# Parton Shower Monte Carlos vs Resummed Calculations for Interjet Energy Flow Observables.

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Parton showers in Monte Carlo event generators reflect to a certain accuracy our understanding of QCD radiation at all orders. For interjet energy flow observables it has been known for some time that relevant all-order dynamics is substantially more complicated than that encoded via angular ordering in parton shower algorithms, even to leading logarithmic accuracy. Here we investigate the extent of the numerical mismatch between leading logarithmic analytical estimates (resummation) and parton showers in an effort to better understand the accuracy of parton showers for such observables.

#### 1 Introduction

Monte Carlo (MC) event generators are the most important tools at our disposal in the search for new physics beyond the standard model. At the large hadron collider (LHC) for example, alongside the hard process where the production of hitherto unseen particles is expected to occur, there will in general be copious amounts of initial and final state QCD radiation, conversion of partons into hadrons (hadronisation), effects due to spectator interactions, multiple hard scatterings and pile-up.

In such a complex hadronic environment as good a modeling as possible of all of the above physics aspects, is of clear benefit in order to exploit the full discovery potential of the LHC. MC tools exist and are being further developed to provide a simulation of the physics described above. However of the whole range of effects mentioned above as accompanying the hard process, the only part that we understand directly from first principles of is perturbative QCD radiation. This understanding is in principle what ought to be reflected in the parton shower algorithms in various event generators.

Another source of information on QCD at all orders is provided by analytical tools such as those employed in resummation of large logarithms in QCD. This field too has seen some interesting relatively recent developments with the observation that for a large class of observables (those measuring flow of hadronic energy into limited regions of phase space and hence called non global observables) relevant all-order dynamics is much more complicated than previously imagined [2, 3]. This more complex soft gluon dynamics is not fully described by parton showers in event generators such as HERWIG and PYTHIA. The HERWIG parton shower for example is based on angular ordering of soft gluon radiation which correctly captures the leading logarithms for several observables. However for non global observables the angular ordering approximation is not formally correct at single logarithmic accuracy, which in some important cases is also leading logarithmic accuracy. In these cases the HERWIG shower cannot be a priori expected to describe even the leading logarithmic perturbative behaviour. This is even more the case for the old PYTHIA shower (before v 6.3) where angular ordering is imposed on showers pre-ordered in invariant mass,

DIS 2007 1019

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which leads to a poor decription of soft emissions at large angles and consequently nonglobal observables in particular. This is potentially worrying since non-global observables such as interjet energy flow are commonly measured experimentally and moreover they are used to improve MC models by tuning the model parameters to data on such observables e.g. hadronic activity in *toward* or *away* regions wrt the leading jet, in hadron collisions.

Given the prevalence and importance of non-global observables in QCD studies, it is worth investigating quantitatively how good a description is provided by the different parton showers e.g. those in HERWIG and PYTHIA. This can be done by comparing the parton showers to the state-of the-art analytical resummations in an effort to see what perturbative accuracy can be relied upon in the MC descriptions in such cases.

In order to get a clearer idea about what one may expect from parton showers such as those ordered in angle we first study to what extent the leading single-logarithmic behaviour can be obtained by assuming angular ordering for energy flow into a rapidity interval between hard jets. Thus we compare the full single-logarithmic resummation (possible only in the large  $N_c$  limit) with a numerical result obtained by addressing just angular ordered configurations. We then check if our conclusions are borne out by comparing the resummation to the real HERWIG parton shower. We then compare the results to the PYTHIA event generator both with the old shower and the new shower and draw some conclusions.

## 2 Angular ordering and non global observables

The observable we shall study is the differential  $E_t$  flow,  $\frac{1}{\sigma}\frac{d\sigma}{dE_t}$  into a rapidity interval of width  $\Delta\eta$  between a pair of jets. For simplicity we shall take these to be back-to-back jets produced in  $e^+e^-$  annihilation but our conclusions generalise straightforwardly to gaps between jets in any hard process. This observable involves other than the scale  $E_t$  an additional scale Q, the hard scale for the process. Typically  $E_t \ll Q$  and one then has to deal with logarithms  $\alpha_s^n \ln^m Q/E_t$ , with  $m \leq n$ . We note that the leading logarithms in this case are single logarithms i.e those with m=n.

The resummation of the leading logarithms has been possible only in the large  $N_c$  limit [2, 3]. In this limit the complex colour algebra involved in the soft large-angle multi-gluon emission probabilities is greatly simplified and can be encoded in a dipole evolution Monte-Carlo algorithm, since the emitting ensemble reduces to a system of dipoles. Considering a dipole configuration C we can write the probability of emitting a soft gluon at scale  $L' = \ln Q/\omega'$ , where  $\omega'$  is the gluon energy, as:

$$P_C'(L') = \alpha_s(L')\Delta_C(L', L)F_C(\theta'\phi')P_C(L), \tag{1}$$

where C' is the new configuration of dipoles after the emission of the gluon,  $\Delta(L', L)$  is the no-emission probability between scales L and L' and  $F_c(\theta', \phi')$  is the angular part of the dipole real emission probability. Thus explicitly we have

$$F_C(\theta_k, \phi_k) = \sum_{\text{dipoles-ij}} \frac{2C_A (1 - \cos \theta_{ij})}{(1 - \cos \theta_{ik} (1 - \cos \theta_{jk}))}$$
(2)

Then the result that contains the resummation of the leading single-logarithms is a form factor,  $\Sigma$ , which can be written

$$\Sigma(\alpha_s L) = \sum_{C \mid \Omega_{empty}} P_c(L), L = \ln Q / E_t.$$
 (3)

1020 DIS 2007

In other words the resummed result for the probability that the transverse energy in the gap is less than some value  $E_t$  is obtained by summing over all dipole configurations such that the gap region  $\Omega$  is free from emissions above that scale. In order to study the impact of angular ordering we replace F by an angular ordered (AO) approximation <sup>a</sup>:

$$F(\theta_k, \phi_k) \to \frac{(\cos \theta_{ik} - \cos \theta_{ij})}{(1 - \cos \theta_{ik})} + \frac{(\cos \theta_{jk} - \cos \theta_{ij})}{(1 - \cos \theta_{jk})} \tag{4}$$

such that the emission k is produced in cones around the hard legs i and j with angular size set by the opening angle of dipole ij. This angular ordering is expected to correspond to the piece included in e.g. the HERWIG shower.

In Fig. 1,we plot the resummed integrated  $E_t$  cross-section (equivalently the form factor  $\Sigma$ ) as a function of  $t \sim \frac{\alpha_s}{2\pi} \ln \frac{Q}{E_t}$  in both the AO approximation as well as the resummation in the large  $N_c$  limit, for  $\Delta \eta = 1.0$ . We note that angular ordering has only a modest effect and the results at say t=0.15 corresponding to  $Q=100~{\rm GeV}$   $E_t=1~{\rm GeV}$  differ by just 10 %. Also shown there ('primary' curve) is the resummation in the independent emission approximation assuming soft gluons to be emitted by just the hard partons with no correlated gluon emission other than effects included in the running coupling. The angular ordered and

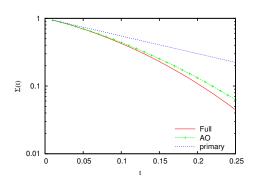


Figure 1:

full results differ substantially from this stronger assumption.

### 3 Comparison to HERWIG and PYTHIA

We now proceed to compare to actual parton showers in HERWIG and PYTHIA. Since we are interested in the dependence on the logarithmic variable t we can in fact go to very large Q values, which helps us to kill potentially spurious subleading terms of relative order  $\alpha_s(Q)$  that would be present in the MC showers. Once we draw conclusions for a given value of t, we can apply those observations to an appropriate  $E_t$  value for any Q. Given that angular ordering produces results that are in reasonable agreement with resummation we can a priori expect the HERWIG shower to also not differ substantially. This is in fact the case

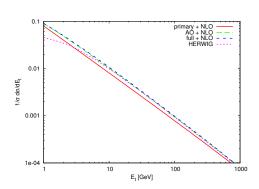


Figure 2:

DIS 2007 1021

<sup>&</sup>lt;sup>a</sup>This replacement would be exactly correct for global observables where one could freely integrate over azimuthal angles.

as can be seen from Fig. 2 where once again for t=0.15 we note just a 10 % difference between HERWIG and resummation.

For the old PYTHIA shower where angular ordering is imposed on top of ordering in invariant mass the results are significantly different. Here one notes from Fig. 3 a discrepancy of 50 % for t=0.15 which may be misattributed to other (nonperturbative) physics during the procedure of tuning PYTHIA to data. Bearing in mind that the non global logarithmic effects are not universal and are absent for other (global) observables this is a potentially dangerous and inaccurate way to account for them.

For the new PYTHIA shower which implements angular ordering of soft radiation

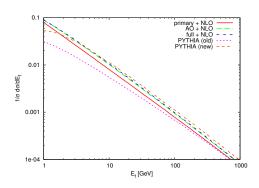


Figure 3:

via a dipole type phase-space the results show a marked improvement and a difference of only 7.5 % is seen at t=0.15. However as we increase the width of the rapidity slice in question the description from the new PYTHIA shower deteriorates and we observed that for  $\Delta \eta = 3.0$  the new shower performs poorly when compared to resummation and HERWIG results.

#### 4 Conclusions

We can conclude from our studies that while angular ordering as implemented in QCD parton showers does not formally give the correct single logarithmic behaviour for non-global observables, numerically one does not have to worry too much about the difference between angular ordered and resummed results even in this case. However ordering in other variables such as invariant mass and angle (PYTHIA old) gives rise to a poor perturbative description. This incorrect perturbative estimate may be adjusted for in other non-perturbative aspects of the MC model but this is not optimally accurate. It is imperative in our opinion, especially for observables related to energy flow between hard jets, to compare the results from HERWIG and PYTHIA both at the parton and hadron level. If large discrepancies are observed at parton level information from analytical resummed calculations where available could be exploited to better understand the uncertainty and limitations of the MC descriptions. We also observed that the new PYTHIA shower is substantially better than its earlier counterpart but noted a puzzling discrepancy at large values of the interjet rapidity interval  $\Delta \eta$ , which we hope can be clarified in the near future.

#### References

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1022 DIS 2007