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# Scaling Behaviour of Jet Shapes in $p\bar{p}$ and $ep$ Collisions

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## Abstract

We have calculated jet shapes in resolved  $\gamma p$  and  $p\bar{p}$  collisions in perturbation theory at order  $\alpha_s^3$  for the hard parton-parton processes. We compared the jet shapes for different c.m. energies  $\sqrt{S}$  and between the two processes for fixed  $x_T = 2E_T/\sqrt{S}$  and fixed cone parameters. We found a simple scaling behaviour of the jet shape which allows its comparison for different reactions and c.m. energies.

## 1 Introduction

A large fraction of the final state in hadron-hadron, electron-hadron and electron-positron collisions consists of high energy jets. These jets have an extended structure in phase space which can be studied experimentally and theoretically. One possible measure of such jet structure is the so-called jet shape or jet profile which depends on variables like transverse energy and rapidity of the jets, the jet algorithm and the extension of jets.

Some months ago we presented results for jet shapes in resolved  $\gamma p$  collisions based on perturbation theory at order  $\alpha_s^3$  for the hard parton-parton scattering processes [1][2]. We studied the jet shape concerning its dependence on transverse energy, rapidity and the inner cone extension. These functional dependences came out quite similar to those found earlier for  $p\bar{p}$  processes at  $\sqrt{S} = 1.8 \text{ TeV}$  by Ellis, Kunszt and Soper [3]. We studied this similarity of jet shapes in  $p\bar{p}$  and resolved  $\gamma p$  collisions further and found interesting scaling properties which allow a direct comparison of jet shapes in these two reactions or in one of these processes for different center of mass energies.

The measure of the jet profile is the function  $\rho(r, R, E_T, \eta)$  where  $E_T$  is the transverse energy of the jet and  $\eta$  is its rapidity with  $\phi$ , its azimuth, integrated out. This function  $\rho$  measures the fractional  $E_T$  profile, i. e., given a jet sample with transverse energy  $E_T$  defined with a cone radius  $R$ , then  $\rho(r, R, E_T, \eta)$  is the average fraction of the jets' transverse energy that lies inside an inner cone with radius  $r < R$ . Then the quantity  $1 - \rho(r, R, E_T, \eta)$  stands for the fraction of  $E_T$  that lies in the cone segment between  $r$  and  $R$ . This quantity is easily calculated from the contributing  $2 \rightarrow 3$  parton subprocesses in  $p\bar{p}$  or in resolved  $\gamma p$  collisions as for  $r > 0$  it avoids the collinear singularities at  $r = 0$ . Therefore it can be computed in a straightforward way from the  $E_T$  weighted integral of the  $p\bar{p} \rightarrow 3 \text{ partons} + X$  or  $\gamma p \rightarrow 3 \text{ partons} + X$  cross sections, respectively, over the cone segment between  $r$  and  $R$ , normalized to  $E_{T,J}$  (which is the  $E_T$  of the jet) times the Born cross section. This  $1 - \rho$  being a ratio of cross sections is  $O(\alpha_s)$  since the numerator is proportional to  $\alpha_s^3$ , whereas the denominator is  $O(\alpha_s^2)$ . In the following we shall consider the  $E_T$  profile  $\rho(r, R, E_T, \eta)$  for  $\gamma p$  and  $p\bar{p}$  reactions with varying c.m. energies  $\sqrt{S}$ . In the  $\gamma p$  process actually our calculations are for ep scattering where the photon spectrum is obtained in the Weizsäcker-Williams approximation as used in our earlier work [1].

## 2 Scaling Behaviour of $E_T$ Profile

As explained in the introduction the  $E_T$  profile  $\rho(r, R, E_T, \eta)$  has the following form

$$\rho(r, R, E_T, \eta) = 1 - \alpha_s(\mu) f(r, R, E_T, \eta) + O(\alpha_s^2) \quad (1)$$

where  $\mu$  is the scale of the  $QCD$  coupling. We take  $\alpha_s$  in one-loop approximation with  $\Lambda = 194 \text{ MeV}$ , i. e. equal to the  $\Lambda$  value of the chosen proton structure function MT-B1 [4].  $\mu = M_{\gamma p} = E_T$  where  $M_{\gamma p}$  is the factorization scale of the photon and the proton (antiproton) structure function, respectively. For the  $\gamma p$  case the photon structure function is taken from the work of Glück, Reya and Vogt [5] in  $NLO$  and  $M\bar{S}$  factorization. Since  $\rho$  is a ratio of cross sections the exact form of the structure functions is not really important. Sometimes  $\alpha_s$  in two-loop approximation is preferred [3]. This is essentially equivalent to a change of the scale  $\mu$  or of the value for  $\Lambda$ .

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Now we ask, how the function  $f(r, R, E_T, \eta)$  defined in (1) behaves when different c.m. energies  $\sqrt{S}$  are employed for  $ep$  and  $p\bar{p}$  processes. As we explained in the introduction  $f(r, R, E_T, \eta)$  is given as a ratio of cross sections with an additional factor  $E_T$  in the numerator and in the denominator. Therefore  $f$  is dimensionless. The  $E_T$  dependence in  $f$  enters through the structure functions via the scale choice  $M \propto E_T$  and through the  $E_T$  dependence of the  $2 \rightarrow 3$  parton-parton scattering cross sections in the numerator and the  $2 \rightarrow 2$  parton-parton scattering cross section in the denominator. We expect the  $E_T$  dependence through the parton distributions being cancelled in the ratio. This has been checked by direct computation [2]. The parton-parton scattering cross sections depend only on dimensionless variables  $x_T = 2E_T/\sqrt{S}$ ,  $\eta$  and the momentum fractions  $x_{e,s}$  of the incoming partons apart from a dimensional factor that cancels in the ratio. From these arguments we expect that for fixed  $\eta, r, R$  the function  $f(r, R, E_T, \eta)$  depends only on  $x_T$ . Therefore  $f$  should not depend on the c.m. energy  $\sqrt{S}$  when  $x_T$  is held fixed. We tested this by calculating  $f(r, R, E_T, \eta)$  for various values of  $r$  between 0.1 and 0.95, for  $x_T = 0.1$  and 0.5, respectively, and  $\eta_S = 0$ , where  $\eta_S$  is the rapidity in the c.m. system of the ingoing hadrons or electrons. The chosen jet sample has  $R = 1$ . We considered the following four cases, the two  $ep$  processes (resolved photoproduction only) with  $\sqrt{S} = 314 \text{ GeV}$  (HERA c.m. energy) and  $\sqrt{S} = 1.8 \text{ TeV}$  (TEVATRON c.m. energy, which perhaps could be measured with LEP-LHC) and the two  $p\bar{p}$  processes for the same c.m. energies  $\sqrt{S} = 314 \text{ GeV}$  and  $\sqrt{S} = 1.8 \text{ TeV}$ , respectively. The results are collected in Tab. 1. We see from these results that the  $f(r, R, E_T, \eta)$  for fixed  $r$  and  $x_T$  are almost identical although  $\sqrt{S}$  changes by the factor 5.7, if we compare the results for  $p\bar{p}$  and  $\gamma p$  separately. The differences between column 2 and column 4 ( $x_T = 0.1$ ) and between column 3 and 5 ( $x_T = 0.5$ ) in the table are on the percent level. The same is true if we compare the columns with the results for the  $p\bar{p}$  case. If we compare the  $f$ 's for  $p\bar{p}$  and  $ep$  reactions, keeping  $r$  and  $x_T$  fixed, we find again that the results are very similar, in particular for  $x_T = 0.1$  and less for  $x_T = 0.5$ . This is easy to understand. We see the influence of the point-like component of the photon structure function coming in at large  $E_T$ , i. e. at  $x_T = 0.5$ , which corresponds to  $E_T = 79 \text{ GeV}$  and  $E_T = 450 \text{ GeV}$  for the low and high c.m. energy, respectively. This difference is expected to be even larger if we had taken into account also the contribution of the direct photon [6]. But at  $x_T = 0.1$ , i. e.  $E_T = 16 \text{ GeV}$  and  $E_T = 90 \text{ GeV}$  respectively, the corresponding values for  $f$  differ by less than a few percent. This result is remarkable since even for small  $x_T$  we expect some difference between the photon and the antiproton structure functions and also the superposition of the various parton-parton scattering cross sections is certainly different in  $ep$  and  $p\bar{p}$  reactions. It appears that, since  $f$  is calculated from a ratio of cross sections, these differences largely cancel. This means that the whole  $E_T$  dependence of the jet profile  $1 - \rho$  originates from the fact that the coupling  $\alpha_s$  depends on  $E_T$ . So, for example for  $x_T = 0.1$  the jets at  $\sqrt{S} = 1.8 \text{ TeV}$  are in average narrower by the factor  $\alpha_s(E_T = 90 \text{ GeV})/\alpha_s(E_T = 16 \text{ GeV}) \simeq 0.7$  than at  $\sqrt{S} = 314 \text{ TeV}$  ( $\alpha_s$  is calculated in one-loop with  $\Lambda = 194 \text{ MeV}$  and four flavours). Therefore, since the variation of  $\alpha_s$  with  $E_T$  is essentially known, it is possible to predict the  $E_T$  profile for any c.m. energy as long it has been measured for one energy. As we have seen this remains true even when we consider different processes as for example  $p\bar{p}$  or  $ep$  reactions as long as  $x_T$  is small ( $x_T \simeq 0.1$ ). In case the fractional  $E_T$  profile would be measured for several c.m. energies, say, between 300 and 1800 GeV, the running of  $\alpha_s$  with  $E_T$  could be studied in detail. Of course with data from LHC this would be possible even more.

That the jet profile  $1 - \rho$  is determined from a ratio of cross sections seems to be essential for the close similarity of  $\rho(r)$  at small  $x_T$  for different reactions. For cross sections we do not

expect this. This is demonstrated in Fig. 1 where we compare the single-jet inclusive cross section  $d^2\sigma/dE_T d\eta$  for  $ep$  scattering and  $p\bar{p}$  scattering. For these cross sections we have chosen in both cases  $\sqrt{S} = 298 \text{ GeV}$  in accordance with present HERA conditions with c.m. rapidity  $\eta_S = 0$ . From this comparison it is easily seen that the  $E_T$  distributions with  $E_T = 5 \text{ GeV}$  they are normalized to each other by dividing the  $p\bar{p}$  cross section by 4000) differ appreciably for  $E_T > 20 \text{ GeV}$ . The  $p\bar{p}$  cross section is steeper as a function of  $E_T$  than the  $ep$  cross section at the same c.m. energy. The curves in Fig. 1 are in LO and in NLO with  $R = 1$ . The less steep behaviour of the  $ep$  cross section, of course, originates from the point-like or anomalous part of the quark distribution function of the photon. This effect is even more drastic at larger  $E_T$  when the contribution for direct photoproduction is added [7].

So far we considered the function  $f(r, R, E_T, \eta)$  defined in (1) for fixed rapidity  $\eta$  only. Above we saw that  $f$  does not change with  $\sqrt{S}$  when considered as a function of  $x_T$ . This will be true for all  $\eta$  although in the table we presented evidence only for  $\eta_S = 0$ . It is clear that  $f$  considered as a function of  $r, R, x_T$  and  $\eta$  will vary differently with  $\eta$  depending on the value of  $x_T$  since the phase space limits on  $\eta$  are  $\eta \leq \text{arccosh}(x_T^{-1})$ . In [1] we computed the profile function  $\rho(r, R, E_T, \eta)$  for  $r = 0.3$  as a function of  $\eta$  and for  $E_T = 5, 15$  and  $30 \text{ GeV}$  for  $\gamma p$  collisions with  $\sqrt{S} = 314 \text{ GeV}$ . The curves in Fig. 3 of [1] are rather alike in shape except for the different phase space limits in  $\eta$  which change with  $x_T$ . This suggest that we introduce instead of  $\eta$  the scaled rapidity

$$x_\eta = \frac{\eta_S}{\text{arccosh}(x_T^{-1})} \quad (2)$$

so that  $|x_\eta| \leq 1$  and try the following scaling ansatz for  $\rho$ :

$$\rho(r, R, E_T, \eta) = 1 - \alpha_s(\mu) f_1(r, R, x_T) f_2(r, R, x_\eta) \quad (3)$$

so that the  $x_T$  and the  $x_\eta$  dependence factorize. In Fig. 2 a,b we have plotted  $f_2(r, R, x_\eta)$  for two cases: (a)  $p\bar{p}$  reaction and  $\sqrt{S} = 1.8 \text{ TeV}$  and (b)  $ep$  reaction and  $\sqrt{S} = 314 \text{ TeV}$  where the curves in Fig. 2 a,b are calculated with  $r = 0.3$ ,  $R = 1$  and are for  $x_T = 0.035, 0.1, 0.2$ , respectively. We see that all curves are rather universal, i. e. independent of  $x_T$ , so that the factorization hypothesis in (3) is approximately fulfilled. The factorization in (2) is defined up to a  $x_\eta$  independent factor. The functions in Fig. 2 a,b are normalized, so that

$$f_1(r, R, x_T) = f(r, R, E_T, \eta_S = 0) \quad (4)$$

and

$$f_2(r, R, x_\eta) = \frac{f(r, R, E_T, \eta_S)}{f(r, R, E_T, \eta_S = 0)} \quad (5)$$

or

$$f_2(r, R, x_\eta) = \frac{1 - \rho(r, R, E_T, \eta_S)}{1 - \rho(r, R, E_T, \eta_S = 0)} \quad (6)$$

making (3) consistent with (1). In Fig. 2 b we have included also the three  $p\bar{p}$  curves (dotted) for comparison with the  $ep$  results. It turns out that  $f_2$  depends only weakly on  $r$ . We observe in Fig. 2 a that the  $p\bar{p}$  process is rather symmetric in  $x_\eta$  ( $x_\eta > 0$  is the direction of the incoming antiproton) independent of  $x_T$ . For  $ep$  scattering the curves are not symmetric in  $x_\eta$ , since the parton distributions of the photon and the proton are different. In addition we observe in this case that the maximum of  $f_2$  is at negative  $x_\eta$  for small  $x_T$  and is shifted to positive  $x_\eta$  if  $x_T$  increases. This can be understood by studying the contributing parton-parton scattering

processes. So the shift of the maximum is caused by the  $q_r^{an} g_p$  scattering process where  $q_r^{an}$  stands for the contribution of the point-like part of the photon structure function and  $g_p$  for the gluon induced part of the proton structure function. At small  $x_T$  the  $g_p g_p$  parton-parton scattering process with the corresponding structure functions dominates.

So far experimental data have been published only for  $p\bar{p}$  reactions [8],[9],[10]. Preliminary data from the ZEUS collaboration at HERA exist and better data are expected soon [11]. In Fig. 3 we show the comparison of  $\rho(r)$  with data from CDF [9]. In this plot the data are taken for  $R = 1, 0.1 \leq |\eta| \leq 0.7$  and  $\overline{E_T} = 45, 100 \text{ GeV}$  i. e. the  $E_T$  are in the ranges 40 – 60 and 95 – 120 GeV. For both  $E_T$  ranges we have calculated three curves (with the same averaging over  $E_T$  and  $\eta$  as for the data), two with renormalization scale  $\mu = \overline{E_T}$ , but different separation cone  $R_{sep}$  and one with scale  $\mu = E_T/2$ . The curves with  $\mu = \overline{E_T}$  and  $R_{sep} = 1.5 R$  instead of  $R_{sep} = 2R$ , which is the canonical value without overlap corrections, give the best fit. The parameter  $R_{sep}$  accounts for the problem of jet separation. In the theory two partons are separated if they are more distant than  $2R$ . Experimentally, however, it may happen that the tails of two jets overlap and that the separation between the jet cones is less than  $2R$ . Thus following [3] we inserted a new parameter in the theoretical calculation:  $R_{sep}$  which is the minimum separation between two jets. By comparing with CDF data a value of  $R_{sep} = 1.3$  was found adequate [3]. (Further details for the justification of  $R_{sep}$  are found in [3]). We see that the decrease of  $R_{sep}$  as compared to the canonical value influences the behaviour of  $\rho$  for the  $r$  values near the boundary  $r = R$  whereas the change of the scale parameter influences  $\rho(r)$  for the smaller  $r$  values, larger  $\mu$ 's lead to an increase of  $\rho$ . For very small  $r$  we have the influence of higher order corrections so that we can not expect a good fit anymore. For  $\overline{E_T} = 45 \text{ GeV}$  the fit is better for small  $r$  than for large  $r$ , whereas for  $\overline{E_T} = 100 \text{ GeV}$  it is the opposite. So at  $\overline{E_T} = 45 \text{ GeV}$  we would expect a different combination of  $\mu$  and  $R_{sep}$  to give a "best fit" to the data. In general, looking at  $\rho$  as a function of  $E_T$  (or better  $x_T$ ) while keeping  $r$  fixed would require  $E_T$  dependent  $\mu, R_{sep}$  pairs. This can be seen more directly by comparing with the data of the UA1 collaboration who has measured the dependence of  $\rho$  on  $E_T$  at  $r = 0.2$ . These data show a strong decrease of  $\rho(E_T)$  when  $E_T$  is below 40 GeV ( $x_T \leq 0.12$ ), which can not be explained theoretically with fixed  $\mu/E_T$  and  $R_{sep}$ . We attribute this partly to the small  $r$  value where higher order effects and fragmentation corrections are much more important. The D0 data [10] are very similar to the CDF data and therefore have not been used for comparison with theory. As compared to earlier work [3] who obtained similar results we remark that they used the two-loop formula for  $\alpha_s$  and different structure functions. In particular the formula assumed for  $\alpha_s$  influences the  $\rho(r)$  at smaller  $r$ 's.

In order to demonstrate that the scaling behaviour (1) for the jet shape  $\rho(r)$  is useful we have taken the data for  $\rho(r)$  as measured by CDF in  $p\bar{p}$  collisions and compared in Fig. 3 with our calculations and have converted them on the basis of (1) into a prediction of  $\rho(r)$  for  $ep$  collisions at the HERA energy  $\sqrt{S} = 314 \text{ GeV}$ . We have done this for the data at  $\overline{E_T} = 45 \text{ GeV}$  and 100 GeV. For fixed  $x_T$  this translates into  $\overline{E_T} = 7.85 \text{ GeV}$  and 17.4 GeV at HERA. The averaging in  $E_T$  in the ranges 40 – 60 and 95 – 120 GeV goes over into the ranges 6.98 – 10.4 and 16.6 – 20.9 GeV, respectively. The CDF data were also averaged over  $\eta$  in the interval  $0.1 \leq |\eta| \leq 0.7$ . This averaging over  $\eta$  is not essential since  $f$  does not change for fixed  $\eta$ . In addition in the central region  $f$  is nearly independent of  $\eta$  [1]. The same range of  $\eta$  applies also to the results of the conversion at  $\sqrt{S} = 314 \text{ GeV}$ . They are shown as points in Fig. 4. In our comparison in Fig. 3 the choice of  $R_{sep} = 1.5$  gave a good fit to the CDF data. Therefore the

points in Fig. 4 are also for  $R_{sep} = 1.5$  if they should be compared to a theoretical calculation for  $ep$  scattering. This we have done for  $\sqrt{S} = 314 \text{ GeV}$  and with averaging over the respective  $E_T$  and  $\eta$  ranges given above. The results are shown as dashed ( $\overline{E_T} = 17.4 \text{ GeV}$ ) and as dotted ( $\overline{E_T} = 7.85 \text{ GeV}$ ) curves. The agreement between the "experimental" points and the curves is satisfactory. This shows that the conversion of the CDF data into  $ep$  data works also for  $R_{sep} < 2R$  ( $R_{sep} = 2R$  was chosen for the comparison in Tab. 1). Furthermore, the conversion reproduces the correct dependence of  $\rho(r, R, E_T, \eta)$  as a function of  $r$  and  $E_T$ . For fixed  $r$  the jets become narrower with increasing  $E_T$ . Concerning the quality of agreement between the points and the curves in Fig. 4 we must take into account that the fit of the theory with separation  $R_{sep} = 1.5$  to the CDF data was not perfect either. So, for example, the CDF points for  $\overline{E_T} = 100 \text{ GeV}$  in Fig. 3b are also slightly above the theoretical curve in the range  $r \leq 0.5$ . The same occurs in Fig. 4 for the points at  $\overline{E_T} = 17.4 \text{ GeV}$ .

### 3 Conclusions

We have seen that the  $E_T$  jet profiles in  $p\bar{p}$  and  $ep$  collisions are very much alike. If considered as a function of  $x_T$  instead of  $E_T$  the shape function  $(1 - \rho(r, R, x_T, \eta))/\alpha_s$  for different c.m. energies  $\sqrt{S}$  and different processes are very approximately the same. Thus for  $(1 - \rho)$  the remaining  $S$  dependence appears only via the scale dependence of  $\alpha_s(\mu)$  which is known. This is valid in particular for all  $x_T$  when only the jet shapes of one process but for different energies are considered. It is less valid for large  $x_T$  if we compare jet shapes in  $ep$  and  $p\bar{p}$  processes. In this case the effect of the anomalous quark distribution of the photon comes into play. A conversion of CDF data for  $p$  into jet shapes for  $ep$  at HERA gave very encouraging results. This shows that jet shapes in the perturbative regime, i. e. at large angles at the edge of the cone, are rather universal and independent of the c.m. energy if  $\alpha_s$  is factored out in  $1 - \rho$ . Near the jet axis the jet shape is dominated by collinear soft gluon emission. It would be interesting to see how the scaling law valid in the perturbative regime is changed in this region.

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## Table Caption

**Tab. 1:** Comparison of jet profiles for  $ep$  and  $p\bar{p}$  scattering in terms of  $f(\tau, R, E_T, \eta)$  defined in (1) for  $R = 1$ ,  $\eta_S = 0$ , c.m. energies  $\sqrt{S} = 314 \text{ GeV}$  (HERA) and  $\sqrt{S} = 1.8 \text{ TeV}$  (TEVATRON),  $x_T = 0.1$  and  $0.5$  and various  $r$ .

## Figure Captions

- Fig. 1:** Inclusive single-jet cross section in leading order (full) and in next-to-leading order (dotted) with  $R = 1$  and  $\eta_S = 0$ . Shown are the cross sections for electroproduction (upper lines) and for  $p\bar{p}$  scattering (lower lines) divided by  $4000$  both for  $\sqrt{S} = 298 \text{ GeV}$ .
- Fig. 2:**  $f_2$  as defined by (5) as a function of  $x_T$  (see (2)) for  $R = 1$ ,  $r = 0.3$  and different values of  $x_T = 0.035$  (full),  $0.1$  (dashed) and  $0.2$  (dash-dotted) for a)  $p\bar{p}$  scattering at  $\sqrt{S} = 1.8 \text{ TeV}$  and b)  $ep$  scattering at  $\sqrt{S} = 314 \text{ GeV}$ . The dotted curves are the curves of Fig. 2 a.
- Fig. 3:** The relative  $E_T$  profile versus  $r$  for  $R = 1$  and  $0.1 \leq |\eta| \leq 0.7$ . The CDF data (full circles) are compared with theoretical results for different combinations of  $(\mu/E_T, R_{sep}/E_T) = (1, 2)$  [full],  $(1, 1.5)$  [dotted] and  $(0.5, 1.5)$  [dashed] at a)  $\overline{E_T} = 45 \text{ GeV}$ , b)  $\overline{E_T} = 100 \text{ GeV}$ .
- Fig. 4:** The relative  $E_T$  profile,  $\rho$  versus  $r$  for  $R = 1$ ,  $R_{sep} = 1.5$ ,  $0.1 \leq |\eta| \leq 0.7$ ,  $\overline{E_T} = 7.85 \text{ GeV}$  (dotted) and  $\overline{E_T} = 17.4 \text{ GeV}$  (dashed) compared to  $\rho$ 's obtained from CDF data with the help of the scaling law (1). Open circles for  $\overline{E_T} = 7.85 \text{ GeV}$ , open squares for  $\overline{E_T} = 17.4 \text{ GeV}$ .

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$r$	$f(R; r)$											
	ep [HERA]		ep [ $\sqrt{s} = 1800 \text{ GeV}$ ]		$\bar{p}\bar{p}$ [ $\sqrt{s} = 314 \text{ GeV}$ ]		$\bar{p}\bar{p}$ [TEVATRON]					
	$x_T = 0.1$	$x_T = 0.5$	$x_T = 0.1$	$x_T = 0.5$	$x_T = 0.1$	$x_T = 0.5$	$x_T = 0.1$	$x_T = 0.5$				
0.95	0.142	0.151	0.147	0.154	0.148	0.191	0.146	0.193				
0.9	0.286	0.295	0.285	0.298	0.300	0.373	0.296	0.381				
0.8	0.583	0.573	0.586	0.596	0.606	0.713	0.602	0.729				
0.7	0.909	0.860	0.912	0.884	0.927	1.05	0.920	1.06				
0.6	1.25	1.15	1.25	1.18	1.28	1.37	1.28	1.38				
0.5	1.66	1.50	1.68	1.53	1.70	1.74	1.69	1.74				
0.4	2.13	1.88	2.15	1.92	2.21	2.10	2.19	2.14				
0.3	2.74	2.36	2.75	2.38	2.98	2.62	2.87	2.63				
0.2	3.75	3.09	3.76	3.13	3.91	3.40	3.85	3.40				
0.1	5.72	4.54	5.77	4.58	6.02	4.85	5.91	4.82				

Tab. 1

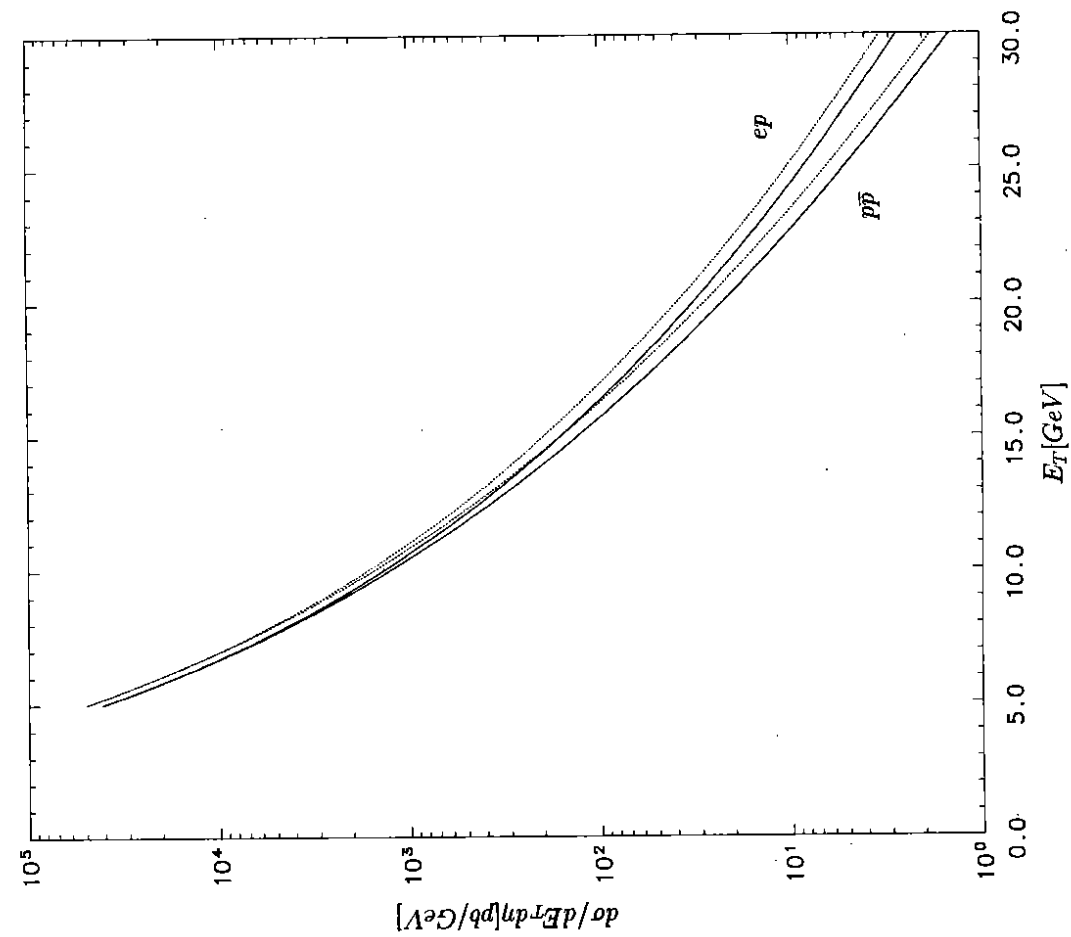


Fig. 1

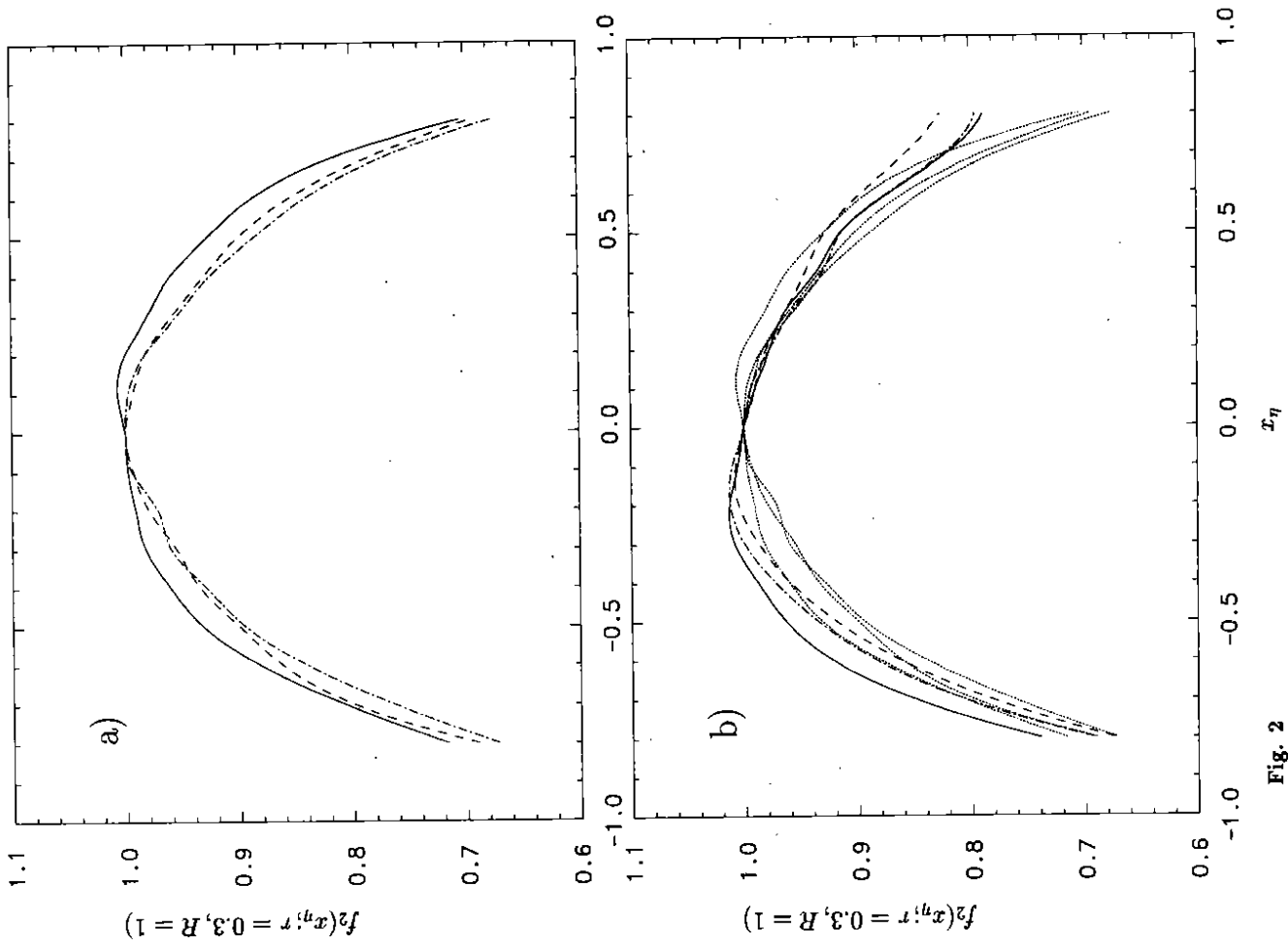


Fig. 2



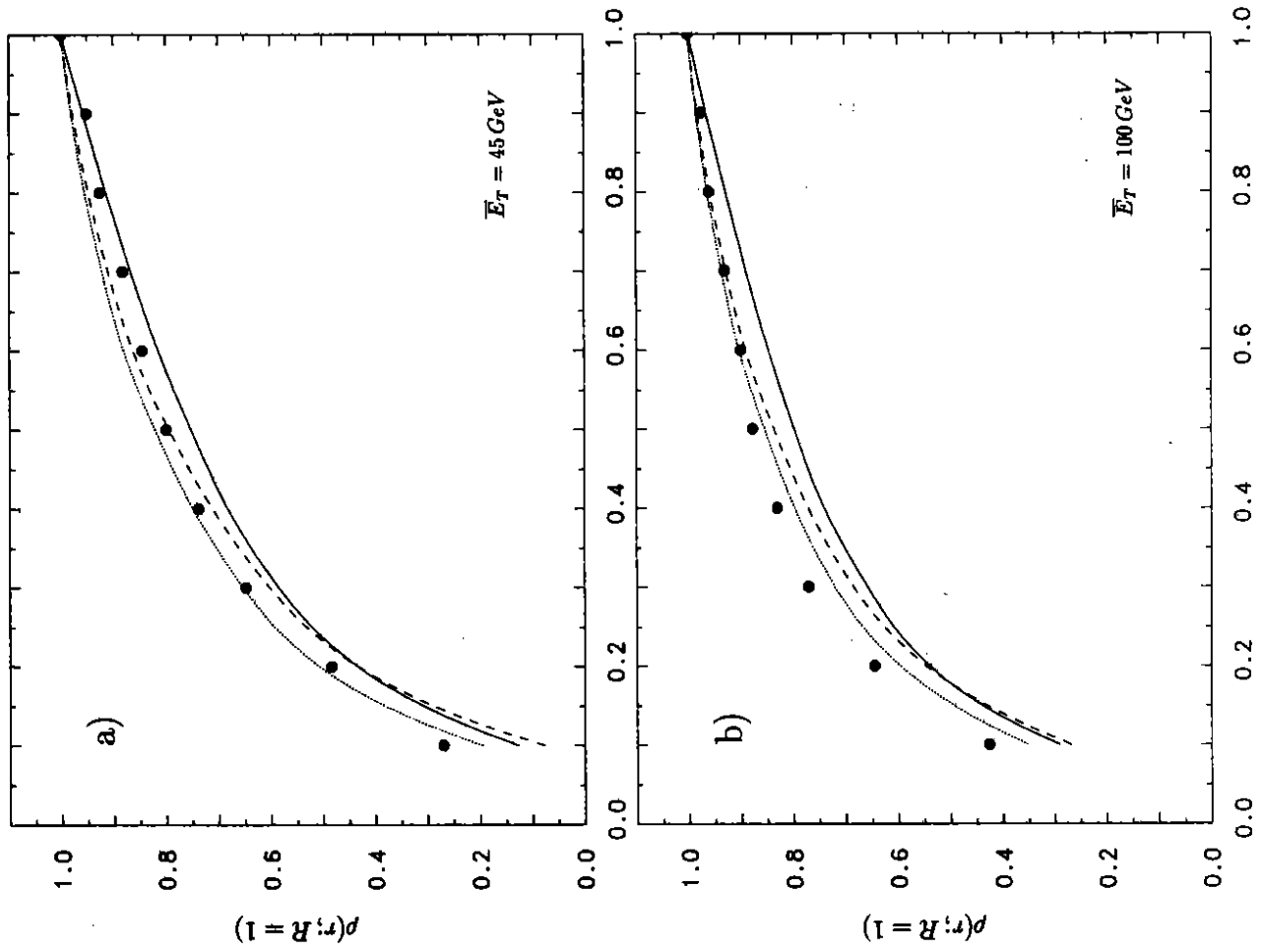


Fig. 3

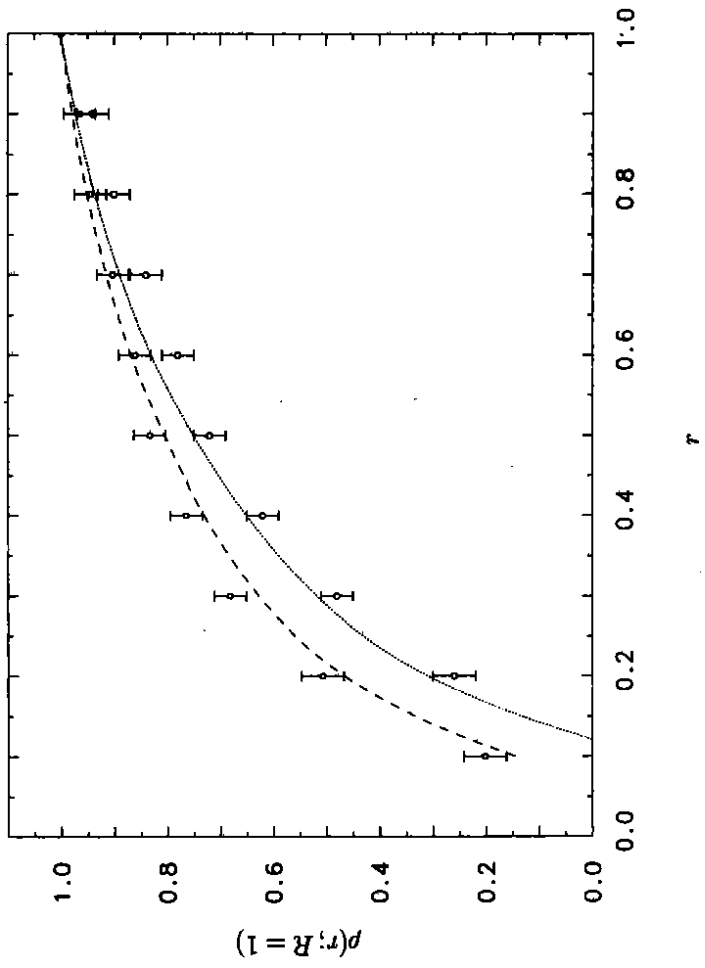


Fig. 4