

Searches for Flavour Changing Neutral Currents and Lepton Flavour Violation at HERA

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A summary of the recent searches for anomalous single top-quark production and lepton flavour violation in high energy $e^\pm p$ collisions is presented. Single top-quark production via an anomalous flavour changing neutral current $\gamma - u - t$ coupling would lead to the reaction $ep \rightarrow etX$, $t \rightarrow Wb$. H1 observed an excess of events above the Standard Model prediction in the leptonic decay channel of the W boson, leading to an isolated lepton, large missing transverse momentum and a jet with large transverse momentum. Five of these events are compatible with single top-quark production, compared to 1.8 events expected from background processes. ZEUS observed no excess above the SM background expectation in the leptonic channel. Neither of the two experiments found a deviation from the SM background expectation in the 3-jet final state, which would result from the hadronic decay of the W boson. Searches for lepton flavour violating interactions of the type $ep \rightarrow \mu X$ and $ep \rightarrow \tau X$ have been performed. No evidence was found for lepton flavour violation and limits were derived on the production of leptoquarks and R_p violating squarks, which could mediate such interactions.

1. Single top-quark production at HERA

Neutral current interactions in the Standard Model (SM) preserve the quark flavours in leading order perturbation theory. Quark flavour changing neutral current (FCNC) processes are only present via higher order radiative corrections and are therefore strongly suppressed. The SM cross section for single top-quark production at HERA is about 1 fb [1]. Due to the large mass of the top quark, close to the electroweak symmetry breaking scale, possible deviations from the SM could be observed first in the top sector. The production of single top quarks through FCNC is predicted by many extensions of the SM [2, 3, 4, 5, 6]. The dominant contribution at HERA is expected to come from an anomalous coupling $\kappa_{tu\gamma}$ at the photon-u-quark-vertex (see Fig. 1).

The experimental signature of the process $ep \rightarrow etX$, $t \rightarrow Wb$ depends on the decay channel of the W boson. For leptonic decays, it consists of isolated leptons, missing transverse momentum and a hadronic system at a large transverse momentum p_T^X . The main background for this process at HERA is the production of real W bosons (see Fig. 2). The hadronic decay of the W boson leads to events with one jet associated with the secondary b quark and two jets from the secondary W decay, all of them at large transverse momenta.

The observation of isolated lepton events with large values of p_T^X by the H1 collaboration [7] has motivated dedicated searches by the H1 and ZEUS collaborations for single top-quark production in both the leptonic and the hadronic channels [8, 9]. The results presented here made use of all available HERA I data.

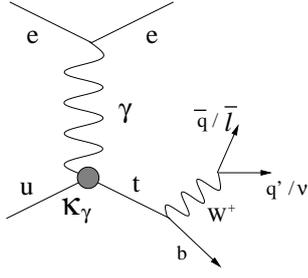


Figure 1. Single top-quark production via flavour changing neutral current transitions at HERA.

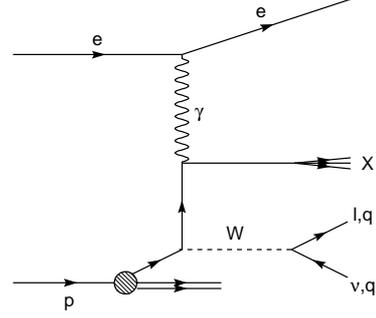


Figure 2. Example for the production of real W bosons at HERA.

	H1 preliminary e^+p , 102 pb $^{-1}$	H1 preliminary e^-p , 14 pb $^{-1}$	ZEUS preliminary $e^\pm p$, 130 pb $^{-1}$
p_T^X range	Obs./expected	Obs./expected	Obs./expected
$p_T^X > 0$ GeV	18 / 10.5 \pm 2.5	0 / 1.8 \pm 0.4	17 / 16.4 \pm 1.7
$p_T^X > 25$ GeV	10 / 2.8 \pm 0.7	-	2 / 2.4 \pm 0.2
$p_T^X > 40$ GeV	6 / 1.0 \pm 0.3	-	0 / 1.0 \pm 0.1

Table 1. Number of observed lepton events, compared to the SM background expectations. The results from ZEUS for $p_T^X > 25$ GeV and $p_T^X > 40$ GeV are with additional single top selection cuts applied, as described in section 1.2.

1.1. Isolated lepton events

The preselection of isolated lepton events requires at least one isolated electron or muon with high transverse momentum p_T^l , large missing transverse momentum p_T^{miss} and at least one hadronic jet with transverse momentum p_T^X . H1 optimized the selection for W -decay signatures [8]. ZEUS performed an inclusive analysis [9], where the dominant background processes are neutral current deep inelastic scattering events (electron channel) and Bethe-Heitler muon pair production (muon channel).

The expectations for direct W production were simulated in leading order QCD calculations by the generator EPVEC [10]. The QCD NLO corrections change the W boson production cross section by less than 10% at large values of p_T^X [11].

The H1 experiment observed 18 events in the data, while 10.5 events are expected from SM processes. Figure 3 (left) shows the distributions of the H1 candidate events in the lepton-neutrino transverse mass M_T (P_T^{miss} being attributed to the hypothetical neutrino). A Jacobian peak around the W boson mass is observed, as expected from the production of real W bosons. Figure 3 (right) shows the distribution of the events in p_T^X . At low values of p_T^X , the measured rates agree with the SM expectation, while at large values of p_T^X , more events are found than expected: Integrated over all p_T^X , 18 isolated lepton events were observed, while 10.5 events are expected from SM processes. For $p_T^X > 40$ GeV, six events are observed with only one expected.

ZEUS finds agreement with the SM, both in the rate and in the distribution of the observed events. Figures 4 and 5 show the distributions of isolated electron and muon events in M_T and p_T^X .

Table 1 compares the number of isolated lepton events observed at HERA with those expected.

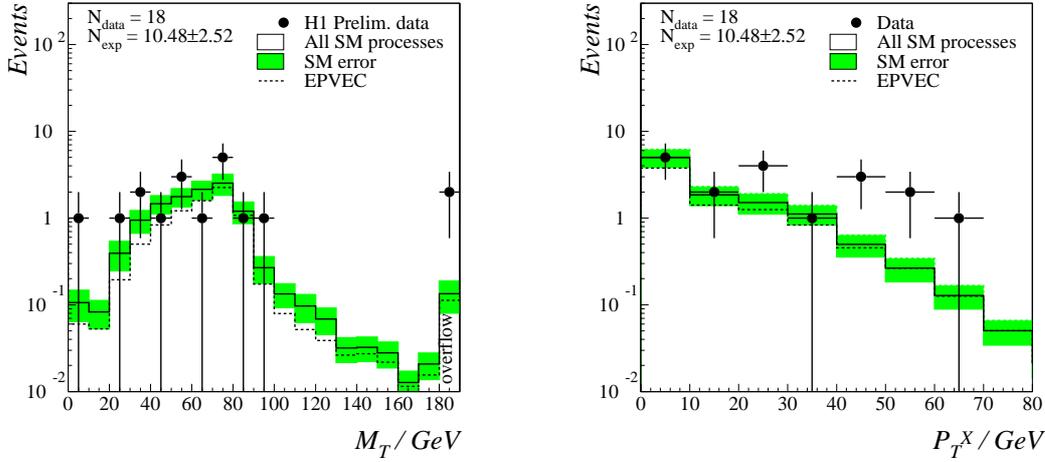


Figure 3. Distribution of the transverse mass (left) and the hadronic transverse momentum (right) for the H1 isolated lepton events, compared to the SM prediction. Only e^+p data are shown.

1.2. Single top search in the leptonic channel

The selections were further optimized for a signal from single top-quark production by requiring a large value of $p_T^X > 40$ GeV (ZEUS) and > 35 GeV or > 25 GeV (H1, depending on the hadronic jet angular range). The W component in the ZEUS selection was enhanced by applying additional cuts on the energy-momentum balance in the calorimeter and on the missing transverse momentum, after correcting for the muon-track momentum. Muon-type events were also rejected, if a second muon was found in the event. H1 required a positive lepton charge and a value of M_T above 10 GeV in order to reduce the contribution from processes with off-shell W bosons. After these cuts, ZEUS observed no event, while 1.0 is expected from SM backgrounds, which are dominated by W production, whereas H1 observed 5 events, while 1.8 ± 0.5 are expected.

Assigning the missing transverse momentum to a hypothetical neutrino and assuming the lepton-neutrino-system to originate from a W boson decay, the lepton-neutrino-hadron invariant mass $M_{l\nu X}$ of the H1 candidates can be computed. The neutrino kinematics were obtained either from the W mass constraint or from the energy-momentum-balance, if the scattered lepton was observed in the calorimeter. Two mass solutions were obtained for each event. For three of the candidate events only one solution is compatible with the kinematic constraints, while for the other two candidates both solutions are acceptable. The reconstructed mass is compatible with that of the top quark for most of the events, as shown in Fig. 6.

1.3. Single top search in the hadronic channel

The hadronic decay of the W boson results in events with one high- p_T jet associated with the secondary b quark and two high- p_T jets from the secondary W decay. The event selection required three jets with $p_T^{jet1} > 40$ GeV, $p_T^{jet2} > 25$ GeV and $p_T^{jet3} > 14$ GeV (ZEUS) or $p_T^{jet1} > 40$ GeV, $p_T^{jet2} > 25$ GeV and $p_T^{jet3} > 20$ GeV (H1). In both cases, the photoproduction background was reduced by requiring one of the 2-jet masses and the 3-jet mass to be compatible with the W boson mass and the top mass, respectively.

Figure 7 shows the distribution of the 3-jet mass in the selected mass windows for the H1 and ZEUS candidate events. The normalisation uncertainties of the photoproduction background, which

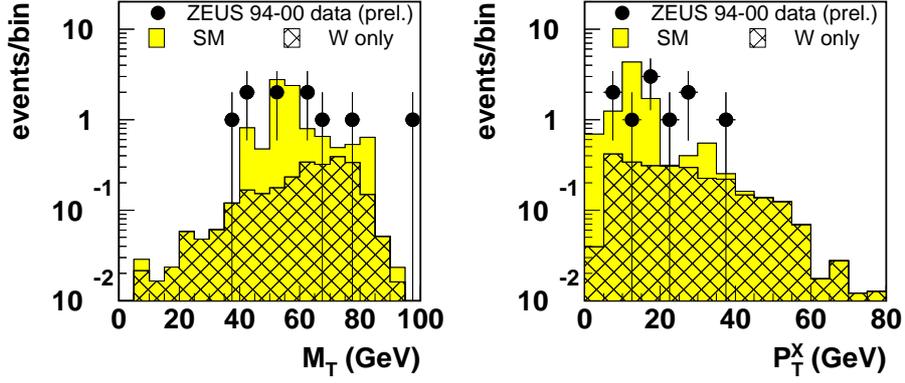


Figure 4. Distribution of the transverse mass of the lepton-neutrino system (left) and of the hadronic transverse momentum (right) for the ZEUS isolated electron events, compared to the SM prediction.

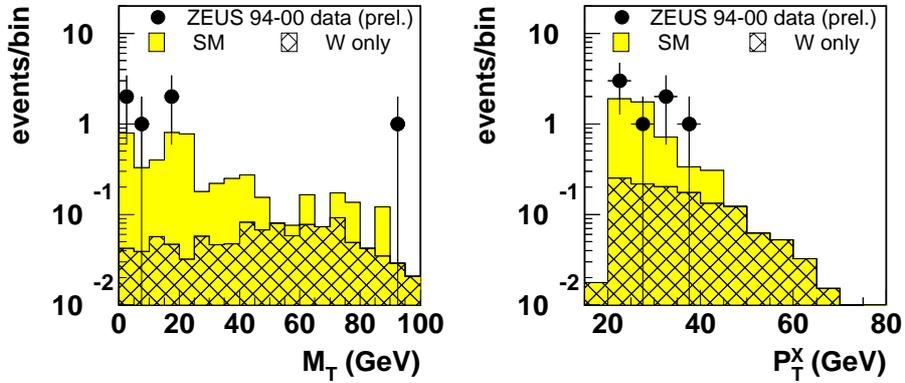


Figure 5. Distribution of the transverse mass of the lepton-neutrino system (left) and of the hadronic transverse momentum (right) for the ZEUS isolated muon events, compared to the SM prediction.

was only evaluated in leading order of QCD, were reduced by normalising the simulated event rates to those observed in the low-mass domain. With the selection cuts described above, H1 observed 14 events, while 19.6 ± 7.8 are expected, whereas ZEUS observed 19 events and expects 20.0.

In both experiments the number of observed events in the hadronic channel is in agreement with SM expectations. The 95% C.L. upper limit on the single top-quark production cross section from the hadronic channel of the H1 analysis corresponds to an upper limit of 5.4 events from single top quark decays in the electron and muon channels. The interpretation of the observed lepton events as anomalous top-quark production is therefore not ruled out by the H1 analysis in the hadronic channel.

1.4. Limits on FCNC couplings

Upper limits on single top-quark production cross sections were set by both experiments, combining the leptonic and hadronic channels. Using an effective Lagrangian, which describes the FCNC top-quark interactions [5], they were converted into 95% C.L. upper bounds on the anomalous coupling $\kappa_{t\nu\gamma}$ of 0.19 (ZEUS) and 0.22 (H1). The ZEUS 95% C.L. upper limit on the top cross section corresponds to an expectation of at most two top events in the H1 leptonic channel analysis.

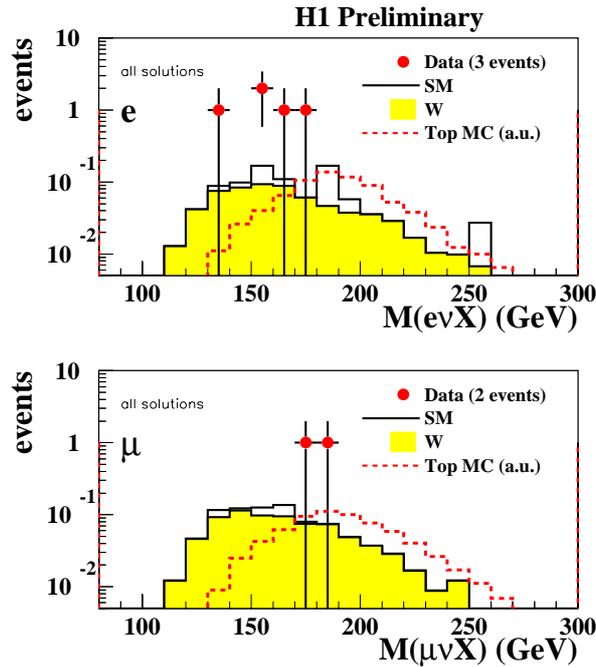


Figure 6. Distributions of the reconstructed invariant mass of the lepton-neutrino-hadron system for the H1 top candidates, compared to expectations from SM W boson production and a hypothetical single top-quark production signal (normalized to one event).

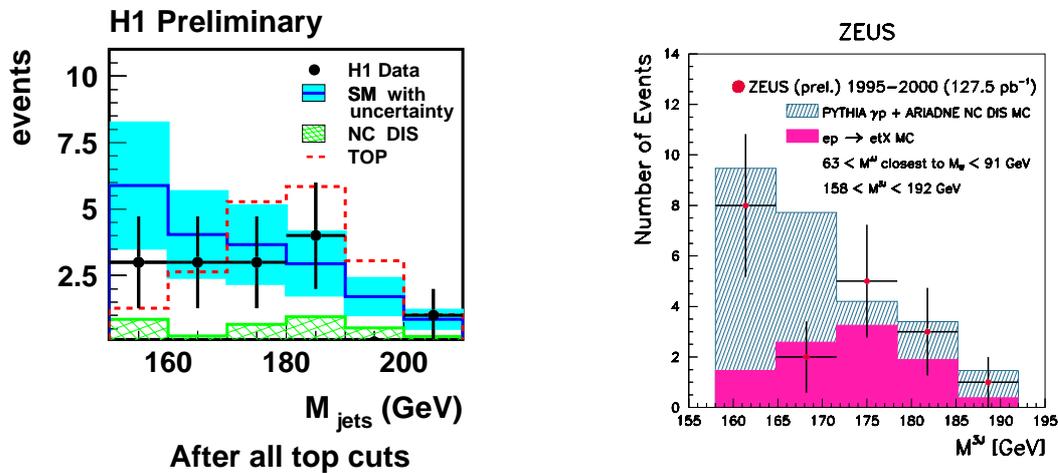


Figure 7. Distribution of the 3-jet mass of the H1 single top candidates (left) and the ZEUS single top candidates (right) in the hadronic channel, compared to expectations from SM photoproduction background and a hypothetical signal from single top-quark production with arbitrary normalisation.

The LEP [12] and TEVATRON [13] experiments have performed similar searches for single top production and rare top decays, respectively. They are sensitive to anomalous top-quark couplings to u and c quarks through both the photon and the Z boson. The results of these searches are

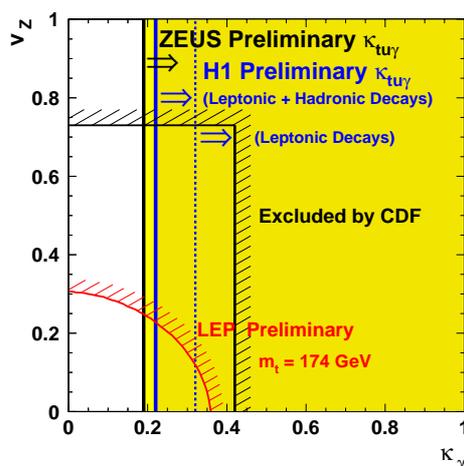


Figure 8. Limits from LEP, TEVATRON and HERA on anomalous couplings of the top quark to other quarks and neutral gauge bosons. The limits from H1 and ZEUS apply to the coupling $\kappa_{\gamma,u}$ to the u quark only. Both the H1 limit for leptonic decays and the combined limit for leptonic and hadronic decays of the top quark are indicated, whereas for ZEUS only the combined limit is indicated.

compared to the HERA limits in Fig. 8. It is evident that HERA is competitive in searches for FCNC couplings through photon interactions.

2. Lepton-flavour violation

Lepton flavour is conserved within the SM. The observation of neutrino oscillations [14], however, is a hint that lepton flavour might be violated for the charged leptons. Minimal extensions of the SM [15], that allow for finite neutrino masses, do not predict measurable rates of LFV at current collider experiments. Many extensions of the SM, however, involve LFV interactions. Such models include grand unified theories [16], models based on supersymmetry [17], compositeness [18] and technicolour [19].

At HERA, LFV can be detected in reactions of the type $ep \rightarrow lX$, where l is either a μ or a τ and X denotes the hadronic final state. Figure 9 shows examples for such reactions, where leptoquarks (LQs) mediate the LFV reaction. LQs are bosons that carry both lepton (L) and baryon (B) numbers and have lepton-quark Yukawa couplings. A LQ that couples to leptons of two different generations would induce LFV. The Buchmüller-Rückl-Wyler (BRW) model [20] was used to classify LQ species and to evaluate cross sections for the LQ-induced processes. A total of 14 LQ types are allowed, seven scalars and seven vectors, with fermion number $F = L + 3B = 0, 2$. For a LQ mass M_{LQ} below the HERA centre of mass energy ($\sqrt{s} = 300$ GeV for 1994-1997 data, $\sqrt{s} = 318$ GeV for 1998-2000 data), it can be produced in a narrow resonance, with the s channel giving the dominant contribution (Fig. 9 left). For a LQ mass above the HERA centre of mass energy, both the s and u channel contribute (Fig. 9 right). In this case the reaction can be approximated by a contact interaction and the cross section becomes proportional to $(\frac{\lambda_{eq_i} \lambda_{lq_j}}{M_{LQ}^2})^2$, where λ_{eq_i} and λ_{lq_j} represent the couplings as shown in Fig. 9.

The LFV processes can also be mediated by R -parity-violating SUSY particles.

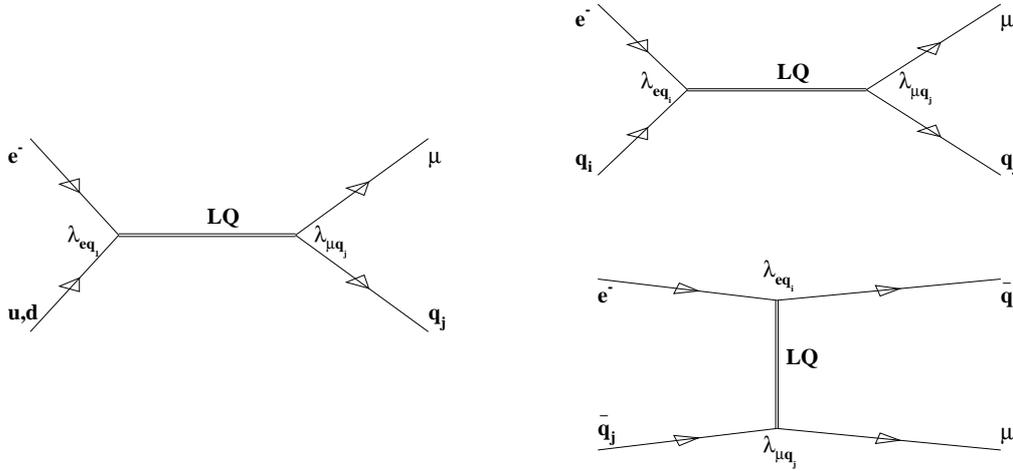


Figure 9. Example Feynman diagrams for LFV through LQs at HERA. For low mass LQs the dominant contribution is due to an s -channel resonance (left). For high mass LQs both u - and s -channels contribute (right).

Indirect searches for LFV processes [21] have yielded strong constraints for cases where light quarks are involved. However, in some cases involving heavy quarks, the sensitivity of HERA extends beyond existing low-energy limits.

The H1 experiment has searched for LFV in e^+p data from 1994-1997, corresponding to an integrated luminosity of 37 pb^{-1} [22]. The ZEUS experiment has searched for LFV of the type $e^+p \rightarrow \tau X$ in data from 1994-1997, corresponding to an integrated luminosity of 47.7 pb^{-1} and for LFV of the type $e^\pm p \rightarrow \mu X$ in the full HERA I dataset from 1994-2000, corresponding to an integrated luminosity of 130 pb^{-1} [23, 24].

2.1. Experimental signature for LFV

The experimental signature for LFV at HERA is a high transverse momentum muon or tau lepton and a jet from the struck quark. The lepton and the jet are in opposite directions in the azimuthal plane. The tau lepton further decays to an electron, a muon or hadrons and neutrino(s). Hence the signature in this channel is an electron or muon at high transverse momentum p_T^l or a narrow, pencil-like jet with low track multiplicity from the hadronic decay of the tau lepton. In all channels, the presence of a muon and/or neutrinos leads to a large value of the missing transverse momentum, p_T^{miss} , measured in the calorimeter, in the direction of the final state lepton. The background from SM processes is low and the detection efficiency is 40% to 60% in the muon channel and 25% to 30% in the tau channel, depending on the LQ mass (for $M_{LQ} \ll \sqrt{s}$) and on the generation of the initial state quark (for $M_{LQ} \ll \sqrt{s}$).

No candidate events for LFV were observed by either H1 or ZEUS. Therefore limits were set on the production of LQs that mediate LFV interactions.

2.2. Low mass LQ limits

Figure 10 shows the 95% C.L. limit on the coupling constant for a $S_{1/2}^L$ LQ decaying into τ , as obtained from the H1 analysis. The result is shown for different branching ratios β_l ($l = e, \tau$) of the LQ into e and τ . Assuming an electromagnetic coupling strength and $\beta_\tau = 0.9$, a limit of 275 GeV

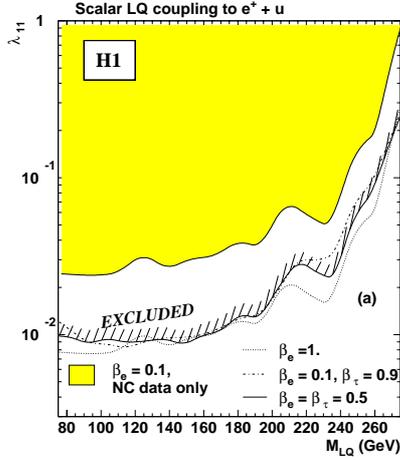


Figure 10. Result from H1 for the 95% C.L. upper limit on the electron-valence-quark coupling of the $S_{1/2}^L$ LQ. The limit is shown as a function of the LQ mass and for different branching ratios of the LQ decay into e and τ .

at 95% C.L. has been set on the LQ mass. The ZEUS collaboration obtained similar results in the τ channel.

Figure 11 shows the 95% C.L. limit on the coupling constant for a V_0^R LQ, decaying into μ , as obtained from the ZEUS analysis. The result is compared to limits from low energy experiments. The HERA limits are competitive to those obtained from rare meson decays in cases where heavy quarks are involved. Assuming an electromagnetic coupling strength and $\beta_\mu = 0.5$, LQs with masses up to 301 GeV are excluded at 95% C.L., depending on the LQ species.

2.3. High mass LQ limits

Table 2 shows the 95% C.L. limits on $(\frac{\lambda_{eq_i} \lambda_{lq_j}}{M_{LQ}^2})^2$ for the μ channel and $F = 2$, as obtained by the ZEUS collaboration. The limits improve those from rare D meson decays, when quarks from the second generation are involved. Similar results were obtained for $F = 0$ and for the tau channel.

3. Outlook

The H1 and ZEUS experiments are expecting a much higher integrated luminosity within five years of operation from the HERA II running period. This will lead to a higher sensitivity for probing coupling strengths in searches for FCNC and LFV. It will in particular help to clarify the origin of the excess of isolated lepton events at high p_T^X , which were observed by the H1 collaboration. In addition, both experiments have improved their detectors, in particular for the forward tracking. The enhanced capability for b -tagging will further improve the sensitivity for new phenomena such as anomalous FCNC and LFV.

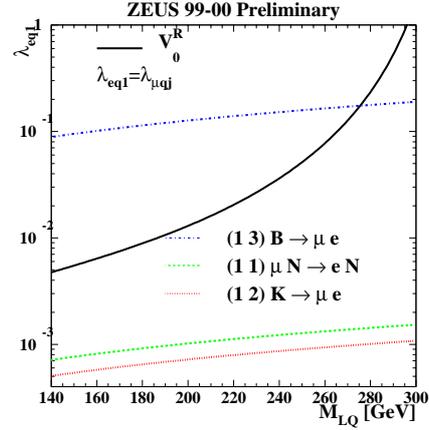


Figure 11. Result from ZEUS for the 95% C.L. upper limit on the electron-valence-quark coupling of the V_0^R LQ, decaying into μq_j (solid line), where q_j denotes a down-type quark from any generation. The limit is shown as a function of the LQ mass. The dotted lines represent the limits from low energy experiments. The second number in the parenthesis denotes the generation of q_j .

$F = 2$		Zeus Preliminary (94-00 combined limits)						$\frac{\lambda_{eq_i} \lambda_{\mu q_j}}{M_{LQ}^2}$ (TeV ⁻²)
$q_i q_j$	S_0^L $e^- u$ $e^+ \bar{u}$	S_0^R $e^- u$ $e^+ \bar{u}$	\tilde{S}_0^R $e^- d$ $e^+ \bar{d}$	S_1^L $e^-(u + \sqrt{2}d)$ $e^+(\bar{u} + \sqrt{2}\bar{d})$	$V_{1/2}^L$ $e^- d$ $e^+ \bar{d}$	$V_{1/2}^R$ $e^-(u + d)$ $e^+(\bar{u} + \bar{d})$	$\tilde{V}_{1/2}^L$ $e^- u$ $e^+ \bar{u}$	
1 1	$\mu N \rightarrow eN$ 7.6×10^{-5} 1.6	$\mu N \rightarrow eN$ 7.6×10^{-5} 1.6	$\mu N \rightarrow eN$ 7.6×10^{-5} 2.1	$\mu N \rightarrow eN$ 2.3×10^{-5} 0.9	$\mu N \rightarrow eN$ 2.6×10^{-5} 0.9	$\mu N \rightarrow eN$ 1.3×10^{-5} 0.5	$\mu N \rightarrow eN$ 2.6×10^{-5} 0.6	
1 2	$K \rightarrow \pi \nu \bar{\nu}$ 10^{-3} 2.4	$D \rightarrow \mu \bar{e}$ 4 2.4	$K \rightarrow \mu \bar{e}$ 2.7×10^{-5} 2.6	$K \rightarrow \mu \bar{e}$ 2.7×10^{-5} 1.1	$K \rightarrow \mu \bar{e}$ 1.3×10^{-5} 1.6	$K \rightarrow \mu \bar{e}$ 1.3×10^{-5} 1.2	$D \rightarrow \mu \bar{e}$ 2 1.7	
1 3	V_{ub} 0.4 *	*	$B \rightarrow \mu \bar{e}$ 0.8 2.8	V_{ub} 0.4 1.4	$B \rightarrow \mu \bar{e}$ 0.4 2.1	$B \rightarrow \mu \bar{e}$ 0.4 2.1	*	
2 1	$K \rightarrow \pi \nu \bar{\nu}$ 10^{-3} 2.1	$D \rightarrow \mu \bar{e}$ 4 2.1	$K \rightarrow \mu \bar{e}$ 2.7×10^{-5} 2.6	$K \rightarrow \mu \bar{e}$ 2.7×10^{-5} 1.1	$K \rightarrow \mu \bar{e}$ 1.3×10^{-5} 0.9	$K \rightarrow \mu \bar{e}$ 1.3×10^{-5} 0.5	$D \rightarrow \mu \bar{e}$ 2 0.6	
2 2	$\mu \rightarrow 3e$ 5×10^{-3} 5.7	$\mu \rightarrow 3e$ 5×10^{-3} 5.7	$\mu \rightarrow 3e$ 1.6×10^{-2} 3.8	$\mu \rightarrow 3e$ 1.3×10^{-2} 1.8	$\mu \rightarrow 3e$ 8×10^{-3} 1.9	$\mu \rightarrow 3e$ 3.7×10^{-3} 1.6	$\mu \rightarrow 3e$ 2.5×10^{-3} 2.9	
2 3	$B \rightarrow l \nu X$ 4 *	*	$B \rightarrow \bar{\mu} e K$ 0.6 4.3	$B \rightarrow \bar{\mu} e K$ 0.3 2.1	$B \rightarrow \bar{\mu} e K$ 0.3 2.9	$B \rightarrow \bar{\mu} e K$ 0.3 2.9	*	
3 1	V_{ub} 0.4 *	*	$B \rightarrow \mu \bar{e}$ 0.8 3.1	V_{ub} 0.4 1.5	$B \rightarrow \mu \bar{e}$ 0.4 1.0	$B \rightarrow \mu \bar{e}$ 0.4 1.0	*	
3 2	$B \rightarrow l \nu X$ 4 *	*	$B \rightarrow \bar{\mu} e K$ 0.6 5.8	$B \rightarrow \bar{\mu} e K$ 0.3 2.9	$B \rightarrow \bar{\mu} e K$ 0.3 2.2	$B \rightarrow \bar{\mu} e K$ 0.3 2.2	*	
3 3	*	*	$\mu \rightarrow 3e$ 1.6×10^{-2} 7.6	$\mu \rightarrow 3e$ 1.3×10^{-2} 3.8	$\mu \rightarrow 3e$ 8×10^{-3} 4.0	$\mu \rightarrow 3e$ 3.7×10^{-3} 4.0	*	

Table 2. Result from ZEUS for 95% C.L. upper limits on $(\frac{\lambda_{eq_i} \lambda_{\mu q_j}}{M_{LQ}^2})^2$ for $F = 2$ LQs. q_i and q_j in the first column indicate the quark generations coupling to LQ- e and LQ- μ , respectively. The low energy process, which provides the most stringent limit, and its value are given in the first and second row of each column and compared to the ZEUS limit value in the third row of each column. The ZEUS limits are enclosed in a box in cases where the ZEUS limits are lower than the ones from low energy experiments. The * indicates the cases where a top quark would have to be involved.

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