



# Variations in the Width, Density, and Direction of the Palomar 5 Tidal Tails

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## Abstract

Stars that escape globular clusters form tidal tails that are predominantly shaped by the global distribution of mass in the Galaxy, but also preserve a historical record of small-scale perturbations. Using deep *grz* photometry from DECaLS, we present highly probable members of the tidal tails associated with the evaporating globular cluster Palomar 5. These data yield the cleanest view of a stellar stream beyond  $\approx 20$  kpc and reveal: (1) a wide, low surface-brightness extension of the leading tail; (2) significant density variations along the stream; and (3) sharp changes in the direction of both the leading and the trailing tail. In the fiducial Milky Way model, a rotating bar perturbs the Palomar 5 tails and can produce streams with similar width and density profiles to those observed. However, the deviations of the stream track in this simple model do not match those observed in the Palomar 5 trailing tail, indicating the need for an additional source of perturbation. These discoveries open up the possibility of measuring the population of perturbers in the Milky Way, including dark-matter subhalos, with an ensemble of stellar streams and deep photometry alone.

*Unified Astronomy Thesaurus concepts:* Globular star clusters (656); Milky Way dynamics (1051); Milky Way stellar halo (1060); Milky Way dark matter halo (1049); Tidal tails (1701)

## 1. Introduction

Direct *N*-body simulations of globular clusters orbiting in a static galactic potential predict that the clusters continually lose stars through evaporation and tidal stripping (e.g., Baumgardt & Makino 2003). Stars escape the cluster with a small relative velocity and thus form thin, kinematically cold streams (e.g., Combes et al. 1999). As a result, globular cluster streams are excellent tracers of the underlying tidal field, and under the assumption of a static potential, they constrain the enclosed mass within their current location (Bonaca & Hogg 2018). Nearby stellar streams have already been used to measure the present-day mass and shape of the Milky Way halo (e.g., Koposov et al. 2010; Küpper et al. 2015; Bovy et al. 2016).

However, streams are long-lived and also witness the host galaxy evolve, including its gradual increase in mass, its rotating bar, and, in the context of the prevailing  $\Lambda$  Cold Dark Matter ( $\Lambda$ CDM) cosmology, a score of low-mass dark-matter subhalos predicted to orbit massive galaxies like the Milky Way (e.g., Diemand et al. 2008; Springel et al. 2008). The presence of dark-matter subhalos beyond the threshold for galaxy formation has been identified as a test of  $\Lambda$ CDM (Bullock & Boylan-Kolchin 2017) that can distinguish it from other dark-matter theories (e.g., Hu et al. 2000; Bode et al. 2001), as well as cosmological models without dark matter (e.g., Milgrom 1983; Kroupa 2015). Stellar streams simulated in  $\Lambda$ CDM halos are no longer thin, coherent structures, but instead can develop non-uniform density and width profiles (e.g., Bonaca et al. 2014; Ngan et al. 2015). Recently, Price-Whelan & Bonaca (2018) detected gaps and off-the-stream

features in the GD-1 stellar stream that could be signatures of perturbation by a low-mass object (Bonaca et al. 2019b). This discovery establishes stellar streams as an observational test of dark matter on small scales. However, streams can also be affected by baryonic perturbers, such as giant molecular clouds (Amorisco et al. 2016), the Galactic bar (Pearson et al. 2017), and spiral arms (Banik & Bovy 2019). Additionally, stream debris can spread out rapidly in phase space if their progenitors are evolving on non-regular orbits (e.g., Fardal et al. 2015; Pearson et al. 2015; Price-Whelan et al. 2016a, 2016b). Streams can even naturally develop epicyclic overdensities and asymmetries in their density profile during cluster evaporation (e.g., Küpper et al. 2008; Just et al. 2009; Küpper et al. 2010). To infer the abundance of dark-matter subhalos from density variations in stellar streams, and thus test the  $\Lambda$ CDM paradigm, we need to confirm the origin of these features first.

In this paper, we revisit the tidal tails of the Palomar 5 (Pal 5) globular cluster (Odenkirchen et al. 2001; Rockosi et al. 2002). The Pal 5 stream features density variations, but neither their significance nor their origin have been established (Carlberg et al. 2012; Bernard et al. 2016; Ibata et al. 2016; Thomas et al. 2016; Erkal et al. 2017). Arguably, Pal 5 provides the best opportunity for disentangling different mechanisms that shape the stream as it has a surviving progenitor. Such an endeavor, however, requires a robust map of the entire tidal debris. Pal 5 is located too far from the Sun to enable efficient membership selection based on *Gaia* proper motions, while accurate mapping using the existing photometry is limited because the catalogs are either wide but shallow

(Bernard et al. 2016), or deep but narrow (Ibata et al. 2016). To confidently identify Pal 5 members over a wide area, we use deep, wide-field photometry from the DECam Legacy Survey (Section 2). In Section 3 we use the updated map of Pal 5 to quantify how the stream track, width, and density vary along the stream. We then explore how these properties change across Pal 5 models simulated in a range of Galactic potentials (Section 4) and conclude with a discussion of perturbers that jointly could have caused the observed Pal 5 features (Section 5).

## 2. Data

We study the Pal 5 system in the photometric catalog of DECam Legacy Survey (DECaLS, part of the DESI Legacy Imaging Surveys; Dey et al. 2019).<sup>11</sup> The survey was designed to provide deep *grz* imaging at high galactic latitudes, with the targeted  $5\sigma$  depth of  $g = 24$ ,  $r = 23.4$ , and  $z = 22.5$ . In addition to data obtained as a part of the survey, DECaLS also includes imaging from publicly available DECam data in the survey footprint. We conducted a targeted survey of Pal 5 whose data products are now a part of DECaLS (NOAO Proposal ID nos. 2014A-0321, PI: Geha; 2014A-0611, PI: Munoz; 2015A-0620, PI: Bonaca). The median (minimum)  $5\sigma$  point-spread function (PSF) depth in the Pal 5 region is  $g = 25.6(25.3)$ ,  $r = 25.1(24.8)$ ,  $z = 24.1(23.4)$ , which makes DECaLS the deepest and largest-area survey of Pal 5.

To select likely Pal 5 stars, we first queried the DECaLS DR8 sweep catalogs<sup>12</sup> for point sources. The catalog was constructed using *The Tractor* forward-modeling code for source extraction<sup>13</sup> and a source was classified as ‘PSF’ if the PSF model was preferred to the round exponential model used to represent galaxies.<sup>14</sup> We removed spurious sources by requiring `allmask_g==0`, `allmask_r==0` and `bright-starinblob==0`. With this clean stellar catalog, we identified stars on Pal 5’s main sequence in the dereddened color–magnitude diagram (CMD)<sup>15</sup> (using the re-calibrated Schlegel–Finkbeiner–Davis dust map; Schlegel et al. 1998; Schlafly & Finkbeiner 2011). Specifically, we selected stars following an 11.5 Gyr MIST isochrone with  $[\text{Fe}/\text{H}] = -1.3$  (Choi et al. 2016) between  $20 < g < 23.7$ .

In the top panel of Figure 1 we present the sky distribution of likely Pal 5 main-sequence stars. The  $(\phi_1, \phi_2)$  coordinate frame is oriented along the great circle that best-fits the Pal 5 stream, while keeping the cluster at the origin ( $\phi_1 = 0^\circ$ ,  $\phi_2 = 0^\circ$ ) and its motion in the direction of positive  $\phi_1$  (Price-Whelan 2017). There is a distance gradient along the Pal 5 stream (Ibata et al. 2016), so to increase its contrast against the field Milky Way stars, we applied the isochrone selection at two distances: 23 kpc for  $\phi_1 \leq 0^\circ$  and 19 kpc for  $\phi_1 > 0^\circ$ . With our map, Pal 5 is continuously detected between  $\phi_1 = -15^\circ$  and  $7^\circ$ .

The CMDs of stars in different regions of the Pal 5 stream are shown in the bottom of Figure 1. Each panel contains stars from a  $3^\circ$  long and  $0.8^\circ$  wide area marked in the top of Figure 1 (see red boxes). The Pal 5 main-sequence turn-off at  $g_0 \approx 20.5$  stands out in all fields, but the depth to which the main

sequence is detected varies from  $g_0 \approx 24$  close to the cluster to  $g_0 \approx 22$  in the leading tail. The non-uniform detection depth is partly due to variable photometric depth (the coverage is shallower in the leading tail), and partly due to contamination from the Sagittarius stellar stream (main-sequence turn-off at  $g_0 \approx 22$  for  $\phi_1 \gtrsim -5^\circ$ ) and faint galaxies ( $g_0 \gtrsim 23$ ). Despite these challenges, the Pal 5 main sequence is evident even in field 9 ( $9^\circ < \phi_1 < 12^\circ$ ), beyond the apparent leading tail truncation at  $\phi_1 \approx 7^\circ$ . This indicates that Pal 5 tails may be longer than previously thought (Bernard et al. 2016).

To improve our selection of Pal 5 members, we first employ the *z*-band to distinguish between faint stars and galaxies more efficiently. In DECam filters, the  $g - z$  color of stars bluer than  $g - r \lesssim 1.2$  is approximately linear with the  $g - r$  color (e.g., Dey et al. 2019). We adopted the stellar locus of  $(g - z)_0 = 1.7 \times (g - r)_0 - 0.17$ . On the other hand, galaxies span a wider distribution of redder  $g - z$  colors at a fixed  $g - r$  color. To exclude faint galaxies, we restrict to sources within 0.1 mag of the stellar locus. We limit the sample to sources with  $g_0 < 23$  to reduce inhomogeneities due to the shallow *z*-band coverage.

To further refine the Pal 5 membership, we next perform the isochrone selection that varies the distance along the stream. In each panel of Figure 1, an isochrone has been manually placed to the distance that matches the main-sequence turn-off of the Pal 5 population. This procedure is sufficiently precise to select Pal 5 members at high confidence, so we defer more precise modeling of Pal 5’s stellar population along the tails to future work (e.g., by using isochrone-fitting methods implemented in Speagle et al. 2018). The adopted distance modulus relative to the cluster bin (segment 6) is indicated in CMD panels at the bottom of Figure 1, and the corresponding isochrone is shown in orange. Qualitatively matching the location of the turn-off, we find that the leading tail is closer than the trailing tail, in agreement with the precise RR Lyrae distance trend found in Price-Whelan et al. (2019). We perform the updated isochrone selection in  $2^\circ$  bins of  $\phi_1$  by interpolating the location of the main-sequence selection box between these distance estimates. With the improved star–galaxy separation and a selection that accounts for the distance gradient along the stream, Pal 5 tails are prominent between R.A.  $\approx 223^\circ$  and  $\approx 245^\circ$  (Figure 2). There is still some contamination remaining, which cannot be reduced with *Gaia* data due to the faint magnitudes of our sources. Future surveys, e.g., *WFIRST*, will deliver precise proper motions for faint stars (The WFIRST Astrometry Working Group et al. 2017), and enable additional selection of Pal 5 members based on kinematics. At the present, however, Figure 2 shows the cleanest selection of Pal 5 stars.

The DECaLS map of Pal 5 presented in Figure 2 reveals qualitatively new features in the stream. First, the leading tail extends to decl.  $\approx -7^\circ$ , beyond the previously detected edge at decl.  $\approx -5^\circ$  (Bernard et al. 2016). This newly detected extension of the leading tail is very wide ( $\sigma \approx 0.25^\circ$ ) and in stark contrast with the trailing tail at the same distance from the cluster ( $\sigma \approx 0.1^\circ$ ). We refer to this wide, low surface-brightness extension as the “fan” (Pearson et al. 2015). In the right panels of Figure 2, we compare the CMD of the fan to an off-stream control field. The fan has a stellar population consistent with Pal 5 (orange isochrone; see also Figure 1), in contrast to the control field, and is therefore likely an extension of the leading tail.

<sup>11</sup> See also [www.legacysurvey.org](http://www.legacysurvey.org)

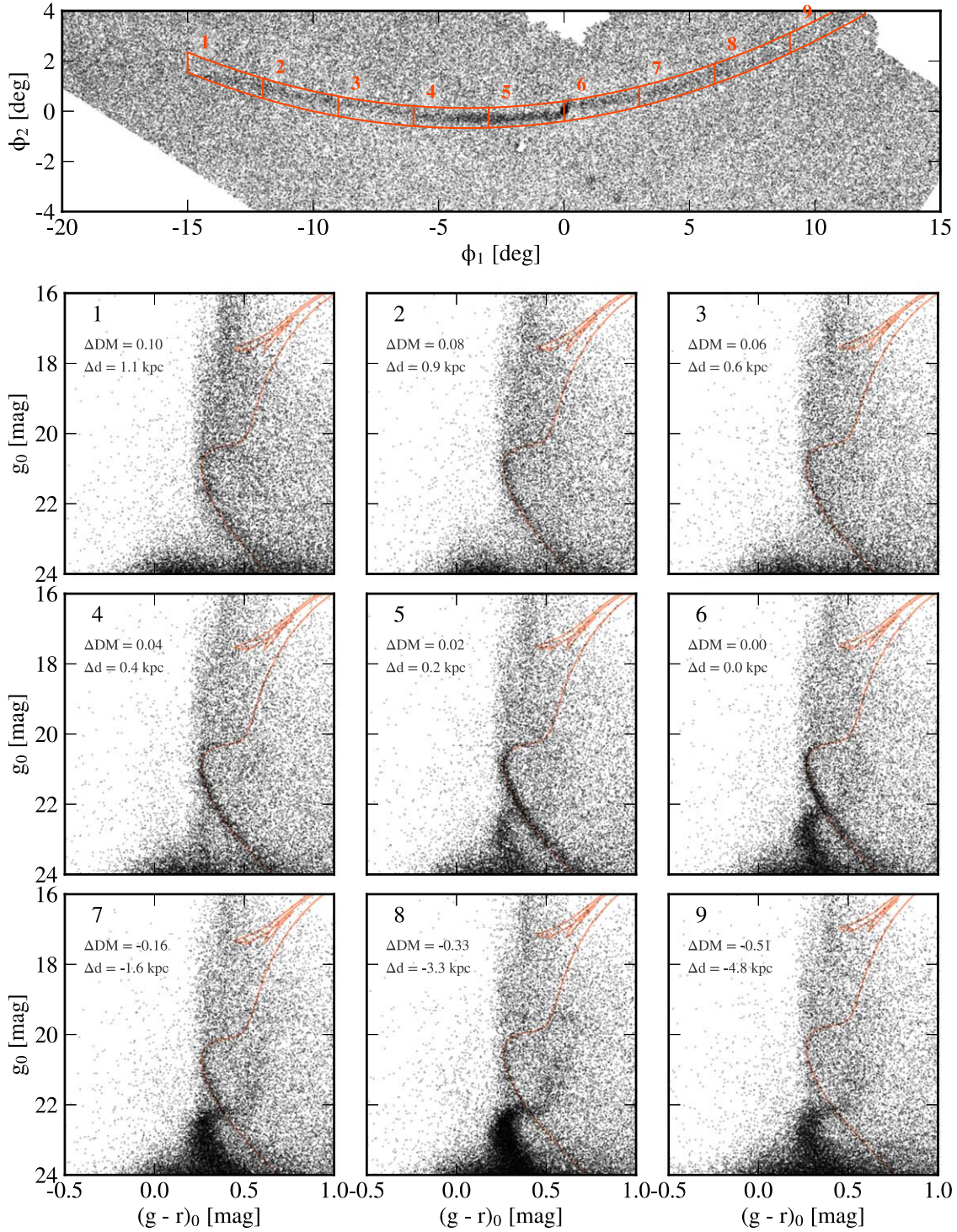
<sup>12</sup> <http://legacysurvey.org/dr8/files/#sweep-catalogs-region-sweep>

<sup>13</sup> <https://github.com/dstndstn/tractor>

<sup>14</sup> <https://github.com/legacysurvey/legacypipe>

<sup>15</sup> Dereddened photometry is designated with the subscript 0, e.g.,  $g_0$  and  $(g - r)_0$ .



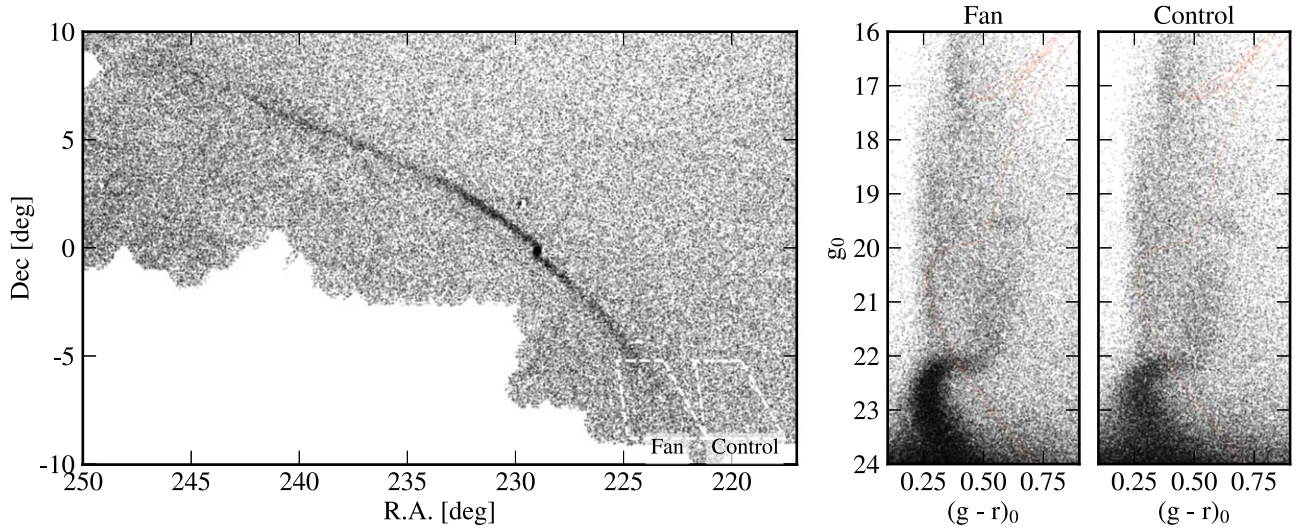


**Figure 1.** Top: Legacy Surveys detection of the Palomar 5 (Pal 5) globular cluster in a coordinate system aligned with its tidal tails (see the Appendix). Bottom: Color-magnitude diagrams of  $\approx 0.8 \times 3 \text{ deg}^2$  windows along the tails. The regions are labeled in the top left of each panel, and their sky locations are marked in the top panel. A stellar population consistent with Pal 5 is evident in every region, although its prominence varies between the fields. There is a distance gradient along the stream, with the end of the trailing tail ( $\phi_1 \approx -15^\circ$ ) being the most distant, and end of the leading tail ( $\phi_1 \approx 10^\circ$ ) the closest. The fiducial Pal 5 isochrone is offset in every panel so that it matches the location of the main sequence (offsets in distance modulus and distance from the fiducial Pal 5 values are indicated in the top left).

Next, there are significant variations in the stellar density along the stream. At a fixed distance from the cluster, the trailing tail is denser than the leading tail. Furthermore, both tails feature a prominent gap in the stellar density, located at R.A.  $\approx 227^\circ$  and  $235^\circ$  for the leading and trailing tail, respectively. Finally, the stream track sharply changes direction at R.A.  $\approx 226^\circ$  and  $233^\circ$ .

### 3. Stream Density Modeling

We quantify the variations along the Pal 5 stream and measure the stream track, width, and surface density by constructing a joint model of the stream and background stellar density. In bins of  $\phi_1$ , we model the (CMD-filtered) density distribution in  $\phi_2$  using a single Gaussian component for the



**Figure 2.** Optimized Legacy Surveys detection of the Pal 5 system (left) reveals: (1) prominent underdensities at R.A.  $\approx 227^\circ$  and  $235^\circ$ , (2) sharp changes in the direction of the stream track at R.A.  $\approx 226^\circ$  and  $233^\circ$ , and (3) an extremely wide, low surface-brightness extension (“fan”) of the leading tail beyond decl.  $\lesssim -5^\circ$ . The “fan” has a stellar population consistent with Pal 5 (see the color–magnitude diagram comparison to a control field, right, with the Pal 5 isochrone overplotted in orange). These features may be evidence of Pal 5’s perturbed dynamical history.

stream and a linearly varying background (similar to the density modeling described in Price-Whelan & Bonaca 2018). We initialize bin centers between  $\phi_1 \in (-20, 10)^\circ$  with a spacing of  $h_{\phi_1} = 0.75$ , but when modeling the density in  $\phi_2$  in any bin, use partially overlapping bins of width  $1.5 h_{\phi_1}$ .

In detail, within each  $\phi_1$  bin, we construct a model for the CMD-filtered density distribution in  $\phi_2$  as

$$p(\phi_2 | \theta) = f p_{\text{str}}(\phi_2 | \mu, \sigma) + (1 - f) p_{\text{bg}}(\phi_2 | a, b), \quad (1)$$

$$p_{\text{str}}(\phi_2 | \mu, \sigma) = \mathcal{N}(\phi_2 | \mu, \sigma^2), \quad (2)$$

$$p_{\text{bg}}(\phi_2 | a, b) \propto a \phi_2 + b, \quad (3)$$

where  $\theta = (f, \mu, \sigma, a, b)$  are the density model parameters,  $f$  is the fraction of stars in Pal 5 in the current bin,  $\mu$  is the stream centroid (track),  $\sigma$  is the stream width,  $a, b$  are parameters of the linear background model, and  $\mathcal{N}(x | \mu, \sigma^2)$  denotes the normal distribution over  $x$  with mean  $\mu$  and variance  $\sigma^2$ . We assume uniform prior probability distributions,  $\mathcal{U}(\alpha, \beta)$  (defined over the domain  $(\alpha, \beta)$ ), for  $(f, a, b)$ , a Gaussian prior on  $\mu$  to keep it close to the initialized stream track, and a prior that is uniform in  $\ln \sigma$  for the stream width,

$$p(f) = \mathcal{U}(f | 0, 1), \quad (4)$$

$$p(\mu) = \mathcal{N}(\mu | \mu_0, 1^\circ), \quad (5)$$

$$p(\sigma) = \mathcal{U}(\ln \sigma | -10, 10), \quad (6)$$

$$p(a) = \mathcal{U}(a | -10, 10), \quad (7)$$

$$p(b) = \mathcal{U}(b | -10, 10), \quad (8)$$

$$p(\theta) = p(f) p(\mu) p(\sigma) p(a) p(b), \quad (9)$$

where  $\mu_0$  is the initialized location of the stream track in any bin.

We use an ensemble Markov Chain Monte Carlo sampler *emcee* (Foreman-Mackey et al. 2013) to generate samples from the posterior probability distribution over our model

parameters

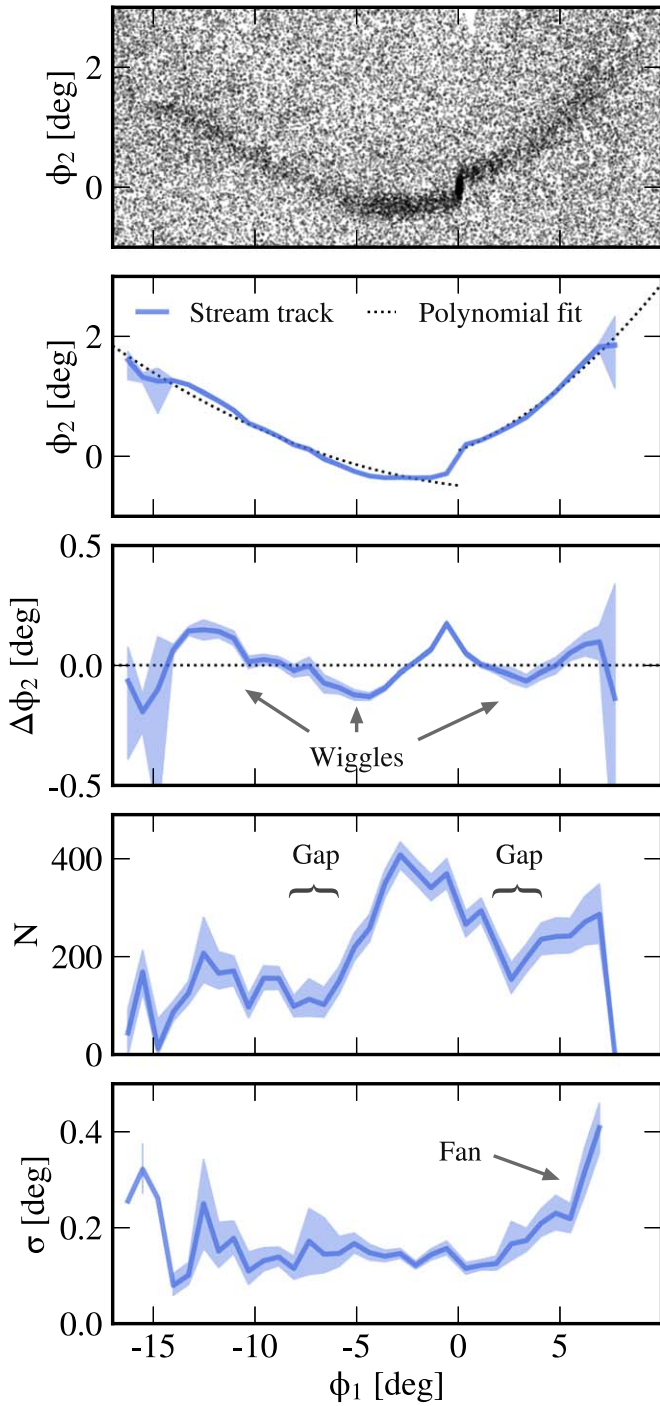
$$p(\theta | \phi_{2N}) \propto p(\theta) \prod_n^N p(\phi_{2,n} | \theta), \quad (10)$$

where  $\phi_{2N}$  are the  $\phi_2$  positions of all  $N$  CMD-filtered stars in the given  $\phi_1$  bin. We use 64 walkers in the sampler and, for a given  $\phi_1$  bin, initialize the positions of the walkers by sampling from a small Gaussian (with dispersion  $10^{-4}$ ) around the fiducial parameter position  $\theta_0 = (0.2, \mu_0, 0.1, 0, 1)$ , with  $\mu_0$  determined by binning the  $\phi_2$  distribution and taking the bin center with the most stars. We initially burn-in the samplers for 512 steps, then reset and re-run for an additional 1024 steps. We then compute the median and (16, 84)th percentile parameter values in each  $\phi_1$  bin.

Figure 3 shows the results of running this density model on the observed distribution of Pal 5 members (top row). In the second row, we present the inferred stream track (solid blue line and confidence interval). As previously found by Bernard et al. (2016), the trailing tail is significantly longer than the leading tail ( $\approx 16^\circ$  versus  $\approx 8^\circ$  in our data). The general curvature of the stream is well-captured by second-order polynomials (fits to the leading and the trailing arm are shown as dotted lines). However, the stream track changes direction at several locations, as evident in the track’s deviation from the polynomial fits (third row). Two of these wiggles appear almost symmetrically in the leading and trailing tails at  $\phi_1 \approx 3.5^\circ$  and  $\phi_1 \approx -4.5^\circ$ , respectively, while the trailing tail has another wiggle at  $\phi_1 \approx -13^\circ$ .

Next, we quantify the total number of stars in the Pal 5 stream, as well as its density profile (fourth row). Accounting for the field Milky Way population, we find  $3000 \pm 100$  Pal 5 stars between  $20 < g_0 < 23$  excluding the progenitor. Integrated out to  $|\phi_1| = 8^\circ$  (limited by the extent of the leading arm), the trailing and the leading tail have approximately the same number of stars. But much like the total stream extent, the density profile is also asymmetric, so within  $5^\circ$  from the cluster, the trailing tail has a 50% excess over the leading tail. On top of these global density variations, Pal 5 features two prominent





**Figure 3.** Members of the Pal 5 stream, in a coordinate system aligned with the stream (see the [Appendix](#)), used for 1D density modeling (top row). The inferred stream track and its residual from second-order polynomial fits to each tidal arm (rows 2 and 3, respectively) show sharp changes in the tails’ direction (“wiggles”). The density profile (row 4) is asymmetric overall, and features two prominent underdensities (“gaps”). The trailing tail remains thin even far from the cluster, while the leading has a marked increase in width past  $\phi_1 \gtrsim 5^\circ$  (the “fan,” row 5).

underdensities at  $\phi_1 \approx -7^\circ$  and  $\phi_1 \approx 3^\circ$ . Even in these underdense regions, deep DECaLS data enabled us to detect the stream more confidently above the background than in earlier data sets (see [Bernard et al. 2016](#); [Erkal et al. 2017](#)).

Finally, we measure how the width of Pal 5 varies along the stream (fifth row). Close to the cluster, both the leading and the

trailing tail are thin,  $\sigma \approx 0^\circ.15$ . The trailing tail remains as thin throughout, with the exception of lower-density regions, where the inference is more uncertain due to a higher level of contamination. On the other hand, the leading tail rapidly increases in width to  $\sigma \approx 0^\circ.4$  (130 pc) at  $\phi_1 \approx 7^\circ$  (assuming a distance of 18.9 kpc, see [Figure 1](#)). Since the tidal debris is fanned over a larger area, its surface density is low, and thus this part of the stream avoided detection in shallower data sets.

To summarize, we detected variations in the direction, density, and width of the Pal 5 stream. In [Section 4](#) we explore the origin of these features by running the same density model on four different Pal 5 simulations.

#### 4. Simulations of Pal 5’s Evolution

To explore plausible mechanisms that could produce the observed morphology of the Pal 5 stream, we run a suite of Pal 5 simulations. In particular, we investigate whether Pal 5’s wide leading tail can be explained due to chaotic regions in the potential, or whether torques from the Galactic bar are necessary to explain its width. We further investigate what might have caused the length asymmetry between the leading and trailing tail, as well as the gap in the trailing tail. In [Section 4.1](#), we describe the potentials we use to simulate the evolution of Pal 5, and in [Section 4.2](#) we describe our simulation setup. We show the results of our analyses in [Section 4.3](#).

##### 4.1. Gravitational Potentials

We simulate the evolution of Pal 5 in two classes of three-component Galactic potentials implemented in the *gala* package ([Price-Whelan 2017](#)):

1. *Static potentials*: we use the `MWPotential2014` ([Bovy 2015](#)) consisting of a Miyamoto–Nagai disk ([Miyamoto & Nagai 1975](#)), a bulge modeled as an exponentially cut off, power-law density profile, and an axisymmetric Navarro–Frenk–White (NFW) dark-matter halo ([Navarro et al. 1996](#)). We set the flattening of the NFW halo either to the canonical value,  $q_z = 0.94$ , or to an unphysical  $q_z = 0.5$  to investigate Pal 5’s morphology on a regular as well as chaotic orbit, respectively (see [Section 4.2](#)).
2. *Barred potentials*: we use the same disk and halo as in the `MWPotential2014` ([Bovy 2015](#)), but include a Galactic bar instead of a bulge. Following [Wang et al. \(2012\)](#), we compute the barred potential as a basis-function expansion (BFE) representation of a triaxial, exponential density profile:

$$\rho_{\text{bar}} = \rho_0 [\exp(-r_1^2/2) + r_2^{-1.85} \exp(-r_2)], \quad (11)$$

$$r_1 = [((x/x_0)^2 + (y/y_0)^2)^2 + (z/z_0)^4]^{1/4}, \quad (12)$$

$$r_2 = \left[ \frac{q^2(x^2 + y^2) + z^2}{z_0^2} \right]^{1/2}, \quad (13)$$

where the scale lengths are  $x_0 = 1.49$  kpc,  $y_0 = 0.58$  kpc,  $z_0 = 0.4$  kpc, and  $q = 0.6$ . We include terms up to  $n = 6$ ,  $l = 6$  in the “self-consistent field” ([Hernquist &](#)

Ostriker 1992) BFE formalism.<sup>16</sup> We explore barred potentials with pattern speeds of  $\Omega_b = 30\text{--}60$   $\text{km s}^{-1} \text{ kpc}^{-1}$  in increments of  $0.5 \text{ km s}^{-1} \text{ kpc}^{-1}$ , and we test bar masses of  $M_{\text{bar}} = 5 \times 10^9 M_\odot$  and  $M_{\text{bar}} = 1 \times 10^{10} M_\odot$  (Portail et al. 2017). We fix the present-day angular offset from the Galactic  $x$ -axis in the direction of rotation to  $\alpha = 27^\circ$ .

Note that Wang et al. (2012) constructed a bar with a pattern speed of  $\Omega_b = 60 \text{ km s}^{-1} \text{ kpc}^{-1}$ , which has a co-rotation radius,  $r_{\text{CR}} = 3.7 \text{ kpc}$ . In this paper, however, we explore a range of pattern speeds, which will lead to different co-rotation radii for different pattern speeds.

As bars are not expected to extend much beyond their co-rotation radius (e.g., Weiner & Sellwood 1999; Debattista et al. 2002a, 2002b), we adjust the physical scaling of the bar when we vary the pattern speed. In particular, we compute the co-rotation radius,  $r_{\text{CR}}$ , for the mass profiles of the static potential for any given pattern speed,  $\Omega_b$ . We then scale the bar potential for a given pattern speed,  $\Omega_b$ :

$$r_{s,\Omega_b} = r_{\text{CR},\Omega_b} / r_{\text{CR},\text{Wang2012}}. \quad (14)$$

If the scaling in Equation (14) is not included (as in, e.g., Erkal et al. 2017; Pearson et al. 2017; Banik & Bovy 2019), the gravitational influence of the bar at a fixed radius will be too strong (weak) for faster (slower) pattern speeds, respectively.

#### 4.2. Stream Simulation Setup

To simulate the evolution of Pal 5 in a given potential model, we first fit the stream track of Pal 5 in the static potential—that is, we fit for Pal 5 initial conditions that generate mock-stream models that fit the observed sky track of the stream (Section 3). We use the observed 6D phase space coordinates of the Pal 5 cluster (sky positions from Odenkirchen et al. 2002, distance from Harris 2010, radial velocity from Kuzma et al. 2015, and proper motion from Fritz & Kallivayalil 2015, see also Table 1 in Pearson et al. 2017) to initialize the track fit and transform our fitted 6D phase space coordinates into a Galactocentric frame by assuming  $v_{\text{lsr}} = (11.1, 24.0, 7.25) \text{ km s}^{-1}$ ,  $v_{\text{circ}} = 220 \text{ km s}^{-1}$ , and a distance from the Sun to the Galactic center of  $8.1 \text{ kpc}$  (Schönrich et al. 2010; Schönrich 2012). The best-fit present-day kinematics of Pal 5 that reproduce the observed sky track in the static potential are  $\alpha = 229^\circ.0264$ ,  $\delta = -0^\circ.1368$ ,  $d = 22.5 \text{ kpc}$ ,  $v_r = -56.2 \text{ km s}^{-1}$ ,  $\mu_{\alpha \cos \delta} = -2.21 \text{ mas yr}^{-1}$ , and  $\mu_\delta = -2.23 \text{ mas yr}^{-1}$ .

With the present-day location of Pal 5 in hand, we generate the orbit of the progenitor system by integrating Pal 5’s current 6D position back in time for 3 Gyr in steps of 0.5 Myr. Starting from this point and integrating forward to the present day, we simulate the cluster’s disruption and the formation of the stream by releasing two particles from the progenitor’s Lagrange points at every time step, using the Fardal et al. (2015) distribution function implemented in the *gala* package (Price-Whelan 2017). This method is efficient for generating mock-streams and is similar to methods presented in Küpper et al. (2012; see also Varghese et al. 2011; Lane et al. 2012; Gibbons et al. 2014). We account for the self-gravity of the

Pal 5 cluster by including a Plummer mass component with the initial half-mass-radius of  $r_h = 4 \text{ pc}$  and the initial effective mass,  $M_p = 14,404 M_\odot$ . This mass was obtained from the stream track fitting and sets the scaling between the Lagrange points for the modified “particle-spray” method (Fardal et al. 2015). This is comparable to  $12,200 \pm 200 M_\odot$  that Ibata et al. (2017) report for the present-day mass of the cluster and tails combined. As the star particles are released at each time step, they have dispersions in position and velocity set by the mass and orbit of the progenitor (see Section 2.4 in Fardal et al. 2015).

To investigate Pal 5’s evolution on a regular orbit, we first run a “particle-spray” simulation in the static potential, setting  $q_z = 0.94$  (Bovy et al. 2016). Subsequently, we run the same simulation setting  $q_z = 0.5$  to place Pal 5 on a strongly chaotic orbit. We then simulate the evolution of the stream in time-dependent barred potentials, varying the pattern speed of the bar while updating its physical scaling (see Section 4.1) and varying the mass of the bar as described above.

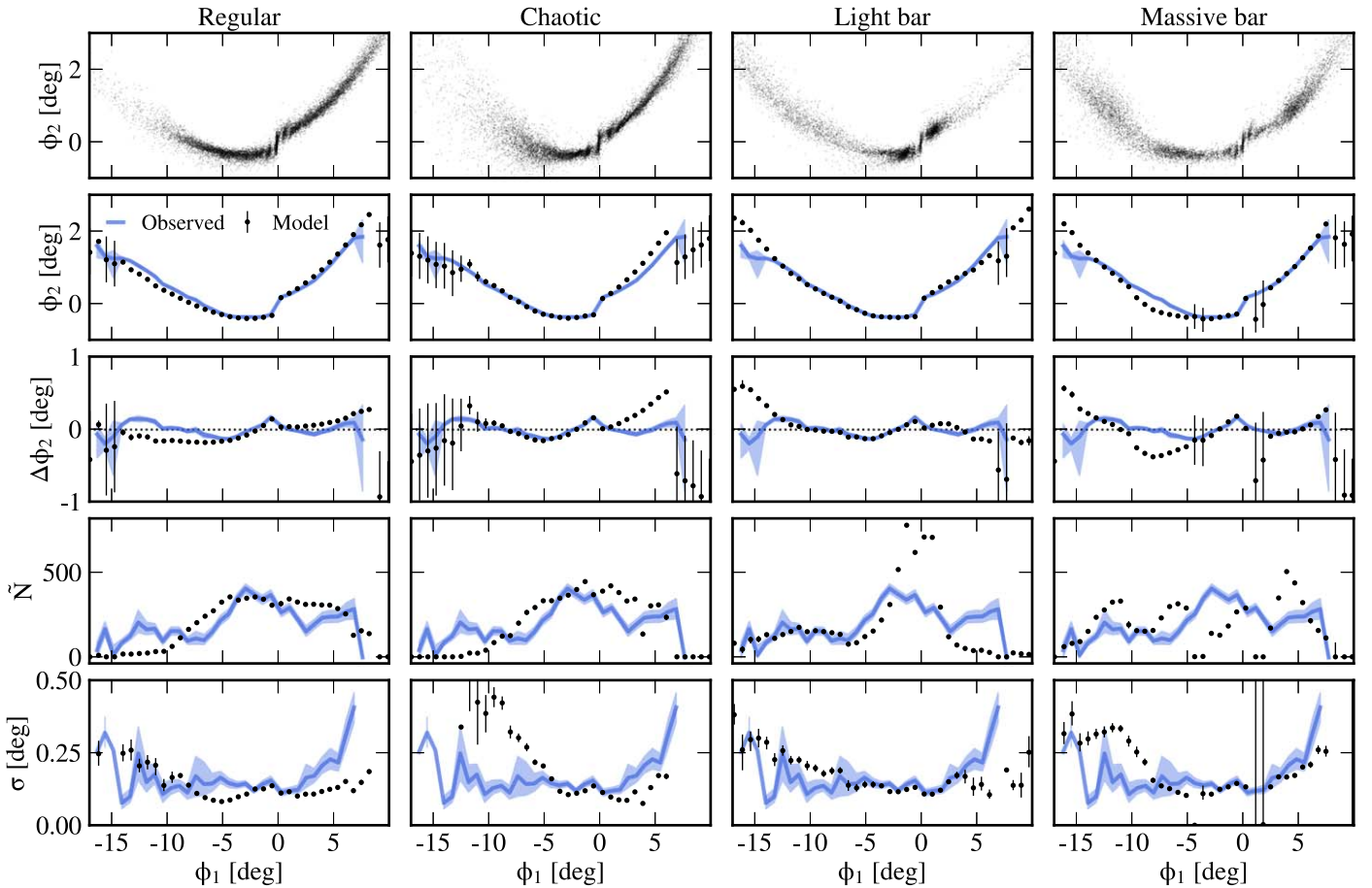
#### 4.3. Simulation Results

In Figure 4 we summarize the results of our suite of Pal 5 simulations. In the top row we present the morphology of the simulated Pal 5 mock-streams evolved in the static potentials with two different flattenings ( $q_z = 0.94$  and  $q_z = 0.5$ ) and we show two examples of mock-streams evolved in the “light” ( $M_{\text{bar}} = 5 \times 10^9 M_\odot$ ) and “massive” ( $M_{\text{bar}} = 1 \times 10^{10} M_\odot$ ) time-dependent barred potentials. All mock-streams are visualized in the coordinate system aligned with Pal 5’s tidal tails (see also Figure 1), and the leading tail is at positive  $\phi_1$  (see the Appendix). The four bottom rows of Figure 4 show results of the 1D density model for the stream track (second row), the track deviations from a second-order polynomial (third row), stream number density (fourth row), and the stream width (fifth row) of the simulated mock-streams (black) as well as of the data (blue shaded region, same as in Figure 3).

We used the mildly flattened ( $q_z = 0.94$ ) static potential to fit the track of the stream (see Section 4.2), and it is therefore not surprising that the track (second row) and track deviations (third row) of the mock stream evolved on the “Regular” orbit (left column, black) looks similar to the track of the data (blue). While the data shows variability in the number density of stars (fourth row), the mock stream, however, has a similar number of stars in both the trailing and the leading tail. Additionally, the width of both the leading and the trailing mock stream are too narrow for  $|\phi_1| < 7$  as compared to the data (fifth row). While the overall width trends for the trailing tail at larger negative  $\phi_1$  are reproduced, the leading tail of the simulated stream is too narrow as compared to the widened “fan” seen in the leading tail of the data.

For the mock stream evolved in a flattened potential, we chose a flattening of  $q_z = 0.5$  in order to investigate the morphology of a mock stream on a chaotic orbit (see also Fardal et al. 2015). The track of the leading tail (third row, black) deviates from the observed stream track (blue) reflecting the extreme flattening of the halo shape. Interestingly, the number density of stars is roughly symmetric for the leading and trailing tail (fourth row), which was also the case for the regular orbit. While the width (fifth row) of the leading tail is slightly wider for the chaotic mock stream than for the mock stream evolved on a regular orbit (left), the mock-stream width is still too narrow when compared to the leading tail data

<sup>16</sup> Banik & Bovy (2019) found that using higher order terms (e.g.,  $n = 9$ ,  $l = 19$ ) for the BFE yields a better representation of the density of the bar. However, this difference does not appreciably change the morphology or kinematics of our simulated streams.



**Figure 4.** Properties of four Pal 5 simulations: “Regular” (static potential and a regular orbit), “Chaotic” (static potential and a chaotic orbit), “Light bar” (time-dependent potential with a  $M_{\text{bar}} = 5 \times 10^9 M_{\odot}$ ,  $\Omega_b = 38 \text{ km s}^{-1} \text{ kpc}^{-1}$  bar), and “Massive bar” ( $M_{\text{bar}} = 1 \times 10^{10} M_{\odot}$ ,  $\Omega_b = 45 \text{ km s}^{-1} \text{ kpc}^{-1}$ ). The top row shows the spatial distribution of tracer particles, while rows 2 through 5 present the derived 1D properties along the stream (black points):  $\phi_2$  positions of the mean stream track, track deviations from a second-order polynomial, number density and width, respectively. These simulations individually reproduce many of the features observed in Pal 5 (blue lines, reproduced from Figure 3), but no model matches all of the features simultaneously.

(blue). The trailing tail, on the other hand, is much wider for the chaotic mock stream than for the data. Thus, the chaotic orbit induces a widening of both the leading and trailing tail, but this widening does not mimic the particular asymmetric widening of the data (see also Pearson et al. 2015; Price-Whelan et al. 2016a).

We selected two specific examples of mock-streams evolved in barred potentials (see “light bar” and “massive bar” columns in Figure 4) through visual inspection of the morphology, track, and width of the simulated streams for streams evolved in the time-dependent potentials with bar pattern speeds ranging from  $\Omega_b = 30\text{--}60 \text{ km s}^{-1} \text{ kpc}^{-1}$ . The “light bar” ( $M_{\text{bar}} = 5 \times 10^9 M_{\odot}$ ,  $\Omega_b = 38 \text{ km s}^{-1} \text{ kpc}^{-1}$ ) mock-stream simulation demonstrates a scenario in which the leading tail has been abruptly truncated (see also Price-Whelan et al. 2016b; Erkal et al. 2017; Pearson et al. 2017). This truncation is apparent in both the morphology (top row) and number density of stars (fourth row), as well as in the width of the mock-stream (fifth row). In particular, the number of stars in the leading tail at  $\phi_1 > 2.5$  is low when compared to the data (blue). The width of the trailing mock-stream matches the observed data well, and the part of the leading tail that has not been truncated also follows the overall trends of the data.

The mock stream evolved in a potential including the “massive bar” ( $M_{\text{bar}} = 1 \times 10^{10} M_{\odot}$ ,  $\Omega_b = 45 \text{ km s}^{-1} \text{ kpc}^{-1}$ ), demonstrates a scenario in which the leading tail has been

widened by the bar (fifth row), to a similar width as observed in the data. In this scenario, the leading tail has not been truncated and there is a comparable number of stars in the leading and trailing tail. The bar has, however, induced over- and underdensities (“gaps”) throughout both the leading and trailing tail (fourth row). While this is also seen in the data, the mock stream visualized here does not follow the gaps seen in the data exactly (located at R.A.  $\approx 227^\circ$  and  $235^\circ$  for the leading and trailing tail, respectively, which is equivalent to  $\phi_1 \approx 2.5$  and  $-7^\circ$ ). Interestingly, for this particular pattern speed, the bar has shifted the stream track of the trailing tail (see second and third row). This effect is apparent in the data on small scales where the track also appears to be “wiggling.” Thus, this mock stream demonstrates a scenario in which both the leading and trailing tails have been perturbed by the bar, and where the leading tail width is similar to the width of the data.

While none of the above mock-stream simulations reproduce all aspects of the data simultaneously, they do provide insight into the mechanisms that could be perturbing the stream. In the next section we discuss the implications of our results.

## 5. Discussion

We presented deep *grz* photometry of the Pal 5 tidal tails from the Legacy Surveys catalog that enables the cleanest



selection of Pal 5 members to date. This detailed view has revealed Pal 5 as a complex system, adding to the numerous examples of stellar streams that show signs of perturbations (e.g., Sesar et al. 2016; Price-Whelan & Bonaca 2018; Bonaca et al. 2019a). One-dimensional modeling of the Pal 5 debris’ spatial distribution revealed significant changes in the width and density along the tidal tails, as well as changes in their direction. Stream simulations in different gravitational potentials separately capture many of the features observed in Pal 5, including gaps and an asymmetry in the length and the width of the leading and trailing tail. However, these simulations fail to reproduce the specific gaps in the stream density and the specific wiggles of its track. Furthermore, they span only a subset of possible environments for stream formation. In this section we discuss mechanisms that could jointly explain this transformed view of the Pal 5 stream.

We first address the striking asymmetry in the length and width of Pal 5’s two tidal arms that is immediately obvious from Figure 2. Recently, Starkman et al. (2019) reported an extension of Pal 5’s leading tail that nearly matches the extent of the trailing tail based on a selection of main-sequence turn-off stars that have proper motions similar to the Pal 5 cluster. This choice of sparse tracers limits the confidence in estimating both the width and the density along the tails. So while our deep photometry also indicates the leading tail extending further (Figure 2), this extension (i.e., the fan) has a significantly larger width and lower surface density. At a fixed density threshold, we confirm the original Bernard et al. (2016) discovery that Pal 5’s leading tail is only half as long as the trailing tail.

In this work we explored the influence of the Milky Way’s Galactic bar on Pal 5 as a way to explain the asymmetry between its tails. Our approach was motivated by Pearson et al. (2017) who showed that Pal 5’s short leading tail may be truncated through a bar perturbation. This scenario predicts that the bar sweeps tidal debris from the leading tail to a much wider area. Deep, wide-field DECaLS photometry enabled us to trace the leading tail as it fans out to  $\text{decl.} \approx -7^\circ$ , while the CMD implies Pal 5 debris has been spread out to even lower surface-brightness level between  $-7^\circ \gtrsim \text{decl.} \gtrsim -10^\circ$ . In Section 4.3, we showed that this low surface-brightness feature can indeed be induced if Pal 5 has been perturbed by the bar.

However, an asymmetry between the leading and the trailing arm of a tidal stream can be produced via other mechanisms. For example, some asymmetry is expected due to dynamical friction of the progenitor (although only  $0.02$  for Pal 5, Kipper et al. 2019). A more significant asymmetry is predicted by simulations of Pal 5 in Milgromian gravity (Thomas et al. 2018). Unlike Newtonian gravity, the coupling of the Galactic gravitational potential and the potential of the globular cluster is nonlinear in this formalism, which results in the breaking of the strong equivalence principle, and a shorter, more diffuse leading tidal arm. Establishing the full extent of the Pal 5 system through deeper imaging would therefore both improve constraints on the mass and pattern speed of the Galactic bar (e.g., Bovy et al. 2019; Clarke et al. 2019; Sanders et al. 2019) and test the theory of gravity.

Next, we discuss density variations detected along Pal 5 tails. Close to the progenitor, the trailing arm is twice as dense as the leading arm. Küpper et al. (2010) showed that the density of tidal tails varies with the orbital phase, with the tails being stretched out close to the pericenter and contracted at the

apocenter. Density asymmetries of the detected magnitude can occur when the progenitor approaches its apocenter, such that the trailing tail is still being contracted, while the leading is already being stretched out. Our procedure for generating model streams has been tuned to reproduce such features (see Küpper et al. 2012; Fardal et al. 2015), so the fact that the unperturbed model (“regular”) is approximately symmetric (while on an eccentric orbit) likely means our models mismatch the true orbital phase of Pal 5. This disagreement is hardly surprising since we determined the orbit by only fitting the stream track (see Section 4). Our results suggest that stream modeling by matching the global density profile would put additional constraints on the inferred orbital phase of Pal 5, as well as on the underlying gravitational potential (see Küpper et al. 2015; Bovy et al. 2016).

We also detect small-scale density variations in Pal 5. The most prominent overdensities are at  $\phi_1 \approx \pm 0.5$  (consistent with Küpper et al. 2015), while the most prominent underdensities (gaps) are at  $\phi_1 \approx -7^\circ$  and  $3^\circ$  (consistent with Erkal et al. 2017). The density peaks are likely epicyclic overdensities (predicted by Küpper et al. 2008; Just et al. 2009; Küpper et al. 2010), and are prominently reproduced in our static Pal 5 models (see Figure 4). On the other hand, static models fail to reproduce the large gaps detected in Pal 5. However, similar gaps can be induced in an encounter with objects such as the spiral arms, molecular clouds, or dark-matter subhalos (e.g., Johnston et al. 2002; Ibata et al. 2002; Yoon et al. 2011; Amorisco et al. 2016; Banik & Bovy 2019). Based on mass arguments, Erkal et al. (2017) suggested that the small gap in Pal 5 may have been produced by a molecular cloud, while the large gap originates from a dark-matter subhalo encounter. In addition to the perturber’s mass, details of the gap profile also depend on the time since the encounter and its impact parameter (Erkal & Belokurov 2015a). Our data set enables a confident measurement of the gap profile above the Milky Way field contamination, which will help in disentangling different encounter parameters, and ultimately determining the origin of these perturbations.

The depth of the DECaLS catalog also allows for a more confidently determined stream track and reveals its surprising deviations: a global change in Pal 5’s curvature  $\approx 5^\circ$  from the cluster, and  $\approx 20'$  oscillations, or wiggles, in the trailing tail (Figure 3). While different simulations capture some of these features (the curvature in the leading tail is reproduced in the “Chaotic” and “Light bar” models, and the “Regular” and “Massive bar” models match the curvature in the trailing tail), no model recovers the whole stream track. Fisher information considerations in a static gravitational potential imply that the stream track encodes the enclosed mass at the current location of the stream (Bonaca & Hogg 2018). The change in the curvature of Pal 5’s tidal arms occurs at a nearly symmetric position along the leading and the trailing arm, so this may indicate a sudden change in the enclosed mass inside Pal 5’s orbit. For example, when a stream encounters a massive object, its overall orbit can change and produce a misalignment between the proper motions and the stream track (Erkal et al. 2018; Koposov et al. 2019). Measuring the relative angle between the proper-motion vector and the stream track along the Pal 5 tails would therefore test whether the change in their curvature originates from an encounter with a massive perturber.



Similarly, the small-scale wiggle in the trailing tail may be another signature of an impact, especially as it coincides with a very prominent gap (Figure 3). During the encounter, nearby stream stars receive a velocity kick that changes their orbital energies and opens a gap in the stellar stream (e.g., Erkal & Belokurov 2015b). In addition, stream stars affected by the perturber can be displaced from the original stream track (Bonaca et al. 2019b). Simultaneous fitting of the Pal 5 stream track and its density profile could determine the origin of the trailing tail gap. Should the encounter scenario be confirmed, track wiggles may put additional constraints on the impact geometry.

More generally, our finding that deep photometry alone can be leveraged to cleanly map tidal debris has important implications for future studies of stellar streams. Within the Milky Way, this enables detailed mapping of streams that reside outside of *Gaia*'s scope (see Ibata et al. 2019), and therefore exploring the level of perturbation in the outer halo. Because streams at greater Galactocentric radii are less likely to have been affected by baryonic structures (e.g., Banik & Bovy 2019), they are especially valuable as more robust tracers of dark-matter subhalos. Outside of the Milky Way, stellar streams have been detected almost exclusively photometrically (e.g., Martínez-Delgado et al. 2010; Kado-Fong et al. 2018), and future photometric surveys are primed to discover numerous low-mass streams (Pearson et al. 2019). Our results suggest that dynamical inferences about the bar, spiral arms, molecular clouds, and dark-matter subhalos from stream perturbations may no longer be limited to the Milky Way, but instead expanded to large samples of galaxies.

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*Software:* *Astropy* (Astropy Collaboration et al. 2013; Price-Whelan et al. 2018), *dustmaps* (Green 2018), *gala* (Price-Whelan 2017), *IPython* (Pérez & Granger 2007), *matplotlib* (Hunter 2007), *numpy* (Walt et al. 2011), *scipy* (Jones et al. 2001).

## Appendix Definition of Pal 5 Coordinates

We use a spherical coordinate system approximately aligned with the Pal 5 stream, with the cluster center at the origin,  $(\phi_1, \phi_2) = (0, 0)^\circ$ . The transformation matrix from ICRS to the Pal 5 coordinate system used in this paper is represented to a precision of 10 significant digits as

$$\begin{pmatrix} x \\ y \\ z \end{pmatrix}_{\text{Pal5}} = \begin{pmatrix} -0.6558203595 & -0.7549138934 & -0.0021642207 \\ -0.6286570070 & 0.5477192750 & -0.5520814915 \\ 0.4179593651 & -0.3607057264 & -0.8337873479 \end{pmatrix} \times \begin{pmatrix} x \\ y \\ z \end{pmatrix}_{\text{ICRS}}$$

and is implemented in the *Gala* Python package (Price-Whelan 2017).

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## References

- Amorisco, N. C., Gómez, F. A., Vegetti, S., & White, S. D. M. 2016, *MNRAS*, **463**, L17
- Astropy Collaboration, Robitaille, T. P., Tollerud, E. J., et al. 2013, *A&A*, **558**, A33
- Banik, N., & Bovy, J. 2019, *MNRAS*, **484**, 2009
- Baumgardt, H., & Makino, J. 2003, *MNRAS*, **340**, 227
- Bernard, E. J., Ferguson, A. M. N., Schlafly, E. F., et al. 2016, *MNRAS*, **463**, 1759
- Bode, P., Ostriker, J. P., & Turok, N. 2001, *ApJ*, **556**, 93
- Bonaca, A., Conroy, C., Price-Whelan, A. M., & Hogg, D. W. 2019a, *ApJL*, **881**, L37
- Bonaca, A., Geha, M., Küpper, A. H. W., et al. 2014, *ApJ*, **795**, 94
- Bonaca, A., & Hogg, D. W. 2018, *ApJ*, **867**, 101
- Bonaca, A., Hogg, D. W., Price-Whelan, A. M., & Conroy, C. 2019b, *ApJ*, **880**, 38
- Bovy, J., Bahmanyar, A., Fritz, T. K., & Kallivayalil, N. 2016, *ApJ*, **833**, 31
- Bovy, J., Leung, H. W., Hunt, J. A. S., et al. 2019, *MNRAS*, **490**, 4740
- Bovy, J. 2015, *ApJS*, **216**, 29
- Bullock, J. S., & Boylan-Kolchin, M. 2017, *ARA&A*, **55**, 343
- Carlberg, R. G., Grillmair, C. J., & Hetherington, N. 2012, *ApJ*, **760**, 75
- Choi, J., Dotter, A., Conroy, C., et al. 2016, *ApJ*, **823**, 102
- Clarke, J. P., Wegg, C., Gerhard, O., et al. 2019, *MNRAS*, **489**, 3519
- Combes, F., Leon, S., & Meylan, G. 1999, *A&A*, **352**, 149
- Debatista, V. P., Corsini, E. M., & Aguerri, J. A. L. 2002a, *MNRAS*, **332**, 65
- Debatista, V. P., Gerhard, O., & Sevenster, M. N. 2002b, *MNRAS*, **334**, 355

- Dey, A., Schlegel, D. J., Lang, D., et al. 2019, *AJ*, **157**, 168
- Diemand, J., Kuhlen, M., Madau, P., et al. 2008, *Natur*, **454**, 735
- Erkal, D., & Belokurov, V. 2015a, *MNRAS*, **454**, 3542
- Erkal, D., & Belokurov, V. 2015b, *MNRAS*, **450**, 1136
- Erkal, D., Koposov, S. E., & Belokurov, V. 2017, *MNRAS*, **470**, 60
- Erkal, D., Li, T. S., Koposov, S. E., et al. 2018, *MNRAS*, **481**, 3148
- Fardal, M. A., Huang, S., & Weinberg, M. D. 2015, *MNRAS*, **452**, 301
- Foreman-Mackey, D., Hogg, D. W., Lang, D., & Goodman, J. 2013, *PASP*, **125**, 306
- Fritz, T. K., & Kallivayalil, N. 2015, *ApJ*, **811**, 123
- Gibbons, S. L. J., Belokurov, V., & Evans, N. W. 2014, *MNRAS*, **445**, 3788
- Green, M. 2018, *JOSS*, **3**, 695, G.
- Harris, W. E. 2010, arXiv:1012.3224
- Hernquist, L., & Ostriker, J. P. 1992, *ApJ*, **386**, 375
- Hu, W., Barkana, R., & Gruzinov, A. 2000, *PhRvL*, **85**, 1158
- Hunter, J. D. 2007, *CSE*, **9**, 90
- Ibata, R. A., Lewis, G. F., Irwin, M. J., & Quinn, T. 2002, *MNRAS*, **332**, 915
- Ibata, R. A., Lewis, G. F., & Martin, N. F. 2016, *ApJ*, **819**, 1
- Ibata, R. A., Lewis, G. F., Thomas, G., Martin, N. F., & Chapman, S. 2017, *ApJ*, **842**, 120
- Ibata, R. A., Malhan, K., & Martin, N. F. 2019, *ApJ*, **872**, 152
- Johnston, K. V., Spergel, D. N., & Haydn, C. 2002, *ApJ*, **570**, 656
- Jones, E., Oliphant, T., Peterson, P., et al. 2001, SciPy: Open Source Scientific Tools for Python, v. 1.3.0, <http://www.scipy.org/>
- Just, A., Berczik, P., Petrov, M. I., & Ernst, A. 2009, *MNRAS*, **392**, 969
- Kado-Fong, E., Greene, J. E., Hendel, D., et al. 2018, *ApJ*, **866**, 103
- Kipper, R., Tenjes, P., Hütsi, G., Tuvikene, T., & Tempel, E. 2019, *MNRAS*, **486**, 5924
- Koposov, S. E., Belokurov, V., Li, T. S., et al. 2019, *MNRAS*, **485**, 4726
- Koposov, S. E., Rix, H.-W., & Hogg, D. W. 2010, *ApJ*, **712**, 260
- Kroupa, P. 2015, *CaJPh*, **93**, 169
- Küpper, A. H. W., Balbinot, E., Bonaca, A., et al. 2015, *ApJ*, **803**, 80
- Küpper, A. H. W., Kroupa, P., Baumgardt, H., & Heggge, D. C. 2010, *MNRAS*, **401**, 105
- Küpper, A. H. W., Lane, R. R., & Heggge, D. C. 2012, *MNRAS*, **420**, 2700
- Küpper, A. H. W., MacLeod, A., & Heggge, D. C. 2008, *MNRAS*, **387**, 1248
- Kuzma, P. B., Da Costa, G. S., Keller, S. C., & Maunder, E. 2015, *MNRAS*, **446**, 3297
- Lane, R. R., Küpper, A. H. W., & Heggge, D. C. 2012, *MNRAS*, **423**, 2845
- Martínez-Delgado, D., Gabany, R. J., Crawford, K., et al. 2010, *AJ*, **140**, 962
- Milgrom, M. 1983, *ApJ*, **270**, 365
- Miyamoto, M., & Nagai, R. 1975, *PASJ*, **27**, 533
- Navarro, J. F., Frenk, C. S., & White, S. D. M. 1996, *ApJ*, **462**, 563
- Ngan, W., Bozek, B., Carlberg, R. G., et al. 2015, *ApJ*, **803**, 75
- Odenkirchen, M., Grebel, E. K., Dehnen, W., Rix, H.-W., & Cudworth, K. M. 2002, *AJ*, **124**, 1497
- Odenkirchen, M., Grebel, E. K., Rockosi, C. M., et al. 2001, *ApJL*, **548**, L165
- Pearson, S., Küpper, A. H. W., Johnston, K. V., & Price-Whelan, A. M. 2015, *ApJ*, **799**, 28
- Pearson, S., Price-Whelan, A. M., & Johnston, K. V. 2017, *NatAs*, **1**, 633
- Pearson, S., Starkenburg, T. K., Johnston, K. V., Williams, B. F., & Ibata, R. A. 2019, *ApJ*, **883**, 87
- Pérez, F., & Granger, B. E. 2007, *CSE*, **9**, 21
- Portail, M., Gerhard, O., Wegg, C., & Ness, M. 2017, *MNRAS*, **465**, 1621
- Price-Whelan, A. M. 2017, *JOSS*, **2**, 388
- Price-Whelan, A. M., & Bonaca, A. 2018, *ApJL*, **863**, L20
- Price-Whelan, A. M., Johnston, K. V., Valluri, M., et al. 2016a, *MNRAS*, **455**, 1079
- Price-Whelan, A. M., Mateur, C., Iorio, G., et al. 2019, *AJ*, **158**, 223
- Price-Whelan, A. M., Sesar, B., Johnston, K. V., & Rix, H.-W. 2016b, *ApJ*, **824**, 104
- Price-Whelan, A. M., Sipócz, B. M., Günther, H. M., et al. 2018, *AJ*, **156**, 123
- Rockosi, C. M., Odenkirchen, M., Grebel, E. K., et al. 2002, *AJ*, **124**, 349
- Sanders, J. L., Smith, L., & Evans, N. W. 2019, *MNRAS*, **488**, 4552
- Schlaflly, E. F., & Finkbeiner, D. P. 2011, *ApJ*, **737**, 103
- Schlegel, D. J., Finkbeiner, D. P., & Davis, M. 1998, *ApJ*, **500**, 525
- Schönrich, R. 2012, *MNRAS*, **427**, 274
- Schönrich, R., Binney, J., & Dehnen, W. 2010, *MNRAS*, **403**, 1829
- Sesar, B., Price-Whelan, A. M., Cohen, J. G., et al. 2016, *ApJL*, **816**, L4
- Speagle, J. S., et al. 2018, Brutus: Modeling Stellar Photometry with Brute Force Methods, <https://github.com/joshspeagle/brutus/>
- Springel, V., Wang, J., Vogelsberger, M., et al. 2008, *MNRAS*, **391**, 1685
- Starkman, N., Bovy, J., & Webb, J. 2019, arXiv:1909.03048
- The WFIRST Astrometry Working Group, Sanderson, R. E., Bellini, A., et al. 2017, arXiv:1712.05420
- Thomas, G. F., Famaey, B., Ibata, R., et al. 2018, *A&A*, **609**, A44
- Thomas, G. F., Ibata, R., Famaey, B., Martin, N. F., & Lewis, G. F. 2016, *MNRAS*, **460**, 2711
- Varghese, A., Ibata, R., & Lewis, G. F. 2011, *MNRAS*, **417**, 198
- Walt, S. V. D., Colbert, S. C., & Varoquaux, G. 2011, *CSE*, **13**, 22
- Wang, Y., Zhao, H., Mao, S., & Rich, R. M. 2012, *MNRAS*, **427**, 1429
- Weiner, B. J., & Sellwood, J. A. 1999, *ApJ*, **524**, 112
- Yoon, J. H., Johnston, K. V., & Hogg, D. W. 2011, *ApJ*, **7317**, 58