

# Horizontal Theories and Soft Breaking

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## Flavour Physics

- 3 fermionic families with identical gauge numbers ?
- Origin of the mass hierarchy ?
- Intergenerational mixing ?

### SM

12 masses  
10 mixing angles  
and phases ...

### MSSM

fermion + sfermion  
masses + mixings  
= 124 !!!!



# Flavour and $CP$ Problems

- Yukawa couplings in Superpotential and soft breaking masses different origins.
- In general, not simultaneously diagonalizable
- New complex parameters in  $W$  and soft breaking terms.



Too large Flavour Changing and  
 $CP$  violating contributions

Stringent bounds on sfermion mass matrices  
and SUSY phases at  $M_W$ .

Solutions:

Universality, Alignment ...



# Minimal Supergravity

Canonical Kähler potential for chiral Superfields  $K = \sum_i |\phi^i|^2$  and Superpotential

$$W = W^{hid}(\chi_k) + \left(\frac{\theta}{M}\right)^{\alpha(i,j)} H_a Q_{Li} q_{Rj}^c + \dots$$

with (perhaps several)  $\theta/M$  generate Yukawa structure.

Scalar potential (F-terms):

$$V = e^K \left[ \sum_i \left| \frac{\partial W}{\partial \phi_i} + \phi^{i*} W \right|^2 - 3|W|^2 \right]$$

with  $F_{\phi_i} = -e^{K/2} (W_i^* + \phi_i W^*)$ .

SUSY breaking in hidden sector  $\langle W \rangle \simeq m_{3/2}$ , we obtain Soft Breaking terms.

Canonical Kähler potential  $\rightarrow$  Universal scalar masses

$$m_{\phi_i}^2 \phi_i \phi^{i*} = |\langle W \rangle|^2 \phi_i \phi^{i*}$$



However trilinear couplings:

$$A_{ij} Y_{ij} H_a \tilde{Q}_{Li} \tilde{q}_{Rj}^c = \left( \frac{\partial W}{\partial H_a} H_a + \frac{\partial W}{\partial \tilde{Q}_{Li}} \tilde{Q}_{Li} + \frac{\partial W}{\partial \tilde{q}_{Rj}^c} \tilde{q}_{Rj}^c \right) \langle W^* \rangle + \frac{\partial W}{\partial \theta} \theta \langle W^* \rangle = (3 + \alpha(i, j)) \langle W^* \rangle Y_{ij} H_a \tilde{Q}_{Li} \tilde{q}_{Rj}^c$$

Yukawa matrices as effective operators as powers of scalar vevs. Irrespective of the source of SUSY breaking



Nonuniversal trilinear terms !!

Universality and Alignment not possible in this framework.



New sources of FCNC



# Yukawa Textures and Soft breaking

- Explain fermion masses and mixings in terms of a few fundamental parameters
- Off-diagonal entries small relative on-diagonal
- Approximate texture zeros: mixings in terms of masses

Textures fitting the experimental data:

R. G. Roberts, A. Romanino, G. G. Ross and  
L. Velasco-Sevilla, Nucl. Phys. B **615** (2001) 358

## Symmetric Texture

$$\frac{M_u}{m_t} = \begin{pmatrix} 0 & b'\epsilon^3 & c'\epsilon^4 \\ b'\epsilon^3 & \epsilon^2 & a'\epsilon^2 \\ c'\epsilon^4 & a'\epsilon^2 & 1 \end{pmatrix} \quad \frac{M_d}{m_b} = \begin{pmatrix} 0 & b\bar{\epsilon}^3 & c\bar{\epsilon}^4 \\ b\bar{\epsilon}^3 & \bar{\epsilon}^2 & a\bar{\epsilon}^2 \\ c\bar{\epsilon}^4 & a\bar{\epsilon}^2 & 1 \end{pmatrix}$$

with  $\epsilon \simeq 0.05$  and  $\bar{\epsilon} \simeq 0.15$



if  $\epsilon = \langle \theta \rangle / M$  and  $\bar{\epsilon} = \langle \bar{\theta} \rangle / M$  we obtain as trilinear

$$(Y^A)_{ij} \equiv Y_{ij} A_{ij} = h_3 m_{3/2} \begin{pmatrix} 0 & 6b'\epsilon^3 & 7c'\epsilon^4 \\ 6b'\epsilon^3 & 5\epsilon^2 & 5a'\epsilon^2 \\ 7c'\epsilon^4 & 5a'\epsilon^2 & 3 \end{pmatrix}$$

### Asymmetric Texture

$$\frac{M_u}{m_t} = \begin{pmatrix} 0 & c\epsilon\epsilon' & 0 \\ c\epsilon\epsilon' & \beta\epsilon^2 & b\epsilon \\ 0 & a\epsilon & 1 \end{pmatrix} \quad \frac{M_d}{m_b} = \begin{pmatrix} 0 & \epsilon' & 0 \\ \epsilon' & \alpha\epsilon & \epsilon \\ 0 & t & 1 \end{pmatrix}$$

with  $\epsilon \simeq 0.08$ ,  $\epsilon' \simeq 0.006$  and  $t \simeq 0.3$ .

if  $\epsilon = \langle \theta \rangle / M$ ,  $\bar{\epsilon}' = \langle \bar{\theta}' \rangle / M$  and  $t = \langle \bar{\theta}_t \rangle / M$

$$(Y_u^A)_{ij} = h_t m_{3/2} \begin{pmatrix} 0 & 5c\epsilon\epsilon' & 0 \\ 5c\epsilon\epsilon' & 5\beta\epsilon^2 & 4b\epsilon \\ 0 & 4a\epsilon & 3 \end{pmatrix}$$

$$(Y_b^A)_{ij} = h_b m_{3/2} \begin{pmatrix} 0 & 4\epsilon' & 0 \\ 4\epsilon' & 4\alpha\epsilon & 4\epsilon \\ 0 & 4t & 3 \end{pmatrix}$$

Non diagonal Trilinear couplings  $\Rightarrow$  Left-Right FCNC



# FCNC and $CP$ Phenomenology

- Soft breaking terms at high scale  $\sim M_{GUT}$
- RGE evolution to electroweak scale.
  - 1.- Diagonal elements receive large gaugino contribution

$$(m_{\tilde{f}}^2)_{ii}(M_W) \simeq 6 m_{1/2}^2 + (m_{\tilde{f}}^2)_{ii}(M_{Pl})$$

- 2.- Trilinear couplings align with gaugino

$$A_t(M_W) \simeq 0.25 A_t^0 - 2 m_{1/2}$$

$$A_u(M_W) \simeq 0.6 A_u^0 - 2.9 m_{1/2}$$

$$A_d(M_W) \simeq 1 A_d^0 - 3.6 m_{1/2}$$

small  $\tan \beta \simeq 5$  :

$$A_b(M_W) \simeq 1 A_b^0 - 3.4 m_{1/2}$$

large  $\tan \beta \simeq 30$  :

$$A_b(M_W) \simeq 0.74 A_b^0 - 2.9 m_{1/2}$$



“String  $CP$  problem” and MI bounds





# “String $CP$ problem”

S. Abel, S. Khalil and O. Lebedev, hep-ph/0112260.

- Yukawa matrices contain  $\mathcal{O}(1)$   $CP$  violating phases ( $\delta_{CKM}$ )
- If nonuniversal, even real  $A$  can overproduce EDMs

## Super CKM basis

$$V_{qL}^\dagger Y_q V_{qR} = \text{Diag}(h_1, h_2, h_3) \quad \tilde{Y}_q^A = V_{qL}^\dagger Y_q^A V_{qR}$$

Can we have  $(\tilde{Y}_u^A)_{11} \propto \epsilon m_t e^{i\phi}$  ??

Abel et al., assume nonuniversal  $A$  terms and  $(V_{L,R})_{ij} \sim V_{ij}^{CKM}$ , both in up and down sector

However

- Before diagonalizing Yukawas, with real trilinear terms  $\arg(Y_q^A)_{ij} = \arg(Y_q)_{ij}$ .

$$h_u = (V_L)_{i1}^* (Y_u)_{ij} (V_R)_{j1} \simeq \epsilon^4$$

$$(\tilde{Y}_u^A)_{11} = (V_L)_{i1}^* (\tilde{Y}_u^A)_{ij} (V_R)_{j1}$$

If there is a single leading contribution

$h^u \simeq (V_L)_{21}^* (Y_u)_{21}$  then  $(\tilde{Y}_u^A)_{11}$  is also real .



If several terms of the same order contribute to the up mass,

$$\begin{aligned} h^u &\simeq (V_L)_{21}^* (Y_u)_{21} + (V_L)_{21}^* (Y_u)_{22} (V_R)_{21} + \dots \\ &= a e^{\phi_a} \epsilon^4 + b e^{\phi_b} \epsilon^4 + \dots \\ (\tilde{Y}_u^A)_{11} &= \alpha(1, 2) a e^{\phi_a} \epsilon^4 + \alpha(2, 2) b e^{\phi_b} \epsilon^4 + \dots \end{aligned}$$

which is not real in general... EDMs constrain this element to have a phase  $\lesssim 10^{-2}$

$\Rightarrow$  “String  $CP$  problem”.

However, freedom to rotate away 6 phases from Yukawa  $\Rightarrow$  observable effects must involve all three generations .

Possible solutions:

- Hermitian Yukawa (and trilinear)
- single contribution to  $h_u$
- Higher order  $3^{rd}$  generation contrib. to  $Y_{11}^A$

Important constraints on the structure of the Yukawas  $\Rightarrow$  Talk by G. G. Ross tomorrow



# Mass Insertion limits

## Mass Insertions

$$\begin{aligned}(\delta_A^d)_{ij} &= \frac{(m_{\tilde{D}_A}^2)_{ij}}{m_{\tilde{q}}^2} \\ (\delta_{LR}^q)_{i \neq j} &= \frac{v_q (\tilde{Y}_q^A)_{ij}}{6 m_{1/2}^2 + m_0^2}\end{aligned}$$

$$\tilde{Y}_q^A \simeq \sqrt{3} m_{3/2} M_q / v_q + \frac{m_{3/2}}{\sqrt{3}} V_L^\dagger (\alpha(i, j) Y_{ij}) V_R$$

## Symmetric Texture

$$(\delta_{LR}^d)_{21} \simeq \frac{m_{3/2} m_b \bar{\epsilon}^3}{6 m_{1/2}^2 + m_0^2} \simeq \frac{m_b \bar{\epsilon}^3}{18 m_{3/2}} \simeq 8 \times 10^{-6}$$

$$(\delta_{LR}^d)_{32} \simeq \frac{2 m_{3/2} m_b \bar{\epsilon}^2}{6 m_{1/2}^2 + m_0^2} \simeq \frac{m_b \bar{\epsilon}^2}{9 m_{3/2}} \simeq 1 \times 10^{-4}$$

using  $m_{\tilde{q}} \simeq 500 \text{ GeV} \Rightarrow m_{3/2} \simeq 120 \text{ GeV}$  with  $m_{1/2} = \sqrt{3} m_{3/2}$ .



## Asymmetric Texture

$$(\delta_{LR}^d)_{32} \simeq \frac{m_{3/2} m_b t}{6 m_{1/2}^2 + m_0^2} \simeq \frac{m_b t}{18 m_{3/2}} \simeq 4 \times 10^{-4}$$

$$(\delta_{LR}^u)_{32} \simeq \frac{m_{3/2} m_t \epsilon}{6 m_{1/2}^2 + m_0^2} \simeq \frac{m_t \epsilon}{18 m_{3/2}} \simeq 7 \times 10^{-3}$$

minimal suppression in down

$m_b / (6m_{3/2}) \lesssim 5 \times 10^{-3}$ , no suppression a priori  
in up sector.

However, in the leptonic sector, even  
symmetric texture

$$(\delta_{LR}^e)_{12} \simeq \frac{m_{3/2} m_\tau \bar{\epsilon}^3}{1.5 m_{1/2}^2 + m_0^2} \simeq \frac{m_\tau \bar{\epsilon}^3}{5.5 m_{3/2}} \simeq 1.3 \times 10^{-5}$$

with  $m_{\tilde{\nu}} = 280$  GeV, while the  
phenomenological bound with photino...

$$(\delta_{LR}^l)_{12} \lesssim 6.6 \times 10^{-6}$$

Requires larger sfermion masses: OK for  
 $m_{3/2} = 170$  GeV.



## MI limits

| $x$ | $\sqrt{ \text{Im}(\delta_L^d)_{12}^2 }$ | $\sqrt{ \text{Im}(\delta_{LR}^d)_{12}^2 }$ | $\sqrt{ \text{Im}(\delta_R^d)_{12} }$ |
|-----|-----------------------------------------|--------------------------------------------|---------------------------------------|
| 0.3 | $2.9 \times 10^{-3}$                    | $1.1 \times 10^{-5}$                       | $1.1 \times 10^{-4}$                  |
| 1.0 | $6.1 \times 10^{-3}$                    | $2.0 \times 10^{-5}$                       | $1.3 \times 10^{-4}$                  |
| 4.0 | $1.4 \times 10^{-2}$                    | $6.3 \times 10^{-5}$                       | $1.8 \times 10^{-4}$                  |

| $x$ | $\sqrt{ \text{Re}(\delta_{13}^d)_{LL}^2 }$ | $\sqrt{ \text{Re}(\delta_{13}^d)_{LR}^2 }$ | $\sqrt{ \text{Re}(\delta_{13}^d)_{LL}(\delta_{13}^d)_{RR} }$ |
|-----|--------------------------------------------|--------------------------------------------|--------------------------------------------------------------|
| 0.3 | $4.6 \times 10^{-2}$                       | $5.6 \times 10^{-2}$                       | $1.6 \times 10^{-2}$                                         |
| 1.0 | $9.8 \times 10^{-2}$                       | $3.3 \times 10^{-2}$                       | $1.8 \times 10^{-2}$                                         |
| 4.0 | $2.3 \times 10^{-1}$                       | $3.6 \times 10^{-2}$                       | $2.5 \times 10^{-2}$                                         |

