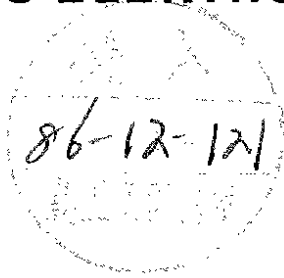


DEUTSCHES ELEKTRONEN-SYNCHROTRON **DESY**

DESY 86-118
September 1986



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ISSN 0418-9833

NOTKESTRASSE 85 · 2 HAMBURG 52

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THE F_2 PHOTON STRUCTURE FUNCTION AND Λ_{QCD}

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(Presented by J.H. Field)

The real photon structure function F_2^Y is discussed in the QPM and QCD taking into account the signature of hadronic or point-like parts provided by the final state jet structure. A re-derivation of Witten's result for the non singlet part of F_2^Y indicates that hadronic and point-like terms have been mis-identified in recent calculations that have been widely compared to experiment, leading to overly optimistic estimations of the sensitivity of F_2^Y to Λ_{QCD} .

1. INTRODUCTION

For several years now there has been a controversy over whether measurements of F_2^Y for almost real photons can/cannot precisely determine Λ_{QCD} . It was stated many years ago /1,2/ that modifications to the Quark Parton Model (QPM) predictions /3/ are expected to be small at experimentally accessible Q^2 values and that unavoidable non-perturbative effects would largely obscure sensitivity to Λ . More recently this conclusion has been re-stated by other authors /4,5/ who stressed the importance of retaining non leading-log terms in the LO /6/ and HO /7/ QCD solutions at non-asymptotic Q^2 values.

This point of view has not however gained universal acceptance /8/ and in particular it has been claimed /9-12/ that except for very small x -values (≈ 0.15) F_2^Y is indeed $\approx \ln(\frac{Q^2}{\Lambda^2})$ even for Q^2 as low as 5 (GeV/c)², so that existing F_2^Y measurements /13/ can determine Λ with good precision /14/.

In recent work /15,16/ we have found that the resolution of the controversy rests on a correct definition, in QCD, of the 'hadronic' (HAD) and 'point-like' (PL) parts of F_2^Y . For clarity we first discuss F_2^{HAD} and F_2^{PL} in the QPM.

2. F_2 IN THE QUARK PARTON MODEL

The transverse momentum of final state particles or jets relative to the z -axis gives a signature of

F_2^{HAD} and F_2^{PL} /17/.

F_2^{HAD} is characterised by a steep exponential distribution ($\approx \exp(-6 p_T)$ for light hadrons) whereas F_2^{PL} gives a flatter (p_T^{-4}) power law behaviour. These two components in the p_T distribution have now been seen in many different experiments /13/. F_2^{HAD} and F_2^{PL} can then be separated, in an approximate way, by a cut (p_T^0) in the parton (or jet) p_T :

$$F_2 = \int_0^{p_T^0} dF_2^{HAD} + \int_{p_T^0}^w \frac{w}{p_T^4} dF_2^{PL} \quad (1)$$

Such a description gives a good fit to the PLUTO measurement of F_2^Y /18/ with $\langle Q^2 \rangle = 5.3$ (GeV/c)². Using $p_T^0 = 1$ GeV/c for $w > 6$ GeV/c² and $p_T^0 \propto w$ for $w < 6$ GeV/c² gives the solid line in Fig. 1. Setting $p_T = 0$,

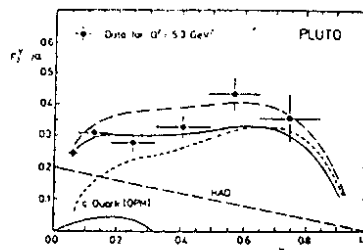


Fig. 1: Comparison of QPM predictions with PLUTO data for F_2^Y [see text for curve definitions]

$m_u = m_d = 300$, $m_s = 500$, $m_c = 1700$ MeV/c² (Fig. 1 broad dashed line) overestimates the data near $x = 0.3$ (F_2^{HAD} is 'double counted'), while neglecting $F_2^{\text{HAD}} = 0.2\alpha(1-x)$ (Fig. 1 fine dashed line) under the same conditions fails to fit the data at small x values (F_2^{HAD} must be included).

In /15/ the $O(\alpha_s)$ QCD correction for $\langle Q^2 \rangle = 5.3$ (GeV/c)² is found to be small, so the fit given by the solid line in Fig. 1 is little changed by this correction. The choice $p_T^0 = 1$ GeV/c agrees well with the exponential-power law transition region observed in the final state jet structure /13/.

3. QCD CORRECTIONS TO F_2

The LO QCD solution for F_2 factorises:

$$F_2 = \left[P_{qY}^{\text{HAD}} + P_{qY}^{\text{PL}} \right] \sigma(\gamma^*q+X) \quad (2)$$

$P_{qY}^{\text{HAD,PL}}$ are photon+quark splitting functions and $\sigma(\gamma^*q+X)$ is the cross section for the probe photon and a virtual quark from the target photon to scatter into the state X :

$$\sigma(\gamma^*q+X) = \sigma(\gamma^*q+q) + \sigma(\gamma^*q+gq) + \dots \quad (3)$$

The first term on the RHS of (3) gives the QPM prediction, the other terms QCD corrections.

In terms of quark densities q, \bar{q} :

$$F_2 = \sum_q e_q^2 x [q + \bar{q}] \quad (4)$$

the non-singlet (NS) contribution to F_2 where N real gluons are radiated comes from $q_N^{\text{HAD,NS}} + q_N^{\text{PL,NS}}$ where:

$$q_N^{\text{HAD,NS}} = \int_{y_2}^1 q(t_0, y_1) \frac{dy_1}{y_1} C_N^{\text{NS}} \quad (5a)$$

$$q_N^{\text{PL,NS}} = \frac{3\alpha e_q^2}{2\pi} \int_{y_2}^1 [y_1^2 + (1-y_1)^2] \frac{dy_1}{y_1}$$

$$\int_{t_0}^{t_1^{\text{MAX}}} \frac{dt_1}{t_1} C_N^{\text{NS}} \quad (5b)$$

The convolution integral C_N^{NS} and all variable definitions are given in Ref. /15,16/.

t_0 is related to the (space-like) virtuality of the off-shell quark at the target photon vertex at the boundary of hadronic and point-like phase space:

$$t_0 = y_1 p^2 + [m_q^2 + (p_T^0)^2] / (1-y_1)$$

If $p^2/19/$ or $m_q/1/$ are large F_2^{HAD} vanishes, but t_0^q still defines the lower limit of the (now purely point-like) phase space. In this case $p_T^0 = 0$. Eqn (5) refers to light quarks ($m_q \ll p_T^0$) and a real photon target ($p^2=0$).

The LO solution is derived from (4) by performing the t integrals in ordered phase-space ($t_i < t_{i+1}$), and taking moments:

$$f(n) = \int_0^1 f(x) x^{n-1} dx$$

to decouple the convolution integral in the energy fraction variables y_1 /16/:

$$q_N^{\text{HAD,NS}}(Q^2, n) = q_N^{\text{HAD,NS}}(t_0, n) \frac{[-B \ln R]^N}{N!} \quad (6a)$$

$$q_N^{\text{PL,NS}}(Q^2, n) = a(n) B^N \left\{ \ln \left(\frac{Q^2}{t_0} \right) - \ln \left(\frac{t_0}{\Lambda^2} \right) \sum_{M=1}^N \frac{(\ln R)^M}{M!} \right\} \quad (6b)$$

where:

$$R = \ln(t_0/\Lambda^2) / \ln(Q^2/\Lambda^2) =$$

$$B = d_{\text{NS}}^n < 0 \quad \alpha_s(Q^2) / \alpha_s(t_0),$$

d_{NS}^n are proportional to the non singlet elements of the anomalous dimension matrix.

(6b) implies that the leading log term at any order in α_s is independent of Λ /15/.

The complete LO, NS solution /6/ is given by summing (5) from $N = 0$ to infinity:

$$q_N^{\text{HAD,NS}}(Q^2, n) = q_N^{\text{HAD,NS}}(t_0, n) (R)^{-d_{\text{NS}}^n} \quad (7a)$$

$$q_N^{\text{PL,NS}}(Q^2, n) = \frac{a(n)}{1-d_{\text{NS}}^n} \ln \left(\frac{Q^2}{\Lambda^2} \right) \left[1 - R^{1-d_{\text{NS}}^n} \right] \quad (7b)$$

The leading log term in the complete solution, as is well known, depends on Λ . It is the sum of two terms,

$a(n) \ln \left(\frac{Q^2}{t_0} \right) / (1-d_{\text{NS}}^n)$ coming from the sum of the leading log terms at each

order in α_s , and $a(n) \ln \left(\frac{t_0}{\Lambda^2} \right) / (1-d_{\text{NS}}^n)$ coming from the sum of loglog terms.

The non leading-log (NLL) point-like terms (proportional to $R^{1-d_{\text{NS}}^n}$ in (7b))

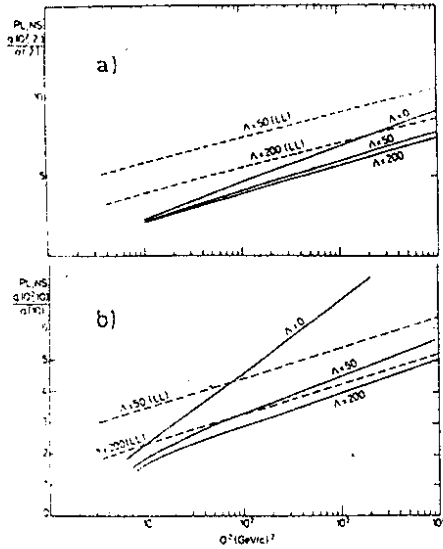


Fig. 2: Non singlet moments
a) $n=2$, b) $n=10$
Solid line LO solution,
dashed line LL term only

are never negligible for any value of Q^2 or n . This is illustrated in Fig. 2a,b where $q(Q^2, n)/a(n)$ for $n = 2, 10$ (with $t_0 = 1 \text{ (GeV/c)}^2$ and $\Lambda = 0, 50, 200 \text{ MeV/c}$) is compared (as a function of Q^2) with the leading log (LL) solution given by setting $R = 0$ in (7). The much reduced sensitivity to Λ of the full solution (7) as compared to the LL solution is evident.

In Fig. 3a,b $q(Q^2, n)/a(n)$ for $n = 2, 10$ (with $t_0 = 1 \text{ (GeV/c)}^2$ and $\Lambda = 100 \text{ MeV/c}$) is compared with solutions given by truncating the perturbation series in (6b) at $N = 1$ (fine dashed line) and $N = 2$ (broad dashed line). The $O(\alpha_s)$ solution is seen to give a good approximation to the all orders solution for $Q^2 \leq 100 \text{ (GeV/c)}^2$.

The LO singlet contributions to F_2 have the same form as (7) with different anomalous dimension parameters (d^n , d_n^n) and $a(n)$ coefficients. Here also the NLL terms are large for all experimentally relevant Q^2 values and all n .

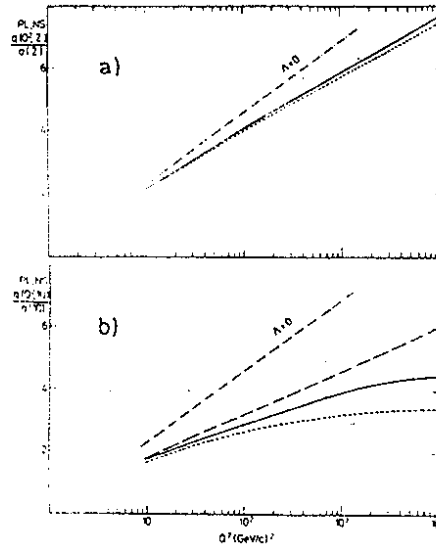


Fig. 3: Non singlet moments with $\Lambda = 100 \text{ MeV/c}$
a) $n=2$, b) $n=10$
Solid line all orders.
Fine, broad dashed lines $O(\alpha_s), O(\alpha_s^2)$ solutions

4. COMPARISON WITH THE SCHEME OF ANTONIADIS, GRUNBERG AND MARLEAU

The solution (7) can be re-written as:

$$q^{NS} = q^{HAD, NS} + q^{PL, NS} = A(t_0, n) (R)^{-d_{NS}^n} + \frac{a(n)}{1-d_{NS}^n} \ln\left(\frac{Q^2}{\Lambda^2}\right) \quad (8)$$

where:

$$A(t_0, n) = q(t_0, n) + \frac{a(n)}{1-d_{NS}^n} \ln\left(\frac{t_0}{\Lambda^2}\right) \quad (9)$$

Comparing the first term on the RHS of (8) with (7a) it can be seen that $A(t_0, n)$ has the same Q^2 evolution as the hadronic part of F_2 . This led Antoniadis, Grunberg and Marleau /9-12/, following Bardeen /22/, to identify $A(t_0, n)$ with q^{HAD} and to assume that the point-like contribution is given solely by the LL term in (8).

However, as is clear from our derivation of (7) $A(t_0, n)$ contains both hadronic and point-like parts. The second term on the RHS of (9) is purely point-like, coming from the region of phase space where $t_1 > t_0$.

As already pointed out by Glück and Reya /4/ the much discussed /9-12, 20-22/ problem of singularities related to the zeros of $1-d^n$ in the LO solution and of d_i^n in the HO solution for certain n values ($i=NS,+,-$) goes away when the numerically important (see Fig. 2) NLL terms are retained in both the LO and HO solutions.

Our analysis shows that the hadronic (7a) and point-like (7b) terms are separately singularity free, the NLL terms coming entirely from the point-like phase space region $t_1 > t_0$.

Many published QCD analyses based on Ref. /9,10/ have given plausible /14/ but actually incorrect 'measurements' of A . In these analyses the NLL point-like terms are set to zero except for values of n where a singularity occurs in the LL term or the HO correction terms, in which case arbitrary parameters are introduced by hand to 'regularise' these singularities. Such a procedure has no physical justification, and the additional parameters are quite unrelated to F_2^{HAD} , which has now been directly measured at low Q^2 /13/.

An $O(\alpha_s^2)$ calculation of the QCD correction to the QPM, assuming factorisation, but using exact kinematics in the final state phase space integrations is given in Ref. /15/. The QCD correction is found to be less sensitive to A than to the poorly known phenomenological cut-off p_T^2 .

Further progress in the comparison of theory and experiment for F_2^Y can perhaps be achieved by exact Feynman diagram calculations at $O(\alpha_s^2)$ or $O(\alpha_s^3)$, since the LO QCD solution suggests small corrections at $O(\alpha_s^2)$ and higher (Fig. 3) where in any case confinement effects limit the validity of perturbative calculations. In this way tests of the many approximations /16/ which underlie the derivation of the existing LO, HO calculations can be done allowing more quantitative comparisons of theory and experiment for F_2^Y .

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