

LEPTOGENESIS

AND

SUPERSYMMETRY

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SISSY02

at DESY

NEUTRINOS HAVE SMALL MASSES !!

ATMOSPHERIC ν OSCILLATION:

Super K

$$\sqrt{\Delta m_{\nu_{3,2}}^2} \approx 0.05 \text{ eV}$$

SOLAR ν OSCILLATION:

Super K
SNO

$$\sqrt{\Delta m_{\nu_{2,1}}^2} \approx (0.3-1) \times 10^{-2} \text{ eV}$$

IN THE STANDARD THEORY:

$$\mathcal{L} = \frac{1}{M} \ell \cdot \ell H \cdot H$$

$$\ell = \begin{pmatrix} \nu \\ e \end{pmatrix}$$

$$\langle H \rangle \approx 250 \text{ GeV}$$

$$M \approx 10^{15} - 10^{16} \text{ GeV}$$

NEW SCALE!

$\neq G_F^{-1/2}$; Planck

THE FIRST EVIDENCE.



SUSY

I. LEPTOGENESIS VIA FLAT DIRECTIONS

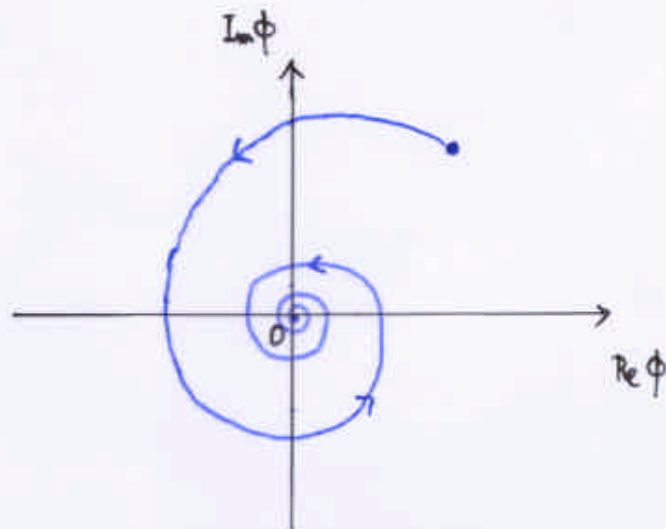
SUSY THEORY HAS MANY FLAT DIRECTIONS ϕ CONSIST OF SQUARKS, SLEPTONS AND HIGGS.

THEY MAY HAVE LARGE CLASSICAL VALUE DURING INFLATION AND START OSCILLATING WHEN $H \sim m_\phi$.

IF B OR L OPERATOR EXISTS, PHASE ROTATION OCCURS WHEN ϕ STARTS THE OSCILLATION, PRODUCING B OR L NUMBER.

$$B, L \sim -\frac{i}{2} \{ \phi^* \dot{\phi} - \dot{\phi}^* \phi \}$$

Affleck, Dine
(1985)
B-PRODUCTION



B OR L PRODUCTION

NOW, WE KNOW THE PRESENCE OF \not{L} OPERATOR:

$$W = \frac{1}{M} (LH)(LH) \quad \rightarrow \text{NEUTRINO MASS}$$

L-NUMBER PRODUCTION IS POSSIBLE BY TAKING A FLAT DIRECTION:

$$\tilde{L} = \frac{1}{\sqrt{2}} \begin{pmatrix} \phi \\ 0 \end{pmatrix}, \quad H = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ \phi \end{pmatrix}.$$

Murayama, T.Y.
(1994)

• SUSY INDUCES

$$V(\phi) = a \frac{m_{3/2}}{8M} \phi^4 + \text{h.c.},$$

WHICH GIVES THE PHASE ROTATION OF ϕ :

* INITIAL VALUE OF ϕ_0 :

DURIN INFLATION ϕ MAY HAVE SUSY SOFT MASS OF ORDER OF H_{inf} . IF $m_{\text{eff}}^2 > 0$, ϕ MOVES TO THE ORIGIN $\phi = 0$ AND LEPTOGENESIS DOES NOT OCCUR. BUT, IF $m_{\text{eff}}^2 < 0$, ϕ MOVES TO INFINITY AND STOPS DOWN AT

$$|\phi_0| \simeq \sqrt{H_{\text{inf}} M}.$$

Dine, Randall, Thomas
(1996)

* THERMAL EFFECTS HAVE TO BE TAKEN INTO ACCOUNT IF $|\phi_{0.1}| \ll M_{\text{Planck}}$.

$$W = Y_u H \bar{u} Q \quad m_u = Y_u \phi < T$$

10^{-5}



$$m_\phi^2 (\text{thermal}) \approx Y_u^2 T^2 > \frac{H^2}{m_{3/2}^2}$$

EARLY OSCILLATION TAKES PLACE. D.R.T.

Allahverdi, Campbell, Ellis
Anisimov, Dine

→ DETAILED ANALYSES WERE GIVEN BY

Asaka, Fujii, Hamaguchi.

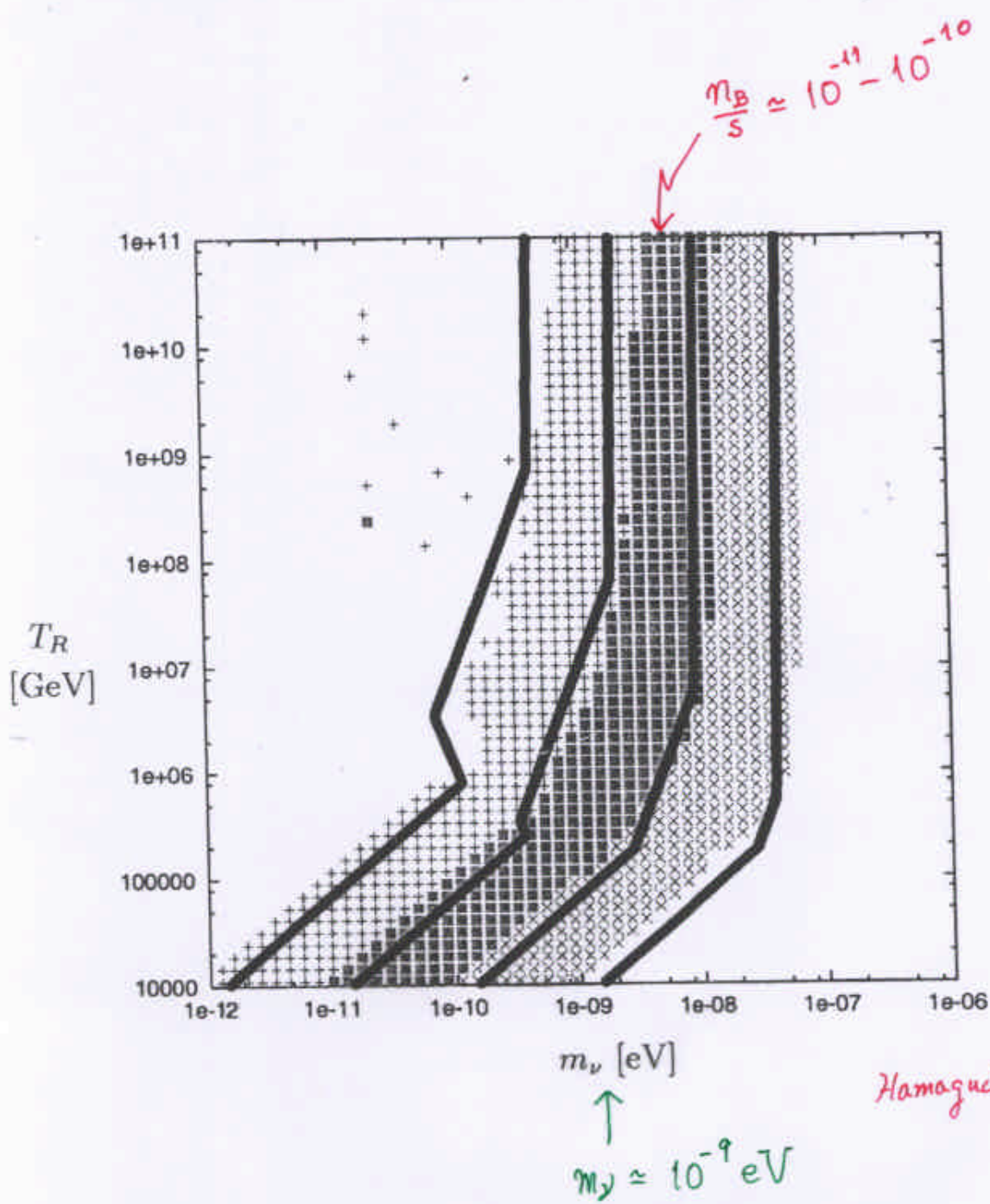
n_L IS VERY INSENSITIVE TO THE REHEATING TEMPERATURE T_R IN THE RANGE $T_R \approx 10^5 - 10^{12}$ GeV.

$H_{inf} \uparrow \Rightarrow \dot{H} \uparrow \Rightarrow n_L \uparrow$
BUT $T \uparrow \Rightarrow$ EARLY oscillation.
 $n_L \downarrow$

* L -ASYMMETRY IS CONVERTED TO B -ASYMMETRY IN THE UNIVERSE THROUGH THE SPHALERON EFFECTS.

Kuzemina, Rubakov, Shaposhnikov (1985); Fukugita, T. Y. (1986)

$$\frac{n_B}{s} \approx (-0.35) \times \frac{n_L}{s} \approx 10^{-10} \delta_{\text{eff}} \left(\frac{m_\nu}{10^{-9} \text{eV}} \right)^{-3/2} \left(\frac{m_{3/2}}{1 \text{TeV}} \right)$$



Hamaguchi, Fujii

Fig. 1

THE BARYON ASYMMETRY IN THE PRESENT UNIVERSE

$$\frac{n_B}{s} \approx (0.4 - 1) \times 10^{-10}$$

SUGGESTS

$$m_\nu \approx (0.1 - 3) \times 10^{-9} \text{ eV}.$$

SEE FIG.

DIFFICULT TO TEST THIS.

$$\text{BUT, } \underline{m_{\nu_1}} \ll m_{\nu_{2,3}},$$

CAN BE TESTED, SINCE THIS LARGE HIERARCHY
PREDICTS $0\nu 2\beta$ DECAY AS

$$\langle m_{\nu_e \nu_e} \rangle \approx (0.5 - 3) \times 10^{-3} \text{ eV}$$

FOR THE NORMAL MASS HIERARCHY.

$$\langle m_{\nu_e \nu_e} \rangle \approx (2 - 5) \times 10^{-2} \text{ eV}$$

FOR THE INVERTED MASS HIERARCHY.

$$\begin{pmatrix} a & b \\ b & c \end{pmatrix}$$

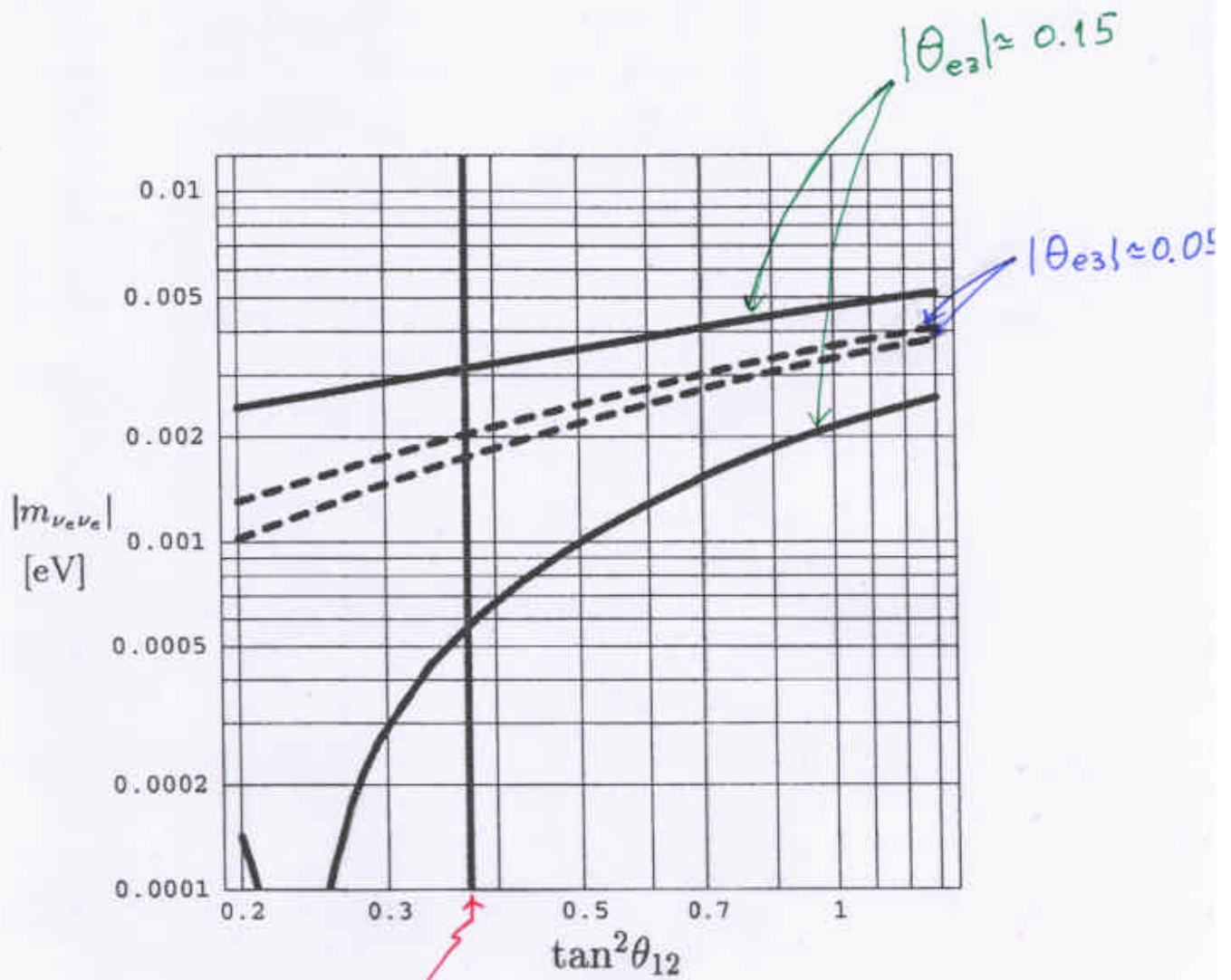
Visseri

Fuji, Hamaguchi

SEE FIGS.

$$\begin{aligned} \text{LARGE MIXING} &\rightarrow b \sim |c-a| \\ m_1 \ll m_2 &\rightarrow \det M \approx 0 \\ &\downarrow \\ &\rightarrow a \sim c \sim b \quad (a \neq 0) \end{aligned}$$

NORMAL MASS HIERARCHY, $m_{\nu_3} > m_{\nu_2} > m_{\nu_1}$.

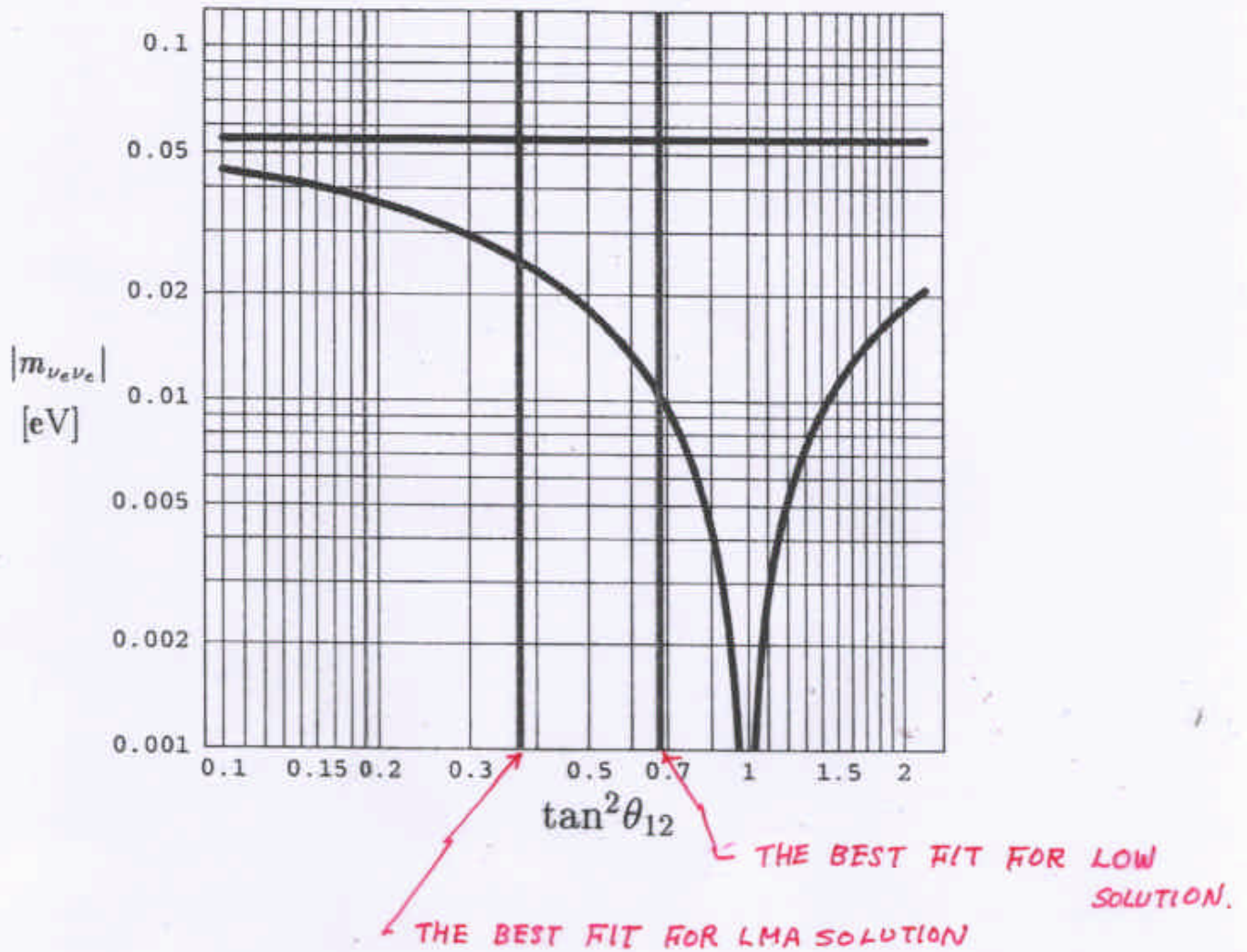


THE BEST FIT VALUE FOR LMA SOLUTION.

$$\langle m_{\nu_e \nu_e} \rangle \approx 5 \times 10^{-4} - 3 \times 10^{-3} \text{ eV}$$

Fig. 2

INVERTED MASS HIERARCHY, $m_{\nu_2} > m_{\nu_1} > m_{\nu_3}$.



$$m_{\nu_e \nu_e} \simeq (2-5) \times 10^{-2} \text{ eV} \text{ FOR LMA.}$$

$$\simeq (1-5) \times 10^{-2} \text{ eV} \text{ FOR LOW.}$$

Fig. 3

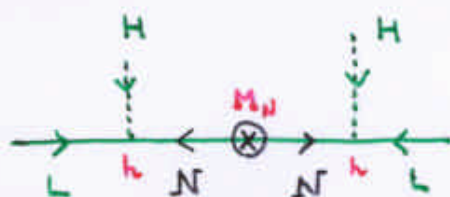
II. LEPTOGENESIS VIA N DECAY

THE MOST NATURAL MODEL INDUCING THE EFFECTIVE OPERATOR, $\frac{1}{M} (LH)(LH)$, IS GIVEN BY

THE SEESAW MECHANISM OF GRSY.

Gell-Mann, Ramond, Slansky,
Yanagida (1979)

THIS ASSUMES SUPER-HEAVY MAJORANA FERMIONS N .



$$W = \frac{h^2}{M_N} (LH)(LH)$$

$$M \equiv \frac{M_N}{h^2}$$

$$M_N \simeq 10^{12} - 10^{15} \text{ GeV}$$

FOR $h \simeq 0.03 - 1$

- N IS A KEY POINT FOR UNIFICATION.
- MANY APPLICATIONS WERE PROPOSED AFTER THE GRSY.

F. Wilczek (1979) SO(10)

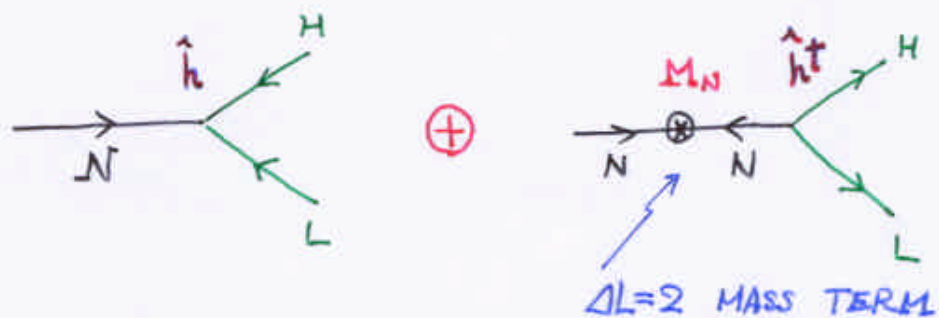
S. Weinberg (1979) Genera

E. Witten (1980) SO(10)

Holmstrom, Senjanovic (1980) L-R sym

N 's MAY BE PRODUCED IN THE EARLY UNIVERSE
IF $T_R \gtrsim M_N$.

N DECAY HAS LEPTON-NUMBER VIOLATION.



IF THE Yukawa COUPLING CONSTANTS \hat{h}_{ij} HAVE ~~CP~~
PHASES, N DECAY PRODUCES **LEPTON ASYMMETRY**:

$$\text{BR}(N \rightarrow \bar{L} + H) \neq \text{BR}(N \rightarrow L + H).$$

PRODUCED L ASYMMETRY \Rightarrow B ASYMMETRY
CONVERTED

Miyagita, T.Y.
(1986)

BARYON ASYMMETRY :

$$\frac{n_B}{S} \approx -0.35 \frac{n_L}{S}$$

chemical equilibrium conditions
 $\rightarrow \left\{ \Delta B = \frac{8N_f + 6N_H}{22N_f + 12N_H} \Delta(B-L) \right\}$

$$\frac{n_L}{S} \approx \kappa \left(\frac{1}{g_*} \right) \mathcal{E}$$

degrees of freedom

Dynamical Factor from out-of-equilibrium condition

$$\frac{n_B}{S} \approx \kappa \times 10^{-3} \mathcal{E}$$

* ESTIMATION OF \mathcal{E} : ASSUMING $M_3 > M_2 > M_1$

CONSIDER N_1 DECAY :

Flanzer, Paschos, Sarikar
 Covi, Roulet, Vissani
 Buchmuller, Plumacher
 Pilaftsis. (1996)

$$\mathcal{E}_{(1)} \equiv \frac{\Gamma(N_1 \rightarrow L+H) - \Gamma(N_1 \rightarrow \bar{L}+\bar{H})}{\Gamma(N_1 \rightarrow L+H) + \Gamma(N_1 \rightarrow \bar{L}+\bar{H})}$$

$$\approx \frac{3}{16\pi} (\sin \delta) \frac{m_{D_3} M_1}{\langle H \rangle^2}$$

$$\approx (\sin \delta) \times 10^{-6} \left\{ \frac{M_1}{10^{10} \text{ GeV}} \right\}$$

FOR $m_{D_3} \approx 0.05 \text{ eV}$, $\langle H \rangle \approx 170 \text{ GeV}$.

$$\frac{n_B}{s} \simeq \kappa (\sin \delta) 10^{-9} \left(\frac{M_1}{10^{10} \text{ GeV}} \right)$$

↙ CP PHASE

κ SHOULD BE DETERMINED BY SOLVING THE Boltzmann EQUATIONS :

$$\kappa = f(h_i, M_i).$$

$$\kappa \lesssim 0.1 - 1 \quad ; \quad |\sin \delta| \leq 1$$

$M_1 \gtrsim 10^9 \text{ GeV}$ TO EXPLAIN THE OBSERVATION:

$$\frac{n_B}{s} \simeq (0.4 - 1) \times 10^{-10}$$

ON THE OTHER HAND, $T_R \lesssim 10^{10} \text{ GeV}$ TO AVOID THE OVERPRODUCTION OF GRAVITINOS. Weinberg (1980)

Khlopov, Linde
Ellis, Kim, Nanopoulos
Kusuki, Moroi

$$M_i \lesssim T_R$$

$$\begin{cases} M_1 \simeq 10^9 - 10^{10} \text{ GeV} \\ m_{\nu} \simeq 10^{-3} - 10^{-2} \text{ eV} \end{cases}$$

SEE Fig.

$$\text{c.f. } \begin{cases} m_{\nu_3} \simeq 0.05 \text{ eV} \\ m_{\nu_2} \simeq 0.005 \text{ eV} \end{cases}$$

SEESAW : $m_{\nu} \simeq m_D^2/M$: $m_{\nu_3} \simeq 0.05 \text{ eV}$, $m_D \simeq m_t \rightarrow M_3 \simeq 10^{15} \text{ GeV}$

IF $M_3 : M_2 : M_1 \simeq m_t : m_c : m_u$; $M_1 \simeq 10^{10} \text{ GeV} !!$

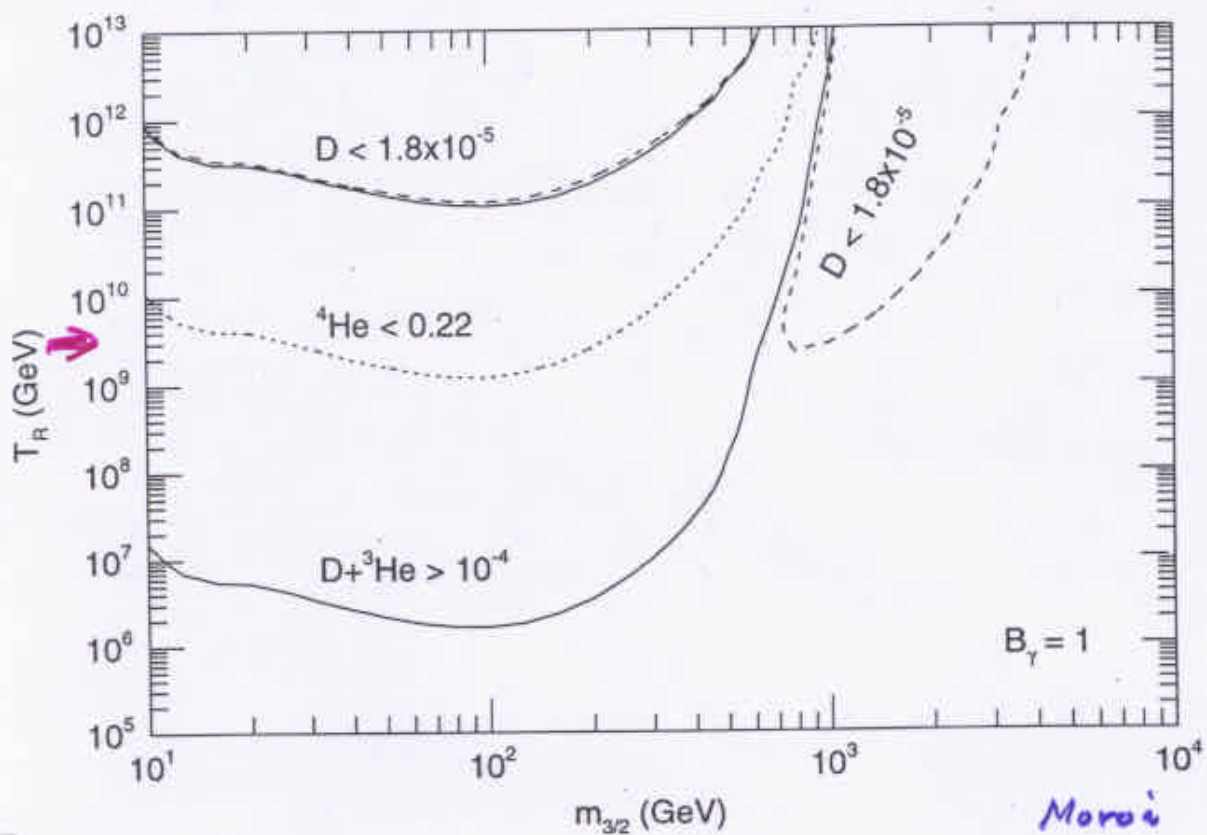
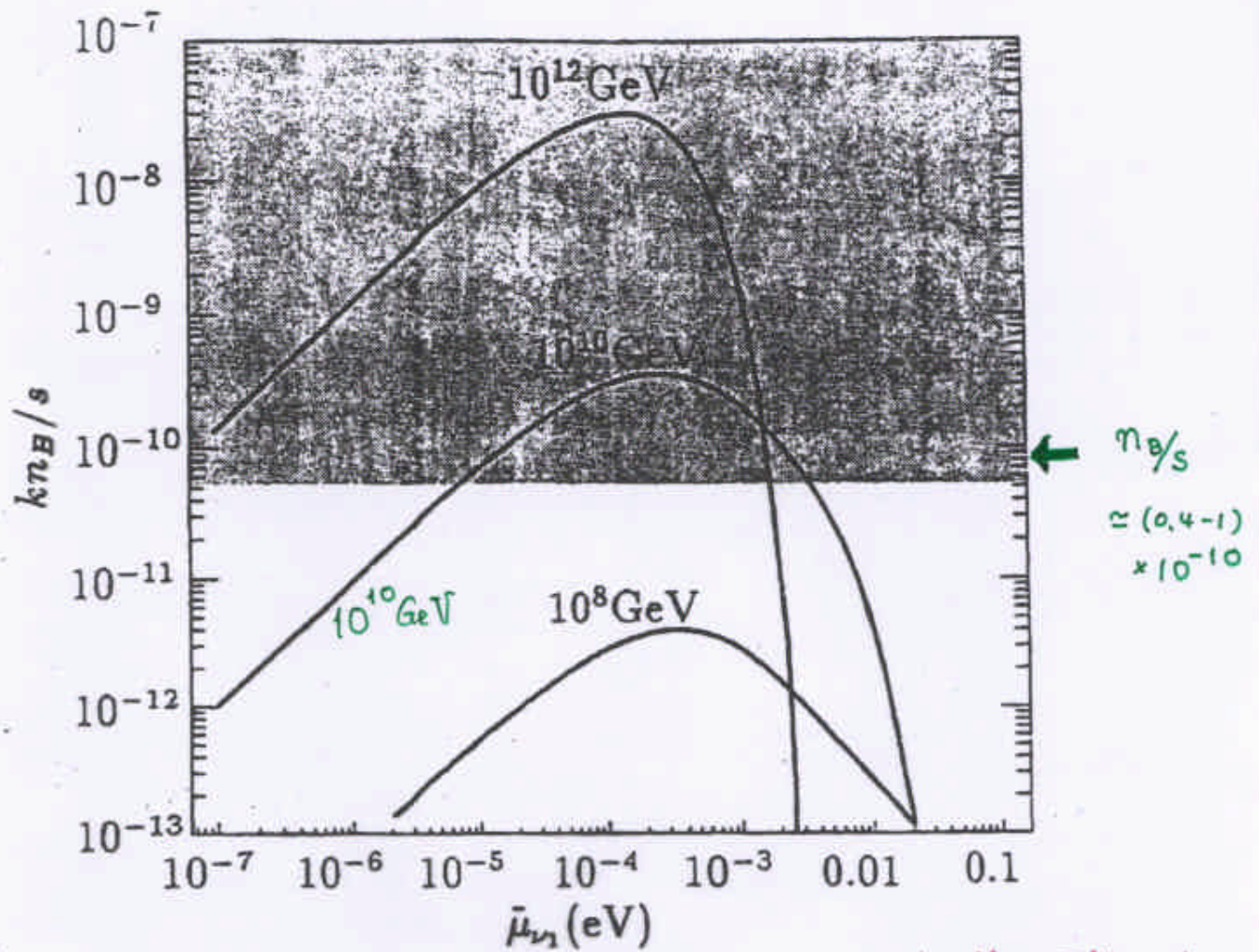


Figure 6.6: Upperbound on T_R as a function of $m_{3/2}$. Here, we take $B_\gamma = 1$. In the region above the solid curve ^3He and D are overproduced, the abundance of ^4He is less than 0.22 above the dotted curve and the abundance of D is less than 1.8×10^{-5} above the dashed curve.

$$T_R \lesssim 10^{9-10} \text{ GeV}$$

$$\text{FOR } m_{3/2} \approx O(1) \text{ TeV}$$

$$\eta_B/s \approx (0.4 - 1) \times 10^{-10}$$



Buchmüller, Plümacher

$$M_1 \approx 10^9 - 10^{10} \text{ GeV}$$

$$T_{\text{leptogenesis}} \approx 10^{10} \text{ GeV}$$

Fig. 5

TEMPERATURE FOR LEPTOGENESIS

$$T_{L.G.} \simeq 10^{10} \text{ GeV.}$$

Buchmüller, Plumacher
(2001)



$$m_{3/2} < 1 \text{ keV} \quad \text{OR} \quad m_{3/2} \geq 1 \text{ TeV}$$

$$\left(m_{3/2} \sim (30 - 50) \text{ GeV} \right.$$

GRAVITINO DARK MATTER

Buchmüller)

* THE BARYON ASYMMETRY CAN BE NATURALLY EXPLAINED BY OBSERVED NEUTRINO MASSES !!

m_1 SHOULD NOT BE TOO LARGE ($m_1 > 0.1 \text{ eV}$)

AND SHOULD NOT BE TOO SMALL ($m_3 < 10^{-3} \text{ eV}$)

SEE FIG.

* IF $M_1 \simeq M_2$,  DOMINATES, $M_1 - M_2 > \Gamma_N$

$$\mathcal{E}_{(1)} \simeq \frac{\ln(kk^*)_{12}^2}{M_1 - M_2} \times \frac{1}{M_1 - M_2}$$

$$\mathcal{E}_{(2)} \simeq \frac{\ln(kk^*)_{21}^2}{M_2 - M_1} \times \frac{1}{M_2 - M_1}$$

$$\mathcal{E}_{(1)} + \mathcal{E}_{(2)} \simeq 2 \times \mathcal{E}_{(i)}$$

\mathcal{E} IS ENHANCED WHEN $M_1 \sim M_2$!! Flanz, Paschos, Savoca, Iliadis

$$\left\{ \begin{array}{l} M_1 \sim M_2 \sim 10^8 \text{ GeV} \\ T_R \sim 10^8 \text{ GeV} \end{array} \right.$$

Ellis, Rindal, T.Y.

11.

$$m_{3/2} \geq \text{a few} = 100 \text{ GeV}$$

III. LEPTOGENESIS FROM \tilde{N} -DOMINATED EARLY UNIVERSE

$$\frac{h^2}{M_N} \approx \frac{1}{10^{15} \text{ GeV}}$$

FOR $h \ll 1$, $M_N \ll 10^{15} \text{ GeV}$.

IF $M_N < H_{\text{inf}}$, SCALAR N , \tilde{N} , MAY HAVE LARGE CLASSICAL VALUE AND IT DOMINATES THE UNIVERSE IF THE LIFE TIME IS SUFFICIENTLY LONG.

Murayama, T. Y. (1994)

BUT, WHY $h \ll 1$, AND $M_N \ll M_{\text{GUT}}$?

WHY $\tilde{N}_0 \sim M_{\text{Planck}}$?



$\tilde{N}_0 \sim M_{\text{GUT}}$ IS NATURAL.

THESE TWO SERIOUS PROBLEMS HAVE BEEN SOLVED.

Hebecker, March-Russell, T. Y.

FIVE DIMENSIONAL SPACETIME WITH S^1/\mathbb{Z}_2 ORBIFOLD.

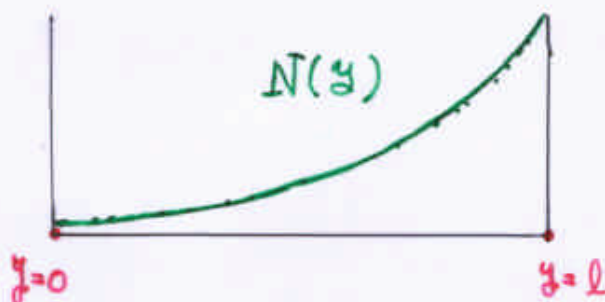
Hebecker, March-Russell

INTRODUCE 3 PAIRS OF N AND \bar{N} IN THE BULK,
WHICH HAVE MASSES OF ORDER THE FUNDAMENTAL
SCALE M_* .

$$-M \cdot \bar{N} \cdot N$$

$$M \sim M_*$$

$$\mathbb{Z}_2 : \begin{cases} N \rightarrow N \\ \bar{N} \rightarrow -\bar{N} \\ M \rightarrow -M \end{cases}$$



$$N(y) = e^{-M(l-y)}$$

CONSIDER (B-L) BREAKING AT $y=0$ FIXED POINT :

$$\langle \Phi_{B-L} \rangle = M_* \delta(y), \rightarrow M_* N \bar{N} \delta(y)$$

WHICH LEADS TO 4-DIM. MASSES FOR N 'S :

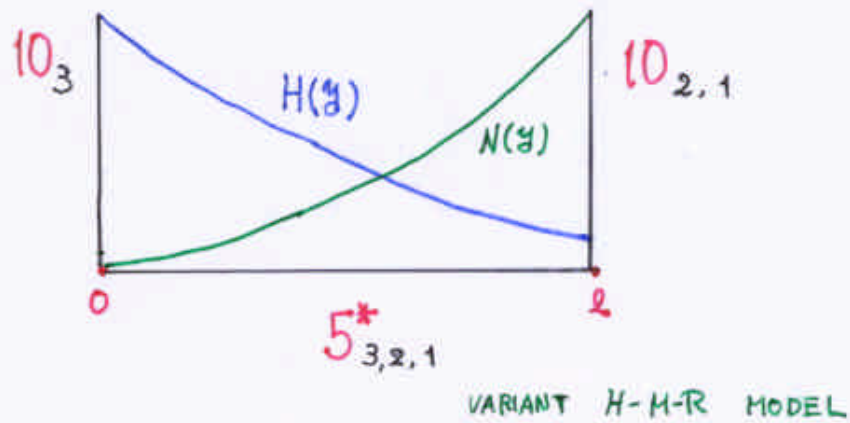
$$M_R \simeq M_* e^{-2Ml}$$

FOR $M_* l \simeq 12$, $M_* \simeq 7 \times 10^{19} \text{ GeV}$ ($\because M_*^2 (M_* l) \simeq M_{\text{Planck}}^2$).

THEN, ONE GETS $M_R \simeq 10^7 \text{ GeV}$.

$$\tilde{N}_0 \simeq M_* \sim 10^{18} \text{ GeV}.$$

Yukawa COUPLING $h N \cdot 5^* H$:



Higgs H AND \bar{H}' HAVE A BULK MASS $\sim M_H H \cdot \bar{H}'$.

$$m_c/m_t \approx e^{-M_H l} \approx 1/400$$

$$M_H l \approx 6$$

$$h N 5^* H : \quad h \sim \frac{h_0}{\sqrt{M_H l}} e^{-M_H l} \sqrt{\frac{M_H}{M_*}} \sim 10^{-4}$$

FOR $h_0 \sim 0.2$
 $(m_c/m_t \approx 0.02$
 $\tan \beta = 3)$

$$m_D \sim \frac{h^2 \langle H \rangle^2}{M_R} \approx 0.01 \text{ eV} !!$$

WE HAVE SMALL Yukawa COUPLINGS h_{ij} , NATURALLY:

$$h \approx 10^{-5} - 10^{-4}$$

HISTORY OF UNIVERSE WITH \tilde{N}_i ,

WHOSE MASS $\sim 10^9 \text{ GeV}$ AND Yukawa COUPLING $\sim 10^{-5}$.

Hamaguchi, Murayama, T. Y.

* DURING INFLATION \tilde{N}_i HAS A LARGE CLASSICAL VALUE,
 $\tilde{N}_0 \simeq 10^{18} \text{ GeV}$, AS $H_{\text{inf}} \gg m_N$.

AFTER THE INFLATION ENDS, H DECREASES AND WHEN
 $H \simeq m_N$, \tilde{N} STARTS OSCILLATING. THE \tilde{N} OSCILLATION
DOMINATES THE EARLY UNIVERSE AS LONG AS \tilde{N} LIVES
MUCH LONGER THAN THE INFLATON χ : $\Gamma_N \ll \Gamma_\chi$.
 $\{|h_i| \ll 1\}$

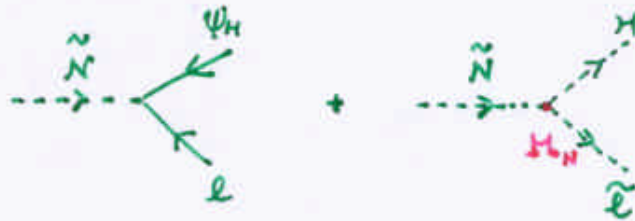
ONCE \tilde{N} DOMINATES THE UNIVERSE
MOST OF THE IMPORTANT INPUTS OF THE
UNIVERSE ARE DETERMINED BY NATURE OF \tilde{N} .

• \tilde{N} DECAY GIVES LEPTON ASYMMETRY (B ASYMMETRY)
AND ENTROPY (T_R).

• $\frac{\delta \rho_{\tilde{N}}}{\rho_{\tilde{N}}}$ BECOMES THE ADIABATIC FLUCTUATION $\frac{\delta \rho}{\rho}$.

Lyth, Wands
Moroi, Takahashi

LEPTON ASYMMETRY FROM \tilde{N}_1 DECAY:



$$\mathcal{E}_{(1)} \approx 1 \times 10^{-10} \delta_{\text{eff}} \left(\frac{M_N}{10^6 \text{ GeV}} \right) \left(\frac{m_{D_3}}{0.05 \text{ eV}} \right)$$

\tilde{N} DECAY PRODUCES THE RADIATIONS AND THE ENTROPY DENSITY IS GIVEN BY

$$S = \frac{2\pi^2}{45} g_* T_N^3$$

T_{N_1} IS DETERMINED BY THE DECAY RATE Γ_N AS

$$\begin{aligned} \frac{\pi^2}{30} g_* T_N^4 &\approx M_N^2 |\tilde{N}_D|^2 \\ &\approx 3 M_{Pl}^2 \Gamma_N^2 \end{aligned}$$

$$\frac{\eta_L}{S} \approx \frac{3}{4} \mathcal{E}_{(1)} \left(\frac{T_N}{M_N} \right)$$

$$\approx 0.7 \times 10^{-10} \left(\frac{T_N}{10^6 \text{ GeV}} \right) \left(\frac{m_{D_3}}{0.05 \text{ eV}} \right) \delta_{\text{eff}}$$

$$\frac{\eta_B}{S} \approx 0.35 \times \frac{\eta_L}{S} \approx 0.3 \times 10^{-10}$$

FOR $T_N \approx 10^6 \text{ GeV}$, $\delta_{\text{eff}} \approx 1$

$$\text{O.B.S. } \frac{\eta_B}{S} = (0.4-1) \times 10^{-10}$$

$$\Gamma_N \approx \frac{h^2}{8\pi} M_N$$

$$T_N \approx 0.1 \cdot h \sqrt{M_{Pl} M_N} \approx 3 \times 10^6 \text{ GeV}$$

$$\text{FOR } M_N \sim 10^9 \text{ GeV} \\ h \sim 10^{-5}$$

✱ NO GRAVITINO PROBLEM.

GRAVITINOS PRODUCED AT THE REHEATING EPOCH AFTER INFLATION ARE DILUTED BY THE ENTROPY PRODUCTION IN \tilde{N} DECAY.

$$T_{\text{eff}} \approx T_{\text{RH}} \sim 10^6 \text{ GeV}$$

$$\text{FOR } T_R \lesssim 10^{12} \text{ GeV}.$$

A WIDE RANGE OF $m_{3/2}$ IS CONSISTENT WITH THE PRESENT SCENARIO:

$$m_{3/2} \gtrsim \underline{10} \text{ MeV}$$

$$\text{OR } m_{3/2} < 1 \text{ keV}.$$

✱ GAUGE-MEDIATION MODEL WITH $m_{3/2} \approx 10 \text{ MeV}$ — 1 GeV IS CONSISTENT.

* SCALE-INVARIANT DENSITY FLUCTUATIONS :

THE OBSERVED CMB POWER SPECTRUM SUGGESTS ALMOST SCALE-INVARIANT DENSITY FLUCTUATIONS :

$$\frac{\delta\rho}{\rho} = \text{SCALE-INVARIANT.}$$

THE DENSITY FLUCTUATIONS ARE PRODUCED DURING INFLATION. THE SIMPLEST POSSIBILITY IS THAT THEY ARE ORIGINATED FROM FLUCTUATIONS OF THE INFLATON FIELD.

$$\frac{\delta\rho}{\rho} \approx \kappa \left[\frac{H_{\text{inf}}^3}{V'_{\text{inf}}} \right] \quad ; \quad V' = \frac{\partial V}{\partial \chi}$$

IN MANY INFLATION MODELS, THE EXPANSION RATE H_{inf} IS ALMOST CONSTANT DURING THE INFLATION.

BUT, THE SLOPE V'_{inf} CAN VARY.

HOWEVER, IF \tilde{N} DOMINATES THE EARLY UNIVERSE, $\delta\rho/\rho$ IS DETERMINED BY THE FLUCTUATIONS OF \tilde{N} .

$$\frac{\delta\rho}{\rho} \Big|_{\tilde{N}} \approx \frac{H_{\text{inf}}}{2\pi} \approx \text{ALMOST CONSTANT.}$$

MAY SOLVE A PROBLEM IN THE **EKPYROTIC** SCENARIO
IN THE BRANE WORLD.

Lyth.
MOROI AT SUS

CONCLUSION :

- THE **SEESAW** MODEL OF GRSY EXPLAINS VERY NATURALLY

NOT ONLY THE SMALL NEUTRINO MASS
BUT ALSO THE UNIVERSE'S BARYON ASYMMETRY

$$\frac{n_B}{s} \approx (0.4-1) \times 10^{-10}$$

EXPERIMENTAL OBSERVATIONS ON

$0\nu 2\beta$ DECAY

AND

CP IN ν OSCILLATION

ARE REQUIRED TO CONVINCING OURSELVES OF

THIS SCENARIO.

- \tilde{N} -DOMINATED UNIVERSE MAY PROVIDE A NEW SCENARIO OF INFLATIONAL UNIVERSE.

