



Where Did They Come From, Where Did They Go: Grazing Fireballs

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Abstract

For centuries extremely long grazing fireball displays have fascinated observers and inspired people to ponder about their origins. The Desert Fireball Network is the largest single fireball network in the world, covering about one third of Australian skies. This expansive size has enabled us to capture a majority of the atmospheric trajectory of a spectacular grazing event that lasted over 90 s, penetrated as deep as ~ 58.5 km, and traveled over 1300 km through the atmosphere before exiting back into interplanetary space. Based on our triangulation and dynamic analyses of the event, we have estimated the initial mass to be at least 60 kg, which would correspond to a 30 cm object given a chondritic density (3500 kg m^{-3}). However, this initial mass estimate is likely a lower bound, considering the minimal deceleration observed in the luminous phase. The most intriguing quality of this close encounter is that the meteoroid originated from an Apollo-type orbit and was inserted into a Jupiter-family comet (JFC) orbit due to the net energy gained during the close encounter with Earth. Based on numerical simulations, the meteoroid will likely spend ~ 200 kyr on a JFC orbit and have numerous encounters with Jupiter, the first of which will occur in 2025 January–March. Eventually the meteoroid will likely be ejected from the solar system or be flung into a trans-Neptunian orbit.

Unified Astronomy Thesaurus concepts: Meteoroids (1040); Meteors (1041); Solar system (1528); Near-Earth objects (1092); Short period comets (1452); Close encounters (255); Fireballs (538)

1. Introduction

1.1. Reports of Grazing Fireballs

People have reported witnessing brilliantly long-lasting and bright meteor processions for at least hundreds of years. The 1783 “Great Meteor” was estimated to have traveled >1600 km through the atmosphere over western Europe (Cavallo 1784). The “Great Comet of 1860,” which was most likely an Earth-grazing fireball over the eastern United States, was accounted for in a painting by American landscape artist Frederic Church entitled “The Meteor of 1860” and by American poet Walt Whitman in his poem “Year of Meteors” (Olson et al. 2010). Additionally, the “1913 Great Meteor Procession” reported sightings across Canada, the north-eastern United States, Bermuda, and many ships in the Atlantic as far south as Brazil. The event was initially hypothesized to have been formed by a natural Earth satellite that had a grazing encounter with the atmosphere (Chant 1913; Denning 1916).

A grazing event is considered to be when a meteoroid impacts the atmosphere at an extremely low angle relative to the horizon, and there are generally three possible outcomes. It can either escape back to interplanetary space after passing through the atmosphere, fully ablate, or slow down enough to fall to Earth. The first scientifically observed and triangulated grazing event was not until 1972 over Canada and the northwestern United States (Ceplecha 1979, 1994). The 1972 fireball lasted ~ 100 s, covering over 1500 km, and reached a minimum height of 58 km. Ceplecha (1979) estimated the mass to be between 10^5 and 10^6 kg with the most likely diameter of about 5 m. The original analysis done by Rawcliffe et al. (1974) and Jacchia (1974) is known to contain mistakes, and the values given should not be relied upon (Ceplecha 1979).

Since the 1972 fireball, there have been several atmospheric grazing events reported within scientific literature:

1. In 1990, Borovicka & Ceplecha (1992) published an analysis of the first Earth-grazing fireball observed by a photographic fireball network in which the meteoroid was estimated to be 44 kg with the closest approach of 98 km detected by two Czech stations of the European Fireball Network.
2. In 1992 October, a bright fireball endured for over 700 km over the eastern United States before dropping a meteorite in Peekskill, New York (Brown et al. 1994; Beech et al. 1995; Ceplecha et al. 1996).
3. In 1996 a fireball was observed to hit the western United States and only briefly escape for one orbit before allegedly impacting Earth (Revelle et al. 1997).
4. On 2006 March 29, a ~ 40 s grazing fireball was observed over Japan (Abe et al. 2006). The meteoroid traveled over 700 km through the atmosphere and reached a minimum height of 71.4 km. It appeared to come from a JFC-like orbit and the spectra collected was consistent with a chondritic composition.
5. On 2007 August 7, a grazing fireball was observed by the European Fireball Network originating from a Aten-type orbit (Spurný et al. 2008).
6. In 2012 June, the first grazing meteoroid associated with a meteor shower in the scientific literature was recorded by 13 stations with a 98 km minimum altitude over Spain and Portugal and belonged to the daytime ζ -Perseid shower (Madieto et al. 2016).
7. In 2003, another grazing meteor, mass loss $\approx 5 \times 10^{-3}$ g, was detected over Ukraine before exiting back into interplanetary space (Kozak & Watanabe 2017).
8. In 2014 December, a 1200 km long grazing event occurred over Algeria, Spain, and Portugal and lasted approximately 60 s, reaching a minimum height of 75 km (Moreno et al. 2016).

9. On 2014 March 31, a ~ 34 s fireball over Germany and Austria originating from an Apollo-type orbit was observed. The meteoroid was estimated to have an initial mass of about 200 kg, but no material is believed to have exited back into interplanetary space (Oberst et al. 2014). Many meteorites may have survived to the ground, however, the uncertainty on the fall ellipse is very large due to the extremely shallow entry angle.

For some of these grazing meteoroids mentioned above, the object was able to survive its passage through the atmosphere. The rock then re-entered interplanetary space on an altered orbit, sending material from one part of the inner solar system to another. This could be significant since various parts of the inner solar system are thought to be dynamically and physically distinct from one another.

1.2. Small Inner Solar System Bodies

The classical view of the solar system says that the Sun formed with a debris disk around it that was originally compositionally heterogeneous within bands of constant radial distance from the Sun. The snow line denoted the boundary between the planetesimals in which water ice and other volatiles would be retained and the bodies which were unable to hold ice, thus remaining dry. This classically separated the small bodies within the solar system into two main groups: comets and asteroids respectively.

Although, we have seen that this classical ideology does not usually fit our observations of the small bodies within the solar system. The solar system is complicated and dynamic. In the last 4.5 billion years, small bodies have been jumbled around and altered. The layout and distribution of the solar system is much more complicated than the idealized stratified one we tend to imagine.

Within the inner solar system there are short-period comets, main-belt objects (MBOs), and near-Earth objects (NEOs). Traditionally, the MBOs were considered asteroidal and inner solar system in origin, and NEOs primarily evolved from the MBO space after entering an orbital resonance (Bottke et al. 2002; Granvik et al. 2018). However, with the identifications of main-belt comets (MBCs; Hsieh & Jewitt 2006) and dry asteroidal material in the Kuiper belt (Meech et al. 2016), we have realized that the material in the solar system is more mixed than previously believed (Fernández & Sosa 2015). Additionally, the starkly drawn lines between asteroidal and cometary material have since faded with the identification of active asteroids, extinct comets, and mixing between populations (Fernández et al. 2001, 2002, 2005; Jewitt 2012; Kim et al. 2014). In reality, the physical properties of small bodies in the solar system most likely exist in a spectrum from primitive volatile-rich (comet-like) to dry volatile-poor (asteroid-like). We are still trying to determine the most probable mechanism by which this mixing could have occurred, but several models such as the “Nice Model” and the “Grand Tack” have begun to elucidate some of these mysteries (Walsh et al. 2011; Tsiganis et al. 2005).

Jupiter-family comets (JFCs) are a class of short-period comets, believed to have evolved from scattered disk and Kuiper belt orbits (Fernández 1980; Duncan & Levison 1997; Levison & Duncan 1997; Binzel et al. 2004). JFCs are primitive and contain a large amount of hydrated minerals and volatile ices (Kelley & Wooden 2009; Jenniskens et al. 2012).

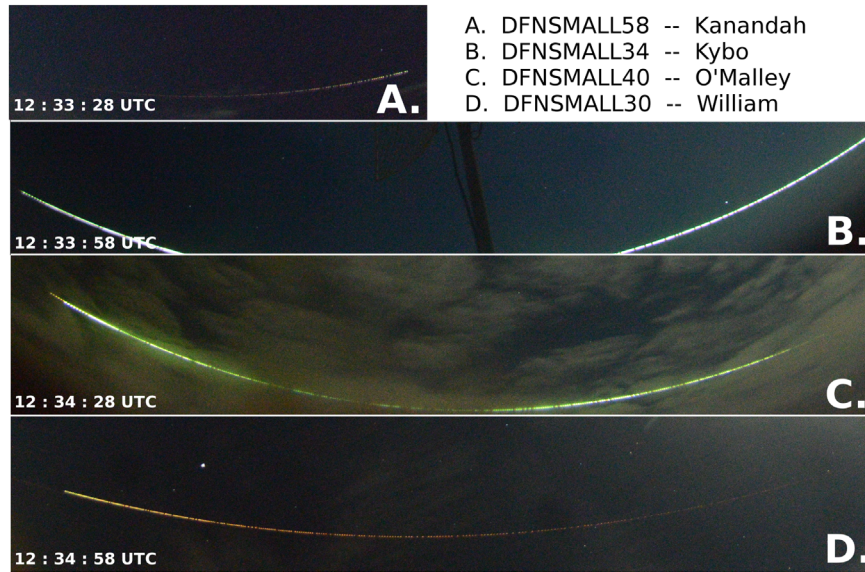
They are also characterized by their orbits being strongly linked to the orbit of Jupiter, typically defined by their Tisserand’s parameter to be $2 < T_J < 3$ (Carusi & Valsecchi 1987; Levison & Duncan 1994). JFCs usually have multiple low-velocity encounters with the gas giant over their lifetime (Duncan & Levison 1997; Levison & Duncan 1997; Duncan et al. 2004). These encounters with Jupiter make the orbits of JFCs more unpredictable compared to other small bodies, where the median dynamic lifetime of a JFC is ~ 325 kyr (Duncan et al. 2004). However, as described by Fernández & Sosa (2015), JFCs that display cometary features frequently encounter Jupiter at distances of ≤ 0.1 au making them highly unstable compared to a small subset of near-Earth asteroidal JFCs that typically exist on more stable orbits comparatively. A tiny fraction of JFCs are also thought to decouple from Jupiter and become Encke-like comets through either nongravitational perturbations or close planetary encounters (Steel & Asher 1996; Levison et al. 2006).

1.3. The Desert Fireball Network

Since 2003, the Desert Fireball Network (DFN) has been operating observatories across southwestern Australia to capture images of fireball events (Bland 2004). The network has since grown from 4 observatories by 2007 to over 50 observatories in western Australia and southern Australia by 2015 (Bland et al. 2012; Howie et al. 2017a). No other fireball camera network in the world is this expansive. Furthermore, we have expanded this effort worldwide with the start of Global Fireball Observatory (GFO) collaboration (H. A. R. Devillepoix et al. 2020, in preparation) with a coverage area expected to increase to 2% of Earth’s entire surface. This coverage area makes the GFO particularly well suited to characterize grazing meteoroids and other more rare fireball events (Shober et al. 2019).

2. DFN Observations

On 2017 July 7, a 90 s extremely shallow fireball was observed to graze the atmosphere above western Australia and southern Australia, entering the atmosphere at a slope of $\sim 4^\circ.6$ (Figure 1). Ten DFN observatories made observations of the fireball as it traveled over 1300 km through the atmosphere. The luminous phase started at about 85 km and penetrated as deep as 58 km before ceasing to be visibly ablating at 86 km. This event is only equaled by the “Great Daylight Fireball of 1972,” which reached a similar depth and lasted ~ 9 s longer than our witnessed event (Ceplecha 1979). However, unlike the 1972 event, the DFN was able to photographically image the majority of the atmospheric trajectory of the fireball (including the beginning and the end), with observations from many of our fireball observatories spread across western Australia and southern Australia. Thus, providing us with a substantial amount of data to accurately fit a trajectory to our observations (2541 astrometric data points). A summary of the observations made of event DN170707_01 and the fitted trajectory are provided in Table 1. The number of observations refers to the number of 30 s exposures. Whereas, “without timing” denotes when observations of the fireball were collected, however, either the angular velocity of the meteoroid was too slow or the fireball was too bright to distinguish the encoded de Bruijn sequence (Howie et al. 2017b). Unfortunately, due to the DFN’s viewing geometry at the beginning of the observed luminous trajectory, the initial observation convergence angle



A. DFNSMALL58 -- Kanandah
 B. DFNSMALL34 -- Kybo
 C. DFNSMALL40 -- O'Malley
 D. DFNSMALL30 -- William

Figure 1. Long exposure images of event DN170707_01. The event lasted over 90 s and spanned four 30 s exposures (A, B, C, D). The fireball was first observed at 85 km altitude, reached as low as 58 km, and then was visible until 86 km before escaping Earth's atmosphere. The initial velocity was 16.1 km s^{-1} , and the exit velocity after passing through the atmosphere was about 14.6 km s^{-1} . The images are all oriented so that the fireball travels from left to right (west to east).

Table 1

Observations and Triangulated Trajectory for Event DN170707_01, Recorded over Western Australia and Southern Australia on 2017 July 7

	Entry Conditions	Exit Conditions
Time (UTC) after 2017 Jul 7	12:33:45.900	12:35:16.050
Height (km)	85.66 ± 0.03	86.04 ± 0.02
Mass range (depending on density; kg)	14–92	9–62
Latitude (deg)	-28.6933 ± 0.0003	-28.4144 ± 0.0002
Longitude (deg)	122.7161 ± 0.0010	136.3318 ± 0.0002
Velocity (km s^{-1})	15.71 ± 0.13	14.24 ± 0.10
Slope (deg)	4.6	7.8
Duration (s)	90.15	
Minimum height (km)	58.5	
Best convergence angle (deg)	45.9	
Number of observations (with timing)	13	
Number of observations (without timing)	7	
Number of data points	2541	

Note. The mass range was determined by varying the density between 2800 and 7300 kg m^{-3} and includes formal uncertainties. The timing uncertainty is nominally 10^{-4} – 10^{-5} s, considerably less than other sources of uncertainty for the trajectory (Howie et al. 2017b).

is only a few degrees (1° – 2°). Therefore, the uncertainty associated with the initial velocity is higher than usual, however, still sufficient to determine what part of the solar system the meteoroid originated.

At the meteoroid's closest approach, a fragmentation event occurred in which a smaller piece of the primary object broke off (Figure 2). DFN observatories captured the fragmentation event on video, and an uncalibrated light curve was able to be extracted (Figure 3). There are no other instances of fragmentation observed during the trajectory. This fragmentation event was taken into account when triangulating the path of the primary and determining the mass of the meteoroid.

3. Methods

3.1. Triangulation

In the past, fireball and meteor observation networks estimated the trajectories they witnessed using a simplified straight-line fit approach (Ceplecha 1987; Borovicka 1990). These simplified straight-line fit techniques are sufficient enough to obtain meaningful results when the trajectory is shorter than 100 km. However, recent studies have shown that more satisfactory results can be obtained with the use of more rigorous methodologies (Sansom et al. 2015, 2019; Jansen-Sturgeon et al. 2019a). This is particularly true for a grazing fireball where the meteoroid is traveling hundreds to thousands of kilometers through the atmosphere. In previous grazing fireball studies, this nonlinearity was accounted for in several different ways. Ceplecha (1979) was the first to recognize that a grazing trajectory should fit a hyperbola when neglecting the atmosphere, but is otherwise slightly more curved due to the atmospheric drag experienced. Thus, Ceplecha (1979) fit osculating circles to the trajectory of the 1972 grazing daylight fireball to account for this added curvature with reasonable accuracy. Borovicka & Ceplecha (1992) utilized the fact that one of the observation stations was nearly directly below the fireball (passed nearly through zenith) and saw the entire trajectory. They took their observations and performed a least-squares fit to an osculating circle at the point of pericenter, neglecting drag in this case based on fireball type. Similar methodologies using osculating circular trajectory fits have been utilized by other studies as well (Abe et al. 2006). Kozak & Watanabe (2017) triangulated a small, fast grazing, high-altitude meteor detected by video observatories in Ukraine by assuming minimal drag and fitting the observations to a hyperbolic orbit in the geocentric frame. Meanwhile, Madieto et al. (2016) determined the atmospheric trajectory of a meteor belonging to the daytime ζ -Perseid shower using a segmented method-of-planes approach adapted from Ceplecha (1987).

For standard DFN events, we implement a modified straight-line least-squares (SLLS) method with an extended Kalman smoother (EKS) for velocity determination (Sansom et al. 2015).

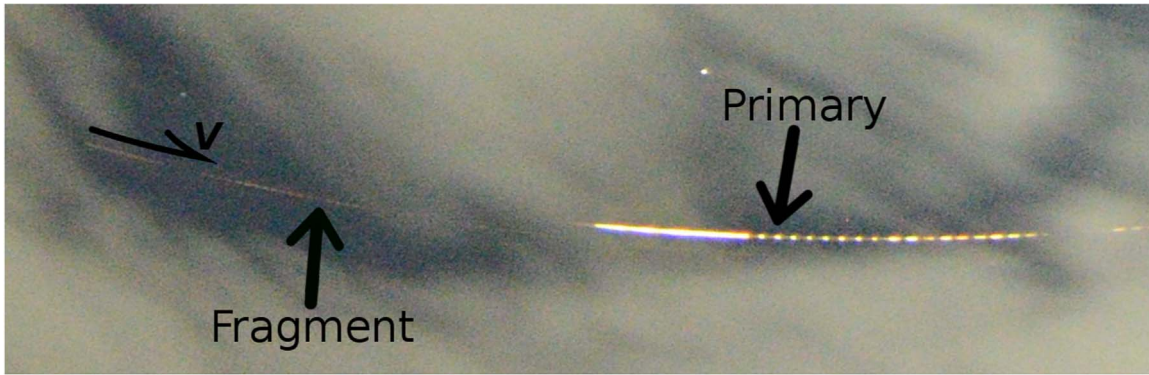


Figure 2. Fragmentation event captured for event DN170707_01 near the closest approach of its trajectory. The image shows two distinct paths offset from each other. The brighter path on the right side of the image belongs to the primary piece, whereas on the left the trail of a smaller fainter fragment can be seen. The decrease in velocity due to the observed fragmentation was not significant relative to the velocity scatter, and thus was not included during the trajectory fit. Additionally, only one camera observed the fragment due to cloud coverage and geometry, and therefore a trajectory for the fragment was unable to be determined. No other fragmentation events were detected along the path.

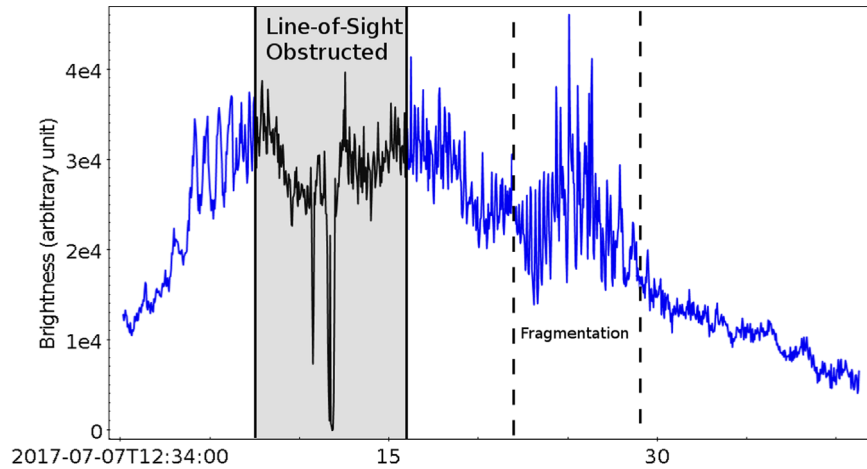


Figure 3. Light curve based on video from observatory DFNSMALL34-Kybo in the Nullarbor Plain in western Australia during the fragmentation of event DN170707_01. The fragmentation occurs about 25 s into this exposure (enclosed by dashed vertical lines), forming one detectable fragment. The y-axis is brightness in arbitrary units due to the photometry data lacking calibration. The ram pressure on the meteoroid just prior to the fragmentation was ~ 0.08 MPa. The line of sight was briefly obstructed by a telephone pole, reducing the brightness.

We then numerically determine the meteoroid’s orbit by including all relevant perturbations. Numerical methods are a slightly more accurate way to handle the orbit determination, especially for meteoroids that were slow or closely approached the Moon (Clark & Wiegert 2011; Dmitriev et al. 2015; Jansen-Sturgeon et al. 2019a). For longer and/or shallower fireball events, where the meteoroid trajectory can have noticeable curvature, the SLLS method cannot account for the nonlinear motion. Within this study, we implemented a dynamic trajectory fit (DTF) triangulation method that fits the observation rays directly to the equations of motion for fireballs (Jansen-Sturgeon et al. 2019b). This non-straight-line approach to the event triangulation represents the physical system more veraciously. Consequently, the DTF method produces a much better fit to the observations compared to the SLLS for both positions and velocities (Figures 4 and 5). We then use this trajectory (Figure 6) to numerically estimate the pre- and post-grazing orbits. Although, currently the DTF method does not provide adequate formal velocity errors, thus an EKS was utilized to determine the velocity uncertainties for this study.

3.2. Mass Determination

During the DTF procedure, the meteoroid’s ballistic parameter and ablation coefficient are determined alongside its dynamic parameters, based directly on the line-of-sight observations. By assuming the meteoroid’s shape and density, a mass estimation can be deduced from the meteoroid’s fitted ballistic parameter.

3.3. Orbital Integration

After triangulating the grazing event, we initialized several orbital integrations using the publicly available REBOUND code¹ (Rein & Liu 2012). We utilized the 15th order nonsymplectic IAS15 integrator for our simulations of the event (Rein & Spiegel 2015). This integrator is based upon the RADau-15 integrator developed by Everhart (1985). It improves upon its predecessor by minimizing the systematic error generated by the algorithm to well below machine precision, implementing an adaptive time step, and adding the

¹ <http://github.com/hannorein/REBOUND>

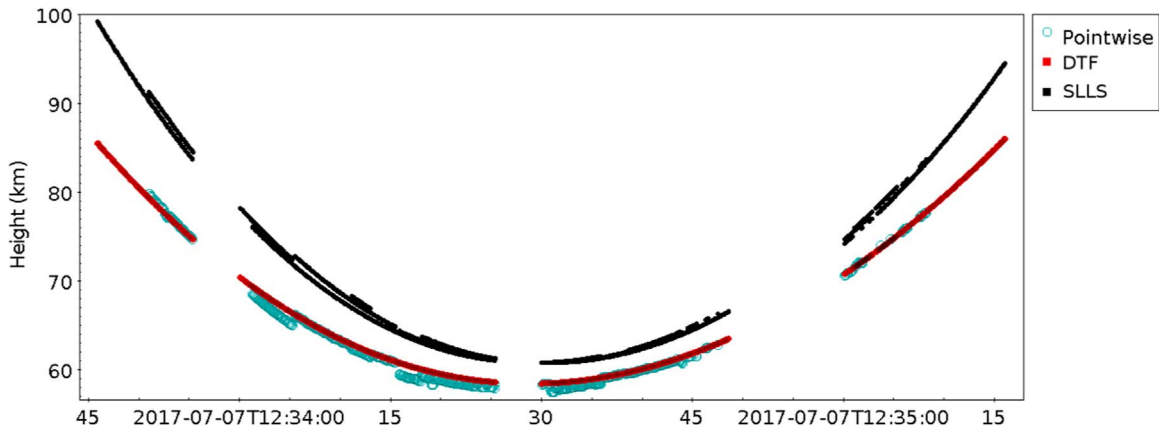


Figure 4. Height variation as a function of time determined by the straight-line least-squares (SLLS) and the dynamic trajectory fit (DTF) methods. The pointwise heights represent the points that minimize all the angular distances between the simultaneous lines of sight (given >2), the respective observatory, and the point itself. The DTF fits much better to the pointwise than the SLLS due to its incorporation of gravity, drag, and ablation. This non-straight-line fit produces a much more useful model to understand these grazing fireball events. The shape of the trajectory is somewhat misleading, as the trajectory would be concave with respect to a global, inertial reference frame instead of convex, as shown here. The three distinct gaps in the trajectory are due to latency between observation periods (Howie et al. 2017a). This lapse in observations occurs once every 30 s and is only typically noticeable for the longest fireball trajectories observed by the DFN. Toward the end of the trajectory, the largest lapse in observations was also due to the cloud coverage at the time.

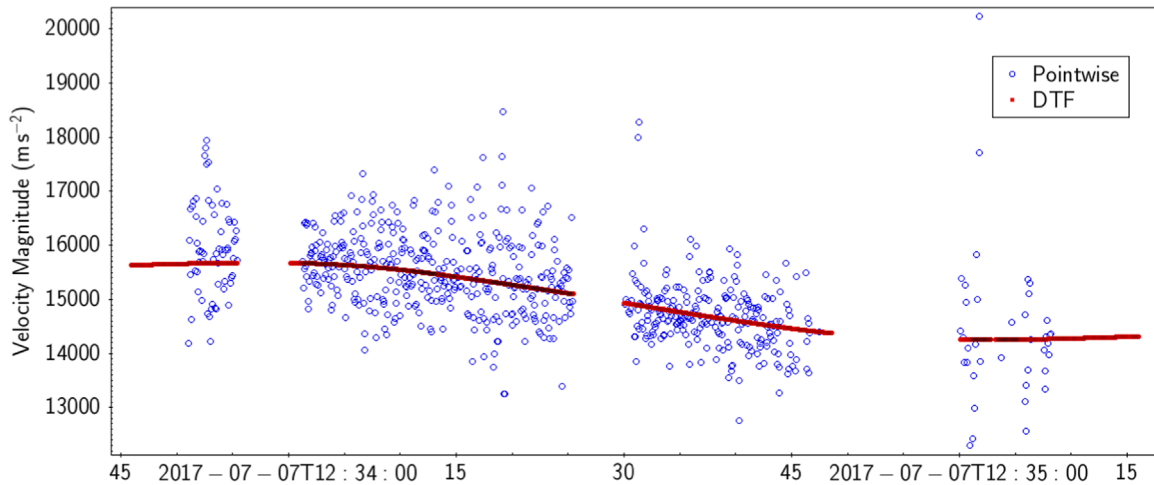


Figure 5. Velocity of the DN170707_01 meteoroid event as determined using both the dynamic trajectory fit (DTF) model (red) and a pointwise triangulation fit (blue). The DTF method fits the line-of-sight observations directly to the dynamic equations of motion that describe the motion of fireballs. Pointwise scattered instantaneous speeds correspond to the center difference between adjacent data points seen by >2 observatories. These points in 3D space are calculated by minimizing all the angular distances between the simultaneous lines of sight, the respective observatory, and the point itself.

ability to include in nonconservative forces easily while ensuring that the round-off errors are symmetric and at machine precision.

Initialization. From the trajectory determined by the DTF method, the pre- and post-atmospheric state vectors for the meteoroid can be used to initialize orbital simulations. These simulations contain N number of particles within the meteoroid state's uncertainties produced by the triangulation. Currently, the DTF methodology does not provide formal uncertainties as model errors are not accounted for (Jansen-Sturgeon et al. 2019b). Subsequently, for this event, we determined the velocity uncertainties using the EKS method in conjunction with the DTF trajectory fit. Additionally, we assume a Gaussian distribution for the errors, although this may not be strictly true. However, the results from the integration should not deviate significantly due to this assumption. The particles' positions are generated from the initial and final latitude, longitude, and height determined from the DTF triangulation. The speed of the particles and their R.A. and decl. are given in the Earth-

centered Earth-fixed frame and then converted to the Earth-centered inertial frame in order to generate the particles in the simulations.

Integration. Initial simulations were run within ± 100 yr of the grazing event in order to accurately characterize the short-term evolution of the meteoroid. The number of outputs recorded was increased so that any close encounters with Jupiter or Earth would be well resolved. Afterward, a series of long-term integrations were done in a similar manner. The primary goal of these more extended integrations was to determine what were the lasting effects of the meteoroid's grazing encounter with Earth. Does it stay on a JFC orbit as long as any typical JFC, and where does it evolve to after? Each integration recorded the positions, velocities, and osculating orbital elements for the meteoroid particles for a total period of 500,000 yr forward relative to the event epoch. Close encounters with other planets were also considered and inspected, particularly with Jupiter.

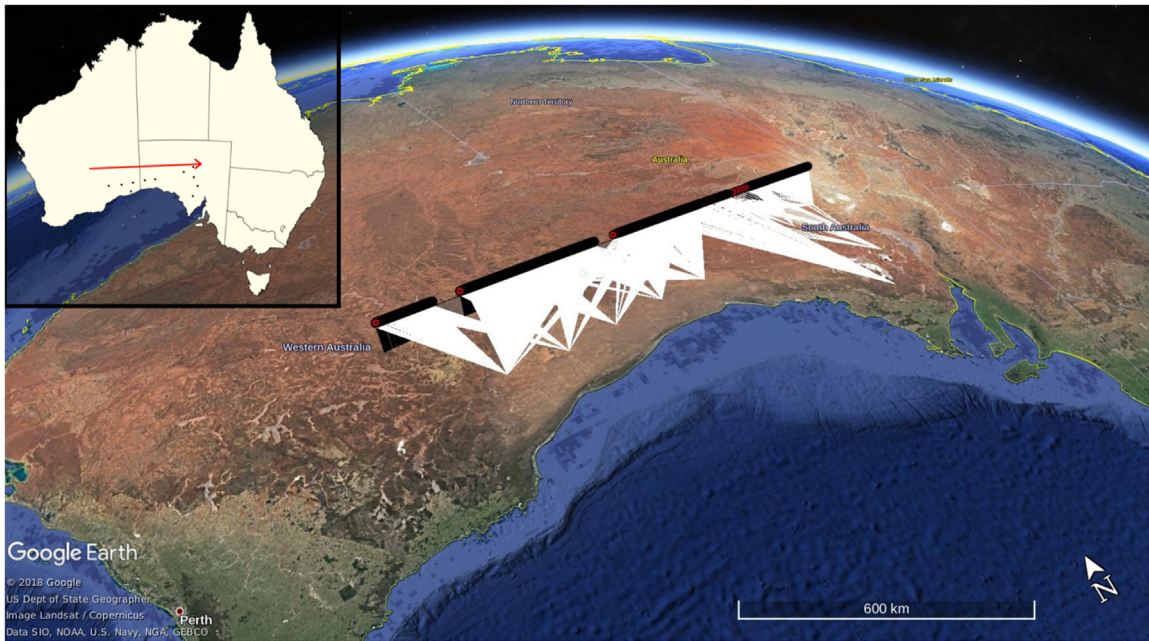


Figure 6. Triangulated luminous atmospheric trajectory for event DN170707_01, as seen over western Australia and southern Australia. The triangulation method used involves fitting the line-of-sight observations directly to the meteoroid’s dynamic equations of motion, thereby dropping any straight-line assumptions (Jansen-Sturgeon et al. 2019b). The event lasted 90 s, initially hitting the atmosphere at $4^{\circ}6'$ and covering over 1300 km through the atmosphere. The white rays indicate the line-of-sight measurements from each DFN observatory, whereas the black path marks the triangulated trajectory based on the observations of the fireball.

4. Results and Discussion

4.1. Atmospheric Trajectory

As seen in Figure 4, the DTF methods fit the pointwise observations much better than the SLLS method for an event that is thousands of kilometers in length. The pointwise heights are given by minimizing the angular distance between the lines of sight when at least two observations are made. If a center difference is taken between all these points, a velocity scatter can be generated (Figure 5). The velocity scatter for event DN170707_01 is very large in some circumstances considering the low convergence angles, especially for the beginning of the trajectory. A majority of the fireball’s trajectory was north of the DFN observatories (Figure 6), thus reducing the accuracy of each measurement. However, since we gathered over 2500 data points from 10 DFN observatories, a reasonably good trajectory was able to be extracted. There are also three distinct gaps in the observations of event DN170707_01 primarily due to the latency between the 30 s observation periods. These lapses in observations are typically only noticeable for the longest enduring fireballs observed by the DFN. The longest gap, toward the end of the trajectory, is compounded by the poor visibility for the DFN observatories in that area of the network due to the cloud coverage at the time.

During the DTF procedure, the ballistic parameter was determined throughout the trajectory based directly on the line-of-sight measurements, and hinges on the deceleration profile of the observed meteoroid. The meteoroid’s mass was estimated by assuming its shape and density, as seen in Figure 7. For instance, assuming a spheroid of chondritic density (3500 kg m^{-3}), the DN170707_01 meteoroid was estimated to have a 60 kg initial mass and a 40 kg outbound mass. A majority of the mass loss is predicted to have occurred during the fragmentation observed near the closest approach of the object. However, as minimal deceleration was observed during the luminous atmospheric

encounter (Figure 5), this mass estimate would be more accurately viewed as a lower bound.

The loading ram pressure for the meteoroid at the time of fragmentation was also calculated using

$$p = \rho_h v_h^2, \quad (1)$$

where ρ_h is the atmospheric density at the height h of the fragmentation and v_h is the speed of the meteoroid at that instant. For event DN170707_01, we determined the fragmentation height based on the time of fragmentation observed in the light curve from video observations. We estimated the meteoroid to have fragmented at $58.49 \pm 0.01 \text{ km}$, just before the minimum height was reached, with a velocity of $15.5 \pm 0.1 \text{ km s}^{-1}$. We then used the NRLMSISE-00 global atmospheric model to determine the density of the atmosphere at the fragmentation height (Picone et al. 2002). The ram pressure experienced by the meteoroid just before fragmentation was calculated to be $0.084 \pm 0.01 \text{ MPa}$. This very low value is consistent with the results of Popova et al. (2011), in which it was found that bulk strengths determined by initial fragmentation are consistently much lower than the strength of recovered meteorites. Thus, this value likely reflects macro-scale fractures in the object and not the intrinsic material strength. For example, the Dingle Dell ordinary chondrite meteorite recovered by the DFN in 2016 also experienced similar low-pressure fragmentations (0.03–0.11 MPa) early in its bright flight, despite having a recovered bulk density of 3450 kg m^{-3} (Devillepoix et al. 2018).

4.2. Short-term Simulations

As shown in Table 2, the meteoroid that skipped off the atmosphere over western Australia and southern Australia in 2017 July originally came from an orbit in the inner main-belt, between the 4:1 and the 3:1 mean-motion resonances with

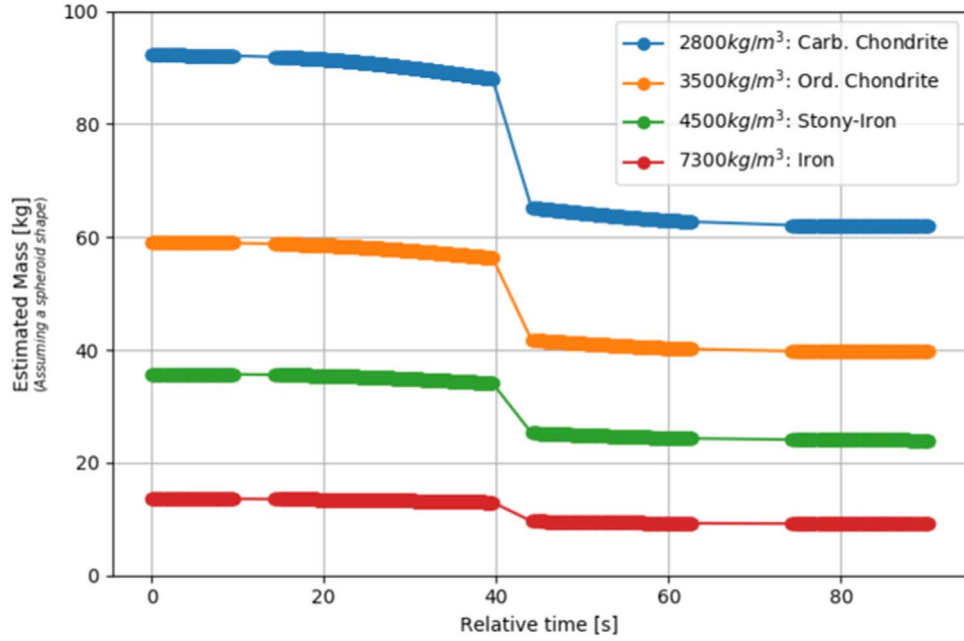


Figure 7. Mass estimation based on DTF triangulation fit to the DFN’s observations. The fragmentation event was taken into account, as seen by the sudden mass loss experienced at ~ 40 s into the luminous phase. Each line represents a different density estimate for the object, given the DTF ballistic parameter.

Table 2

Heliocentric Orbital Elements for the Meteoroid Associated with Event DN170707_01 Just before and after its Grazing Encounter with Earth

	Before	After
a (au)	2.23 ± 0.06	3.26 ± 0.12
e	0.59 ± 0.01	0.69 ± 0.01
i (deg)	2.79 ± 0.04	3.30 ± 0.04
Ω (deg)	286.46 ± 6.03	285.29 ± 0.01
ω (deg)	316.43 ± 3.56	350.91 ± 0.29
q (au)	0.9104 ± 0.0003	1.007 ± 0.0004
Q (au)	3.458 ± 0.114	5.36 ± 0.2300
T_J	3.41 ± 0.05	2.75 ± 0.05

Note. The uncertainties of the orbital elements were determined by a short Monte Carlo simulation consisting of 5000 particles randomly generated within triangulation errors and numerically integrated forward and backward relative to the grazing event. The immediate effect of the encounter on the orbit is apparent; the semimajor axis, eccentricity, and argument of perihelion of the meteoroid were all significantly increased. The grazing encounter changed the orbit of the meteoroid from an Apollo-type NEO to a JFC orbit. The resulting orbit is comparatively unstable due to its aphelion being very similar to the semimajor axis of Jupiter, increasing the chance of a close encounter with the gas giant.

Jupiter (Figure 8). It most likely evolved into an Earth-crossing orbit after passing through either the 3:1 or the ν_6 complex, which are the two most significant entry routes into the NEO region (Bottke et al. 2002; Granvik et al. 2018). As a result of the grazing encounter with Earth, the meteoroid was flung into an orbit with a higher energy (Figure 9). The geometry of the encounter enabled the meteoroid to gain angular momentum around the Sun (Figure 10). As a result, the semimajor axis and eccentricity both increased due to the increase in energy, and the object was inserted into a JFC orbit. Hereon, the object’s future is strongly governed by its interactions with the gas

giant. Figure 8 shows the evolution of the orbital elements for the meteoroid ± 100 yr relative to the grazing encounter.

With an post-encounter aphelion near Jupiter’s orbit, the meteoroid is likely to have multiple close encounters with the planet in the future. Thus, the object is unpredictable on relatively short timescales compared to other small bodies in the solar system. This is to be expected for an object on a JFC-like orbit that originated from the trans-Neptunian region (Fernández & Sosa 2015). As seen in Figure 8, the object will tend to decrease in eccentricity and slightly increase in semimajor axis over time. This will occur slowly for a majority of particles over about 10–100 kyr, as Jupiter perturbs them. If the orbit of the meteoroid evolves into an orbit with a similar semimajor axis to Jupiter, the close encounters with the gas giant will begin to increase the eccentricity of the meteoroid again and throw the body toward the outer solar system. The meteoroid is also nearly centered on the 2:1 mean-motion resonance (Figure 8), however, this resonance is not as destabilizing as the other prominent resonances on such short timescales (Morbidelli et al. 2002).

The first of these close encounters will most likely occur between 2025 January and March (~ 7.52 yr after encountering Earth) in which the meteoroid will very likely come within 3 Jupiter Hill radii (JHR) of the planet. A series of short-term highly resolved integrations were performed with 5000 test particles to analyze this first close encounter with Jupiter. As shown in Figure 11(a), the meteoroid is likely to get close to Jupiter (blue path) just 1.5 orbits after our observations of the fireball. Figure 11(b) shows the minimum distances reached by every particle in the integration, many of which (40%) approaching within 1 JHR with the mean approach of all particles being 0.7 JHR. After this close encounter, the test particles disperse relatively quickly, and precisely predicting the future orbit of the meteoroid becomes unrealistic.

As seen in Figure 12, the well-constrained orbit prior to the close encounter with Jupiter rapidly spreads out in the orbital

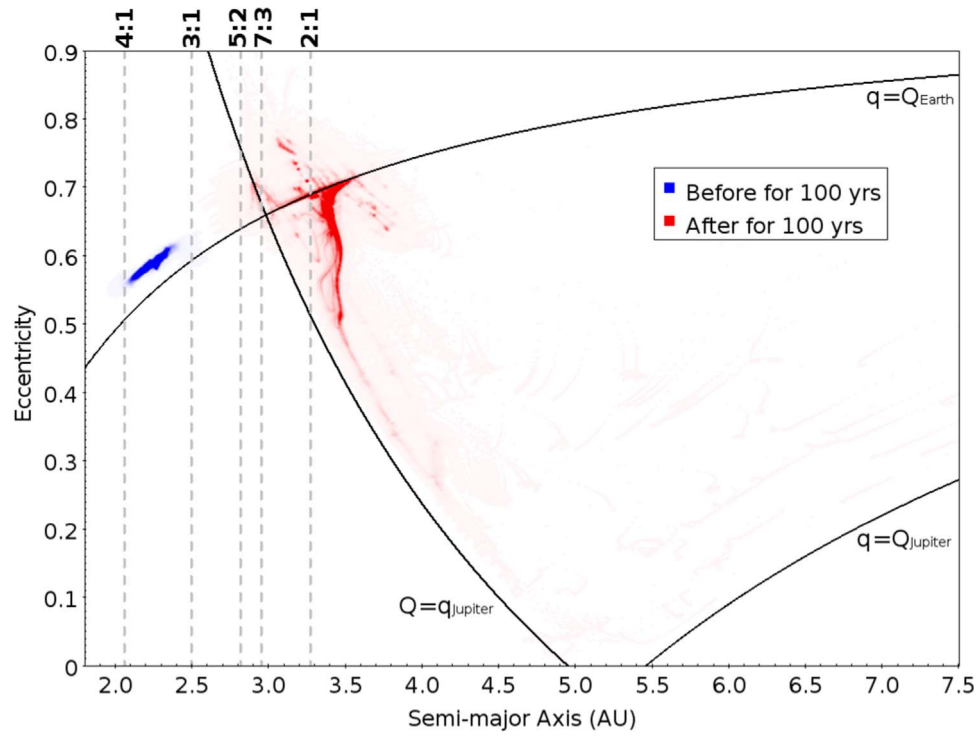


Figure 8. Semimajor axis vs. eccentricity during ± 100 yr of integrations involving 10,000 test particles. Particle density over time is indicated by opacity. A majority of the particles remain close together after the grazing encounter, with a small number of particles being scattered by Jupiter very quickly. The significant mean-motion resonances are also plotted as vertical dotted lines. The object came from an eccentric orbit between the 4:1 and 3:1 mean-motion resonances. After the grazing encounter with Earth, the object gained energy and was transferred onto a JFC orbit near the 2:1 resonance with Jupiter. In this orbit, the future of the meteoroid is strongly influenced by the gas giant. Over time, the meteoroid will tend to follow the aphelion and perihelion lines for Jupiter.

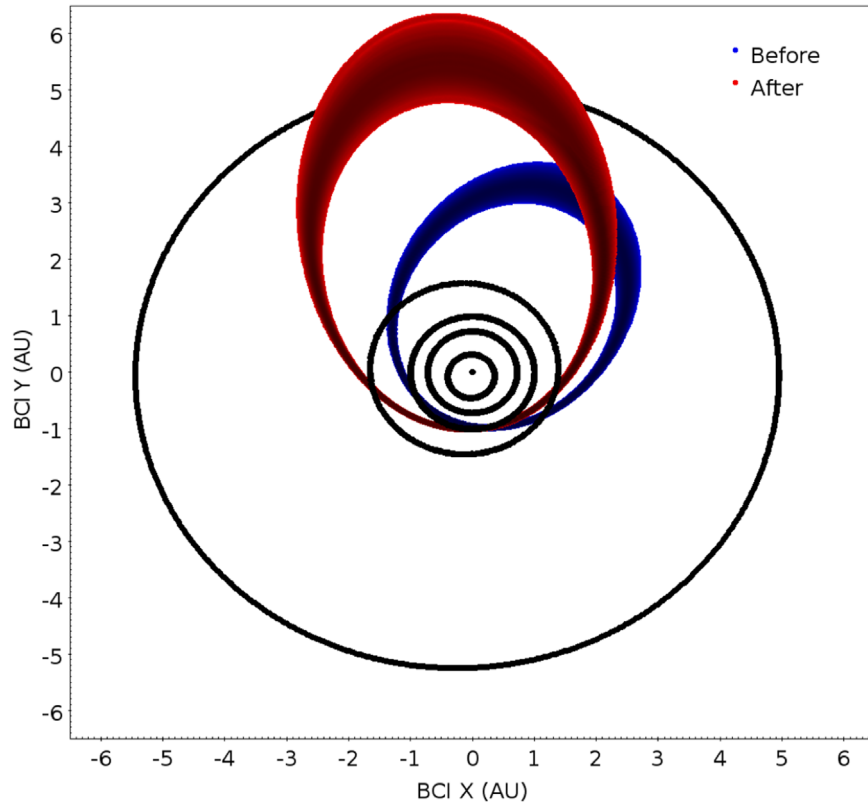


Figure 9. The meteoroid's orbit before and after the grazing encounter with Earth. The meteoroid originated from an Apollo-type asteroidal orbit and was inserted into a JFC orbit. Once in this JFC orbit, the object's path rapidly becomes less certain due to multiple close encounters with Jupiter.

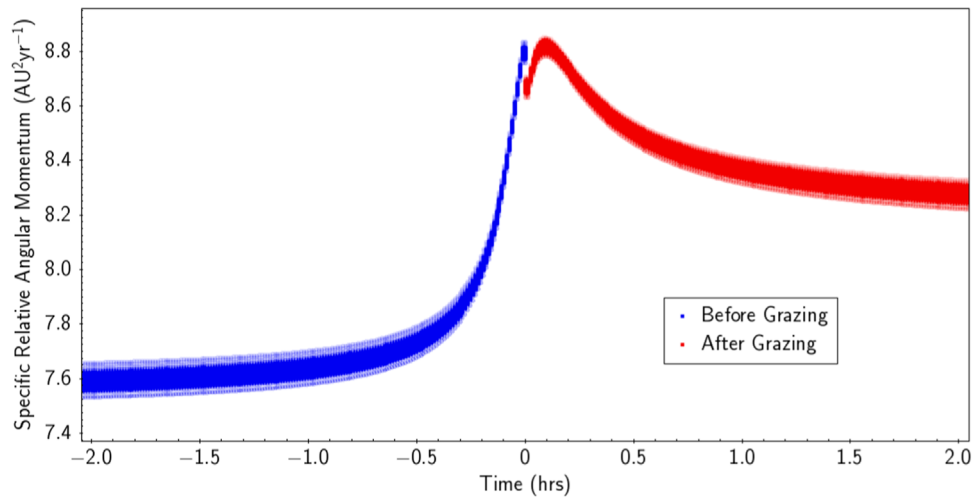


Figure 10. Specific relative angular momentum of the meteoroid ± 12 hours relative to the grazing event. The meteoroid gains energy after its encounter with Earth despite losing some energy during the atmospheric passage. At time $=0$, the discontinuity is due to the exclusion of the time when the meteoroid was passing through the atmosphere. The “instant” drop in energy here corresponds to the energy lost due to atmospheric drag. The object continues to gain angular momentum briefly after leaving the atmosphere before losing some energy as it travels away from Earth. This net gain in angular momentum effectively increased the semimajor axis and eccentricity of the body.

space. Following the likely meteoroid–Jupiter close encounter of 2025, the orbit of the meteoroid can only be treated statistically. The density plots in Figure 12 show the evolution of the semimajor axis, eccentricity, and inclination of 10,000 test particles forward in time only 100 yr. Most of the particles stay together, indicated by the darker portions of the plot. However, as seen by the multiple jumps in values over time, the meteoroid is likely to have a plethora of close encounters with Jupiter over its lifetime in a JFC orbit, and every one of these encounters obscures the future of the object.

Close Encounters with Earth. In order to determine the likelihood of future or previous close encounters with Earth, two simulations with 5000 particles were integrated both backward and forward 20 yr relative to the event (Figure 13). During these simulations, outputs were collected at a higher frequency in order to accurately characterize all possible close encounters. The probability that there was an encounter with Earth within three and one Hill radii within 20 yr prior to the grazing event was 2.4% and 0.7%, respectively. Additionally, the probability that a future close encounter with Earth will occur within the proceeding 20 yr after the grazing event is 1.4% and 0.5%, respectively. Therefore, the probability of having the opportunity to telescopically observe this object as it re-approaches Earth is very slim. The most likely time for this to occur is in 2023 mid-July, but there is still only a 1.1% chance that it will get within 3 Hill radii of the planet.

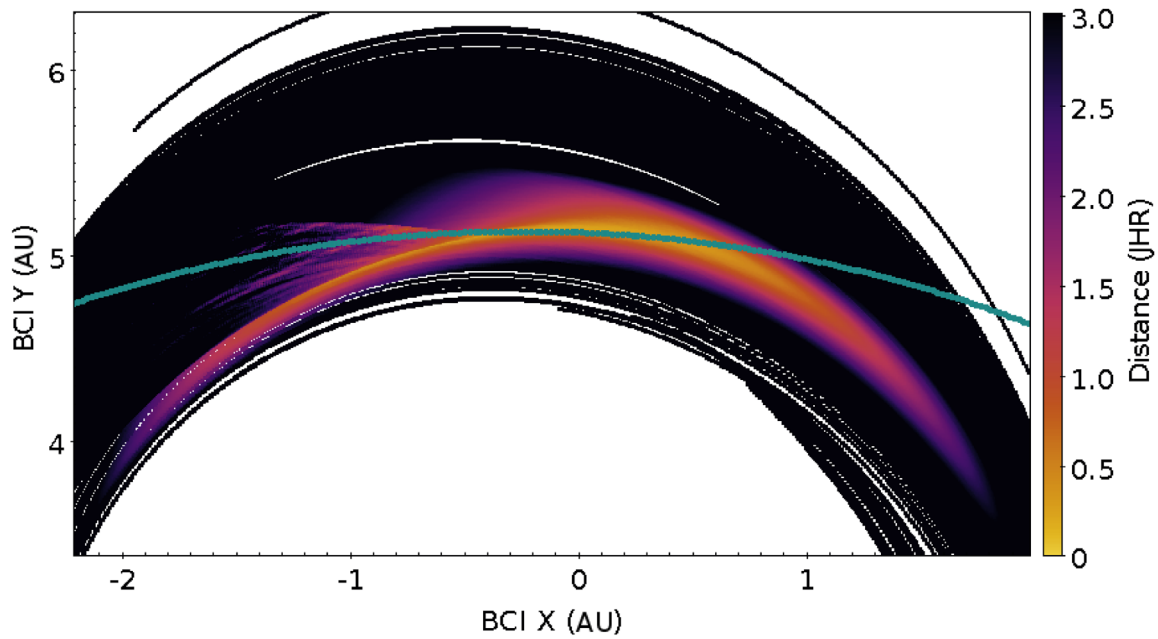
4.3. Long-term Simulations

Further analysis using substantially longer integrations of test particles was performed in order to statistically characterize the meteoroid’s future. The longest of these simulations was a forward integration of 1000 test particles for 500 kyr. Over the course of the 500 kyr forward integration, most of the particles (60.1%) are eventually ejected from the solar system, as expected (Figure 14). The vast majority of the particles that remain in the solar system (heliocentric orbits) stay in JFC

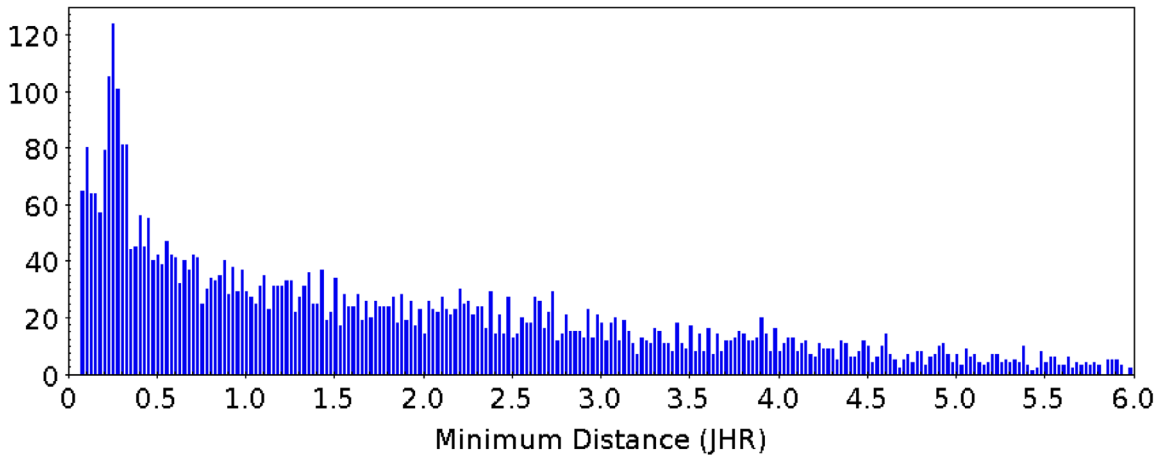
orbits (as defined by the Tisserand’s parameter) for the entire integration (Figure 15).

As seen in Figure 14, there is an exponential decay in the number of particles in heliocentric and JFC orbits. The average dynamical lifetime for the particles in JFC orbits is approximately 200 kyr, which is shorter than the ~ 325 kyr dynamical lifetime estimate for JFCs (Levison & Duncan 1997; Duncan et al. 2004). This is likely due to the initial post-grazing orbit, which has an aphelion very near the orbit of Jupiter. However, bodies in JFC orbits that display cometary features are more likely to have multiple ≤ 0.1 au encounters with Jupiter, reducing the orbital stability compared to asteroidal interlopers within the population (Fernández & Sosa 2015). Therefore, the JFC-orbit dynamical lifetime for the meteoroid is indistinguishable from a JFC from a more traditional source region. In Figure 14, the JFC, asteroidal, and LPC categories are solely determined by the particles’ Tisserand parameter. Whereas, the Centaur and trans-Neptunian objects are defined as having orbits between Jupiter and Neptune, and beyond the orbit of Neptune, respectively. This classification does lend itself to including some Centaurs and trans-Neptunian objects when counting the number of JFCs.

A smaller fraction (31.6%) of the test particles evolve onto asteroidal or long-period cometary orbits as defined by their Tisserand parameter values (Figure 16). The majority of asteroidal particles are determined to be in the outer solar system. These are particles that originated from JFC space that were decoupled from Jupiter over time due to planetary perturbations and are now on Centaur or trans-Neptunian orbits. This portrays a similar mechanism alluded to in the concluding statements in Meech et al. (2004), where they estimate that there should be ~ 20 objects of kilometer-size from the main-belt being scattered by Jupiter every million years in today’s solar system. The object discussed in this study differs in that it was gravitationally scattered by Earth and then by Jupiter, resulting in the possible transfer of volatile-depleted inner solar system material to the outer solar system.



(a) Close encounter of meteoroid with Jupiter (blue path).



(b) Histogram of the minimum distances between the particles and Jupiter.

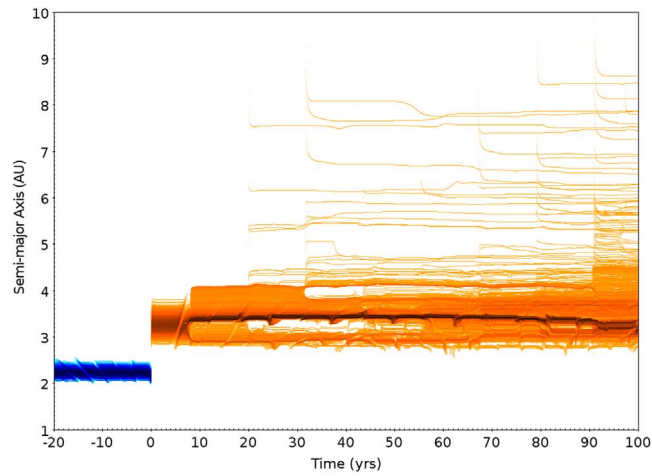
Figure 11. After grazing Earth’s atmosphere, the meteoroid will complete 1.5 orbits around the Sun before likely having its first close encounter with Jupiter. Both plots provide the distance from Jupiter in terms of Jupiter Hill Radii (JHR). Of the 5000 particles in this integration, nearly 40% come within 1 JHR and 80% are within 3 JHR. The mean approach is about 0.7 JHR. Consequently, the orbit of the meteoroid is highly uncertain after this point, approximately 7.52 yr after its grazing encounter with Earth (2025 January–March).

4.4. Analysis of Other Grazing Meteors/Fireballs

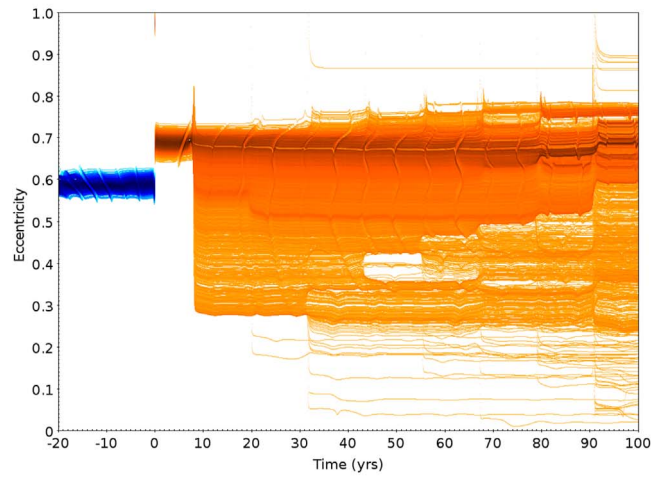
Within the current scientific literature, there have been in total 10 grazing fireballs observed. However, in only six of these cases did the meteoroid survive the atmospheric passage and return to interplanetary space (Table 3). These grazing events demonstrate the orbital changes experienced by meteoroids that come very close to Earth. In most of these occurrences, the objects experience a significant change to their orbits. Although, this does not necessarily change them enough to be orbitally reclassified. For the first photographically observed grazing fireball, in 1990 October, a 10^5 – 10^6 kg meteoroid in a higher inclination Apollo-type orbit with a JFC-like Tisserand parameter was inserted into a lower-energy orbit with a $T_J > 3$. Thus, not only has a meteoroid with a more asteroid-like T_J become more cometary due to close encounters, but the reverse has also been observed. It has been shown

that using Tisserand’s parameter is a better metric to classify small solar system bodies compared to the traditional arbitrary classification based on the orbital period (Carusi & Valsecchi 1987; Levison & Duncan 1997). Nevertheless, as shown in this study, small meter-sized objects occasionally experience close encounters with Earth and have a sufficient orbital energy change to be reclassified even under this scheme.

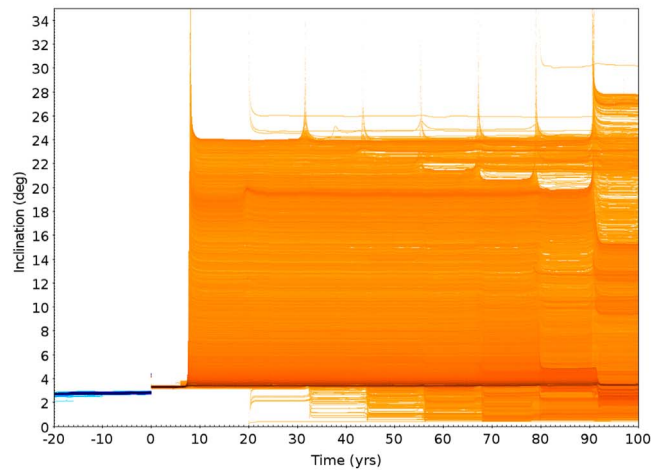
Other Grazing DFN Events. If we consider an fireball event to be grazing simply when the initial slope of the trajectory is $< 5^\circ$ and traveled > 100 km through the atmosphere, in the four years since the DFN has been fully operational, we have observed $\sim 1.2\%$ of the DFN data set to be grazing events. Indicating that although somewhat uncommon, grazing events are not extremely rare. However, in most of the events detected, the meteoroid either does not survive the atmospheric passage or loses enough velocity to be incapable of re-entering interplanetary space.



(a) Semi-major axis variation.



(b) Eccentricity variation.



(c) Inclination variation.

Figure 12. Due to the grazing encounter with Earth, the meteoroid from event DN170707_01 was sent into a Jupiter intersecting orbit. On this new trajectory, the object will likely experience many close encounters with Jupiter over its lifetime. In these density plots, the blue and orange particles represent the meteoroid before and after the grazing encounter, respectively. The darker coloration is indicative of a higher particle density. The many possible close encounters with Jupiter manifest as discrete “jumps” in the semimajor axis, eccentricity, or inclination. Over time the orbits tend to spread out due to numerous close encounters with Jupiter. Thus, the orbit of the meteoroid becomes less clear over a relatively short period of time.

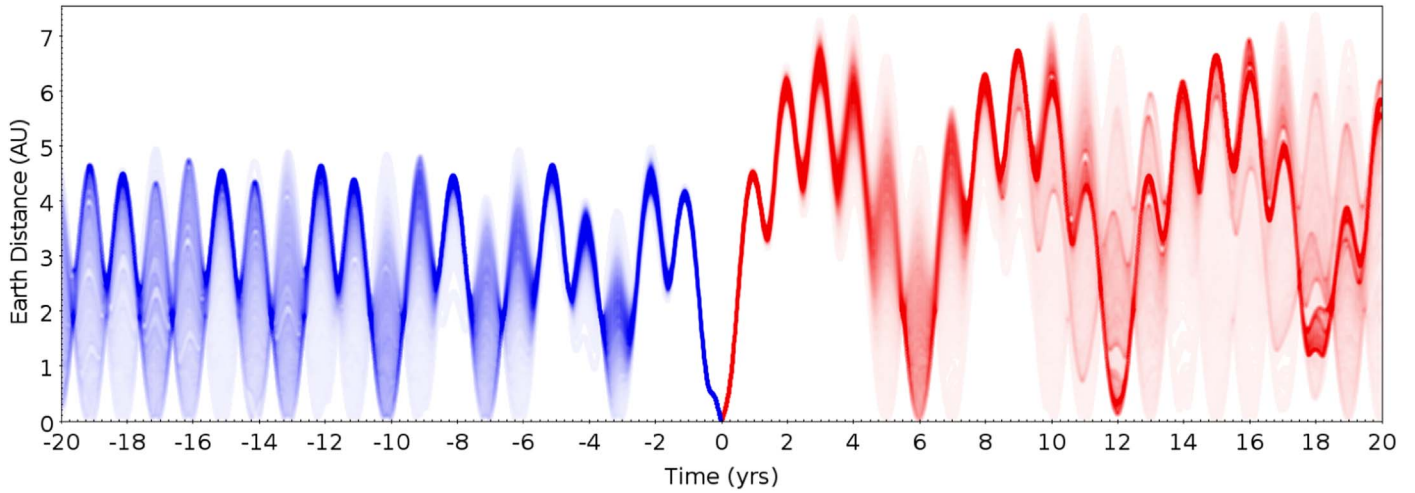


Figure 13. Plot of distance relative to Earth over time. These two simulations were conducted with 5000 particles and lasted 20 yr (forward and backward). The time on the x-axis is relative to the event epoch. The probability of an encounter with Earth for the 20 yr before and after the fireball observation is extremely low. There is a 2.4% probability of coming within 3 Hill radii and a 0.7% probability having a 1 Hill radii encounter with Earth within 20 yr before the grazing encounter. Meanwhile, there is a 1.4% and a 0.5% probability of the meteoroid encountering Earth again within one and three Hill radii in the next 20 yr respectively. There is 1.1% that the object will approach within 3 Hill radii in 2023 July.

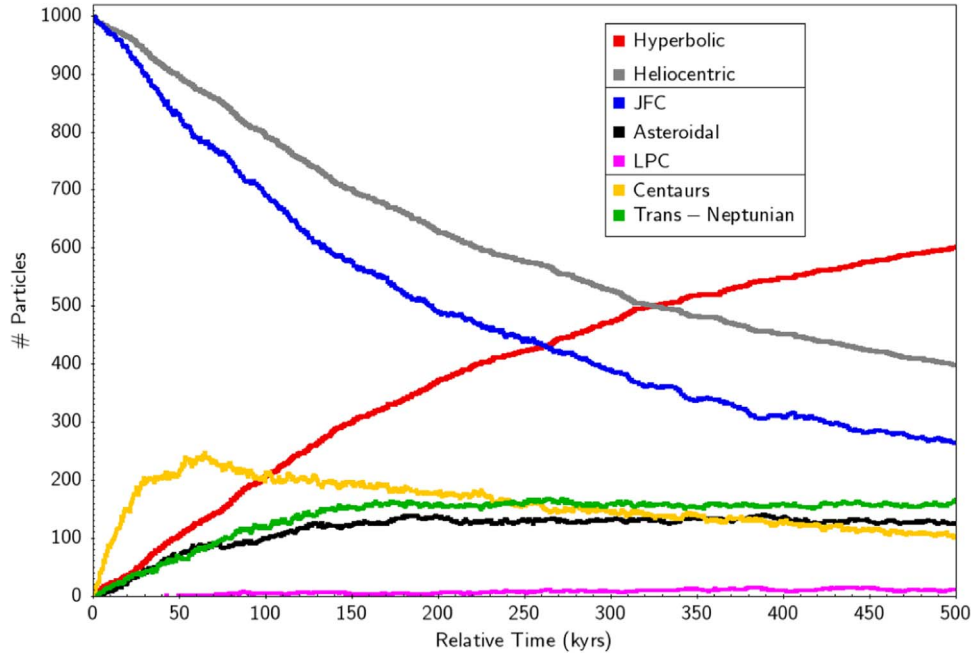


Figure 14. Plot showing the change in the orbital classification of the 1000 particles in the forward integration of event DN170707_01 for 500 kyr. The lines separating the labels in the legend group classifications together that are mutually exclusive (e.g., particles cannot be simultaneously hyperbolic and heliocentric). Over time, the likelihood that the meteoroid will have a close enough encounter to eject it from the solar system increases. By the end of the simulation, 60.1% of the particles are ejected, 27.3% are still on JFC orbits, and 12.6% have remained in the solar system but have either gone onto long-period cometary or asteroid-like orbits. Many of the particles ($\sim 20\%$) evolve onto Centaur and then trans-Neptunian orbits due to close encounters with Jupiter.

4.5. Implications and Further Research

Grazing fireballs indicate that meter-scale NEOs are occasionally inserted into categorically new orbits due to close encounters with Earth, or indeed other planets. How effective this mechanism is for mixing material in the inner solar system for small objects is still to be determined. Current work is being done to produce an artificial data set of close encounters undetected by telescopes based upon the entire orbital data set of the DFN (P. M. Shober et al. 2020, in preparation). This analysis will be extremely valuable to conclusively determine how significant this process is

for small objects in the inner solar system. If it is non-negligible, what populations in the near-Earth space may be more or less contaminated by genetically unrelated material, how significant are the orbit alterations, and what may this imply about where meteorites come from?

5. Conclusions

On 2017 July 7, the DFN observed a >1300 km long grazing fireball by 10 of its high-resolution digital fireball observatories. The meteoroid transited the atmosphere for over 90 s and

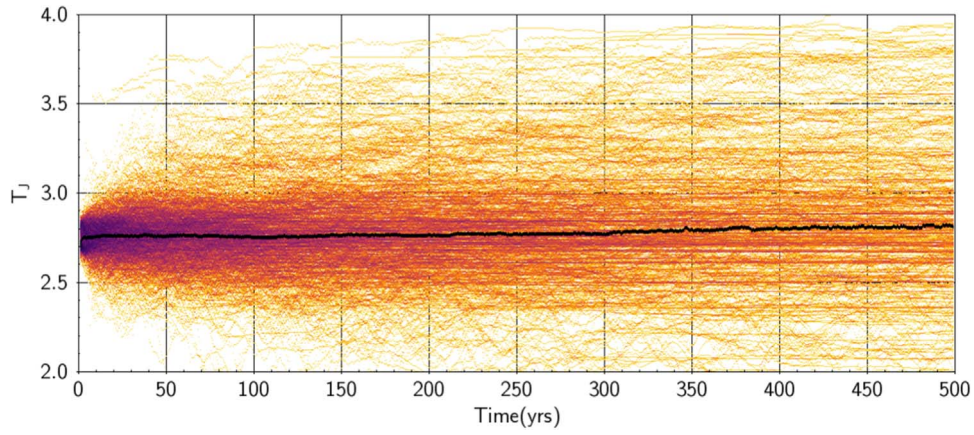


Figure 15. Tisserand’s parameter variation of 1000 particles integrated for 500 kyr post-grazing event for DN170707_01. Particles that are ejected from the solar system are removed. The meteoroid is likely to stay in a JFC orbit for an amount of time normal for a natural JFC object. The coloration in the plot is indicative of density—darker in areas of higher particle density and lighter in areas of lower particle density.

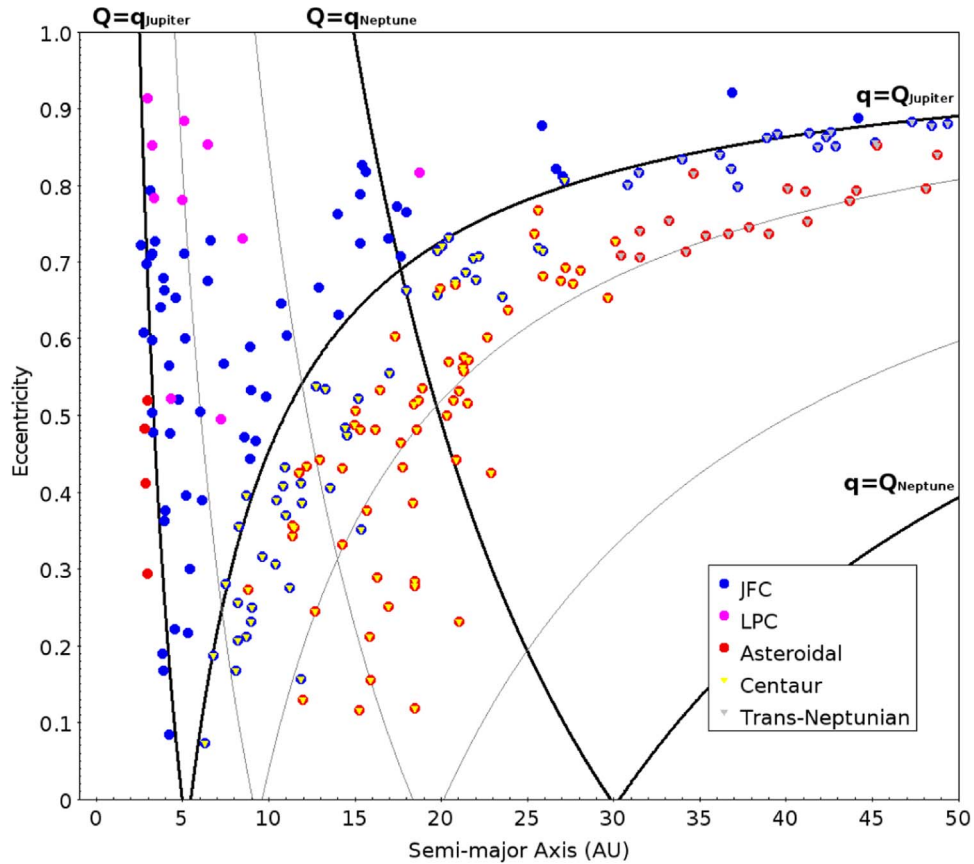


Figure 16. Semimajor axis vs. eccentricity for the particles that are still gravitationally bound to the Sun after the forward integration of 1000 particles for 500 kyr. The lines of equal perihelion and aphelion are plotted for Jupiter and Neptune in black, and in gray for Saturn and Uranus. Most of the remaining heliocentric particles (68.4%) are in JFC-like orbits (blue) according to their Tisserand parameter. However, a considerable number of particles (29.1%) are considered asteroidal, according to their Tisserand parameter with respect to Jupiter (red). Only a very small number of these are in the inner solar system. A vast majority appear to be former JFC particles that have completely decoupled from Jupiter and have drifted onto Centaur and trans-Neptunian orbits due to planetary perturbations over time. The Centaur and trans-Neptunian particles can have either JFC or asteroidal-like Tisserand parameters ($T_J > 2$), as shown by the colorization in this plot. Also, about 2.5% of the particles are categorized as long-period comets despite their low semimajor axis because they are orbiting in retrograde orbits.

reached a minimum height of 58.5 km before returning to interplanetary space. This fireball is only matched by the notorious “Great Daylight Fireball of 1972,” which penetrated to a very similar depth in the atmosphere but lasted ~ 9 s longer. As a result of the grazing encounter with Earth, the meteoroid observed by the DFN underwent a natural slingshot

maneuver in which it was transferred from an asteroidal Apollo-type orbit to a JFC orbit. Additionally, numerical integration of the object forward 500 kyr indicated that it will most likely stay in a JFC orbit for ~ 200 kyr—indistinguishable from any other JFC. Considering there are likely many small objects that go telescopically undetected that have close

Table 3

Summary of Six of the Ten Previous Earth-grazing Meteors within Scientific Literature in Which the Meteoroid Survived the Passage through the Atmosphere

Event Date	Event Location	Detection Method	Initial Mass	Orbit Before	Orbit After	T_J Before	T_J After	References
1972 Aug 10	Western US and Canada	Satellite infrared radiometer	10^5 – 10^6 kg	Amor	Apollo	4.14	4.52	Cepilecha (1979)
1990 Oct 13	Czechoslovakia and Poland	Photographic	~ 44 kg	Apollo	Apollo	2.27	3.07	Borovicka (1990)
2003 Sep 23	Ukraine	Video		Apollo	Apollo	0.66	0.79	Kozak & Watanabe (2017)
2006 Mar 29	Japan	Video, photographic, telescope	~ 100 kg	JFC		2.85		Abe et al. (2006)
2012 Jun 10	Spain	Video	1.5–115 kg	Daytime ζ -Perseid	Daytime ζ -Perseid	3.31	4.04	Madiedo et al. (2016)
2014 Dec 24	Spain	Video		Apollo		5.3		Moreno et al. (2016)

Note. Information omitted in the table was not included in the corresponding study.

encounters with Earth, there may be a non-negligible amount of meter-sized objects in modified orbits within the inner solar system.








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This research made use of Astropy, a community-developed core Python package for Astronomy (Robitaille et al. 2013;?). Simulations in this paper made use of the REBOUND code which can be downloaded freely at <http://github.com/hannorein/REBOUND> (Rein & Liu 2012).

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Software: Astropy (Robitaille et al. 2013; Astropy Collaboration et al. 2018), REBOUND (Rein & Liu 2012).

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