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**Strategies for Directly Observing Particle-Antiparticle Oscillations in the  $B^0$ - $\bar{B}^0$  System\***

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**ABSTRACT**

Time dependent methods for determining the mixing parameter  $x_s$  in the  $B_s$  system are of special interest, particularly for as large values of  $x_s$  as expected in the standard model. Here we concentrate on the situation just above the threshold for  $B_s^* \bar{B}_s^*$  production at an asymmetric  $e^+e^-$  collider. Two methods are considered: the same sign dilepton distribution without any further tag, and the case where one tags on  $D_s$  mesons in addition in order to reduce the background. It turns out that an accuracy of 10% in the quantity  $\Delta|t_1 - t_2|/\tau$  is of crucial importance in both cases. With a number of about  $5 \times 10^6$   $b\bar{b}$  quark pairs such measurements could be sensitive to values of  $x_s$  up to 15.

\* invited talk given at the 24th Recontres de Moriond

**1. Introduction**

In the standard model of electroweak interactions the entries of the fermion mass matrix are free parameters. In order to find the deeper origin of these parameters, it is obviously very important to restrict their allowed ranges by experiment as tightly as possible. The recent observation of  $B_d^0$ - $\bar{B}_d^0$  mixing by ARGUS [1] and CLEO [2] has far reaching consequences in this respect. In the three family standard model, its unexpectedly large magnitude implies, for example, an increased lower bound on the top quark mass [3] and, at the same time leads to improved bounds on the Cabibbo-Kobayashi-Maskawa (CKM) matrix elements [4].

Let us recall some basic facts: It is convenient to parametrize the CKM matrix according to Maiani and Wolfenstein [5],

$$V = \begin{pmatrix} 1 - \frac{1}{2}\lambda^2 & \lambda & A\rho\lambda^3 e^{-i\delta} \\ -\lambda & 1 - \frac{1}{2}\lambda^2 & A\lambda^2 \\ A\lambda^3(1 - \rho e^{i\delta}) & -A\lambda^2 & 1 \end{pmatrix}, \quad (1)$$

where  $\lambda = 0.22$  is the Cabibbo angle and the parameters  $A = 1.05 \pm .17$  and  $\rho \leq 0.9$  are obtainable from  $B$  decay. The allowed range for the phase  $\delta$  is restricted by the parameter  $\epsilon$  of CP violation in the  $K^0$ - $\bar{K}^0$  system and the mixing parameter  $x_d = 0.73 \pm 0.13$  in the system of neutral  $B_d$  mesons. Figs 1 and 2 are taken from Ref [4], where we analyzed the presently allowed ranges in the  $\rho$ - $\delta$  plane and possible restrictions by measuring certain CP violating asymmetries. In Fig 1 we show the allowed domain for fixed values of  $m_t$  ( $= 60, 90, 120$  and  $180\text{GeV}$ ), and in Fig 2 the full range which contains areas of fixed  $x_s$ . As one can easily see, combining direct measurements of  $m_t$  and  $x_s$  would considerably reduce the presently existing freedom.

A problem arises, however, because with  $x_d \sim 0.7$  the three family standard model predicts rather large values of  $x_s$ . One finds:

$$\frac{x_d}{x_s} \geq \left| \frac{V_{ts}}{V_{td}} \right|^2 = \lambda^2 (1 + \rho^2 - 2\rho \cos \delta), \quad (2)$$

and therefore gets as a conservative lower bound  $x_s \geq 3$  [6]. In Ref [7] we discussed various methods for obtaining the quantity  $x_s$  experimentally. Special emphasis was put on the question of what accuracy is necessary for achieving a further reduction of the allowed area in the standard model parameter space. One result was that time integrated methods are not likely to give more information on  $x_s$  than the presently known limit. This is because the observables involved behave at best like  $1 + O(1/x_s^2)$  for large  $x_s$ . Since with time dependent methods the period of oscillation is given by  $T = \frac{2\pi\tau}{x_s}$  ( $\tau =$  proper lifetime), these appear much more promising. It is clear, that because of the short lifetime of  $B$  mesons, a large boost is necessary so that the  $b$  and  $\bar{b}$  quarks are produced with large

momenta in the laboratory system, and in this way their decay paths become visible. In principle there are two possibilities for such experiments—either at energies high above the threshold for  $B_s B_s$  production or at an asymmetric  $e^+ e^-$  collider at a CM energy near the  $\Upsilon(5s)$  mass. Here we concentrate on the latter method and discuss the background contributions and systematic errors. Using these ingredients as input we produce decay time histograms to which afterwards a fitting routine is applied. In this analysis we ignore CP violating effects and lifetime differences in  $B$  decays.

## 2 Oscillations near the $B_s^0 \bar{B}_s^0$ Threshold

Due to mixing, the interaction and mass eigenstates of  $B_s$  mesons do not coincide:

$$B_{H,L} = \frac{1}{\sqrt{1+|\eta|^2}} (B_q \pm \eta \bar{B}_q), \quad (3a)$$

$$\eta = \sqrt{\frac{M_{12}^* - \frac{i}{2}\Gamma_{12}}{M_{12} - \frac{i}{2}\Gamma_{12}}}. \quad (3b)$$

where

In the cases  $B_d$  and  $B_s$ ,  $\eta$  is practically a pure phasefactor. Mixing can be observed as oscillations (as a function of proper time) in the number of decays to final states accessible only for the weak eigenstate  $B_s^0$  but not for  $\bar{B}_s^0$  (or vice versa):

$$|B_s(t)\rangle = f_+(t)|B_s(0)\rangle + \eta f_-(t)|\bar{B}_s(0)\rangle > \quad (4a)$$

$$|\bar{B}_s(t)\rangle = f_+(t)|\bar{B}_s(0)\rangle + \frac{1}{\eta} f_-(t)|B_s(0)\rangle >, \quad (4b)$$

where

$$f_{\pm} = \exp(-i(M - \frac{i}{2}\Gamma)t) \frac{1}{2} \{ \exp(-i\frac{x_s t}{2\tau}) \pm \exp(i\frac{x_s t}{2\tau}) \}, \quad (4c)$$

and  $x_s = \Delta m_{B_s}/\Gamma_{B_s}$ . The oscillation period then is determined by  $x_s$  and  $\tau$ . At energies around the mass of  $\Upsilon(5s)$   $B_s$  mesons can only be produced in the initial state  $B_s^0 \bar{B}_s^0$  or from the decays of the excited states  $B_s^* \bar{B}_s^*$ ,  $B_s \bar{B}_s^*$ , or  $B_s^* \bar{B}_s$ . In any case the  $B_s^0 \bar{B}_s^0$  pair is produced in a definite state of C parity in the  $B^0 \bar{B}^0$  CM frame. The decay time distributions for definite C parity of the  $B_s^0 \bar{B}_s^0$  system show the following dependence on the proper times  $t_1$  and  $t_2$ :

$$N(B_s^0 \bar{B}_s^0 \rightarrow B_s^* \bar{B}_s^*; t_1, t_2) \sim \exp(-\frac{t_1 + t_2}{\tau}) \begin{cases} \cos^2(\frac{x_s}{2} \frac{t_1 + t_2}{\tau}), & \text{for } C = +1; \\ \cos^2(\frac{x_s}{2} \frac{t_1 - t_2}{\tau}), & \text{for } C = -1. \end{cases} \quad (5a)$$

$$N(B_s^0 \bar{B}_s^0 \rightarrow B_s^0 \bar{B}_s^0; t_1, t_2) + N(B_s^0 \bar{B}_s^0 \rightarrow B_s^* \bar{B}_s^*; t_1, t_2) \sim \exp(-\frac{t_1 + t_2}{\tau}) \begin{cases} \sin^2(\frac{x_s}{2} \frac{t_1 + t_2}{\tau}), & \text{for } C = +1; \\ \sin^2(\frac{x_s}{2} \frac{t_1 - t_2}{\tau}), & \text{for } C = -1. \end{cases} \quad (5b)$$

In the  $\Upsilon(5s)$  CM system the  $B_s \bar{B}_s$  pair is produced almost at rest. If an asymmetric  $e^+ e^-$  collider is used to give the whole system a boost which is large enough to measure decay lengths, the energy of the  $B$ 's is known approximately. The beam interaction point, however, is not, so that  $t_1$  and  $t_2$  cannot be individually measured. The  $B_s^0 \bar{B}_s^0$  proper time difference, on the other hand, is an accessible quantity. Integrating Eq (5) with respect to  $t_1 + t_2$ , while keeping  $t_1 - t_2$  fixed, results in the following distributions in  $|t_1 - t_2|$ :

$$N(B_s^0 \bar{B}_s^0 \rightarrow B_s^* \bar{B}_s^*; |t_1 - t_2|) \sim \frac{1}{2} \exp(-\frac{|t_1 - t_2|}{\tau}) \begin{cases} \frac{1}{1+x_s^2} \{ 2 \cos^2(\frac{x_s}{2} \frac{t_1 - t_2}{\tau}) + x_s^2 - x_s \sin(x_s \frac{|t_1 - t_2|}{\tau}) \}, & C = +1, \\ 2 \cos^2(\frac{x_s}{2} \frac{t_1 - t_2}{\tau}), & C = -1. \end{cases} \quad (6a)$$

$$N(B_s^0 \bar{B}_s^0 \rightarrow B_s^0 \bar{B}_s^0; |t_1 - t_2|) + N(B_s^0 \bar{B}_s^0 \rightarrow B_s^* \bar{B}_s^*; |t_1 - t_2|) \sim \frac{1}{2} \exp(-\frac{|t_1 - t_2|}{\tau}) \begin{cases} \frac{1}{1+x_s^2} \{ 2 \sin^2(\frac{x_s}{2} \frac{t_1 - t_2}{\tau}) + x_s^2 + x_s \sin(x_s \frac{|t_1 - t_2|}{\tau}) \}, & C = +1, \\ 2 \sin^2(\frac{x_s}{2} \frac{t_1 - t_2}{\tau}), & C = -1. \end{cases} \quad (6b)$$

As suggested by Feldman [8], these two different classes of distributions can be observed as oscillations in the number of opposite and same sign dileptons. The big advantage of using semileptonic decays lies in their large branching fraction (12% for  $B \rightarrow l\nu X$ ) and good detection efficiencies. These signals will be on top of a background coming from semileptonic  $B_d$  and  $B^{\pm}$  decays. While charged  $B$  decays cause a purely exponential background, the contribution due to neutral  $B_d^0 \bar{B}_d^0$  decays carries a large oscillation period. Moreover, for both the  $B_s$  and  $B_d$  component one does not distinguish between the two different C parity eigenstates. Since the mass splitting between  $B_s$  and  $B_d$  is expected to be close to the  $D_s - D$  mass difference, and since the hyperfine splitting in the  $B_s$  system is likely to be similar to the  $B_d$  system, we will take

$$\Delta m_{B_s - B_d} \simeq 100 \text{ MeV}, \\ \Delta m_{B_s - B_d} \simeq 50 \text{ MeV}. \quad (7)$$

Therefore,  $B_s \bar{B}_s$  pairs are always accompanied by  $B_d \bar{B}_d$ ,  $B_d \bar{B}_d^*$ ,  $B_s^* \bar{B}_d$  and  $B_d^* \bar{B}_s$  pairs. Since the mass of the  $\Upsilon(5s)$  is 310 MeV +  $2m_{B_s}$ , pairs of  $B_s \bar{B}_s^*$  ( $B_s^* \bar{B}_s$ ) are also expected to be produced. However,  $\Upsilon(5s)$  might not be heavy enough to decay into  $B_s^* \bar{B}_s^*$ . In Table 1 we show the ratios of probabilities for the decay of  $\Upsilon(5s)$  into various states for two potential model calculations [9, 10]. In the first row, the mass of the  $\Upsilon(5s)$  is assumed to be smaller than  $2m_{B_s}$ . The following two rows assume that  $B_s^* \bar{B}_s^*$  can be produced.

Table 1

	$B_s^* \bar{B}_d^*$	$B_s^* \bar{B}_s^*$	$B_d \bar{B}_d^*$	$B_s \bar{B}_s^*$	+ c.c.	$B_s \bar{B}_s^*$	+ c.c.	$B_d \bar{B}_d^*$	$B_s \bar{B}_s^*$
BHI [9]	1	—	0.41	0.34	0.03	0.004			
BHII [9]	1	0.67	0.41	0.18	0.03	0.004			
CUSB [10]	1	1.18	1.34	0.1	0.67	0.21			

Since for  $C = +1$  (in contrast to  $C = -1$ ) the distributions Eq (6) show a suppression of the oscillating part compared to the pure exponential, the CM energy should be adjusted to a value for which  $C = -1$   $B_s$  states predominate. In principle this value could be below the  $B_s \bar{B}_s^* + c. c.$  threshold. However, this energy corresponds to a dip in the  $e^+e^-$  cross section. So, clearly energies around the  $\Upsilon(5s)$  would be better suited (maybe slightly above if  $2m_{B_s^*} > m_{\Upsilon(5s)}$ ).

As at the  $\Upsilon(4s)$ , there is the contribution of charged  $B^+B^-$  pairs to the opposite sign dileptons. Its weight relative to that due to  $B_d^0 \bar{B}_d^0$  pairs is given by the quantity  $\lambda$  which is a straightforward generalization of the one used by ARGUS [1]:

$$\lambda = \frac{Br(\Upsilon \rightarrow B^+ B^-)}{Br(\Upsilon \rightarrow B_d^0 \bar{B}_d^0)}, \quad (8)$$

where we have assumed equal semileptonic branching ratios for  $B_d^0$  and  $B^+$  decays, and states with  $C = \pm 1$  are understood to be included in the numerator and in the denominator. The quantity  $\lambda$  is estimated to be in the range 1 - 1.5, and taken to be 1.2 in our analysis. Finally  $B\bar{B}$  pairs can be produced in association with charged or neutral  $\pi^{\pm}$ . In analogy to Eq (8) we parametrize this contribution as  $\rho$ , defined by

$$\rho = \frac{Br(\Upsilon \rightarrow B\bar{B}\pi)}{Br(\Upsilon \rightarrow B_d \bar{B}_d)}, \quad (9)$$

where we have again assumed equal semi-leptonic branching ratios for  $B_d$  and  $B^+$ , and  $C = \pm 1$  states are implicitly included in both numerator and denominator. It is possible to estimate the relative contributions of  $B_d^0 \bar{B}_d^0 \pi^0$ ,  $B^+ B^- \pi^0$ , and  $B^+ \pi^- \bar{B}_d^0$  to  $\rho$  as follows. First, in analogy to Eq (8), the ratio of  $B^+ B^- \pi^0$  production to  $B_d^0 \bar{B}_d^0 \pi^0$  production is expected to be about  $\lambda$ . Secondly, due to isospin considerations, the contribution of  $B_d^0 \bar{B}_d^0 \pi^0$  is four times smaller than that of  $B^+ \bar{B}_d^0 \pi^- + c.c.$ . Therefore we have

$$B^+ B^- \pi^0 : B^+ \bar{B}_d^0 \pi^- + B^- B_d^0 \pi^+ : B_d^0 \bar{B}_d^0 \pi^0 \\ \lambda : 4 : 1. \quad (10)$$

In the following we assume  $\rho$  to be 1 since, apart from phase space, there seems to be no indication that the production of an extra pion would be suppressed. The  $\pi^0$  modes will effectively increase the contributions of both  $B^+ B^-$  and  $B_d^0 \bar{B}_d^0$  pairs. For the contributions with charged  $\pi^{\pm}$ 's, however, one finds a new kind of distribution:

$$N(B^+ \bar{B}_d^0 \rightarrow B^+ \bar{B}_d^0; t_1, t_2) \sim \exp\left(-\frac{t_1 + t_2}{\tau}\right) \cos^2\left(\frac{x_d t_1}{2\tau}\right), \\ N(B^+ \bar{B}_d^0 \rightarrow B^+ B_d^0; t_1, t_2) \sim \exp\left(-\frac{t_1 + t_2}{\tau}\right) \sin^2\left(\frac{x_d t_1}{2\tau}\right), \quad (11)$$

which, after integration over  $t_1 + t_2$  and symmetrization with respect to the sign of  $t_1 - t_2$ , leads to the following expressions:

$$N(B^+ \bar{B}_d^0 \rightarrow B^+ \bar{B}_d^0; |t_1 - t_2|) \sim \\ \frac{1}{4 + x_d^2} \exp\left(-\frac{|t_1 - t_2|}{\tau}\right) \left\{ 3 + \frac{x_d^2}{2} + \cos(x_d \frac{|t_1 - t_2|}{\tau}) - \frac{x_d}{2} \sin(x_d \frac{|t_1 - t_2|}{\tau}) \right\}, \quad (12a)$$

$$N(B^+ \bar{B}_d^0 \rightarrow B^+ B_d^0; |t_1 - t_2|) \sim \\ \frac{1}{4 + x_d^2} \exp\left(-\frac{|t_1 - t_2|}{\tau}\right) \left\{ 1 + \frac{x_d^2}{2} - \cos(x_d \frac{|t_1 - t_2|}{\tau}) + \frac{x_d}{2} \sin(x_d \frac{|t_1 - t_2|}{\tau}) \right\}, \quad (12b)$$

Similar equations are obtained when the initial state is  $B^- B_d^0 \pi^+$ . The process of the type (12a) contributes to the opposite sign dilepton signal, whereas the process of type (12b) affects the same sign dilepton rate.

Combining all these components with their appropriate weights, for example in the model BIII, results in the theoretical distribution [11]. There are, however, experimental errors which one has to take into account. First there is the possibility of charge misidentification. We assume this error to amount to 5% in total ( $\approx 2.5\%$  for each single lepton), but it turns out that this does not affect the shape of the distributions significantly.

Of special importance is a systematic error [10] due to the fact that  $B\bar{B}$  pairs are not produced at rest in the center of mass system (i.e. the Doppler effect). The distance between the decay vertices of the two  $B$  mesons in the lab system is approximately given by\*

$$d = c\gamma\beta(t_1 - t_2) + c\gamma\beta_{cm} \cos(\theta_{cm})(t_1 + t_2) + O(\beta_{cm}^2), \quad (13)$$

where  $\beta_{cm}$  is the velocity of the  $B$  mesons in the center of mass system, and  $\theta_{cm}$  denotes the polar angle with respect to the beam pipe at which this meson is emitted in the CM. Taking  $(t_1 + t_2) \approx 2\tau$  and  $(|\cos \theta_{cm}|) = 2/\pi$ , this leads to a systematic error in  $(t_1 - t_2)$  as extracted from  $d$ :

$$\left[ \frac{\Delta(t_1 - t_2)}{\tau} \right]_{\text{sys}} \approx \frac{4}{\pi} \frac{\beta_{cm}}{\beta} \approx 1.8 \beta_{cm}. \quad (14)$$

In the last step we have assumed a 12.5 GeV on 2.3 GeV collider configuration as proposed in Ref [12]. This Doppler effect affects different modes in different ways. For example, with the center of mass energy just above the threshold for  $B_s^* \bar{B}_s^*$  production, one finds that  $B_s \bar{B}_s$  pairs coming from the decays of  $B_s^* \bar{B}_s^*$  have, on average,  $\beta_{cm} = 0.01$ , while  $B_s \bar{B}_s$ ,

\* This assumes that the  $B$ 's are produced back to back in the CM system. In fact, because of  $B^*$  and  $B\bar{B}\pi$  production, this is not the case. However, a more accurate estimate of this systematic error would require a detailed Monte Carlo simulation.

pairs produced directly have  $\beta_{cm} = 0.14$ . For  $B\bar{B}$  pairs originating from all the various angular momentum states, we have

$$\begin{aligned} B_s^+ B_s^+ , B_s^+ B_s^+ , B_s^+ B_s^+ , B_s^+ B_s^+ , B_s^+ B_s^+ , B_s^+ B_s^+ , B_s^+ B_s^+ , B_s^+ B_s^+ \\ \beta_{cm}: 0.01 , 0.10 , 0.14 , 0.20 , 0.22 , 0.24 , 0.16 \end{aligned} \quad (15)$$

Since the beam energy is expected to be well controlled, the main source of statistical error in  $\frac{\Delta(t_1 - t_2)}{\tau}$  is the finite vertex resolution. Assuming this resolution to be  $25\mu\text{m}$ , one gets:

$$\left[ \frac{\Delta(t_1 - t_2)}{\tau} \right]_{res} \simeq \frac{25\mu\text{m} \cdot \sqrt{2}}{c\gamma\beta\tau} \simeq 1, \quad (16)$$

with the assumed asymmetric collider configuration ( $\beta\gamma = 1$ ). An increase in the asymmetry of the beam energies leads to larger values of  $\gamma\beta$  and therefore decreases the systematic uncertainty slightly. However, an increase in  $\gamma\beta$  in Eq (16) will also result in an increased error in  $d_i$  caused by the higher collimation of the  $B$  decay products. Therefore an optimal choice of the collider configuration might exist which would minimize  $\left[ \frac{\Delta(t_1 - t_2)}{\tau} \right]_{res}$ . In the subsequent discussion we assume this minimal value to be given by Eq (16). We will, however, also consider larger values of the statistical error. This error sets the upper limit for the value of  $x_s$  accessible experimentally. We also note that, because of the systematic error, there is a minimum value of  $\beta$  required to measure  $x_s$ , i.e. there is a minimum necessary asymmetry in the beam energies.

In order to simulate this experimental situation we convolute the theoretical distributions (after taking into account 5% charge misidentification) with a Gaussian error factor. In this way one arrives at linear combinations of terms of the following form:

$$D(v) = \frac{1}{\sigma\sqrt{2\pi}} \int_{-\infty}^{\infty} g(v') e^{-\frac{(v-v')^2}{2\sigma^2}} dv', \quad (17)$$

where  $\sigma$  is the experimental resolution,  $v = \frac{|t_1 - t_2|}{\tau}$ , and  $g(v)$  is one of

$$e^{-v}, \quad e^{-v} \cos xv, \quad e^{-v} \sin xv. \quad (18)$$

A straightforward calculation yields:

$$\begin{aligned} D_1(v, 0) &= \text{Re}(H_1(v, 0) + H_2(v, 0)), \quad \text{for } g(v) = e^{-v}, \\ D_1(v, x) &= \text{Re}(H_1(v, x) + H_2(v, x)), \quad \text{for } g(v) = e^{-v} \cos xv, \\ D_2(v, x) &= \text{Im}(H_1(v, x) + H_2(v, x)), \quad \text{for } g(v) = e^{-v} \sin xv. \end{aligned} \quad (19)$$

The functions  $H_1(v, x)$  and  $H_2(v, x)$  in the above equations are defined as follows:

$$\left. \begin{aligned} H_1(v, x) \\ H_2(v, x) \end{aligned} \right\} = \frac{1}{2} e^{\frac{1}{2}\sigma^2(1-ix)^2 + v(1-ix)} \left[ 1 - \text{erf} \left( \frac{\sigma^2 + v}{\sqrt{2}\sigma} - i\frac{x\sigma}{\sqrt{2}} \right) \right], \quad (20)$$

where  $\text{erf}(z)$  is the error function.

Finally histograms are generated by splitting the resulting continuous distributions into bins of size  $\frac{|t_1 - t_2|}{\tau} = 1$ . The area of each of these bins is proportional to the number of events in the corresponding  $\frac{|t_1 - t_2|}{\tau}$  interval. Interpreting this number as a mean of the Poisson distribution, a random number is generated accordingly and taken to be the actual height of the bin. As an example we show in Fig 3 histograms for same sign dilepton distributions for the scenarios BHII (a, c, e) and equal admixture (b, d, f) of all components ( $B_s, B_d, C = \pm 1$ ) with  $|\Delta(t_1 - t_2)/\tau|_{res} = .1$  and  $x_s = 10$ . Each case is presented for three different numbers of detected dilepton events:  $2 \times 10^4, 5 \times 10^4$  and  $5 \times 10^5$ . Taking into account semileptonic branching ratios, which give a factor  $1/(.24)^2$  and allowing for finite experimental efficiency, the fact that some of the signal goes down the beam pipe and part of the events are lost by imposing a cut on the lepton energy in order to distinguish semileptonic  $B$  from  $D$  decays (an estimated combined factor of 8), these correspond to about  $2 \times 10^6, 5 \times 10^6$  and  $5 \times 10^7$  initial  $b\bar{b}$  quark pairs (at the  $\Upsilon(5s)$ ). While in the BHII scenario the signal is evident with a number of only  $5 \times 10^4$  detected dileptons, it seems to be hard to see it in the more pessimistic equal admixture case.

In order to make these statements more quantitative a least  $\chi^2$  fit using the MNUIT package was performed. In Fig 4a we show the best fit (dots and solid line) to the histogram (vertical bars give the size of the statistical error, horizontal bars the bin size) for  $x_s = 10$  and a number of  $5 \times 10^4$  detected dileptons. This is to be compared with the smooth dashed curve before randomization. The dots (and solid line) were found by fitting to the following four parameter function:

$$F_i(a_1, a_2, a_3, a_4, v) = \frac{1}{2} a_1 (D_1(v, 0) - a_2 D_1(v, a_3) - a_4 D_1(v, x_d)), \quad (21)$$

where  $x_d = 0.7$  and  $a_3$  should give the value of  $x_s$  searched for. The inclusion of a term proportional to  $D_1(v, x_d)$  turns out to be important, since the contribution of  $B_d^0 \bar{B}_d^0$  decays cause a substantial deviation from an exponential behaviour which is modulated by some rapid oscillation. The results of the best fit are:  $\chi^2 = 34.4, a_1 = 0.75 \pm 0.01, a_2 = 0.15 \pm 0.10, a_3 = x_s = 9.90 \pm 0.10$  and  $a_4 = 0.60 \pm 0.02$ . In Fig 4b we show the  $\sigma$  contour plots (up to five standard deviations) in the  $(a_1, x_s)$  plane. Finally in Fig 4c we explore the four dimensional parameter space by finding for each value of fixed  $x_s = a_3$  the best fit in the remaining three parameters and plotting the obtained  $\chi^2$  against  $x_s$ . A very pronounced dip in  $\chi^2$  around  $x_s = 10$  is clearly visible, and in addition one observes a steep rise in  $\chi^2$  for very low  $x_s$ . In the same way (taking the above as an ideal situation for measuring  $x_s$ ) we analyzed the histograms for all kinds of combinations  $\frac{\Delta|t_1 - t_2|}{\tau}|_{res} = 10\%$ ; 20%, statistics of detected dileptons  $2 \times 10^4, 5 \times 10^4$  and  $5 \times 10^5$  for the two scenarios considered in Fig 3. It seems possible to see up to  $x_s = 15$  with  $\frac{\Delta|t_1 - t_2|}{\tau}|_{res} = 10\%$  and

$5 \times 10^4$  dileptons in scenario BHII, while still values up to around 10 might be reasonably well recovered for  $\frac{\Delta|t_1-t_2|}{\tau} = 20\%$ . With the same statistics and the equal admixture scenario  $\frac{\Delta|t_1-t_2|}{\tau} = 20\%$  is sufficient to reach  $x_s = 5$  while for  $x_s = 10$  one definitely needs  $\frac{\Delta|t_1-t_2|}{\tau} = 10\%$ . It is interesting to see that in scenario BHII with  $\frac{\Delta|t_1-t_2|}{\tau} = 10\%$   $2 \times 10^4$  detected dileptons still seem to be sufficient for identifying  $x_s = 10$ , whereas a statistics of  $5 \times 10^5$  is not enough to see  $x_s = 20$ .

There have been suggestions to utilize a  $D_s$  tag in order to enhance the signal to background ratio and in this way manage with a smaller number of  $b\bar{b}$  quark pairs, or to allow for a larger resolution error  $\left[\frac{\Delta|t_1-t_2|}{\tau}\right]_{res}$ . In Fig 5a we show the histogram and best fit for 2000 reconstructed  $llD_s$  events (according to scenario BHII, 5% charge misidentification,  $\frac{\Delta|t_1-t_2|}{\tau} = 10\%$  and the input value  $x_s = 10$ ). Here the following two parameter function was used for the fit:

$$Fi(a_1, a_2, v) = a_1 Odd(a_2, v) + (1 - a_1) Even(a_2, v), \quad (22)$$

where *Odd* and *Even* are the Gaussian convoluted functions of Eq (6b), and  $a_2$  should reproduce  $x_s = 10$ . For  $\frac{\Delta|t_1-t_2|}{\tau} = 10\%$  one finds with quite low  $\chi^2 = 15$   $a_1 = 0.81 \pm .22$  (input value was .79) and  $a_2 = 10.24 \pm 0.11$ . In Fig 5b we show the corresponding  $\sigma$  contour plot in the  $(a_2, x_s)$  plane. This does not look better than for the untagged dilepton distribution (assuming a reconstruction efficiency of 4% for  $D_s$  mesons 2000 detected  $llD_s$  events correspond to 50,000 detected  $ll$  events). In addition Fig 5c, showing the plot  $\chi^2$  vs  $x_s$  (now performing a one parameter least square fit for each fixed value of  $x_s$ ), reveals that the distance of the minimum in  $\chi^2$  to the plateau is much smaller than in the untagged case. Repeating the same analysis but now with  $\frac{\Delta|t_1-t_2|}{\tau} = 20\%$  one only finds an extremely shallow minimum in  $\chi^2$  around  $a_2 = 10.9$  and no reasonable error bars. With 90% confidence level one might exclude  $x_s \leq 3.5$  in this case, without getting any upper bound (in the BHII scenario). This seems to tell us two things: First, tagging on  $D_s$  mesons in addition to the dilepton pair does not look as rewarding as it might seem initially (this is because of the loss of a factor 25 in statistics). Secondly, the range of  $x_s$  reachable depends crucially on the overall resolution error  $\frac{\Delta|t_1-t_2|}{\tau}$ . In many cases it turned out that an improvement by a factor of 2 (from 10% to 20%) is much more rewarding than an increase of one order of magnitude in statistics.

### 3. Conclusions

Analyzing decay time distributions at asymmetric  $e^+e^-$  colliders near the  $\Upsilon(5s)$  resonance we discussed the physics input necessary to find the range of  $x_s$  accessible and the number of initial  $b\bar{b}$  quark pairs required. Same sign dilepton distributions turn out to yield the clearest signal. The loss in statistics caused by tagging on a  $D_s$  meson in addition invalidates the effect of increasing the signal to background ratio. As expected,

by using a fitting routine we find somewhat more optimistic upper values of  $x_s$  accessible with definite statistics and resolution error than by just inspecting the histograms [7]. So, assuming a vertex resolution of  $25\mu\text{m}$  at least, a value of  $x_s$  up to 15 seems not to be out of reach with  $5 \times 10^6$   $b\bar{b}$  pairs (10 for the equal admixture scenario).

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## References

- [1] ARGUS Collaboration: H. Albrecht et al, Phys. Lett. **192B** (1987) 245.
- [2] CLEO Collaboration: A. Jawahery, *Proceedings of the XXIV International Conference on High Energy Physics*, Munich, W. Germany (1988).
- [3] A. Ali, DESY preprint DESY 87-083 (1987); J. Donoghue, T. Nakada, E. Paschos and D. Wyler, Phys. Lett **195B** (1987) 285; J. Ellis, J. Hagelin and S. Rudaz, Phys. Lett. **192B** (1987) 201; I. I. Bigi and A. I. Sanda, Phys. Lett. **104B** (1987) 307; J. Maalampi and M. Roos, Phys. Lett. **195B** (1987) 489; V. Barger, T. Han, D. V. Nanopoulos and R. J. N. Phillips, Phys. Lett. **104B** (1987) 312; H. Harari and Y. Nir, Phys. Lett. **105B** (1987) 586; Y. Nir, SLAC preprint SLAC-PUB-4368, (1987); V. A. Khoze and N. G. Uraltsev, Leningrad preprint 1290, (1987); G. Altarelli and P. Franzini, Z. Phys. **C37** (1988) 271.
- [4] P. Krawczyk, D. London, R. Pecci and H. Steger, Nucl. Phys. **B307** (1988) 19.
- [5] L. Maiani, Phys. Lett. **62B** (1976) 183; L. Wolfenstein, Phys. Ref. Lett. **51** (1983) 1945.
- [6] G. Altarelli and P. Franzini, Z. Phys. **C37** (1988) 271.
- [7] P. Krawczyk, D. London and H. Steger, DESY preprint, DESY 88-163 (1988).
- [8] This suggestion was made by G. Feldman at Snowmass '88.
- [9] N. Byers and D. S. Hwang, *Proceedings of the Workshop on High Sensitivity Beauty Physics at Fermilab*, ed. A. J. Slaughter, N. Lockyer, and M. P. Schmidt (Fermi National Accelerator Laboratory, Batavia, 1987) p. 199.
- [10] J. Lee-Franzini, SUNY preprint Print-88-047 (Stony Brook) (1988).
- [11] For further literature on potential model calculations see: A. D. Martin and C. K. Ng, Z. Phys **C40** (1988) 133; S. Ono, A. I. Sanda and N. A. Törnqvist, Phys. Rev. **D38** (1988) 1619.
- [12] R. Alekseev, J. E. Bartel, P. Burchat, and A. Seiden, SLAC preprint SLAC-PUB-4673 (1988).

## Figure Captions

- Fig 1: The domain in  $\rho$ - $\delta$  space ( $\delta$  in radians), within which the standard model is compatible with the measurements of  $\epsilon$  and  $x_d$  (90% c.l.).  $B_K$  and  $f_B$  are allowed to vary within the ranges  $1/3 \leq B_K \leq 1$  and  $100 \text{ MeV} \leq (f_B)^{1/2} \leq 200 \text{ MeV}$ .
- a) The areas 1, 2, 3, 4 correspond to fixed values  $m_t = 60, 90, 120, 180 \text{ GeV}$ , respectively.
- Fig 2: As in Fig 1, but now all three parameters  $m_t$ ,  $(f_B)^{1/2}$  and  $B_K$  are varied:  $40 \text{ GeV} \leq m_t \leq 180 \text{ GeV}$ ,  $100 \text{ MeV} \leq (f_B)^{1/2} \leq 200 \text{ MeV}$  and  $1/3 \leq B_K \leq 1$ . In addition, the further restrictions by fixed  $x_s = 3, 7, 15$  are shown.
- Fig 3: Simulation of the actual experimental data for the same sign dilepton distribution with  $x_s = 10$  for the two scenarios BHII (a,c,e) and equal mixture (b,d,f), with  $\left[ \frac{\Delta(t_1-t_2)}{\tau} \right]_{res} = 0.1$ , and  $2 \times 10^4$  (a,b),  $5 \times 10^4$  (c,d),  $5 \times 10^5$  (e,f) reconstructed dileptons.
- Fig 4: Best fit to the histogram Fig 3c ( $x_s = 10$ ,  $5 \times 10^4$  reconstructed dileptons, BHII).
- a) The histogram is given by the crosses, where vertical bars give the size of the statistical error and horizontal bars the binsize. The best fit consists in the dots and the solid curve. This is to be compared with the smooth dashed curve, from which the histogram is produced via application of our randomization procedure.
- b) The  $\sigma$  contour plot up to five standard deviations in the plane of the fitting parameters  $a_2$  and  $a_3 = x_s$ .
- c)  $\chi^2$  of the best fit (for fixed values of  $x_s$ ) versus  $x_s$ .
- Fig 5: Like Fig 4, but now for 2000 reconstructed  $l\bar{l}D_s$  events, using again  $x_s = 10$ , scenario BHII, and 5% charge misidentification and  $\frac{\Delta(t_1-t_2)}{\tau} = 10\%$ .
- a) The best fit,
- b) the  $\sigma$  contour plot in the plane of fitting parameters  $a_1$ , and  $a_2 = x_s$ ,
- c) like Fig 4c,  $\chi^2$  of the best fit (for fixed values of  $x_s$ ) versus  $x_s$ .



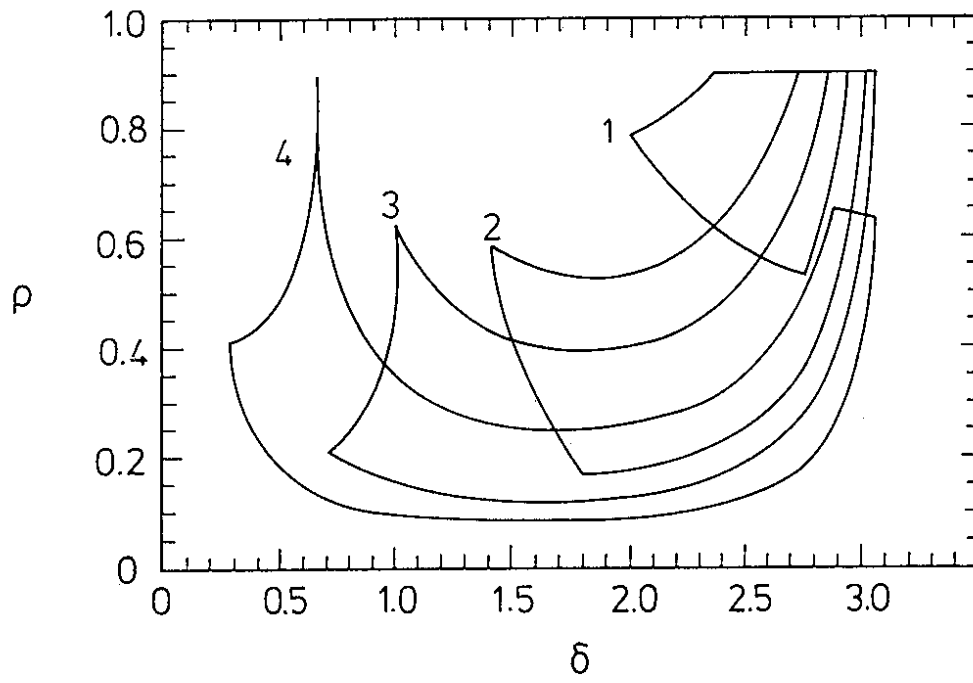


Fig 1

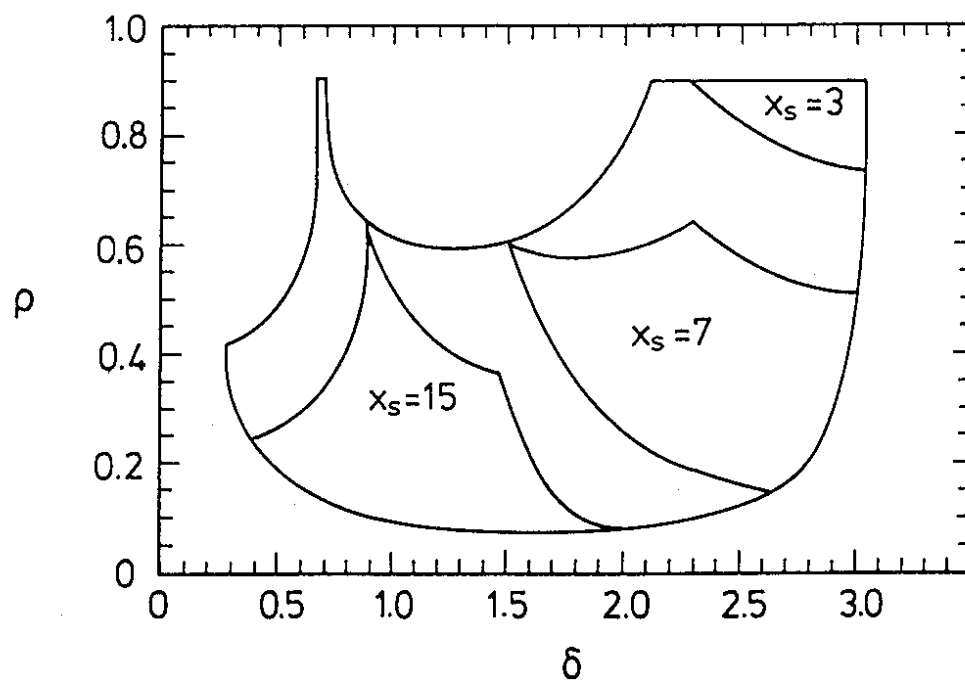


Fig 2

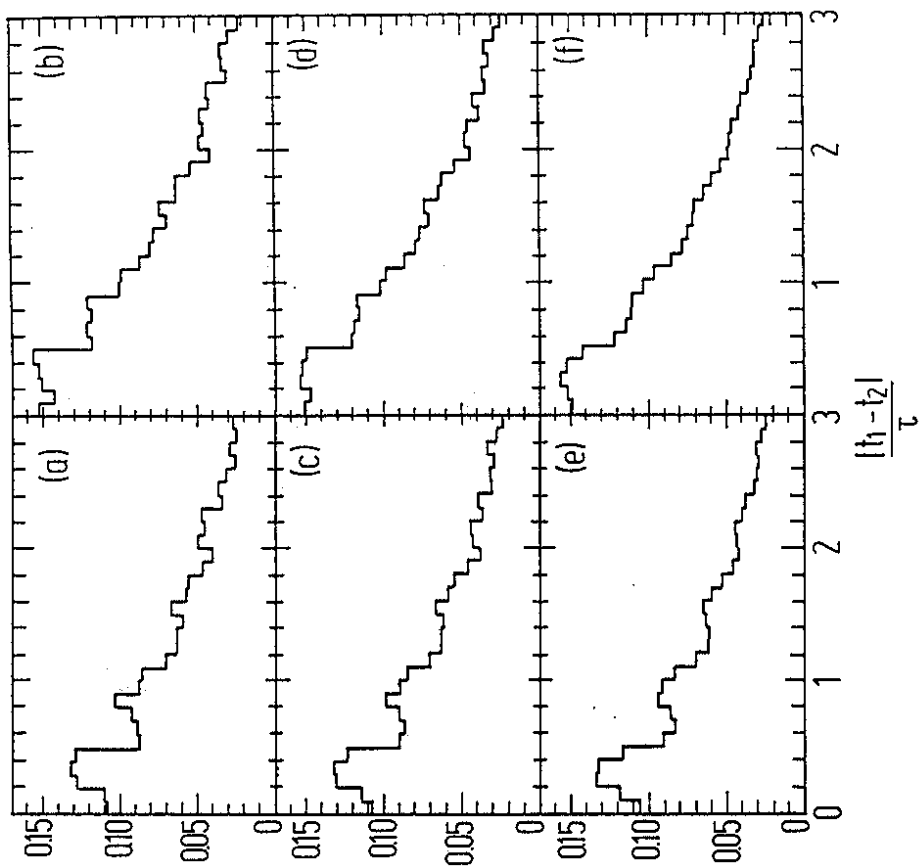


Fig 3

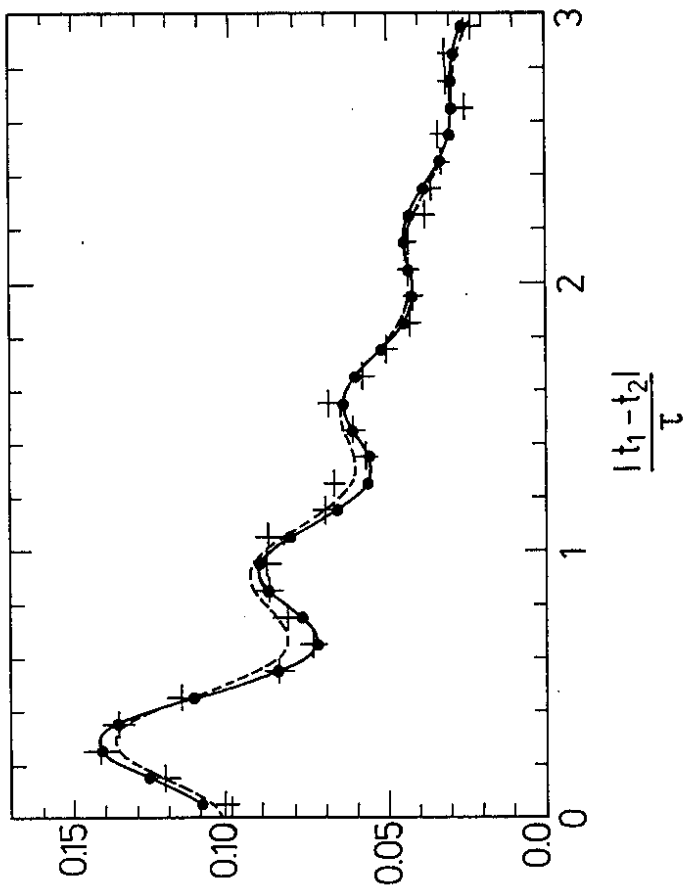


Fig 4a

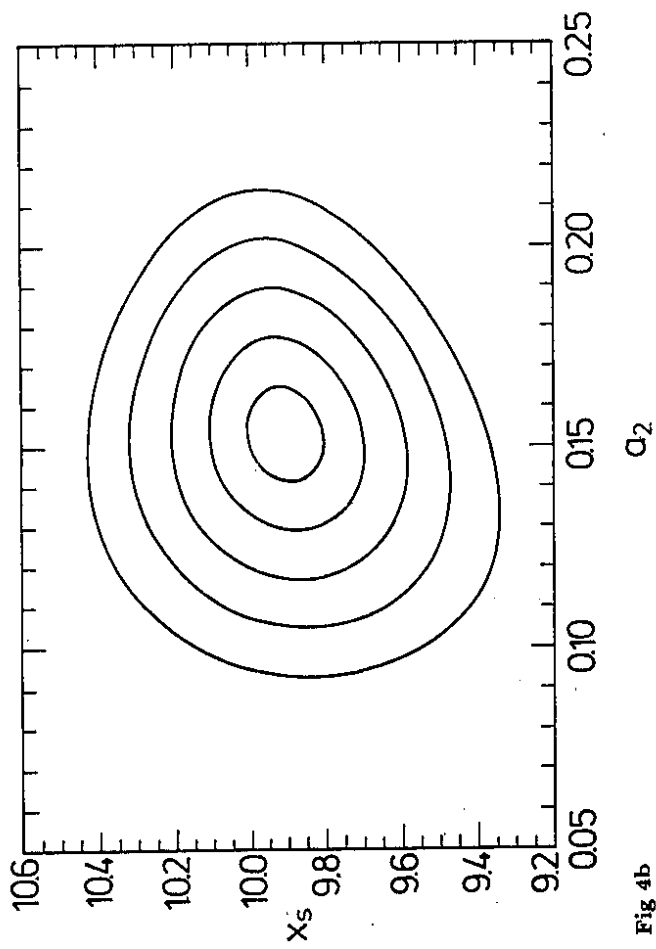


Fig 4b

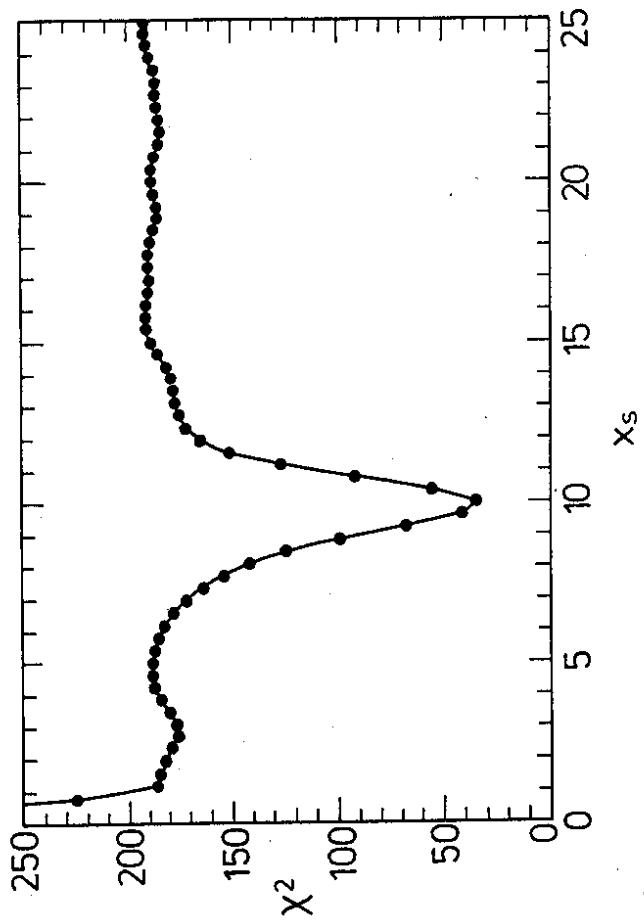


Fig 4c

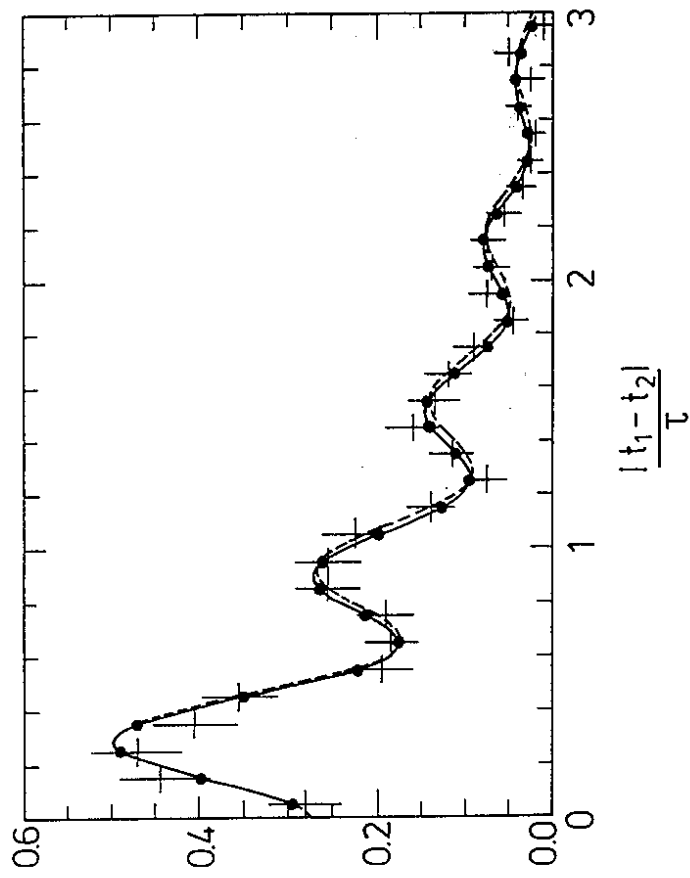


Fig 5a

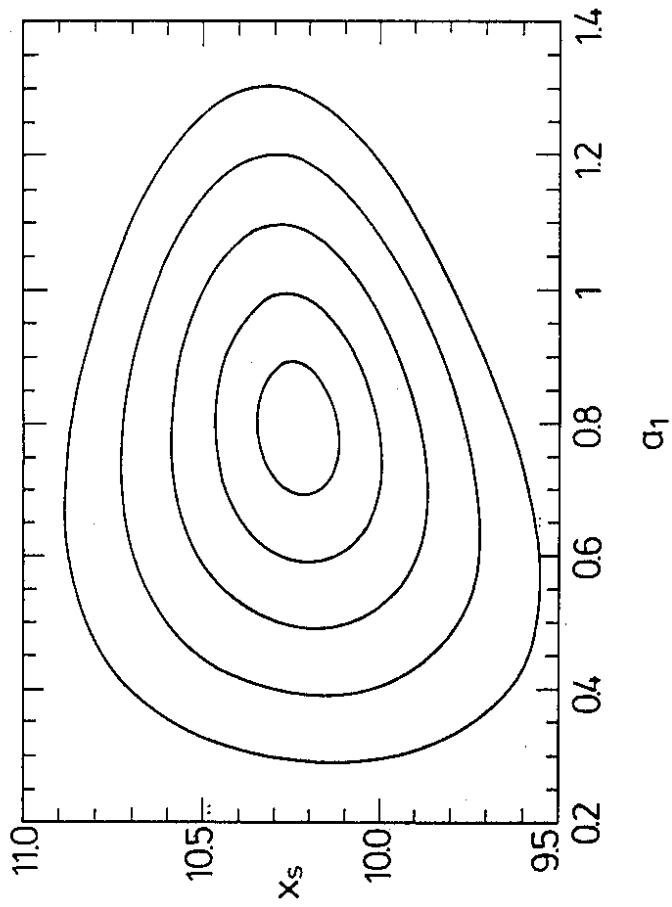


Fig 5b

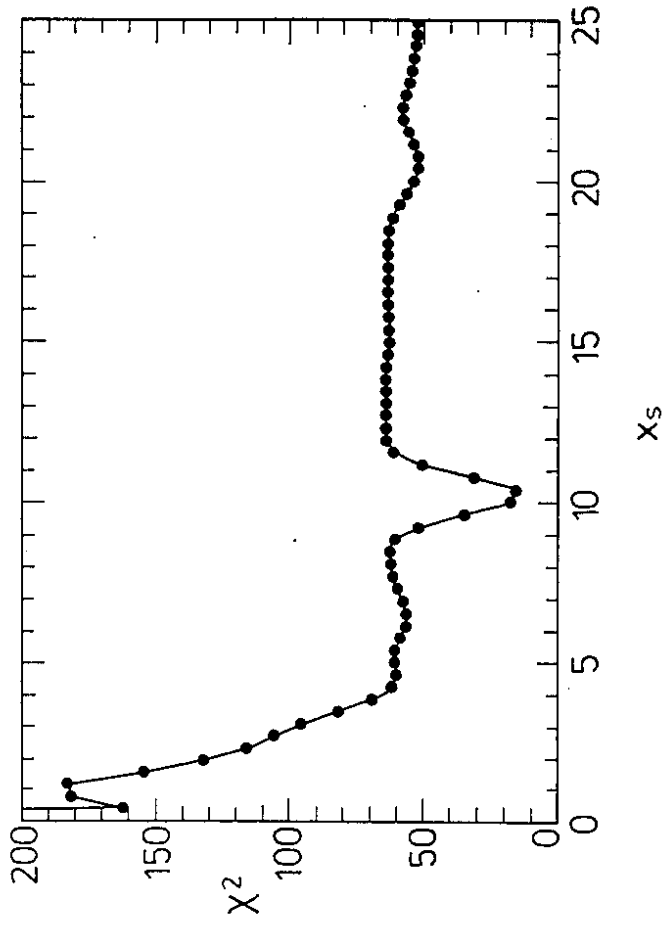


Fig 5c