Design and preparation of a single-band tunable metamaterial absorber in terahertz frequency

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Abstract

A metamaterial-based absorber is designed and measured in the 13–16 THz range. An absorption peak of 93% amplitude is achieved at resonance frequency 14.2 THz, which is excited by the bright-bright modes coupling effect. In the first set of experiments, the structural parameter D is reduced from 26 μm to 25.6 μm, resulting in this absorption peak being enhanced from 93% to 97.2% and the resonance frequency moving from 142.THz to 14.65 THz. In the second set of experiments, the thickness of SU-8 layer is increased from 2 μm to 3 μm, resulting in this absorption peak being increased to 99.1% and the resonance frequency shifting 14.05 THz when the thickness of SU-8 layer is increased from 2 μm to 3 μm. When the incidence angle of electromagnetic wave reaches 75, up to 85% absorption rate is obtained. Since the STO layer reveals the temperature-dependent property, the resonance frequency can be controlled by changing the ambient temperature.

(Some figures may appear in colour only in the online journal)

1. Introduction

Metamaterials with subwavelength scale units have attracted the attention of many researchers. This is because their unique properties that can't be found in nature, for example, negative index of refraction, lensing, and cloaking [1–7]. For example, a reported grapheme-based metamaterial device revealed the surface impedance properties different with natural materials [8]. Most of reported electromagnetic metamaterials structures contain metallic resonators, which leads to an inevitable loss of the electromagnetic wave energy. These energy absorption losses maybe degrades their performances. On the one hand, many structural design strategies are proposed to reduce this absorption loss, such as, optimizing the structure, using the gain materials to compensate loss, and using low loss materials, and so on [9–11]. On the other hand, the electromagnetic wave energy absorption loss can be leveraged to develop metamaterials absorbers. The first metamaterial absorber with a

metallic cut wire and a split ring is proposed and verified by *Landy et al* [12], which revealed an absorption peak of 88%. Since then, high-performance electromagnetic absorber based on metamaterials are developed and validated in many frequency bands [13–15]. Since it can only be operated at a fixed frequency, many proven absorbers can't be used in industrial production. Therefore, tunable metamaterial absorbers have attracted researchers' attention. *Chen et al* reported a tunable metaferrite based on grapheme layer, which revealed resonance modes in the THz and IR bands [16]. Another multi-band metamaterial-based perfect absorber is proposed by Rasoul Alaee *et al* [17]. Many tunable strategies have been proposed and proved, such as photo excitation, electric stimuli, temperature, or MEMS [18–24]. To date, another temperature tunable dielectric layer, the strontium titanate (STO) layer, has received the attention of researchers. The dielectric constant of STO can be modulated in a continuous temperature spectrum.

In this paper, a single-band tunable metamaterial absorber is designed and measured in the 13–16 THz range. An absorption peak of 93% amplitude is achieved based on the

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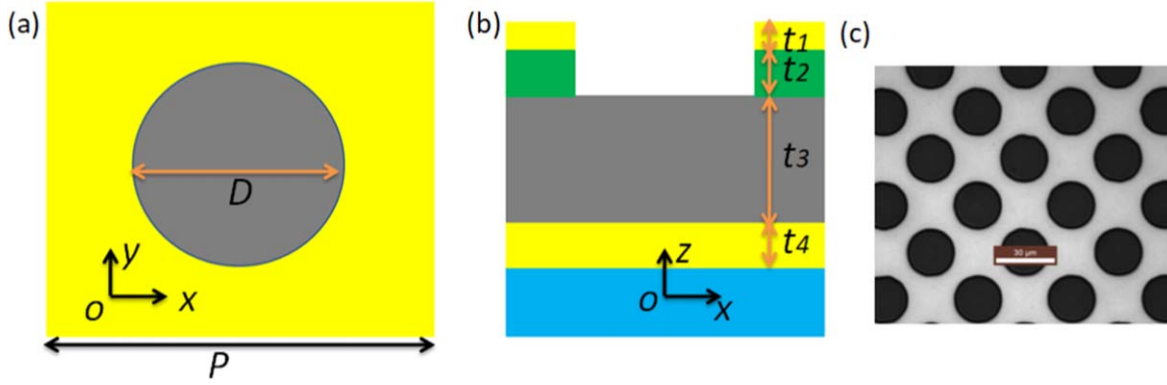[1] Author to whom any correspondence should be addressed.

Figure 1. (a) The top view of unit cell. (b) The side view of unit cell. The yellow parts are metal layers. The gray part is SU-8 layer. The green part is STO layer. The blue part is substrate. (c) Sample photo.

Table 1. Geometric parameters.

Parameter	P	D	$t1$	$t2$	$t3$	$t4$
Value(μm)	30	26	0.055	0.1	2	0.1

bright-bright modes coupling effect at the resonance frequency 14.2 THz. Specifically, this absorption peak is shifted to higher frequencies and enhanced to 97.2% with the structural parameter D reducing, while it is shifted to lower frequencies and enhanced to 99.1% with the thickness of SU-8 layer increasiong. Moreover, the resonance frequency is shifted from 14.2 THz to 14.9 THz when the environment temperature is increased from 300 K to 380 k. Finally, up to 85% absorption rate can be obtained under incidence angle 75°.

2. Cell structure, model, and experiment

2.1. Unit structure and model

The designed unit cell can be found in figure 1. This unit cell contains four layers: the top metal layer is patterned with a round holes array. The second layer is a STO layer with the same array. The third layer is a complete SU-8 layer. The bottom layer is a complete metal layer. All of structure parameters can be found in table 1. In simulation, metal layers are given as follows:

$$\varepsilon(\omega) = 1 - \frac{\omega_P^2}{\omega^2 - i\omega\gamma_D} \tag{1}$$

In the equation above, $\gamma_D = 9 \times 10^{13}\,\text{s}^{-1}$ is collision frequency, $\omega_p = 1.37 \times 10^{16}\,\text{s}^{-1}$ is plasma frequency [25]. Simulations are revealed by the full-wave HFSS Ansoft. Floquet ports are used at top and bottom of the unit cell, and ideal electromagnetic boundary conditions are applied for sidewalls [26]. The permittivity of the STO layer is calculated as follows [27, 28]:

$$\varepsilon_w = \varepsilon_\infty + \frac{f}{w_o^2 - w^2 - iw\gamma} \tag{2}$$

In the above equation, ε_∞ is high-frequency bulk permittivity. $f = 2.6 \times 10^6\,\text{cm}^{-2}$ is oscillator strength. The w_0 is soft mode frequency, which can be achieved as follows:

$$w_o(T)[\text{cm}^{-1}] = \sqrt{31.2(T - 42.5)} \tag{3}$$

And the γ is soft mode damping factor, which can be revealed as follows:

$$\gamma(T)[\text{cm}^{-1}] = -3.3 + 0.094\,\text{T} \tag{4}$$

In above equation, T is ambient temperature.

2.2. Experiments

The samples are produced as follows: Before the experiments, a glass piece (cleaning and drying) is first selected as the substrate. Second, the bottom metal layer is deposited on the glass piece (Equipment device: ZZL-U400C). Third, the SU-8 will be spun on this metal layer (Equipment device: MSC-400Bz-6N spinner) and dried (Equipment device: C-MAG HP10). Fourth, the STO layer is deposited on the SU-8 layer (Equipment device: ZZL-U400C). Fifth, the top metal layer is deposited on the STO layer (Equipment device: ZZL-U400C). Sixth, the proposed array is defined through electron beam lithography (CABL-9000C) on the top metal layer.

3. Results and discussion

3.1. Physical mechanism of absorption peaks

The measured absorption spectrum is shown in figure 2. An absorption peak of 93% amplitude is achieved at the resonance frequency 14.2 THz. The simulated absorption spectrum is achieved by the HFSS, as shown in figure 2. In simulation, the transmission rate is zero due to the bottom metal layer is thick enough. The simulated reflection rate can be achieved based on the coupled mode theory (CMT), as follows [29–31]:

$$r = \frac{s_-}{s_+} \frac{j(\omega - \omega_o) + \delta - \gamma_e}{j(\omega - \omega_o) + \delta + \gamma_e} \tag{5}$$

$$A = 1 - |r|^2 = \frac{4\delta\gamma_e}{(\omega - \omega_o)^2 + (\delta + \gamma_e)^2} \tag{6}$$
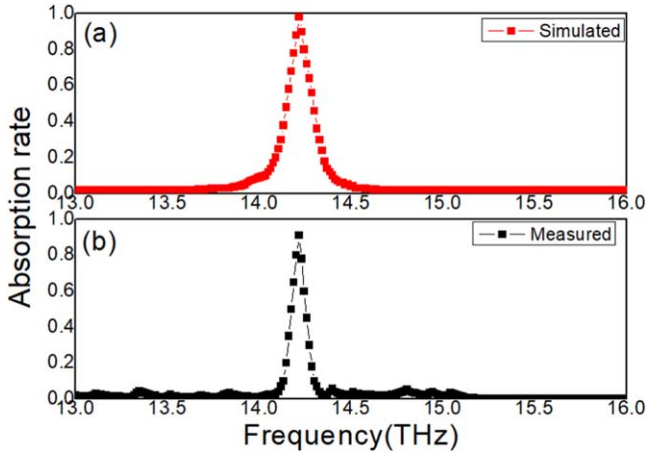
Figure 2. (a) Simulated absorption spectrum. (b) Measured absorption spectrum.

In this above equation, $s+$ and $s-$ are input and output waves of amplitudes. The δ is intrinsic loss rate. The γ_e is external leakage rate. The quality factor Q can be revealed as follows:

$$Q = \frac{f_o}{\Delta f} \tag{7}$$

Here, the f_o is the resonance frequency, and the Δf is the full width at half maximum (FWHM). Based on the measured results in figure 2, the total quality factor is Q = 142. To reveal the physical mechanism of this absorption peak, the electric field strength and current intensity are simulated at the resonance frequency 14.2 THz, as shown in figure 3. It is found that the current intensity is mainly concentrated on the surface of the top metal layer, as shown in figures 3(a), (b). Two bright modes are excited on the edges of the metal holes array, as shown in figures 3(c), (d). Moreover, the bright-bright modes coupling effect is also achieved, which results in the absorption peak at the resonance frequency 14.2 THz.

3.2. Influence of structural parameters

In the first set of experiments, the structural parameter D is set as 26 μm, 25.8 μm, and 25.6 μm, respectively (other structural parameters are unchanged). Figure 4 shows the measured absorption spectrum with different structural parameter D. It can be found that the absorption is enhanced from 93% to 97.2% by reducing the diameter of holes, as shown in figure 4. The resonance frequency of peak shows a blue shift from 14.2 THz to 14.65 THz for the change of 0.4 μm in the structural parameter D. In the second set of experiments, the thickness of SU-8 layer is set as 2 μm, 2.5 μm, and 3 μm, respectively (other structural parameters are also unchanged). The maximum peak absorption is enhanced from 93% to 99.1%, as shown in figure 5. The resonance frequency shows a red shift from 14.2 THz to 14.05 THz for the change of 1 μm in the structural parameter $t3$. The shift of resonance frequency is obviously smaller than that of figure 4.

To reveal the physical mechanism of these resonance behaviors in figures 4 and 5, an equivalent *LC* circuit model is proposed, as shown in figure 6. When electromagnetic waves are incident on the sample, the induced electric fields and current are achieved on the surface of metal layers. Two equivalent capacitances are also achieved based on these induced electric fields. Therefore, the equivalent *LC* circuit model can be given as follows [9, 32, 33]:

$$f = \frac{1}{2\pi \sqrt{(2L_1 + L_2) \cdot \dfrac{2C_1 \cdot C_2}{C_1 + 2C_2}}} \tag{8}$$

Here, the above formula can be simplified. This is because the majority induced current is excited on the surface of the top metal layer, and the equivalent capacitance C_2 is much higher than that of the equivalent capacitance C_1, which leads to the equivalent capacitance of the total sample is equal to C_1:

$$f \approx 2\pi \sqrt{C_1 \cdot (2L_1 + L_2)} \tag{9}$$

When the structural parameter D is reduced, the equivalent capacitance C_1 is increased synchronously. Therefore, the absorption peak is shifted to higher frequencies according to the equation (9). When the thickness of the SU-8 layer $t3$ is increased, the vertical distance between the top and bottom metal layers is increased. The equivalent inductance L_2 in the bottom metal layer is reduced, which results in the reduction of the resonance frequency according to the equation (9).

3.3. Influence of temperature

The effect of temperature on the absorption peak is revealed in experiments. The measured absorption spectrum with different temperatures (D = 26 μm, and t3 = 2 μm) is shown in figure 7. The maximum absorption value is reduced from 93% to 90.4% with the ambient temperature increasing from 300 K to 380 K. Moreover, the resonance frequency of samples is shifted from 14.2 THz to 14.9 THz. The total frequency shift is 0.7 THz, which is corresponding to 80 K of temperature change. The resonance properties of the metal layers, the SU-8 layer, and the substrate are stable to temperature. This resonance frequency shift is directly related to the STO layer in samples. To understand this relationship, the permittivity and loss tangent of the STO layer are calculated under different temperature conditions, as shown in figure 8. When the temperature is increased, the real part of permittivity of the STO layer is reduced significantly, as shown in figure 8(a), which is also consistent with the equation (2). Based on the perturbation theory, the resonance frequency shift of samples due to the material perturbation of STO layer can be given as follows [34–36]:
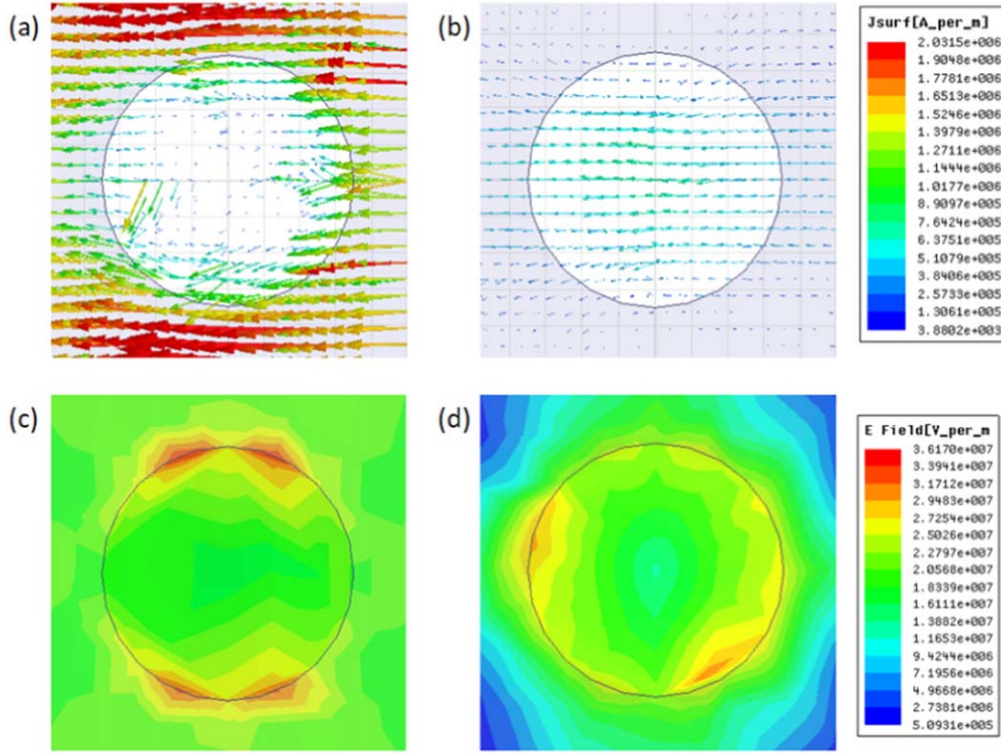
Figure 3. (a) The simulated current intensity on the surface of the top metal layer at resonance frequency 14.2 THz. (b) The simulated current intensity on the surface of the bottom metal layer at resonance frequency 14.2 THz. (c) The simulated electric field strength on the sur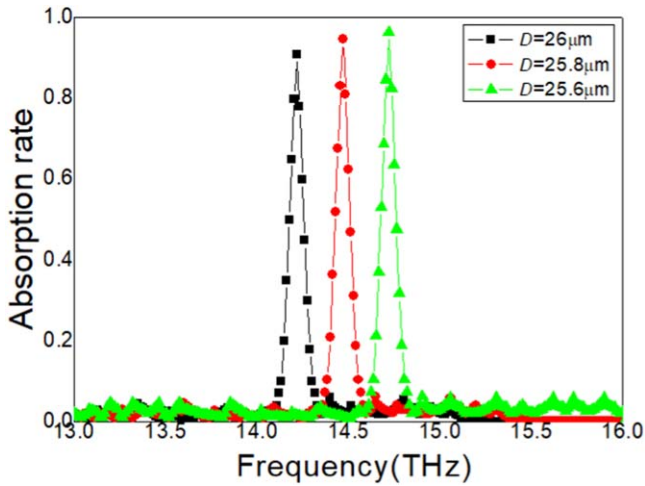face of the top metal layer at resonance frequency 14.2 THz. (d) The simulated electric field strength on the surface of the bottom metal layer at resonance frequency 14.2 THz.

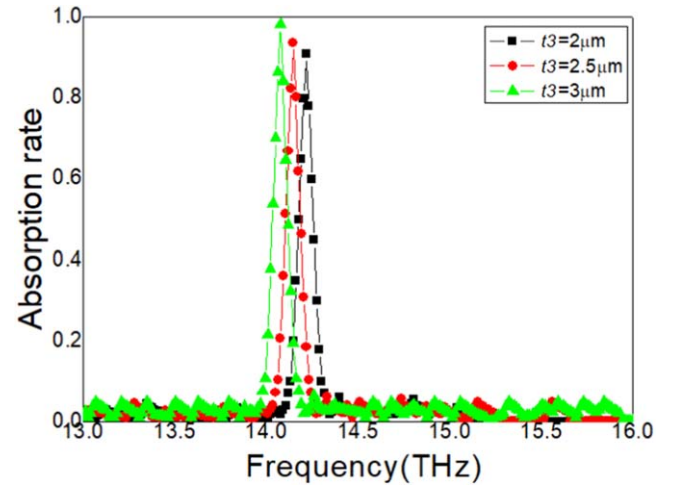**Figure 4.** The measured absorption spectrum with different structural parameter *D*.

Figure 5. The measured absorption spectrum with different structural parameter t3.

$$\frac{\Delta \omega}{\omega} = \frac{\omega - \omega_o}{\omega_o}$$

$$\approx \frac{- \iiint_V [(\Delta \vec{\varepsilon} \cdot \vec{E}) \cdot \vec{E}_o^* + (\Delta \vec{\mu} \cdot \vec{H}) \cdot \vec{H}_o] dV}{\iiint (\varepsilon |\vec{E}_o|^2 + \mu |\vec{H}_o|^2) dV} \quad (10)$$

Where, the $\Delta \vec{\varepsilon}$ is the change of permittivity of the STO layer and $\Delta \vec{\mu}$ is the change of permittivity of the STO layer. The $\vec{E}_o$ and $\vec{H}_o$ are the unperturbed electric and magnetic fields, respectively. The $\vec{E}$ and $\vec{H}$ are the perturbed electric and magnetic fields, respectively. As the temperature increases, the real part of the permittivity is reduced, which results in a $\Delta \vec{\varepsilon}$ less than zero. Moreover, the resonance frequency of samples is increased according to the equation (10). Therefore, the absorption peak is shifted to higher frequencies in figure 7. On the other hand, the loss tangent of the STO layer
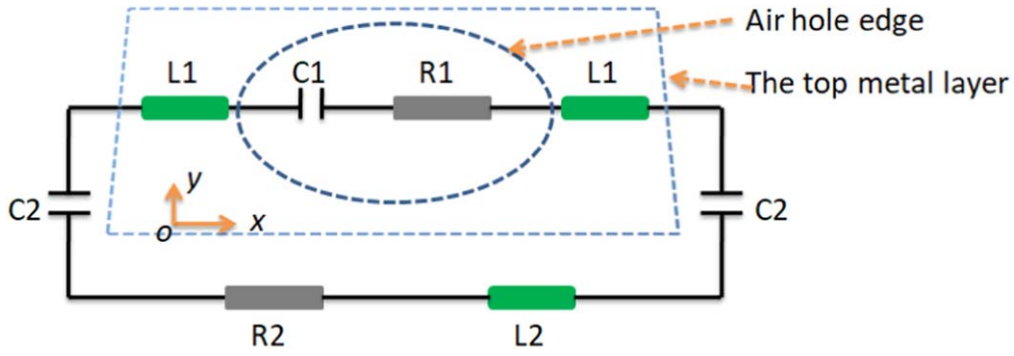
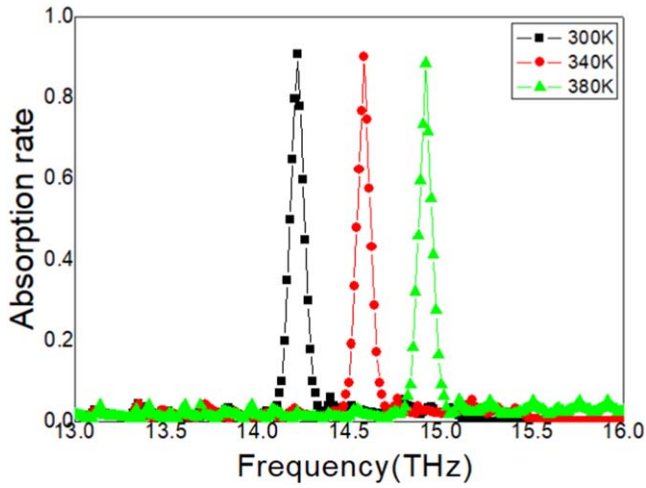**Figure 6.** Equivalent *LC* circuit model of unit cell.

Figure 7. The measured absorption spectrum with different temperatures.
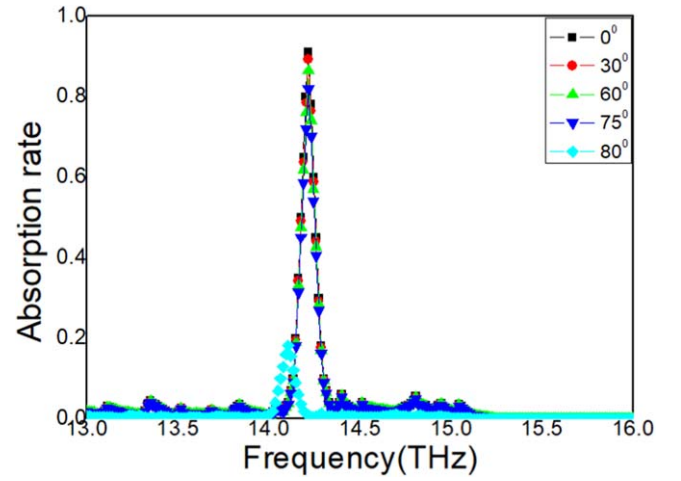

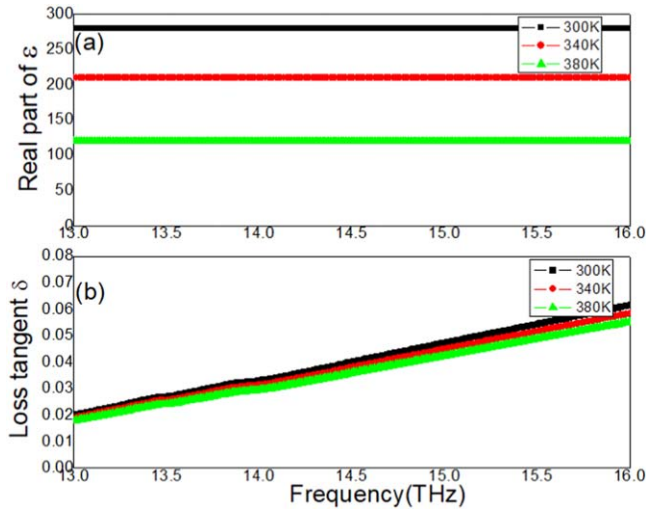**Figure 9.** The measured absorption spectrum with different incidence angles.

Figure 8. (a) The real part of permittivity of the STO layer with different temperature. (b) The loss tangent of the STO layer with different temperature.

is reduced with the temperature increasing, which leads to the dielectric loss of electromagnetic energy in the STO layer reduce and the absorption peak reduce synchronously.

3.4. Influence of incident angle

The absorption stabilities of samples with oblique incidence angles are also measured. The measured absorption spectrum is shown in figure 9 ($D = 26 \ \mu$m, t3 = 2 μm, and T = 300 K). The resonance frequency of the absorption peak is almost unchanged with the incidence angle incresing from $0°$ to $75°$. When the incidence angle is increased to $80°$, the resonance frequency is shifted to the lower frequency 14.1 THz, as shown in figure 9. The maximum absorption is larger than 85% when the incidence angle is lower than $75°$. However, when the incidence angle is increased to $80°$, the maximum absorption is abnormally reduced. Therefore, the high absorption performance can be obtained when the incidence angle is lower than $75°$. To reveal the abnormally reduction of the absorption peak in figure 9, the electric field strength distribution is calculated at the resonance frequency point 14.1 THz, as shown in figure 10. Only one bright mode is excited in the top layer, and no bright mode can be excited in the bottom metal, as shown in figure 10(a). The resonance intensity of this bright mode is so weakly, far below the results of figure 3(c). Moreover, the coupling between bright-bright modes can't be found, which leads to the abnormally reduction of the absorption peak. This is because the absorption peak is derived from the resonance and coupling
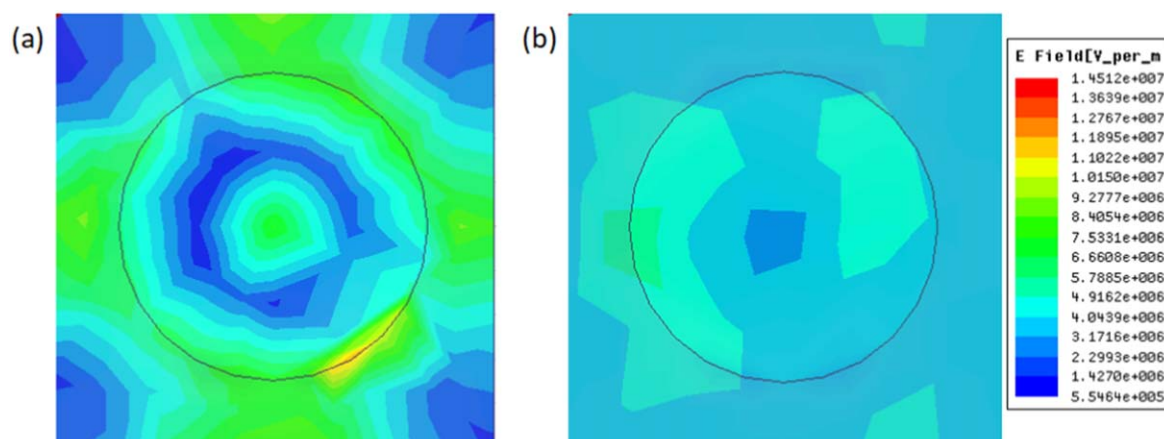
Figure 10. The simulated electric field strength distribution at the resonance frequency point 14.1 THz. (a)The top metal layer. (b) The bottom metal layer.

of bright modes, as shown in figure 3. When the incidence angle is larger than 80°, the coupling effect between the electromagnetic wave and the induced electric field is failed. As a result, these bright modes are not to be effectively activated, as shown in figure 10.

4. Conclusion

In conclusion, a single-band tunable metamaterial absorber is demonstrated in the 13–16 THz range. The absorption peak (93% amplitude) is excited by the bright-bright modes coupling effect at the resonance frequency 14.2 THz. The effect of the structural parameters (D and t3) on the absorption peak is revealed in experiments. The absorption peak is tunable through changing the structure parameters individually. High absorption performance (up to 85%) is obtained under the incidence angle 75°. Since the permittivity of the STO layer is sensitive to the temperature change, this absorption peak is tunable by changing the ambient temperature. The resonance frequency is shifted from 14.2 THz to 14.9 THz with the environment temperature increasing from 300 K to 380 k.

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