

# Final Results on the Measurement of the Structure Functions $g_1^p$ and $g_1^d$ at HERMES

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Final results on precise measurements of the spin structure functions of the proton  $g_1^p(x, Q^2)$  and deuteron  $g_1^d(x, Q^2)$  are presented over the kinematic range  $0.0041 \leq x \leq 0.9$  and  $0.18 \text{ GeV}^2 \leq Q^2 \leq 20 \text{ GeV}^2$ . The data were collected at the HERMES experiment at DESY, in deep-inelastic scattering of 27.6 GeV longitudinally polarized positrons off longitudinally polarized hydrogen and deuterium gas targets internal to the HERA storage ring.

## 1 Introduction

The structure functions  $g_1^{p,d}$  can be extracted from the measurement of double-spin asymmetries  $A_{||}^{p,d}$  of cross sections in inclusive deep-inelastic scattering  $\ell + N \rightarrow \ell + X$  of longitudinally polarized charged leptons off longitudinally polarized protons and deuterons:

$$g_1^{p,d}(x, Q^2) = \frac{1}{1 - \frac{y}{2} - \frac{y^2}{4}\gamma^2} \left[ \frac{Q^4}{8\pi\alpha^2 y} \frac{\partial^2 \sigma_{UU}^{p,d}(x, Q^2)}{\partial x \partial Q^2} A_{||}^{p,d}(x, Q^2) + \frac{y}{2} \gamma^2 g_2^{p,d}(x, Q^2) \right], \quad (1)$$

when a model is used for the unpolarized cross section  $\partial^2 \sigma_{UU}^{p,d}(x, Q^2)/\partial x \partial Q^2$  and the structure function  $g_2^{p,d}$ . In Eq. (1)  $x$  is the fraction of the nucleon's light-cone momentum carried by the struck quark,  $-Q^2$  is the squared four-momentum transferred by the virtual photon, and  $y$  and  $\gamma$  are kinematic factors.

At any order in  $\alpha_s(Q^2)$  and in a leading-twist approximation, the proton and neutron structure functions  $g_1^{p,n}$  are a convolution of singlet ( $\Delta\Sigma(x, Q^2)$ ), non-singlet ( $\Delta q_{NS}^{p,n}(x, Q^2)$ ) and gluon helicity distributions ( $\Delta g(x, Q^2)$ ) [2] with the corresponding Wilson coefficient functions  $\Delta C(x, \alpha_s(Q^2))$  [3]:

$$g_1^{p,n}(x, Q^2) = \frac{1}{2} \langle e^2 \rangle [\Delta C_\Sigma \otimes \Delta\Sigma + 2N_q \Delta C_g \otimes \Delta g + \Delta C_{NS}^{p,n} \otimes \Delta q_{NS}^{p,n}]. \quad (2)$$

The deuteron structure function  $g_1^d$  is related to  $g_1^p$  and  $g_1^n$  by the relation:

$$g_1^d = \frac{1}{2} (g_1^p + g_1^n) \left( 1 - \frac{3}{2} \omega_D \right), \quad (3)$$

where  $\omega_D = 0.05 \pm 0.01$  takes into account the D-state admixture to the deuteron wave function. The last expression allows for the extraction of the neutron structure function  $g_1^n$  from the combined measurements of  $g_1^p$  and  $g_1^d$  at the same values of  $x$  and  $Q^2$ .

These proceedings report on the final results on the HERMES measurement of the structure functions  $g_1^p$  and  $g_1^d$ , with the consequent extraction of  $g_1^n$ . Details can be found in Ref. [4].



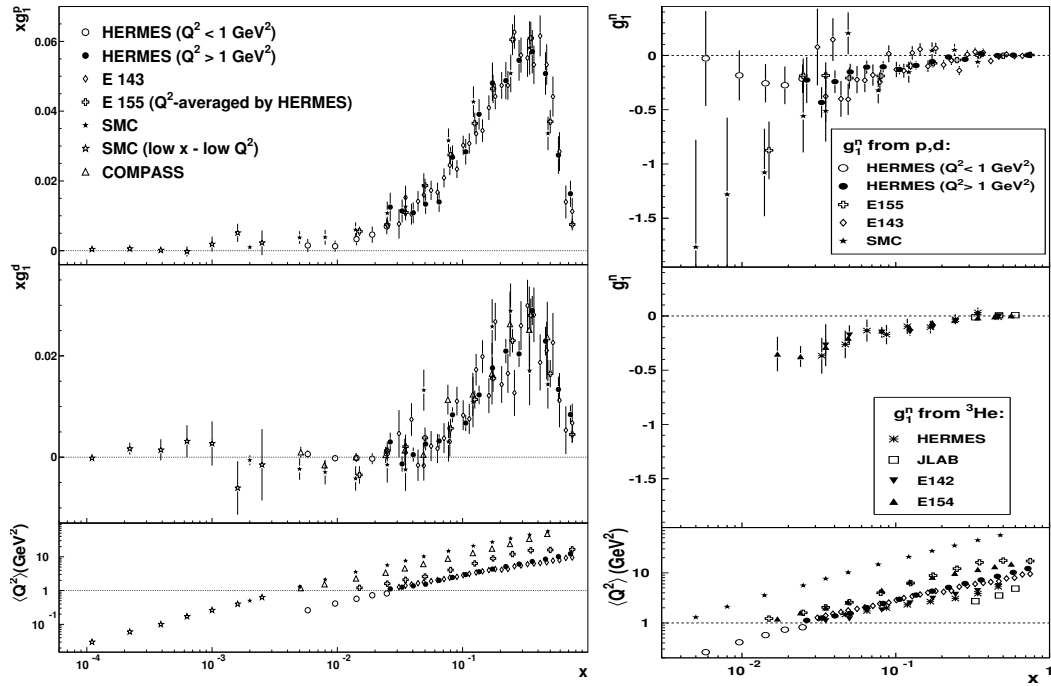


Figure 1: Left panel: HERMES results on  $xg_1^p$  and  $xg_1^d$  vs  $x$ , shown on separate panels, compared to data from SMC [11], E143 [12], E155 [13], and COMPASS [14]. The HERMES data points are statistically correlated by unfolding QED radiative and detector smearing effects. Right panel, top plot: the structure function  $g_1^n$  obtained from  $g_1^p$  and  $g_1^d$ , compared with similar data from SMC [11], E143 [12], and E155 [13] in the HERMES  $x$ -range. Right panel, second plot from the top:  $g_1^n$  as obtained from an  $^3\text{He}$  target [21]. The bottom panels show the  $\langle Q^2 \rangle$  of each data point in the top two panels. In all plots the error bars represent total uncertainties.

computed from a parameterization of all available proton and deuteron data [15, 16, 17, 18, 19]. The values of  $g_1$  at the average  $Q^2$  in each  $x$  bin were obtained from the evolution of the  $g_1$  values in each  $Q^2$  bin to the average  $Q^2$  in each  $x$  bin by using an NLO QCD fit to all available  $g_1$  data based on the 'BB' code [20]. The systematic uncertainties originate from the experiment (beam and target polarizations, particle identification, misalignment of the detector) and the parameterizations ( $g_2$ ,  $F_2$ ,  $R$ ,  $A_{zz}^d$ ,  $\omega_D$ ), with the largest contributions coming from the beam and target polarization uncertainties.

The results are shown in Fig.1 (left), in comparison with those from other experiments. In the case of the proton, the central values of the SMC data points are larger than those of HERMES, in the low- $x$  region. This reflects the difference in  $\langle Q^2 \rangle$  values between the two experiments, and is expected from the  $Q^2$  evolution of  $g_1$ . In the case of the deuteron, the HERMES data are compatible with zero for  $x < 0.04$ . In this region the SMC data favor negative values for  $g_1^d$  while the COMPASS results [14], at a similar  $Q^2$  of SMC, are also consistent with zero.

The neutron structure function  $g_1^n$  was extracted from  $g_1^p$  and  $g_1^d$  using Eq. (3) and is

shown in the right panel of Fig. 1. Compared to previous data,  $g_1^n(x)$  is now very well restricted by the HERMES measurement. The structure function  $g_1^n$  is slightly positive in the very high  $x$  region, and negative everywhere else. The new results suggest that  $g_1^n$  gradually approaches zero from below and, while it is based on data with  $Q^2 \leq 1 \text{ GeV}^2$ , it does not support the earlier conjecture of a strong decrease of  $g_1^n(x)$  for  $x \rightarrow 0$  based on the E154 and SMC data.

The first moments of  $g_1$  provide important information on the spin structure of the nucleon, in particular when results on proton, deuteron and neutron are combined. The precision of the integrals is less affected by the unfolding procedure since all inter-bin correlations from the unfolding procedure are taken into account. For  $x < 0.04$ ,  $g_1^d(x)$  becomes compatible with zero and its measured integral shows saturation. Under this assumption, and assuming of the validity of SU(3) flavor symmetry in hyperon  $\beta$ -decays, the values  $\Delta s + \Delta \bar{s} = -0.085 \pm 0.013(\text{theo.}) \pm 0.008(\text{exp.}) \pm 0.009(\text{evol.})$  (negative and different from zero by about  $4.7 \sigma$ ),  $\Delta u + \Delta \bar{u} = 0.842 \pm 0.004(\text{theo.}) \pm 0.008(\text{exp.}) \pm 0.009(\text{evol.})$  and  $\Delta d + \Delta \bar{d} = -0.427 \pm 0.004(\text{theo.}) \pm 0.008(\text{exp.}) \pm 0.009(\text{evol.})$  are obtained for the quark distributions, using HERMES deuteron data alone, in the  $\overline{MS}$  scheme at order  $\mathcal{O}(\alpha_s^2)$ , at  $Q^2 = 5 \text{ GeV}^2$ . Additionally, the total quark contribution to the nucleon's spin is obtained as  $\Delta\Sigma = 0.330 \pm 0.011(\text{theo.}) \pm 0.025(\text{exp.}) \pm 0.028(\text{evol.})$ . This result suggests that the nucleon helicity gets a substantial contribution from quark helicities, even though there is still need for contributions from gluon helicities and angular momentum.

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