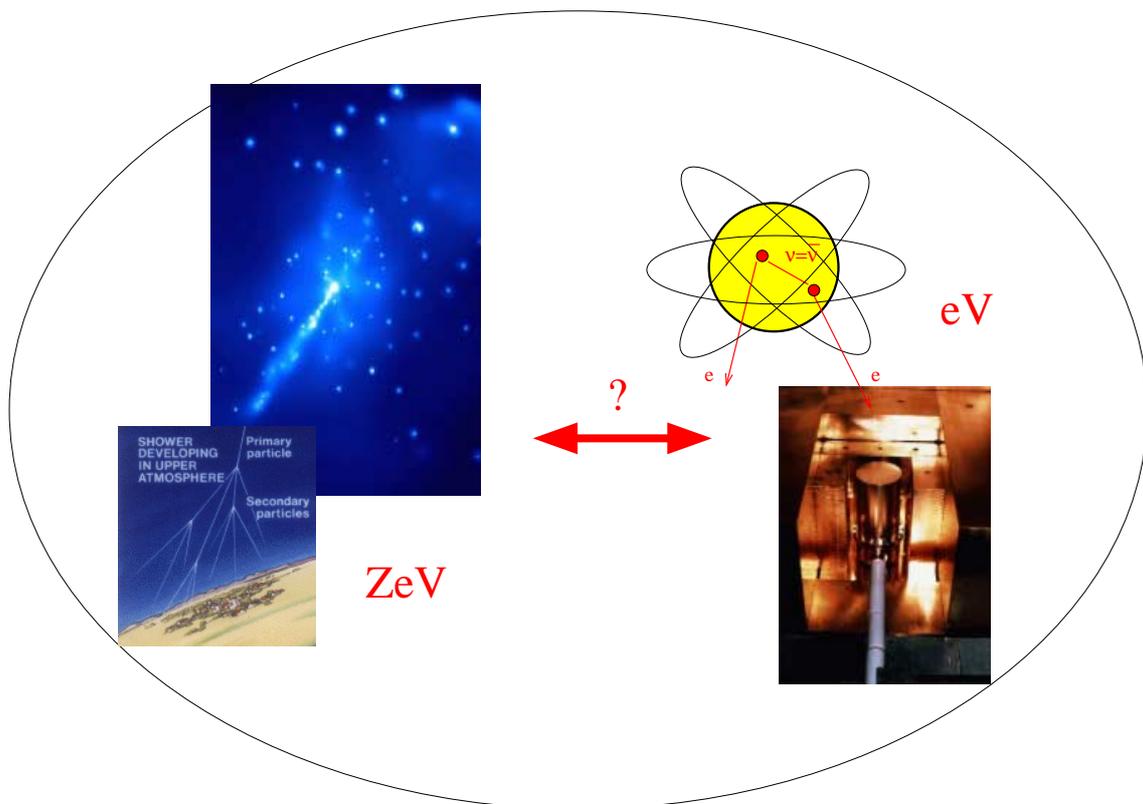
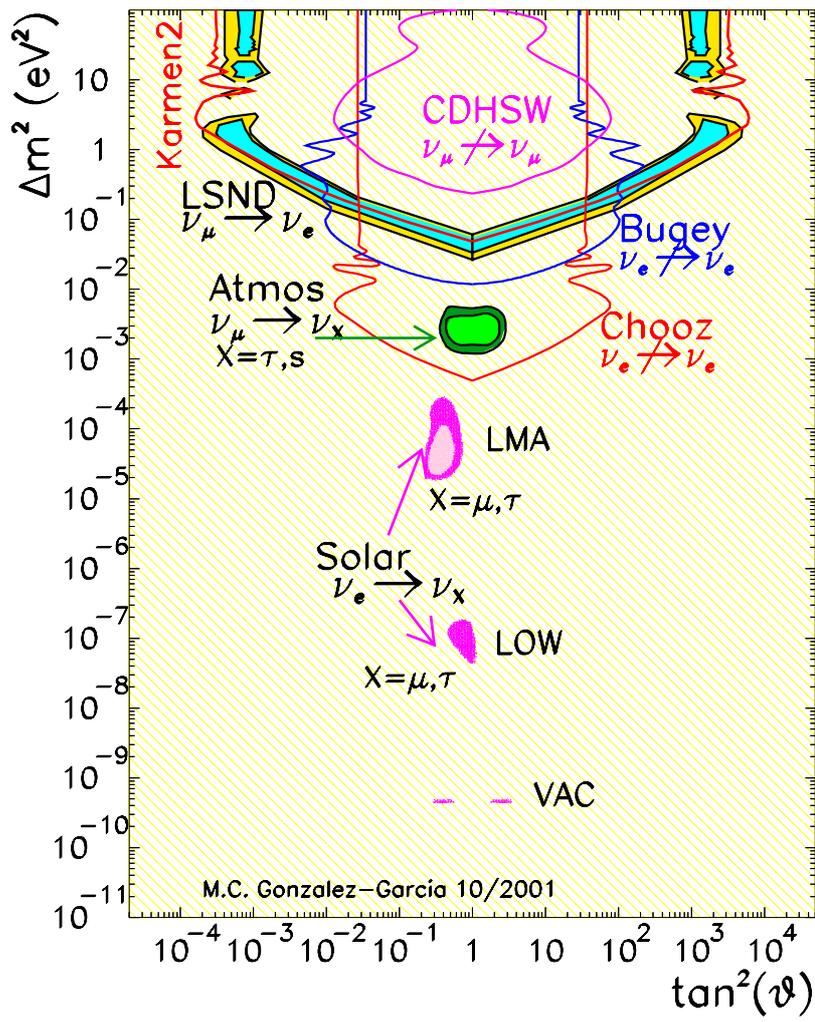




Absolute neutrino mass determination



In Collaboration with:
T.J. Weiler (Vanderbilt University)



Why to bother about absolute neutrino masses?

- SUSY See-Saw Mechanism:**

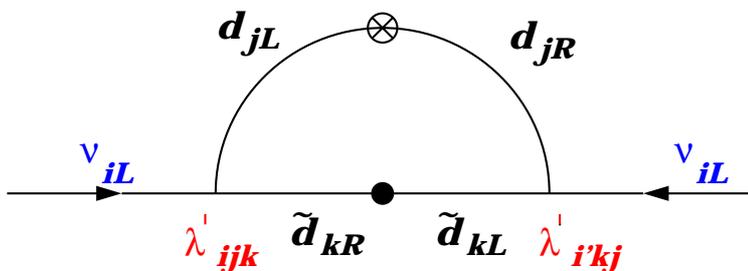
$$\mathcal{M}_\nu = \mathbf{Y}_\nu^T \mathcal{M}_\mathcal{R}^{-1} \mathbf{Y}_\nu \langle H_2^0 \rangle^2$$

LFV processes: $\Gamma \propto (\mathbf{Y}_\nu \mathbf{Y}_\nu^\dagger)^2$

⇒ with \mathcal{M}_ν one gets **information on $\mathcal{M}_\mathcal{R}$**

F. Deppisch, H. Päs, A. Redelbach, R. Rückl, Y. Shimizu, hep-ph/0206122
Talk of A. Redelbach

- Radiative Neutrino mass and \mathcal{R}_p SUSY:**



⇒ $\lambda_{ijk}^{(\prime)} \lambda_{ikj}^{(\prime)}$ products directly **constrained from $\mathcal{M}_{\nu_{ii'}}$** :

Knowing \mathcal{M}_ν improves **bounds on**

SUSY couplings by up to 5 orders of magnitude!

G. Bhattacharyya, H.V. Klapdor-Kleingrothaus, H. Päs, PLB463 (1999) 77)

Absolute neutrino mass determination

Direct measurements:

- arrival time profile of **supernova ν 's**
→ sensitivity $\lesssim 1$ eV
- **tritium decay** → sensitivity $\lesssim 2.3$ (0.3) eV
- π , τ decay → much worse
- (cosmological structure formation **CMB/LSS** → sensitivity $\lesssim 0.6 - 1.8$ eV ($\Omega_m \sim 0.3 - \text{large}$))

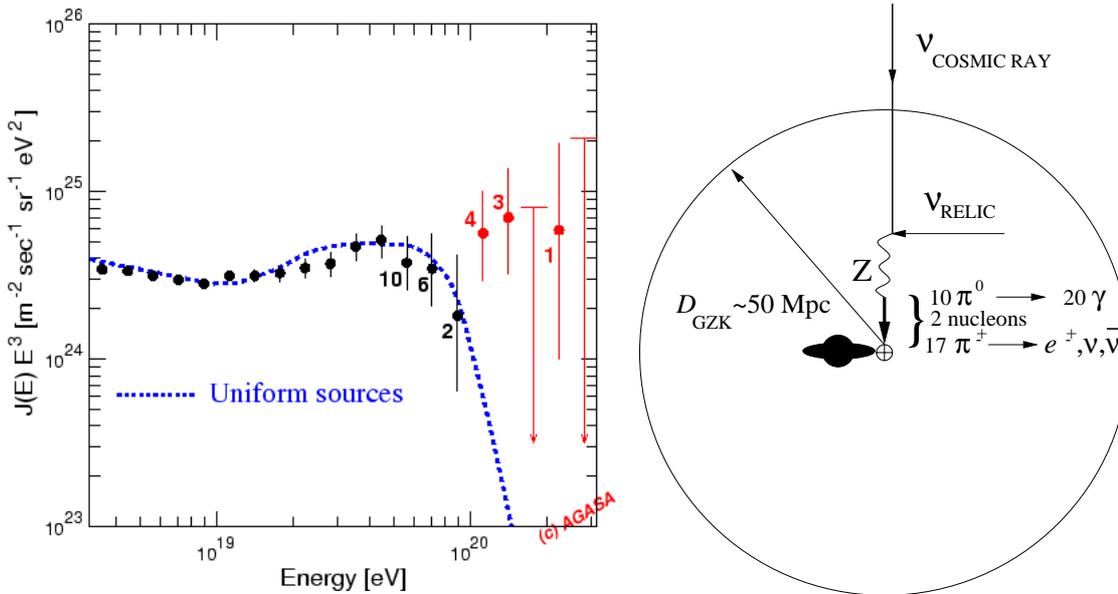
3 assumptions for indirect ν -mass determination:

- ν 's are **Majoranas** (see-saw, R_p -generated, etc.)
- only **3 ν 's** (LSND neglected)
- LMA solar solution realized

Focus:

- **Extreme energy cosmic rays in the Z-burst model**
- **$0\nu\beta\beta$ decay**
- (degenerate neutrinos)

Cosmic rays in the Z-burst model



Anomalie: Extreme energy cosmic rays above GZK cutoff (due to scattering on CMB γ 's)

Possible solution: Resonant scattering of extreme energy ν 's on relic ν background at $E_\nu^R = 2m_Z^2 / (2m_\nu)$

(T.J. Weiler, Astroparticle Physics 11 (1999) 303)

(D. Fargion, B. Mele, A. Salis, Astrophys. J. 517 (1999) 725)

$\Rightarrow m_\nu \gtrsim 0.1$ eV predicted!

\rightarrow Fit to UHECR spectrum: $m_j = 0.26$ eV

(Z. Fodor, S.D. Katz, A. Ringwald, hep-ph/0105064)

The Z-burst and neutrino masses

Necessary condition:

sufficient flux of ν 's with $E \gtrsim 10^{21}$ eV
→ challenging!

Helpful:

- Neutrino clustering in galactic vicinity
 - Large scales: universe too young
 - Galactic halo: Pauli blocking

$$\frac{n_{\nu_j}}{54 \text{ cm}^{-3}} \lesssim 10^3 \left(\frac{m_j}{\text{eV}}\right)^3 \left(\frac{\sigma}{200 \text{ km/s}}\right)^3$$

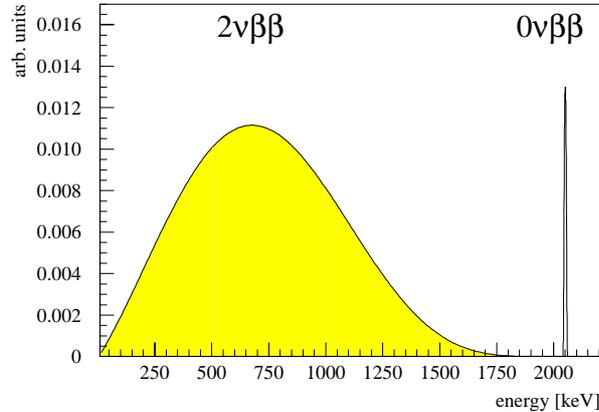
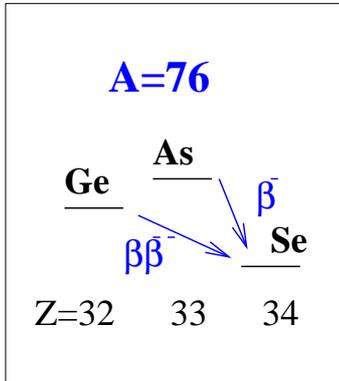
requires $m_j \gtrsim 0.5$ eV for significant increase

- Majorana neutrinos gives factor 2 in CNB
- Neutrino mass degeneracy gives factor 3

Degenerate neutrino masses

$m_j \sim 0.1 - 1 \text{ eV} \gg \sqrt{\Delta m_{\text{atm}}^2} \gg \sqrt{\Delta m_{\odot}^2}$
are back in business!

What is double beta decay?

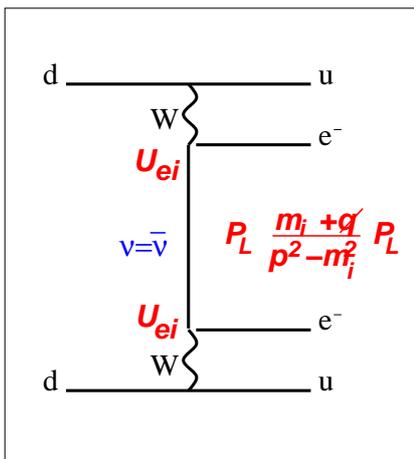


$$2\nu\beta\beta : \frac{A}{Z}X \rightarrow \frac{A}{Z+2}X + 2e^- + 2\bar{\nu}_e$$

- SM allowed: $T_{1/2}^{2\nu} \simeq 10^{19} - 10^{24} \text{y}$
- observed for 10 isotopes

$$0\nu\beta\beta : \frac{A}{Z}X \rightarrow \frac{A}{Z+2}X + 2e^-$$

- Physics beyond SM (L violation)



Sensitive on:

- effective Neutrino–Majorana mass:

$$m_{ee} = \sum_i' |U_{ei}|^2 e^{i\phi_i} m_i$$

$$m_{ee} \lesssim 0.6 \text{ eV}; \text{ Evidence } m_{ee} = 0.39 \text{ eV?}$$

(Heidelberg-Moscow-Experiment)

Future Projects: CUORE: 0.1 eV, MOON: 0.03 eV

EXO, GENIUS 1t, XMASS: 0.02 eV

GENIUS 10 t: 0.002 eV

$0\nu\beta\beta$ and ν oscillations

$0\nu\beta\beta$ observable:

$$|m_{ee}| = \left| \sum_j |U_{ej}|^2 e^{i\phi_j} m_j \right|$$

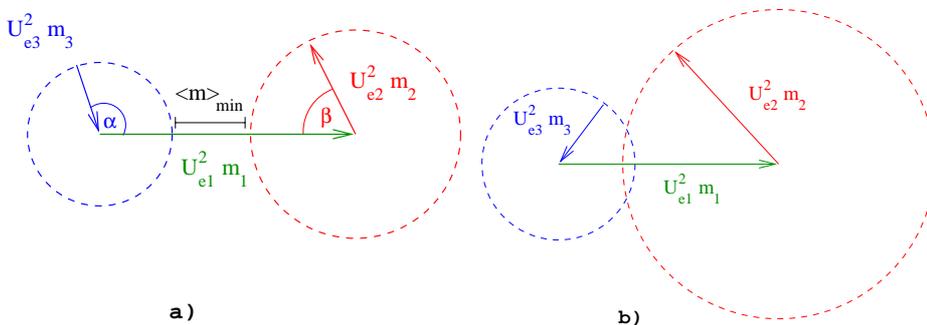
$$m_{ee} = |m_{ee}^{(1)}| + e^{i\phi_2} |m_{ee}^{(2)}| + e^{i\phi_3} |m_{ee}^{(3)}|$$

$$|m_{ee}^{(1)}| = |U_{e1}|^2 m_1$$

$$|m_{ee}^{(2)}| = |U_{e2}|^2 \sqrt{\Delta m_{21}^2 + m_1^2}$$

$$|m_{ee}^{(3)}| = |U_{e3}|^2 \sqrt{\Delta m_{31}^2 + m_1^2}$$

sum of 3 vectors in complex space:



Neutrino oscillations observables:

$$U = \begin{pmatrix} \cos \theta_{\odot} & \sin \theta_{\odot} & \epsilon \\ -\sin \theta_{\odot} / \sqrt{2} & \cos \theta_{\odot} / \sqrt{2} & 1 / \sqrt{2} \\ \sin \theta_{\odot} / \sqrt{2} & -\cos \theta_{\odot} / \sqrt{2} & 1 / \sqrt{2} \end{pmatrix}$$

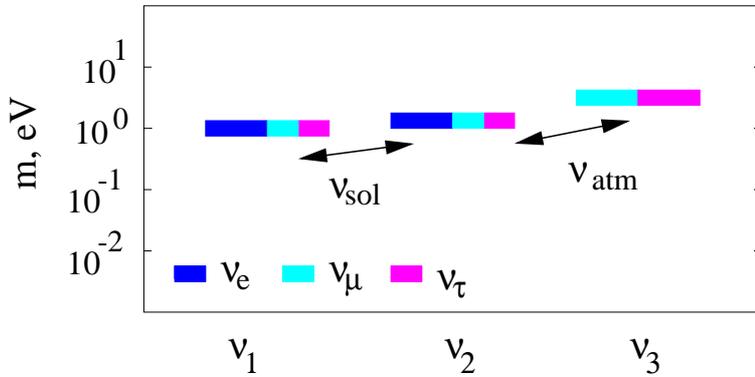
$$\Delta m_{ij}^2 \equiv |m_i|^2 - |m_j|^2, \quad \delta$$

solar neutrinos: $\Delta m_{12}^2, |U_{e1}|^2, |U_{e2}|^2$

atmospheric neutrinos: Δm_{23}^2

CHOOZ, Palo Verde: $\Delta m_{13}^2, |U_{e3}|^2 = \frac{1}{4} \sin^2(2\theta_{e\bar{e}}) < 0.025$

$0\nu\beta\beta$ in degenerate ν mass schemes

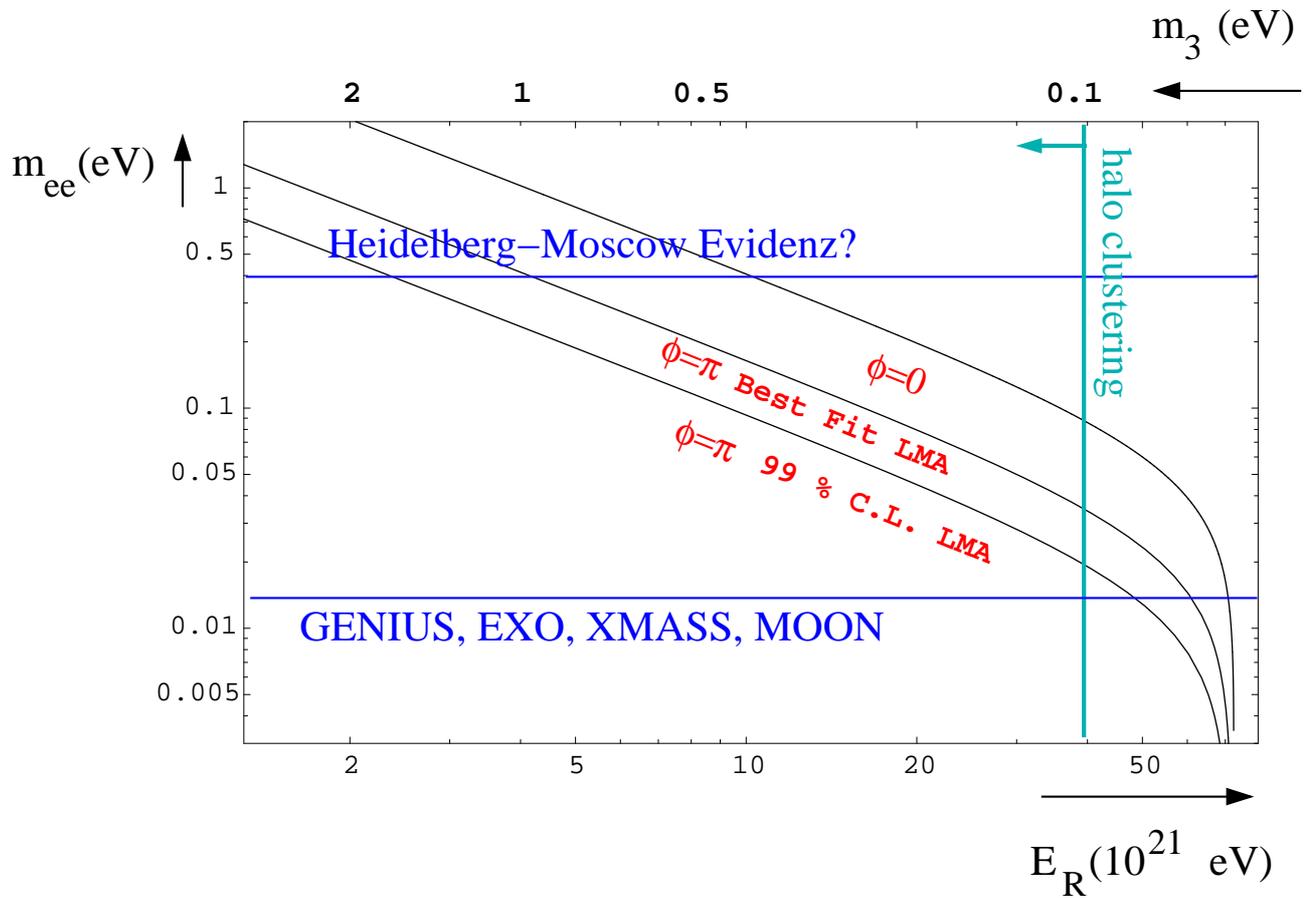


$$m_{ee}^{(1)} = \cos^2 \theta_\odot \cdot m_1$$

$$m_{ee}^{(2)} = \sin^2 \theta_\odot \cdot m_1$$

$$m_{ee}^{(3)} \lesssim 0.025 \text{ eV}$$

$$m_{ee} = (\cos(2\theta_\odot) - 1) \cdot m_1$$



Summary

Future $0\nu\beta\beta$ projects can **test all neutrino mass spectra**:

- $m_{ee} = 0.39$ eV: $m_1 = m_2 = m_3 = 0.04 - 0.4$ eV
- $m_{ee} > 0.1$ eV: Degenerate neutrinos
- $m_{ee} \simeq 0.01 - 0.1$ eV: Degenerate neutrinos, partial degeneracy or inverse hierarchy
- **So far: m_3/E_R will be known with accuracy of $(\cos 2\theta_{\text{sun}})^{-1}$, galactic halo clustering may support Z-burst.**
- **Otherwise: $m_3 \simeq \sqrt{\Delta m_{\text{atm}}^2} \sim 0.5$ eV; no halo clustering and no mass-degeneracy supports Z-burst.**
- $m_{ee} > 0.001 - 0.01$ eV: Partial degeneracy or inverse hierarchy
- $m_{ee} \lesssim 0.001$ eV: Hierarchical spectrum

(H. Päs, T.J. Weiler, PRD 63 (2001) 113015)