



Polarization Constraints on the Geometry of the Magnetic Field in the External Shock of Gamma-Ray Bursts

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Abstract

We study the ensemble of linear polarization measurements in the optical afterglows of long-duration gamma-ray bursts. We assume a non-sideways-expanding top-hat jet geometry and use the relatively large number of measurements under the assumption that they represent a statistically unbiased sample. This allows us to constrain the ratio between the maximum predicted polarization and the measured one, which is an indicator of the geometry of the magnetic field in the downstream region of the external shock. We find that the measured polarization is substantially suppressed with respect to the maximum possible for either a completely ordered magnetic field parallel to the shock normal or to a field that is entirely contained in the shock plane. The measured polarization is limited, on average, to between 25% and 30% of the maximum theoretically possible value. This reduction requires the perpendicular component of the magnetic field to be dominant in energy with respect to the component parallel to the shock front, as expected for a shock-generated and/or shock-compressed field. We find, however, that the data only marginally support the assumption of a simple top-hat jet, pointing toward a more complex geometry for the outflow.

Unified Astronomy Thesaurus concepts: [Gamma-ray bursts \(629\)](#); [Polarimetry \(1278\)](#); [Non-thermal radiation sources \(1119\)](#)

1. Introduction

The structure of gamma-ray burst (GRB) jets and the origin and geometry of their magnetic field are still openly debated. The magnetic field within the GRB outflow is supposed to play a dominant role in the initial collimation of the outflow, and possibly in its acceleration (e.g., Tchekhovskoy et al. 2008). In synchrotron models, such as the internal shock synchrotron model (Rees & Meszaros 1994; Sari & Piran 1997; Daigne & Mochkovitch 1998; Burgess et al. 2019) or the ICMART model (Zhang & Yan 2011), magnetic fields also play a fundamental role in the emission of the γ -ray radiation. By contrast, in the photospheric model radiation is advected in the outflow and released when the flow becomes transparent (Pe’er et al. 2005, 2006; Giannios 2006; Lazzati et al. 2009, 2013; Beloborodov 2011, 2013). Even in this case, however, magnetic fields are expected to play an important role by providing the source of soft photons that is required to explain the low-frequency spectrum of typical GRBs (Vurm & Beloborodov 2016). Despite its important role, little is known about the field’s structure and origin. It could be originating from the inner engine itself (field advected from the engine) or generated at internal shock within the flow.

During the afterglow phase, synchrotron emission originates from the circumburst material swept up by the external shock and the field must be shock-generated (Mészáros & Rees 1997; Sari et al. 1998). Models to predict the amount and temporal evolution of the linear polarization in the external shock phase rely on asymmetries in the field structure and/or in the outflow structure. One possibility is that the field is fully ordered in domains or patches of a size that is smaller than the observed

emitting surface. The field among domains is, however, uncorrelated. This leads to partial cancellation, with a residual variable linear polarization of the order of up to 10% and variable position angle (Gruzinov & Waxman 1999). Alternatively, one can consider a collimated outflow with a shock-generated field. The field is then expected to have cylindrical symmetry around the normal to the shock front, with either the parallel or perpendicular components dominating. If the viewer is not perfectly aligned with the jet axis, linear polarization is expected, with a well-defined intensity evolution and constant position angle, except for a sudden switch of 90° around the time of the so-called jet break (Ghisellini & Lazzati 1999; Sari 1999; Granot & Königl 2003), when the polarization momentarily vanishes. Additional variations of this behavior are predicted in the case of structured outflows, with bright, powerful cores surrounded by layered wings of decreasing energy (Rossi et al. 2002; Zhang & Mészáros 2002; Granot & Kumar 2003; Kumar & Granot 2003). In these geometries, the polarization has a constant position angle and peaks around the time of the jet break, when the powerful jet core comes into view along the line of sight (Rossi et al. 2004).

Despite these predictions, the structure of the magnetic field remains outstandingly unknown. The measured polarization depends on the ratio of the magnetic energy densities in the parallel and perpendicular components (Gruzinov & Waxman 1999; Sari 1999); however, a firm measurement of such ratio is hampered by the fact that the polarization depends on the off-axis angle, which is difficult to measure robustly from the data (e.g., Salmonson 2003; Rossi et al. 2004; van Eerten & MacFadyen 2013). The only event for which an off-axis angle measurement is available is the short-duration burst GRB170817A associated with the gravitational binary merger GW170817 (Gill & Granot 2018; Lazzati et al. 2018; Mooley et al. 2018; Ghirlanda et al. 2019). In this case, however, only an upper limit for the polarization exists. Nonetheless, a



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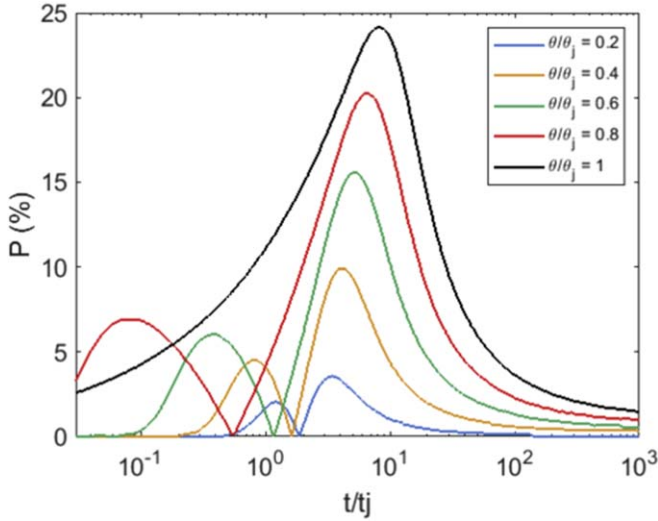


Figure 1. Maximum theoretical polarization curves from a top-hat jet with magnetic field entirely contained in the plane of the shock and no sideways expansion. Each line represents the polarization curve for a value of $\theta_{\text{obs}}/\theta_j$. Data are from Rossi et al. (2004).

constraint on the magnetic field geometry was possible (Gill & Granot 2019).

In this paper we adopt a statistical approach by considering observations from all available GRBs. While the off-axis angle is not known for each individual event, one can safely assume that, within the top-hat jet model, the probability distribution of off-axis angles θ_{obs} is $p(\theta_{\text{obs}}) \propto \sin \theta_{\text{obs}}$. In this way we can derive a robust value for the parameter ζ , the ratio of the measured polarization to the maximum observable for a completely ordered magnetic field. From the value of ζ we can then derive a constraint on the magnetic field intensity ratio. As we thoroughly discuss in Section 4, however, the choice of a top-hat jet brings in some significant simplifications that cannot be overlooked when interpreting our numerical results, and is only marginally supported by the data.

2. Methods

In the following we describe the methodology used to derive a constraint on the ratio between the theoretically achievable linear polarization in a GRB afterglow ($P_{\text{th,max}}$) and the measured value of linear polarization P . We call this ratio $\zeta \leq 1$ and we therefore have

$$P = \zeta P_{\text{th,max}}. \quad (1)$$

We assume that the maximum theoretical value is given by the calculations from various authors (e.g., Ghisellini & Lazzati 1999; Sari 1999; Granot et al. 2002; Granot & Königl 2003; Rossi et al. 2004) and we adopt as our fiducial model the results from Rossi et al. (2004) for a top-hat jet with no sideways expansion (see their Figure 8). The resulting maximum theoretical curves are shown in Figure 1 as a function of time over jet break time and for selected values of the off-axis angle. We also assume that ζ is constant among all bursts and that it is independent of either time or off-axis angle.

We use for our analysis the data collected in Covino & Gotz (2016) that report measurements of linear polarization P and the time t at which each measurement was taken with respect to the start of the burst. An independent literature search was performed to obtain the jet break times t_j for computing the

measurement times in units of the break time, as needed for the model (see Figure 1). The bursts for which reliable linear polarization and break time measurements are available are reported in Table 1, along with a reference for the break time estimates and polarization measurements. Of all the data points available, there were some that did not meet our selection criteria. Any polarization measurement with less than $3 - \sigma$ significance was discarded. In addition, any polarization measurement with an associated jet break time of $\frac{t}{t_j} < 0.1$ was discarded to avoid contamination from the reverse shock emission. The burst GRB090102 was discarded because of a large uncertainty in the jet break time (Gendre et al. 2010), while GRB990712 was discarded due to the lack of an observable jet break (Björnsson et al. 2001). GRB030329 was discarded because its light curve is complex with many re-brightening events (Greiner et al. 2003), and it is therefore not expected to follow the model predictions. Finally, GRB121024A was discarded since it is unique in displaying circular polarization (Wiersema et al. 2014). The final data set is shown in Figure 2.

The main difficulty in evaluating the ratio ζ is that the observation angle θ_{obs} for the bursts in our sample is unknown, while in the model θ_{obs} has a dramatic effect on the polarization levels (see Figure 1). To overcome this difficulty we use a statistical approach under the assumption that, for a top-hat jet, the probability of detecting a burst at an angle θ_{obs} from the jet axis is $p(\theta_{\text{obs}}) \propto \sin \theta_{\text{obs}}$. Since the theoretical polarization depends on the ratio of the observer angle over the jet opening angle $\theta_{\text{obs}}/\theta_j$, we adopt $\theta_j = 10^\circ$ throughout the analysis. We will show, however, that the final result does not depend on this particular choice for any reasonable assumed θ_j .

For each observer time t_{obs}/t_j , we run a Monte Carlo simulation drawing 10^7 observing angles from a $\sin \theta$ probability distribution. We then use the predicted polarization (Rossi et al. 2004) to derive the probability distribution of the observed polarization for $\zeta = 1$. An example of the derived distributions is shown in Figure 3. By repeating this process for every observation we obtain a set of probability distributions, each associated with one polarization measurement. Under our assumption that all bursts are statistically drawn from a single population with only the viewing angle as a variable we can now evaluate a best value for our ratio ζ that maximizes the probability of the measurement sample.

Let $p_1(P, t/t_j)dP$ be the probability of measuring a polarization value within an interval dP around the value P , for an observed time t/t_j , and $\zeta = 1$, i.e., the maximum theoretical value. For a given $\zeta < 1$ we then have

$$p_\zeta(P, t/t_j) = \frac{1}{\zeta} p_1\left(\frac{P}{\zeta}, t/t_j\right). \quad (2)$$

We therefore have that the log-likelihood of all our measurements sharing a single value of $\zeta < 1$ is given by

$$\mathcal{L}_\zeta = \sum_i \log \left\{ \left[\frac{1}{\zeta} p_1\left(\frac{P_i}{\zeta}, t_i/t_j\right) \right] * G(\sigma_{P_i}) \right\}, \quad (3)$$

where the index i runs over all the measurements in Table 1. Note that the probability distributions are convolved with a Gaussian function $G(\sigma_{P_i})$ with standard deviation equal to the uncertainty of the polarization measurements. This is done to smooth out sharp features in the theoretical probability

Table 1
The Observational Data Used in This Simulation

GRB	$\frac{t}{t_j}$	P	Ref (t_j)	Ref (P)
990510	0.51	1.7 ± 0.2	Stanek et al. (1999)	Covino et al. (1999)
	0.57	1.6 ± 0.2		Wijers et al. (1999)
020405	0.73	1.5 ± 0.4	Price et al. (2003)	Masetti et al. (2003)
	1.3	1.96 ± 0.33		Covino et al. (2003)
	1.9	1.47 ± 0.43		Covino et al. (2003)
020813	3.08	1.07 ± 0.22	Lazzati et al. (2004)	Gorosabel et al. (2004)
	3.21	1.42 ± 0.25		Gorosabel et al. (2004)
	3.34	1.11 ± 0.22		Gorosabel et al. (2004)
	3.48	1.05 ± 0.23		Gorosabel et al. (2004)
	3.82	1.43 ± 0.44		Gorosabel et al. (2004)
	6.78	1.26 ± 0.34		Gorosabel et al. (2004)
021004	0.13	0.51 ± 0.1	Holland et al. (2003)	Lazzati et al. (2003)
	0.14	0.71 ± 0.13		Rol et al. (2003)
030328	1.54	2.4 ± 0.6	Maiorano et al. (2006)	Maiorano et al. (2006)
080928	0.68	2.5 ± 0.5	Leventis et al. (2014)	Covino & Gotz (2016)
091018	0.53	1.07 ± 0.3	Wiersema et al. (2012)	Wiersema et al. (2012)
	0.98	1.44 ± 0.32		Wiersema et al. (2012)
	2.46	1.73 ± 0.36		Wiersema et al. (2012)
	2.50	3.25 ± 0.35		Wiersema et al. (2012)
	2.53	1.99 ± 0.35		Wiersema et al. (2012)
	2.57	1.42 ± 0.36		Wiersema et al. (2012)
	3.01	0.97 ± 0.32		Wiersema et al. (2012)
	3.13	1.08 ± 0.35		Wiersema et al. (2012)
	5.16	1.45 ± 0.37		Wiersema et al. (2012)

Note. From left to right: gamma-ray burst, time relative to jet break time, the polarization measurement, and reference for the jet break time.

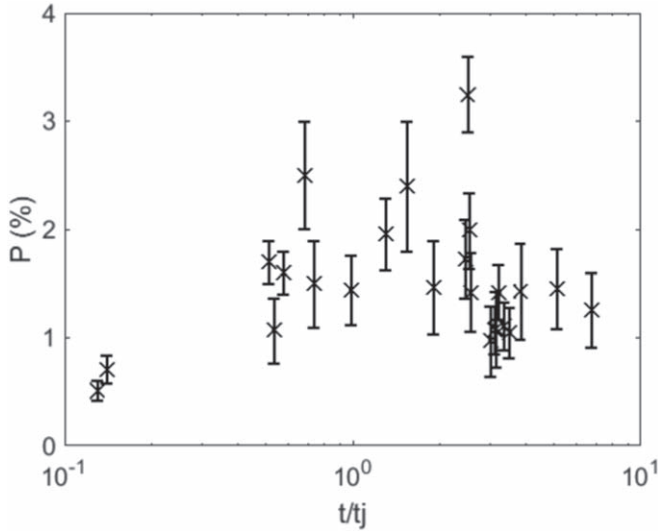


Figure 2. Linear polarization measurements used in this study vs. the time of the measurement in units of the jet break time. Data from Covino & Gotz (2016).

distributions that could not be reproduced in a data set that is affected by uncertainties.

3. Results

The value of the log-likelihood as a function of the parameter ζ is shown in Figure 4. We found that the value of ζ with the maximum likelihood was

$$\zeta \sim 0.25, \quad (4)$$

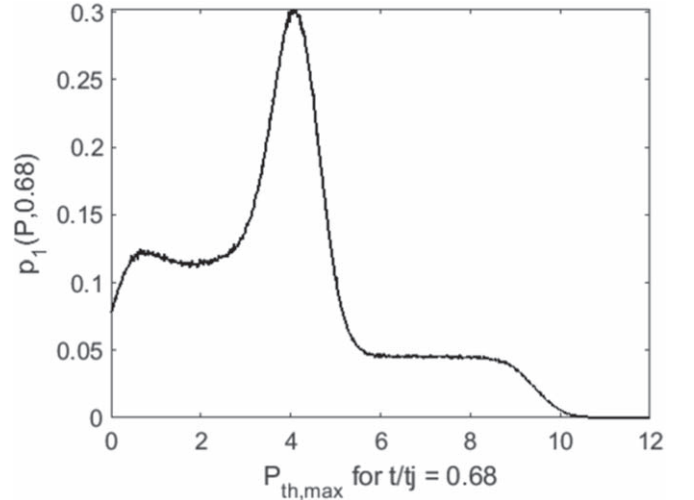


Figure 3. Polarization probability distribution for $\zeta = 1$ at the time $t_{\text{obs}}/t_j = 0.68$.

but a second high-probability peak is visible at $\zeta \sim 0.3$. The red line in Figure 4 marks the $1 - \sigma$ confidence region and is obtained by allowing for a drop of $1/2$ in the log-likelihood below its best value. The most likely value of ζ did not change significantly with a change in the assumed value of θ_j . The independence of the probability distribution on the assumed value of θ_j also ensures that our result would remain unaltered even if we assumed a probability distribution for the jet opening angle of different bursts.

The fact that $\zeta = 0.25$ maximizes the likelihood does not ensure that the model is consistent with the data. In order to verify this, we compare the distribution of measured

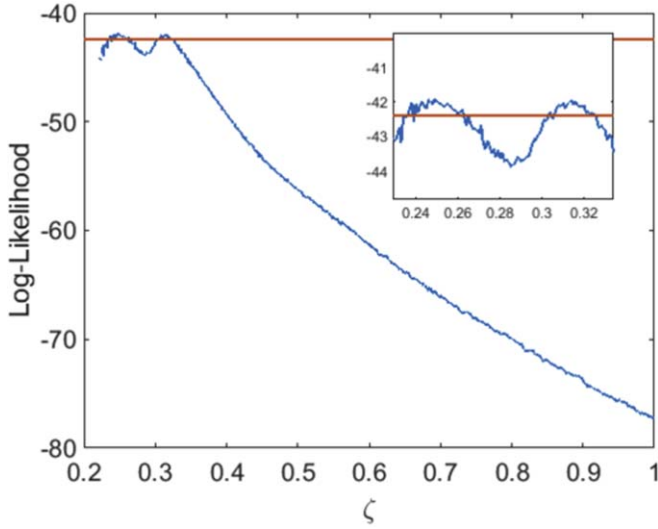


Figure 4. Log likelihood vs. ζ . The red line shows the log-likelihood value of 0.5 less than the maximum that it is used to evaluate the uncertainty on ζ . The inset is a zoom of the region around the maximum.

polarization with the average of the individual distributions $p_{0.25}(P, t_i/t_j)$. The comparison is shown in Figure 5. A comparison of the predicted and observed polarization rates was done using the Kolmogorov–Smirnov test. This test resulted in a probability $p_{KS} = 3 \times 10^{-5}$ that the observed and model points came from the same distribution. As can be seen in Figure 5, there is a range between 2.5% and 6% polarization predicted in the model that is not accounted for in the observations.

To put our result in context, consider that the observed polarization is related to the ratio of the energy density of the parallel and perpendicular components of the magnetic field (Gruzinov & Waxman 1999; Sari 1999; Granot & Königl 2003)

$$b = 2 \frac{\langle B_{\parallel}^2 \rangle}{\langle B_{\perp}^2 \rangle} \quad (5)$$

through the equation

$$\frac{P}{P_{\text{local,max}}} = \frac{(b-1)\sin^2 \theta'}{2 + (b-1)\sin^2 \theta'}, \quad (6)$$

which relates the observed polarization in a given direction P with the one locally achievable in a fully ordered field $P_{\text{local,max}}$ for a viewer at a comoving angle θ' from the shock normal. Since most of the radiation from a burst afterglow comes from a thin ring at $\theta' = 90^\circ$ (Panaitescu & Mészáros 1998; Granot et al. 1999), we simplify the equation as

$$\frac{P}{P_{\text{th,max}}} \simeq \frac{b-1}{b+1} \quad (7)$$

after integration over the emitting surface. A more precise relationship between b and ζ would require a case-by-case integration over the emitting surface that is beyond the scope of this paper (see, e.g., Gill & Granot 2019). Note that the above equation predicts the possibility of negative polarization, which is impossible. Polarization sign, in this case, is used as an indication of the position angle of linear polarization. Polarization of opposite sign imply position angles orthogonal to each other. Since we cannot investigate position angle, our

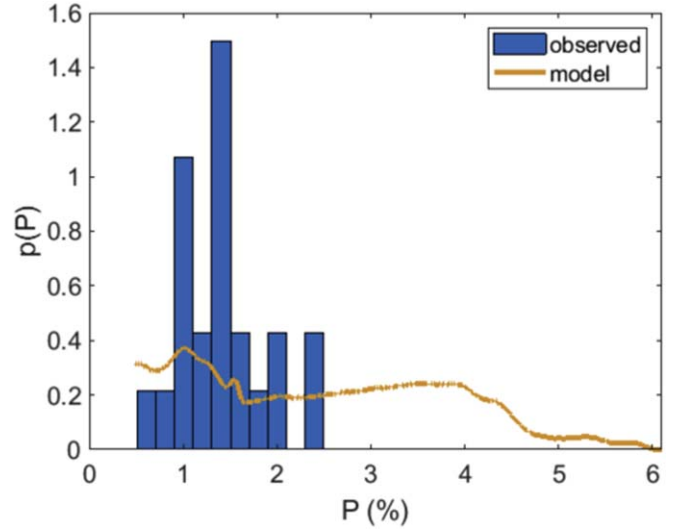


Figure 5. Comparison between the histogram of observed polarization (blue) and the average probability distribution for the most probable value $\zeta = 0.25$ (orange solid line).

value of ζ should be allowed to be negative as well as positive. We therefore find a double constraint on the geometry of the magnetic field:

$$b = 2 \frac{\langle B_{\parallel}^2 \rangle}{\langle B_{\perp}^2 \rangle} \sim 1.67; 1.86 \quad (8)$$

and

$$b = 2 \frac{\langle B_{\parallel}^2 \rangle}{\langle B_{\perp}^2 \rangle} \sim 0.6; 0.54, \quad (9)$$

where the first number corresponds to the most probable $\zeta = 0.25$ and the second to the secondary probability peak at $\zeta = 0.3$. All values are consistent with the estimate $0.5 \lesssim b \lesssim 2$ obtained by Granot & Königl (2003). We notice that, in all cases, the perpendicular component of the field dominates: $\langle B_{\perp}^2 \rangle = 1.2 \langle B_{\parallel}^2 \rangle$, $1.1 \langle B_{\parallel}^2 \rangle$, $3.3 \langle B_{\parallel}^2 \rangle$, and $3.7 \langle B_{\parallel}^2 \rangle$, respectively. An alternative parameterization was recently proposed by Gill & Granot (2019), who define the ratio ξ_{eff} as the amount of stretch of the field along the parallel direction with respect to an isotropic field (which would have $\xi_{\text{eff}} = 1$). They find that $\xi_r \approx b^{1/2}$, and our analysis therefore yields

$$\xi_{\text{eff}} \sim 1.3; 1.4; 0.77; 0.73. \quad (10)$$

4. Discussion

We have presented an analysis of the available ensemble of linear polarization measurements in the optical afterglow of long-duration gamma-ray bursts. The analysis is aimed at finding the ratio ζ between the measured polarization and the maximum theoretically possible, which would be observed if the magnetic field would be either completely ordered parallel to the shock normal or entirely contained in the plane of the shock. The ratio ζ is a proxy for the geometry of the magnetic field that can be quantified either through the parameter $b = 2 \langle B_{\parallel}^2 \rangle / \langle B_{\perp}^2 \rangle$ (Gruzinov & Waxman 1999; Sari 1999) or through the stretch parameter ξ_{eff} (Gill & Granot 2019).

We find that the available measurements are highly constraining of the polarization of the afterglows and, consequently, of the field geometry. We also find that our result is in some tension with the analysis of Gill & Granot (2019), who looked at the upper limit on the polarization of GW170817, a short gamma-ray burst for which the viewing geometry is known. However, several simplifying assumptions were made and significant systematic uncertainties are brought about by the choice of polarization model, outflow geometry, and jet dynamics. Here we discuss all these choices and approximations to inform the reader of their potential impact.

First, we chose to adopt a top-hat jet for our polarization model. The rationale behind this choice is that it makes the probability of detection of an afterglow independent on the observer angle. This makes our calculation more straightforward and robust, since we do not have to assume a detection threshold, nor that all bursts are observed in the same way and with the same sensitivity. On the other hand, it seems likely that real GRB jets are structured, at least to some level (e.g., Granot & Kumar 2003; Kumar & Granot 2003; Rossi et al. 2004; Zhang et al. 2004; Morsony et al. 2007; Lazzati et al. 2018). Since the polarization curve for a structured jet is qualitatively different from that of a top-hat jet, our result would apply to that case only at the order-of-magnitude level. We note that Gill & Granot (2019) adopt a structured jet in their analysis, a difference that is most likely at the origin of the tension between the two results. An extension of this work to include structured jets is planned. As a matter of fact, the polarization measurements shown in Figure 2 do hint at a maximum of the measured polarization at about the jet break time, a feature that is characteristic of structured jets. Another hint that our jet model might be oversimplified can be gleaned from Figure 5. The figure shows how the models predict polarization of up to $\sim 6\%$, which are not observed, yielding a low Kolmogorov–Smirnov probability (see Section 3). Since the highest polarization is predicted for observers right on the edge of the jet, such prediction would be overestimated if the jet had a smooth transition, rather than an abrupt edge as implied by the top-hat model. In support of our choice, however, there are at least two bursts in which the 90° rotation of the polarization angle that is characteristic of a top-hat jet has been observed: GRB091018 (Wiersema et al. 2012) and GRB121024A (which is, however, excluded from the sample due to the peculiarity of having significant circular polarization; Wiersema et al. 2014).

Another important choice we made was selecting the model of Rossi et al. (2004) as our fiducial model. Calculations by different authors differ in the details, and consequently there are differences in the order of a few tens of percent among the theoretical models (see, e.g., Granot et al. 2002). In addition, different assumptions on the sideways expansion dynamics cause different polarization, in some cases even adding to the complexity by causing a third peak to appear in the polarization curve (Sari 1999; Figure 5 in Rossi et al. 2004). To test the sensitivity of our results to the assumption on the sideways expansion, we repeated the analysis using the models in Figure 9 of Rossi et al. (2004), which assume that the jet expands sideways with relativistic speed of sound $c_s = c/\sqrt{3}$. We found a most probable value $\zeta \sim 0.4$, associated with a lower KS probability $p_{\text{KS}} = 2 \times 10^{-5}$. These significantly different values underline the sensitivity of polarization on poorly known dynamic properties of the outflows. We plan to address

some of these uncertainties in future publications. Hopefully, additional data will then be available to further constrain the models and interpretations.

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