

Mathematical model

$$H_{pump}(Q) = A + B \cdot Q + C \cdot Q^2 \quad (1)$$

where A, B, C — pump constants, obtained from the approximation of its hydraulic head characteristic.

Also the hydraulic head at the working point is equal to:

$$H_{friction} = H_{static} + \alpha \cdot Q^2 \quad (2)$$

where $\alpha = 0,0827 \frac{x \cdot l}{d^5}$ — the constant.

If we equate the above hydraulic heads and express flow rate Q , we get:

$$Q_{calculated} = \frac{-B \pm \sqrt{B^2 - 4(\alpha - C)(H_{static} - A)}}{2(\alpha - C)} \quad (3)$$

Analysis of the obtained formula for flow rate Q to the sign before the square root:

$$\alpha > 0, C < 0 \quad (4)$$

It means:

$$\alpha - C > 0 \quad (5)$$

$$H_{pump}(0) = A \quad (6)$$

$$H_{static} < A \quad (7)$$

Or:

$$H_{static} - A < 0 \quad (8)$$

Then:

$$\sqrt{B^2 - 4(\alpha - C)(H_o + y - A)} = \sqrt{B^2 + 4|(\alpha - C)(H_o + y - A)|} > |B| \quad (9)$$

$$Q(y) = \frac{-B + \sqrt{B^2 - 4(\alpha - C)(H_o + y - A)}}{2(\alpha - C)} \quad (10)$$

Similarly for the efficiency curve:

$$\eta(Q) = A_1 + B_1 \cdot Q + C_1 \cdot Q^2 \quad (11)$$

where A_1, B_1, C_1 — the constants of the approximately efficiency curve. Differentiate this expression:

$$\eta'(Q) = 2 \cdot C_1 \cdot Q + B_1 \quad (12)$$

Equate equation (12) to 0 to find the maximum efficiency, and we get the following formula:

$$Q_{optimal} = -\frac{B_1}{2 \cdot C_1} \quad (13)$$

We get following expression from the theory of similarity of centrifugal pumps:

$$\frac{n_2}{n_1} = \frac{Q_{optimal}}{Q_{calculated}} \quad (14)$$

where n_1 — frequency at optimal efficiency;

n_2 — initial frequency;

$Q_{\text{calculated}}$ — calculated volume flow rate.

Then it turns out, taking into account the formulas (14), (10) and (13):

$$n_2 = n_1 \cdot \frac{-B_1 \cdot 2 \cdot (\alpha - C)}{2 \cdot C_1 \cdot \left(\sqrt{B^2 - 4(\alpha - C)(H_o + y - A)} - B \right)} \quad (15)$$

Conclusion

If the centrifugal pump is selected in a particular hydraulic system so that it is not in the range of the "house" of efficiency, but there is a possibility of frequency control, when the above formula (15) allows us to determine the optimal speed of the pump rotor, providing maximum efficiency.

Reference

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