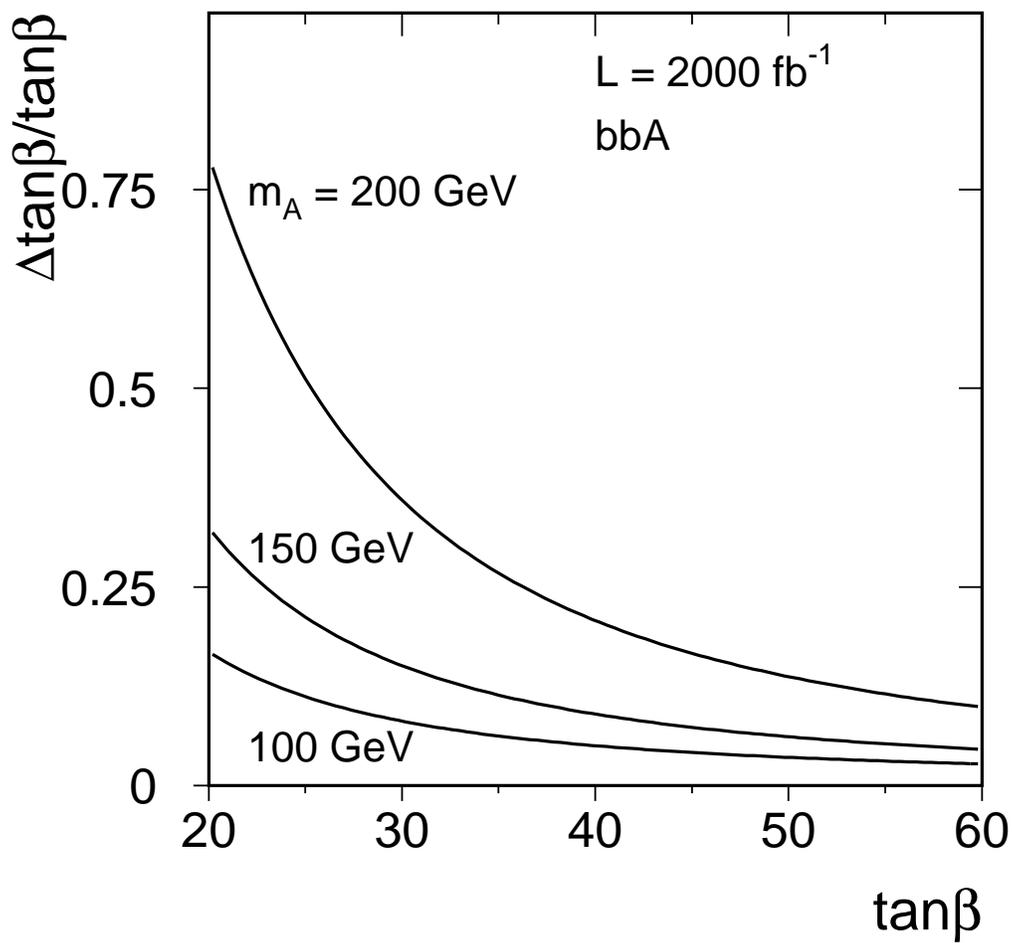
# $e^+e^- \rightarrow b\bar{b} \rightarrow b\bar{b}A$ Rate



At 100 GeV: 1000 events.

At 200 GeV: 200 events.

# $b\bar{b}A$ Results for $2000 \text{ fb}^{-1}$



## $H_A \rightarrow b\bar{b}b\bar{b}$ Event Rate

Assume b-tagging purity 80% per  $b\bar{b}$  pair, thus 40% signal efficiency.

For  $b\bar{b}b\bar{b}$ : 16% efficiency.

Further reduction: kinematic event selection: final efficiency 10%, and negligible background.

Small  $\tan \beta$ : constant MSSM cross section and large variation of branching fraction.

Typical expected signal rate for  $2000 \text{ fb}^{-1}$  and  $m_A = m_H = 200 \text{ GeV}$  for  $\tan \beta = 5$ : 500 events.

$$\Delta \tan \beta / \tan \beta \approx 0.01$$

Nice overlap with  $b\bar{b}A$  results.

# H and A width from $HA \rightarrow b\bar{b}b\bar{b}$

Assumption:  $5 \pm 0.5$  GeV detector resolution.

Reconstruction of mean H and A widths from  $b\bar{b}$ -mass.

There are two  $b\bar{b}$  masses per event.

Wrong jet-jet pairings: 25%.

Available statistics for mass reconstruction:

1.5  $HA \rightarrow b\bar{b}b\bar{b}$  rate.

Determination of intrinsic Higgs width  
by convolution with detector resolution.

$$0.5(\Gamma_H + \Gamma_A) = 12.5 \pm 0.54 \text{ GeV},$$

dominated by error on detector resolution.

$$\Delta \tan \beta / \tan \beta < 0.02 \text{ for } \tan \beta = 55.$$

$$e^+e^- \rightarrow \mathbf{H^+H^-} \rightarrow \mathbf{t\bar{b}\bar{t}b}$$

- 500 GeV and  $10 \text{ fb}^{-1}$ ,  
the charged Higgs can be reconstructed  
*Z. Phys. C* **65** (1995) 449.
- 800 GeV and  $1000 \text{ fb}^{-1}$ ,  
high precision reconstruction,  
M. Battaglia, A. Ferrari, A. Kiiskinen, T.M. Ki,  
hep-ph/0112015.
- Sensitivity for 500 GeV and  $1000 \text{ fb}^{-1}$ ,  
for a 200 GeV charged Higgs boson mass:  
uncertainty about 0.5 GeV.
- Very similar uncertainty as for the HA.
- Similar precision on  $\tan \beta$   
as from HA production  
 $\Delta \tan \beta / \tan \beta \approx 0.02$  for  $\tan \beta = 5$ .

# Further information on $\tan \beta$

- $tbH^\pm \rightarrow tb\tau\nu$

J. L. Feng and T. Moroi, Phys. Rev. D **56**, 5962 (1997).

- A width from  $b\bar{b}A \rightarrow b\bar{b}b\bar{b}$

- Scalar taus (E.Boos et.al.)

# Conclusions

Experimental challenges:

- High luminosity needed.
- Best possible b-tagging performance.
- Precision detector resolution measurement.
- Combined analyses, e.g. Fit of all  $b\bar{b}b\bar{b}$  processes as function of  $\tan\beta$ .
- Precision determination of signal efficiency.
- Precision cross section and decay width meas.
- $b\bar{b}A \rightarrow b\bar{b}b\bar{b}$
- $HA \rightarrow b\bar{b}b\bar{b}$
- $H^+H^- \rightarrow t\bar{t}b\bar{b}$

TESLA: Precision determination of  $\tan\beta$  with different independent complementary methods.