

Erratum: Black holes and gravitational waves in models of minicharged dark matter

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List of corrected errors

The published work has a couple of typos, and incorrect factors of two in the EM fluxes, as well as incorrect combinations of Newton’s constant and its effective version, G and G_{eff} . In particular, eqs. (3.2)-(3.5) should read

$$\frac{dE_{\text{em}}}{dt} \sim \frac{2}{3} \left(\frac{\epsilon_1 e}{m_1} - \frac{\epsilon_2 e}{m_2} \right)^2 \frac{G_{\text{eff}}^2 m_1^2 m_2^2}{c^3 R^4}, \quad (1)$$

$$\frac{dE_h}{dt} \sim \frac{2}{3} \left(\frac{\epsilon_{h,1} e}{m_1} - \frac{\epsilon_{h,2} e}{m_2} \right)^2 \frac{G_{\text{eff}}^2 m_1^2 m_2^2}{c^3 R^4}, \quad (2)$$

$$\frac{dE_{\text{GW}}}{dt} \sim \frac{32}{5c^5} \eta^2 \frac{GG_{\text{eff}}^3 M^5}{R^5}, \quad (3)$$

$$\frac{dE_{\text{dip}}}{dt} := \frac{2}{3} \zeta^2 \frac{G_{\text{eff}}^3 m_1^2 m_2^2}{c^3 R^4}. \quad (4)$$



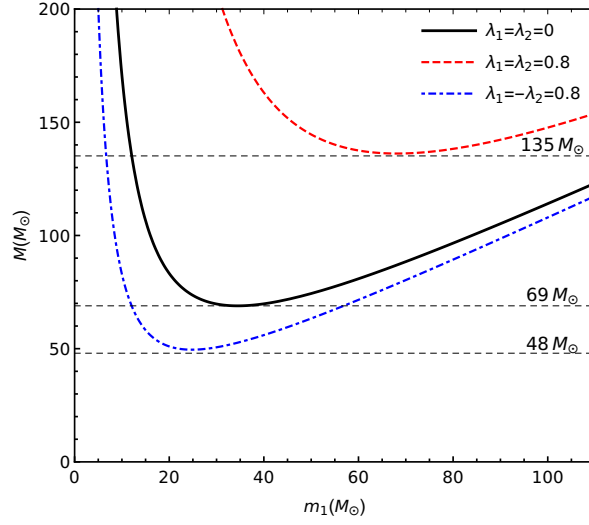


Figure 1. Total mass $M = m_1 + m_2$ of a binary system as a function of m_1 obtained from eq. (7) for fixed $\mathcal{M}_{\text{measured}} \approx 30M_\odot$ and for different values of λ_i . The black curve corresponds to the uncharged case [1]. Note that when $\lambda_1\lambda_2 < 0$ the total mass of the system can be significantly smaller than in the uncharged case.

Equation (3.7) should read as

$$R \ll 480 \frac{GM}{c^2} \left(\frac{0.1}{\zeta} \right)^2, \quad \Omega \gg 0.3 \text{Hz} \sqrt{\frac{G_{\text{eff}}}{G}} \left(\frac{60M_\odot}{M} \right) \left(\frac{\zeta}{0.1} \right)^3, \quad (5)$$

and eq. (3.8), the most important object of the work, along with the definition of chirp mass should read as

$$\begin{aligned} \Psi_+(f) = 2\pi f t_c - \Phi_c + \frac{3}{128} \frac{G_{\text{eff}}}{G} \left(\frac{G_{\text{eff}} \mathcal{M}}{c^3} \pi f \right)^{-5/3} & \left[1 - \frac{5}{84} \eta^{2/5} \zeta^2 \frac{G_{\text{eff}}}{G} \left(\frac{G_{\text{eff}} \mathcal{M}}{c^3} \pi f \right)^{-2/3} \right. \\ & \left. + \left(\frac{3715}{756} + \frac{55}{9} \eta \right) \eta^{-2/5} \left(\frac{G_{\text{eff}} \mathcal{M}}{c^3} \pi f \right)^{2/3} \right], \end{aligned} \quad (6)$$

where t_c and Φ_c are the time and phase at coalescence, f is the GW frequency and $\mathcal{M} := M\eta^{3/5}$ is the chirp mass.

Because to leading order the GW phase depends on the combination $(G_{\text{eff}}/G)^{-2/3}(G\mathcal{M})^{-5/3}$, a rescaling of Newton's constant is degenerate with the measurement of the chirp mass. Extracting the latter from the Newtonian GW phase obtained by neglecting charge effects would yield a result that is rescaled by a factor $(G_{\text{eff}}/G)^{2/3}$ relative to the real chirp mass of the system, namely

$$\mathcal{M} := M\eta^{3/5} = \frac{\mathcal{M}_{\text{measured}}}{(1 - \lambda_1\lambda_2)^{2/3}}, \quad (7)$$

Accordingly, figure 2 in the published version is affected, but the correction is small. The correct numbers are shown in figure 1.

Equation (3.10) should read as

$$r_\Psi := -\frac{18\eta^{4/5}}{743 + 924\eta} \zeta^2 \frac{G_{\text{eff}}}{G} \left(\frac{G_{\text{eff}} \mathcal{M}}{c^3} \pi f \right)^{-4/3}, \quad (8)$$

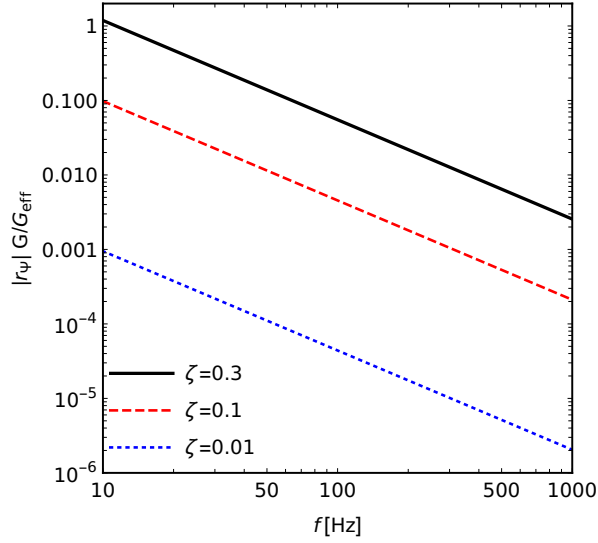


Figure 2. Ratio r_Ψ (normalized by G_{eff}/G) between the hidden-charge-induced GW phase and the first post-Newtonian correction [cf. eq. (8)] for the quasicircular inspiral of two charged masses with $m_1 = m_2 = 30M_\odot$ and different values of the coupling ζ as a function of the GW frequency. Note that $\zeta \approx 0.3$ saturates the bound presented in eq. (11).

and is shown in figure 2 as a function of the GW frequency for a typical inspiral. The only difference with respect to the published version is that the y -axis is now normalized by G_{eff}/G .

The number of cycles should read as

$$\mathcal{N} = \frac{1}{32\pi^{8/3}} \frac{G_{\text{eff}}}{G} \left(\frac{G_{\text{eff}}\mathcal{M}}{c^3} \right)^{-5/3} \left(f_{\text{min}}^{-5/3} - f_{\text{max}}^{-5/3} \right) [1 - \delta_{\mathcal{N}}] ,$$

where

$$\delta_{\mathcal{N}} = \frac{25}{336} \eta^{2/5} \zeta^2 \frac{G_{\text{eff}}}{G} \left(1 + \frac{f_{\text{min}}^{5/3}}{f_{\text{max}}^{5/3}} \right) \left(\frac{G_{\text{eff}}\mathcal{M}}{c^3} \pi f_{\text{min}} \right)^{-2/3} , \quad (9)$$

and we have also expanded for $f_{\text{max}} \gg f_{\text{min}}$ to simplify the final expression. In the small-charge limit, for $f_{\text{max}} \sim 100$ Hz and $f_{\text{min}} \sim 30$ Hz, we obtain

$$\delta_{\mathcal{N}} \approx 0.01 \left(\frac{\zeta}{0.1} \right)^2 . \quad (10)$$

Therefore, dipolar effects change the number of cycles relative to the Newtonian case by a few percent when $\zeta \approx 0.1$ and by less than 0.01% when $\zeta < 0.01$. On the other hand, these corrections become important at smaller frequencies and might produce detectable effects for space-based interferometers such as eLISA [2].

Ref. [3] performed a detailed analysis to derive GW-based constraints on generic dipolar emissions in compact-binary inspirals (see also ref. [4]). It is straightforward to map eq. (4) into this generic parametrization. In our case the parameter B defined in refs. [3, 4] reads $B = \frac{5}{48}\zeta^2$. The analysis of ref. [3] shows that GW150914 sets the upper bound $|B| \lesssim 2 \times 10^{-2}$, whereas a putative eLISA detection of a GW150914-like event with an optimal detector

configuration or a combined eLISA-aLIGO detection set the projected bound as stringent as $|B| \lesssim 3 \times 10^{-9}$. In our case these bounds translate into

$$|\zeta| \lesssim 0.4 \quad \text{aLIGO} \quad (11)$$

$$|\zeta| \lesssim 10^{-4} \quad \text{eLISA-aLIGO (projected)} \quad (12)$$

Acknowledgments

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References

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